## Compare-based lower bound for sorting

Proposition. Any compare-based sorting algorithm must use at least  $lg(N!) \sim N lg N$  compares in the worst-case.

## Pf.

- Assume array consists of N distinct values  $a_1$  through  $a_N$ .
- Worst case dictated by height h of decision tree.
- Binary tree of height h has at most 2 h leaves.
- *N*! different orderings ⇒ at least *N*! leaves.

