Reproduire les résultats de Harvest models of small populations of a large carnivore using Bayesian forecasting par Andrén et al. 2020

### Olivier Gimenez

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### Motivation

Reproduire pour comprendre les résultats de H., Andrén, Hobbs, N. T., Aronsson, M., Brøseth, H., Chapron, G., Linnell, J. D. C., Odden, J., Persson, J., and Nilsen, E. B.. 2020. Harvest models of small populations of a large carnivore using Bayesian forecasting. *Ecological Applications* 30(3):02063. 10.1002/eap.2063.

Les données sont disponibles, mais pas le code. Haha, Erlend le dernier auteur est un fervent défenseur de la science reproductible, c'est loupé sur ce coup-là. Je suppose que les analyses ont été faites par Hobbs, qui a fait plusieurs papiers avec un modèle approchant. Voir par exemple :

- Raiho AM, Hooten MB, Bates S, Hobbs NT (2015) Forecasting the Effects of Fertility Control on Overabundant Ungulates: White-Tailed Deer in the National Capital Region. PLoS ONE 10(12): e0143122. doi:10.1371/journal.pone.0143122
- Hobbs, N.T., Andrén, H., Persson, J., Aronsson, M. and Chapron, G. (2012), Native predators reduce harvest of reindeer by Sámi pastoralists. Ecological Applications, 22: 1640-1654. doi:10.1890/11-1309.1
- Ketz, A. C., T. L. Johnson, R. J. Monello, and N. T. Hobbs. 2016. Informing management with monitoring data: the value of Bayesian forecasting. Ecosphere 7(11):e01587. <10.1002/ecs2.1587>

### Données

On récupère les données de monitoring et harvest pour le lynx. Les colonnes sont : \* year – the year of census (February) \* run – the run in the data \* country – code for country; S = Sweden and N = Norway \* region – code for management region; Z = Jämtland, Y = Västernorrland, AC = Västerbotten, BD = Norrbotten, 2-8 = the different large carnivore management regions in Norway (2-8) \* census – number of lynx family groups censused in that year in that region \* harvest – total number of lynx harvested in that year in that region \* harvest\_F\_>1yr – number of females older than one year harvested in that year in that region \* harvest\_F\_kitten – number of female kittens (10 months old) harvested in that year in that region

```
dat <- read.csv("eap2063-sup-0003-datas1.csv")
dat</pre>
```

```
##
       year run country region census harvest harvest F .1yr harvest F kitten
## 1
       1998
               1
                        S
                                Ζ
                                       82
                                                44
                                                                15
                        S
                                Z
                                                                                    2
## 2
       1999
               2
                                       84
                                                30
                                                                14
## 3
       2000
               3
                        S
                                Z
                                       63
                                                52
                                                                14
                                                                                    7
                        S
                                Z
                                                                                    7
## 4
       2001
                                       49
                                                39
                                                                12
```

##	5	2002	5	S	Z	44	31	8	5
##	6	2003	6	S	Z	39	19	3	1
##	7	2004	7	S	Z	32	17	4	2
##	8	2005	8	S	Z	42	8	2	0
##	9	2006	9	S	Z	44	16	6	3
##	10	2007	10	S	Z	42	16	5	3
##	11	2008	11	S	Z	53	26	7	6
	12	2009	12	S	Z	53	55	22	7
	13	2010	13	S	Z	35	42	15	2
##	14	2011	14	S	Z	39	59	24	6
	15	2012	15	S	Z	31	18	5	3
##	16	2013	16	S	Z	14	9	3	1
	17	2014	17	S	Z	20	1	1	0
##	18	2015	18	S	Z	33	8	2	2
##	19	2016	19	S	Z	38	38	5	15
##	20	2017	20	S	Z	36	36	9	4
##	21	1998	1	S	Y	41	13	4	1
## ##		1999 2000	2 3	S S	Y Y	37 30	16 13	6 5	2 3
##		2000	3 4	s S	Y	28	8	2	2
##		2001	5	S	Y	20	5	3	0
##		2002	6	S	Y	19	6	3	0
##		2003	7	S	Y	7	1	0	0
##		2005	8	S	Y	14	0	0	0
##		2006	9	S	Y	11	2	0	0
##		2007	10	S	Y	12	0	0	0
##		2008	11	S	Y	16	0	0	0
##		2009	12	S	Y	17	4	2	0
##		2010	13	S	Y	18	8	3	1
##	34	2011	14	S	Y	24	12	2	1
##	35	2012	15	S	Y	26	7	2	0
##	36	2013	16	S	Y	14	8	2	0
##	37	2014	17	S	Y	16	6	3	1
##	38	2015	18	S	Y	16	2	0	0
##	39	2016	19	S	Y	18	12	3	2
##		2017	20	S	Y	19	9	2	0
##		1998	1	S	AC	36	5	1	0
	42	1999	2	S	AC	36	7	2	0
##		2000	3	S	AC	34	18	6	1
	44	2001	4	S	AC	38	15	8	2
##		2002	5	S	AC	29	16	8	2
##		2003	6	S	AC	24	7	3	0
##		2004	7	S	AC	21	8	3	0
##		2005	8	S	AC	31	4	0	0
##		2006	9	S	AC	31	2	0	0
## ##		2007 2008	10 11	S S	AC AC	23 37	6 7	2 2	0
##		2008	12	s S	AC	37 41	23	8	1
##		2010	13	S	AC	28	13	6	1
	54	2010	14	S	AC	32	11	4	1
##		2011	15	S	AC	34	26	6	4
##		2012	16	S	AC	22	34	10	2
##		2014	17	S	AC	13	7	2	0
##		2015	18	S	AC	13	3	1	1
	-	-	-		-	-	-		

##	59	2016	19	S	AC	27	12	4	1
##	60	2017	20	S	AC	28	15	7	0
##	61	1998	1	S	BD	35	3	1	0
##	62	1999	2	S	BD	37	4	1	0
##	63	2000	3	S	BD	23	1	1	0
##	64	2001	4	S	BD	34	1	0	0
##	65	2002	5	S	BD	39	0	0	0
##	66	2003	6	S	BD	32	0	0	0
##	67	2004	7	S	BD	25	0	0	0
##	68	2005	8	S	BD	32	2	1	0
##	69	2006	9	S	BD	23	1	0	1
##	70	2007	10	S	BD	24	2	0	0
##	71	2008	11	S	BD	33	0	0	0
##	72	2009	12	S	BD	37	2	0	0
##	73	2010	13	S	BD	33	19	8	2
##	74	2011	14	S	BD	44	13	5	1
##	75	2012	15	S	BD	43	28	13	4
##	76	2013	16	S	BD	30	25	7	4
##		2014	17	S	BD	17	8	3	1
##	78	2015	18	S	BD	32	8	2	2
##	79	2016	19	S	BD	28	14	3	2
##	80	2017	20	S	BD	26	23	6	3
##	81	1996	1	N	2	14	15	1	2
##		1997	2	N	2	20	18	4	2
##	83	1998	3	N	2	14	29	8	4
##		1999	4	N	2	20	21	7	2
##	85	2000	5	N	2	12	18	5	3
##	86	2001	6	N	2	13	16	7	0
##		2002	7	N	2	9	14	6	2
##		2003	8	N	2	4	15	4	2
##		2004	9	N	2	7	7	2	1
##		2005	10	N	2	13	10	3	2
##		2006	11	N	2	13	6	2	2
##		2007	12	N	2	13	10	4	1
##		2008	13	N	2	14	22	4	2
	94	2009	14	N	2	19	27	8	2
##		2010	15	N	2	17	28	10	3
	96	2011	16	N	2	14	26	9	2
	97	2012	17	N	2	16	16	4	2
	98	2013	18	N	2	16	23	9	2
	99	2014	19	N	2	16	29	11	5 3
##		2015 2016	20	N	2	16	37	9	
##		2016	21 22	N	2 2	9 9	21	8 3	0
##		1996	1	N N	3	1	5 4	0	0 1
##		1997	2	N	3	3	5	0	0
##		1998	3			2			
##		1990	4	N N	3 3	3	11 14	4 3	0 1
##		2000	5	N N	3	5 5	9	2	2
##		2000	6	N N	3	5	10	6	1
##		2001	7	N	3	7	12	5	2
		2002	8	N N	3	3	5	3	0
		2003	9	N	3	3	1	1	0
		2004	10	N	3	6	1	1	0
π#	112	2000	10	1//	5	U	1	1	U

##	113 2	2006	11	N	3	5	3	2	0
##	114 2	2007	12	N	3	6	6	4	1
##	115 2	8009	13	N	3	5	11	4	2
##	116 2	2009	14	N	3	6	10	2	3
##	117 2	2010	15	N	3	4	9	5	0
	118 2		16	N	3	4	11	3	0
	119 2		17	N	3	5	5	0	1
	120 2		18	N	3	7	8	2	0
	121 2		19	N	3	5	11	2	1
	122 2		20	N	3	7	9	1	
									0
	123 2		21	N	3	3	6	3	0
	124 2		22	N	3	5	4	1	0
	125 1		1	N	4	2	0	0	0
	126 1		2	N	4	3	0	0	0
	127 1		3	N	4	6	0	0	0
##	128 1	.999	4	N	4	6	10	2	2
##	129 2	2000	5	N	4	1	11	2	1
##	130 2	2001	6	N	4	5	7	2	2
##	131 2	2002	7	N	4	5	11	6	2
##	132 2	2003	8	N	4	5	5	1	0
##	133 2	2004	9	N	4	6	7	3	0
##	134 2	2005	10	N	4	7	4	3	1
	135 2		11	N	4	6	6	3	1
	136 2		12	N	4	6	5	2	0
	137 2		13	N	4	5	7	0	2
	138 2		14	N	4	7	6	2	0
	139 2		15	N	4	9	6	2	0
	140 2		16	N	4	6	11	4	0
	141 2		17	N	4	5	6	1	0
	142 2		18	N	4	1	3	1	0
	143 2		19	N	4	5	0	0	0
	144 2		20	N	4	4	2	0	0
	145 2		21	N	4	1	0	0	0
##	146 2	2017	22	N	4	3	0	0	0
##	147 1	996	1	N	5	9	10	2	1
##	148 1	.997	2	N	5	7	9	3	0
##	149 1	.998	3	N	5	11	14	6	1
##	150 1	999	4	N	5	11	15	3	2
##	151 2	2000	5	N	5	6	12	5	1
##	152 2	2001	6	N	5	9	12	5	2
##	153 2	2002	7	N	5	8	14	6	3
##	154 2	2003	8	N	5	7	17	8	4
	155 2		9	N	5	8	9	0	1
	156 2		10	N	5	7	12	4	0
	157 2		11	N	5	10	7	3	0
	158 2		12	N	5	11	9	3	1
	159 2		13	N	5	10	11	5	0
	160 2			N	5	9	14	3	1
			14						
	161 2		15	N	5	9	10	3	0
	162 2		16	N	5	11	9	3	1
	163 2		17	N	5	6	8	5	0
	164 2		18	N	5	5	5	1	0
	165 2		19	N	5	4	0	0	0
##	166 2	2015	20	N	5	2	0	0	0

##	167 2016	21	N	5	7	0	0	0
##	168 2017	22	N	5	9	0	0	0
##	169 1996	1	N	6	20	34	10	4
##	170 1997	2	N	6	26	40	10	2
##	171 1998	3	N	6	14	32	12	1
##	172 1999	4	N	6	14	14	4	3
##	173 2000	5	N	6	14	15	2	2
##	174 2001	6	N	6	9	7	3	2
	175 2002	7	N	6	11	17	3	4
	176 2003	8	N	6	11	9	2	1
	177 2004	9	N	6	14	3	2	0
	178 2005	10	N	6	14	14	4	4
	179 2006	11	N	6	17	18	6	2
	180 2007	12	N	6	15	29	6	4
##	181 2008	13	N	6	23	30	9	4
##	182 2009	14	N	6	26	36	16	8
##	183 2010	15	N	6	20	59 50	22	3
	184 2011	16	N	6	18	52	16	4
	185 2012 186 2013	17 18	N	6 6	14	17	7 6	3 0
	187 2014	19	N N	6	8 12	15 7	2	1
	188 2015	20	N	6	17	18	6	0
	189 2016	21	N	6	14	31	11	2
	190 2017	22	N	6	19	33	11	5
	191 1996	1	N	7	12	14	6	2
	192 1997	2	N	7	14	16	4	3
	193 1998	3	N	7	10	16	6	1
	194 1999	4	N	7	16	11	5	0
	195 2000	5	N	7	15	20	6	5
	196 2001	6	N	7	5	16	6	2
##	197 2002	7	N	7	6	13	6	0
##	198 2003	8	N	7	5	7	4	0
##	199 2004	9	N	7	2	5	2	0
##	200 2005	10	N	7	4	2	1	0
	201 2006	11	N	7	6	0	0	0
	202 2007	12	N	7	8	0	0	0
	203 2008	13	N	7	9	4	0	1
	204 2009	14	N	7	14	8	4	1
	205 2010	15	N	7	6	16	8	1
	206 2011	16	N	7	8	12	4	1
	207 2012	17	N	7	8	9	2	1
	208 2013	18	N	7	10	6	4	0
	209 2014	19	N	7	4	13	4	0
	210 2015	20	N	7	5	4	2	0
	211 2016	21	N	7	6	5	1	0
	<ul><li>212 2017</li><li>213 1996</li></ul>	22 1	N N	7 8	6 5	6 4	1 2	0
	213 1996 214 1997	2	N N	8	5 7	4 5	1	1
	214 1997 215 1998	3	N	8	7	11	5	0
	216 1999	4	N	8	5	1	1	0
	217 2000	5	N	8	6	10	6	2
	218 2001	6	N	8	6	13	7	1
	219 2002	7	N	8	8	11	2	0
	220 2003	8	N	8	10	4	1	0
		•		-		-	=	-

```
## 221 2004
                9
                          N
                                  8
                                                    3
                                                                      2
                                                                                           0
## 222 2005
               10
                          N
                                  8
                                           3
                                                    1
                                                                      0
                                                                                           0
                                  8
   223 2006
                          N
                                           5
                                                    0
                                                                      0
                                                                                           0
   224 2007
                                  8
                                          12
                                                                                           0
               12
                          N
                                                    1
##
                                                                       1
## 225 2008
               13
                          N
                                   8
                                           9
                                                    4
                                                                      1
                                                                                           0
## 226 2009
                                  8
                                           9
                                                    8
                                                                                           0
               14
                          N
                                                                      4
## 227 2010
                                   8
                                          15
                                                    7
                                                                                           0
               15
                          N
                                                                      1
## 228 2011
                                   8
                                                                      7
               16
                          N
                                          11
                                                   16
                                                                                           1
## 229 2012
               17
                          N
                                   8
                                          13
                                                   18
                                                                      5
                                                                                           4
                                   8
                                          10
                                                                      3
                                                                                           2
## 230 2013
               18
                          N
                                                   13
## 231 2014
               19
                          N
                                   8
                                           5
                                                   10
                                                                      4
                                                                                           0
                                   8
                                                    5
                                                                                           2
## 232 2015
                          N
                                           8
                                                                      1
               20
                                   8
                                           9
                                                    3
                                                                      2
                                                                                           0
## 233 2016
               21
                          N
                                                                      2
## 234 2017
                          N
                                  8
                                           6
                                                    4
                                                                                           1
               22
```

```
dat %>%
```

count(region)

```
##
      region
              n
            2 22
## 1
##
  2
            3 22
## 3
            4 22
            5 22
## 4
## 5
            6 22
            7
              22
## 6
## 7
            8 22
## 8
           AC 20
## 9
           BD 20
## 10
            Y 20
            Z 20
## 11
```

```
dat %>%
  count(country)
```

```
## country n
## 1 N 154
## 2 S 80
```

### Le modèle

Dans leur papier, Henrik et les collègues construisent un modèle démographique structuré en classes d'âge. J'ai pas envie de me lancer dans un truc compliqué, l'idée est simplement de comprendre comment dérouler leur approche.

On part sur un modèle exponentiel. On stipule que les effectifs  $N_t$  à l'année t sont obtenus à partir des effectifs à l'année t-1 auxquels on a retranché les prélèvements  $H_{t-1}$ , le tout multiplié par le taux de croissance annuel  $\lambda$ :

$$N_t = \lambda (N_{t-1} - H_{t-1}).$$

Cette relation est déterministe. Pour ajouter de la variabilité démographique, on suppose que les effectifs sont distribués selon une distribution log-normale, autrement dit que les effectifs sont normalement distribués sur l'échelle log :

$$\log(N_t) \sim \text{Normale}(\mu_t, \sigma_{\text{proc}})$$

avec  $\mu_t = \log(N_t) = \log(\lambda(N_{t-1} - H_{t-1}))$  et  $\sigma_{\text{proc}}$  l'erreur standard des effectifs sur l'échelle log. On aurait pu prendre une loi de Poisson à la place. La stochasticité environnementale est en général captée par le taux de croissance, mais pas ici puisqu'il est constant. C'est une hypothèse forte du modèle. Dans l'idéal, on pourrait coupler le modèle de capture-recapture, et le modèle qui décrit l'évolution des effectifs au cours du temps.

On ajoute une couche d'observation qui capture les erreurs sur les effectifs. Si l'on note  $y_t$  les effectifs observés, on suppose que ces comptages annuels sont distribués comme une loi de Poisson de moyenne les vrais effectifs  $N_t$ :

```
y_t \sim \text{Poisson}(N_t).
```

```
lynx_model <- function(){</pre>
  # Priors
  sigmaProc ~ dunif(0, 10)
  tauProc <- 1/sigmaProc^2</pre>
  lambda ~ dunif(0, 5)
    N[1] \sim dgamma(1.0E-6, 1.0E-6)
    # Process model
    for (t in 2:(nyears)) {
      mu[t] \leftarrow lambda * (N[t-1] - harvest[t-1])
      Nproc[t] <- log(max(1, mu[t]))</pre>
      N[t] ~ dlnorm(Nproc[t], tauProc)
    }
  # Observation model
  for (t in 1:nyears) {
    y[t] ~ dpois(N[t])
}
```

Dans le papier, Henrik fait des regroupements d'aires de gestion, et applique le modèle à chacun de ces regroupements.

### Northern Sweden: management areas Z, Y, BD and AC

On regroupe.

```
## 'summarise()' ungrouping output (override with '.groups' argument)
```

On prépare les données.

```
bugs.data <- list(
   nyears = 20,
   y = dat1$census,
   harvest = dat1$harvest)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("lambda", "sigmaProc","N", "tauProc")
bugs.chains <- 3
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 20
```

## Unobserved stochastic nodes: 22
## Total graph size: 147
##

## Initializing model

## N[6]

## module glm loaded

Jetons un coup d'oeil aux estimations.

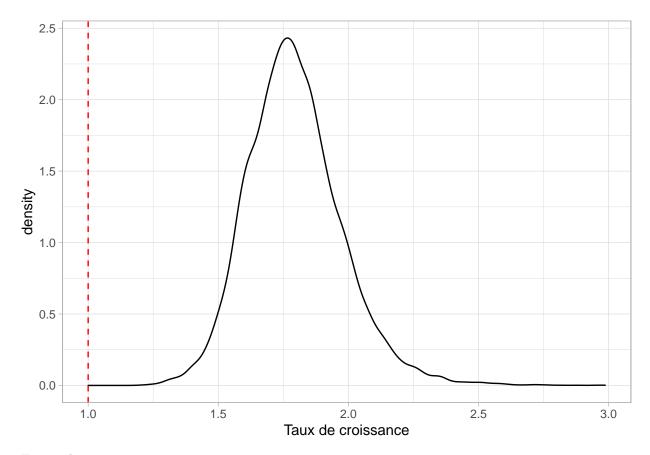
111.142

```
res <- print(lynx_mod, intervals = c(2.5/100, 50/100, 97.5/100))
```

```
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba1
## 3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
   n.sims = 15000 iterations saved
##
            mu.vect sd.vect
                               2.5%
                                         50%
                                              97.5% Rhat n.eff
## N[1]
            192.271 13.414 167.040 191.920 219.567 1.001 15000
## N[2]
            190.865 13.282 165.508 190.511 217.776 1.001 15000
## N[3]
            155.282 11.253 134.178 154.974 178.143 1.001 15000
## N[4]
            146.586 11.284 125.655 146.203 169.886 1.001 8500
## N[5]
            130.321 10.555 110.445 129.919 152.114 1.001 15000
```

9.915 92.568 110.801 131.532 1.001 6600

```
## N[7]
            88.449 8.702 72.331 88.134 106.269 1.001 11000
## N[8]
            ## N[9]
            108.878 9.778 90.544 108.578 128.764 1.001 15000
## N[10]
            103.584 9.424 86.196 103.325 122.888 1.001 15000
## N[11]
            137.649 11.049 116.893 137.258 160.350 1.001 15000
## N[12]
            150.902 10.993 130.452 150.571 173.215 1.001 4700
## N[13]
            126.100 9.314 109.063 125.655 145.578 1.001 13000
            144.183 9.788 126.119 143.828 164.323 1.001 14000
## N[14]
## N[15]
            132.494 9.837 114.412 132.052 152.525 1.001 15000
## N[16]
           97.744 6.134 86.743 97.446 110.526 1.001 5600
## N[17]
            64.755 7.101 51.499 64.534 79.369 1.001 4400
            92.172 8.890 75.482 91.880 110.408 1.001 15000
## N[18]
            118.652 8.918 102.096 118.356 137.173 1.001 13000
## N[19]
## N[20]
            106.611 10.240 87.608 106.297 127.726 1.001 15000
## lambda
              1.793
                    0.182
                            1.477
                                    1.781
                                            2.192 1.001 15000
## sigmaProc
              0.407
                     0.096
                            0.261
                                    0.392
                                            0.635 1.001 6200
## tauProc
              7.036
                    3.169
                             2.481
                                    6.503 14.721 1.001 6200
## deviance 154.850 6.456 144.156 154.241 169.152 1.001 10000
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 20.8 and DIC = 175.7
## DIC is an estimate of expected predictive error (lower deviance is better).
lynx_mod$BUGSoutput$sims.matrix %>%
 as tibble() %>%
# pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
# filter(str detect(parameter, "lambda")) %>%
 ggplot() +
  aes(x = lambda) +
  geom density() +
  geom_vline(xintercept = 1, lty = "dashed", color = "red") +
 labs(x = "Taux de croissance")
```



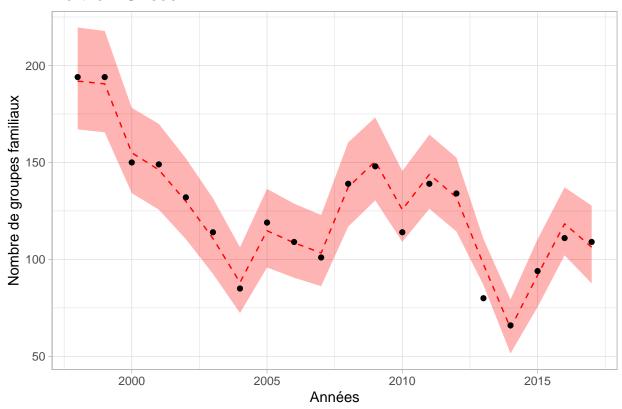
Ensuite les projections.

```
northern_sweden <- lynx_mod$BUGSoutput$sims.matrix %>%
  pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
  filter(str_detect(parameter, "N")) %>%
  group_by(parameter) %>%
  summarize(medianN = median(value),
           lci = quantile(value, probs = 2.5/100),
           uci = quantile(value, probs = 97.5/100)) %>%
  mutate(an = parse_number(parameter) + 1997) %>%
  arrange(an) %>%
  ggplot() +
 geom_ribbon(aes(x = an, y = medianN, ymin = lci, ymax = uci), fill = "red", alpha = 0.3) +
  geom_line(aes(x = an, y = medianN), lty = "dashed", color = "red") +
\# geom_point(aes(x = an, y = medianN), color = "red") +
 geom_point(data = bugs.data %>% as_tibble, aes(x = 1997 + 1:unique(nyears), y = y)) +
  labs(y = "Nombre de groupes familiaux",
      x = "Années",
      title = "Northern Sweden")
```

## 'summarise()' ungrouping output (override with '.groups' argument)

```
northern_sweden
```

## Northern Sweden



## Northern Norway: management areas 6, 7, 8

Idem qu'au-dessus.

## 'summarise()' ungrouping output (override with '.groups' argument)

```
bugs.data <- list(
   nyears = 22,
   y = dat1$census,
   harvest = dat1$harvest)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("lambda", "sigmaProc","N", "tauProc")
bugs.chains <- 2
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

## N[10]

## N[11]

## N[12]

## N[13]

## N[14]

## N[15]

## N[16]

## N[17]

## N[18]

## N[19]

## N[20]

## N[21]

## N[22]

## lambda

## sigmaProc

21.842

28.182

36.322

42.798

50.767

40.696

36.548

35.150

28.266

20.855

30.910

29.181

30.512

3.199

2.942

4.328

5.046

5.488

6.096

7.484

6.351

6.124

6.386

5.736

4.811

5.288

5.787

5.544

1.171

0.520

13.876 21.569

19.559 27.786

36.003

42.750

50.834

40.336

36.152

34.585

27.706

20.377

30.744

28.612

30.149

3.308

2.867

25.565

30.439

36.764

29.433

25.575

24.326

18.261

12.796

20.892

19.258

20.777

0.834

2.134

```
lynx_mod <- jags(data = bugs.data,</pre>
                  inits = bugs.inits,
                  parameters.to.save = bugs.monitor,
                  model.file = lynx_model,
                  n.chains = bugs.chains,
                                                       n.thin = 10,
                                                       n.iter = 100000,
                                                       n.burnin = 50000)
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
##
  Graph information:
      Observed stochastic nodes: 22
##
##
      Unobserved stochastic nodes: 24
##
      Total graph size: 161
##
## Initializing model
Jetons un coup d'oeil aux estimations.
res <- print(lynx_mod, intervals = c(2.5/100, 50/100, 97.5/100))
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba6
    2 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
    n.sims = 10000 iterations saved
##
##
             mu.vect sd.vect
                                 2.5%
                                          50%
                                                97.5% Rhat n.eff
## N[1]
              37.264
                        6.385
                               26.099
                                       36.834
                                               51.898 1.001 6500
## N[2]
              46.855
                       7.105
                               34.343
                                       46.369
                                               62.795 1.001 10000
                       5.587
## N[3]
              30.613
                               20.650
                                       30.302
                                               42.321 1.001 10000
## N[4]
              35.179
                       5.565
                               25.424
                                       34.757
                                               47.311 1.001 10000
## N[5]
              35.201
                        6.203
                               24.384
                                       34.735
                                               48.435 1.001 10000
## N[6]
              19.745
                        4.494
                               11.799 19.451
                                               29.423 1.001 10000
## N[7]
              24.680
                       5.016
                              16.003 24.305
                                               35.517 1.001 10000
## N[8]
              26.087
                        4.819
                              17.325 25.676
                                               36.728 1.001 10000
## N[9]
                        4.228
                              11.968 18.533
                                               28.261 1.001 10000
              18.953
```

31.263 1.001 10000

39.187 1.001 8500

55.287 1.001 10000

65.441 1.001 10000

54.051 1.001 10000

49.751 1.001 10000

49.302 1.001 10000

40.430 1.001 8500

31.974 1.001 10000

41.994 1.001 8000

42.314 1.001 10000

42.309 1.001 9100

4.927 1.001 10000

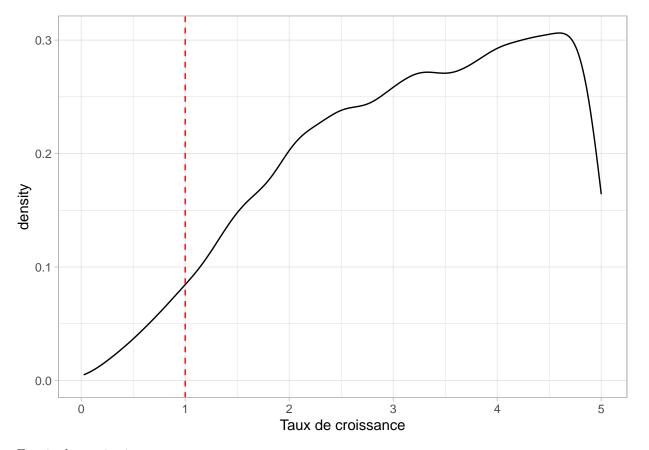
4.167 1.001 5100

3800

47.720 1.001

```
## tauProc   0.126   0.042   0.058   0.122   0.220 1.001 5100
## deviance 138.283   6.758 127.124 137.653 153.386 1.001 3700
##
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
##
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 22.8 and DIC = 161.1
## DIC is an estimate of expected predictive error (lower deviance is better).
```

```
lynx_mod$BUGSoutput$sims.matrix %>%
  as_tibble() %>%
# pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
# filter(str_detect(parameter, "lambda")) %>%
ggplot() +
  aes(x = lambda) +
  geom_density() +
  geom_vline(xintercept = 1, lty = "dashed", color = "red") +
  labs(x = "Taux de croissance")
```



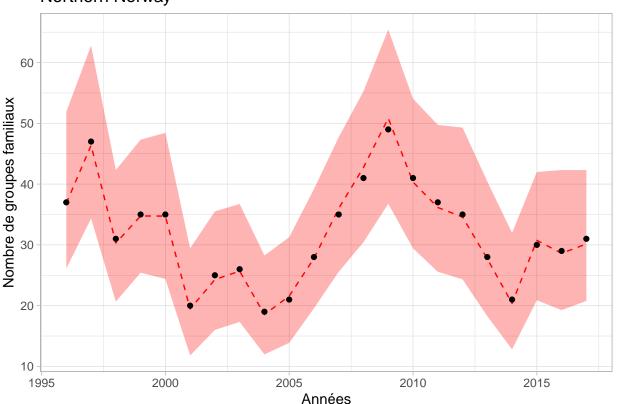
Ensuite les projections.

```
northern_norway <- lynx_mod$BUGSoutput$sims.matrix %>%
  as_tibble() %>%
  pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
  filter(str_detect(parameter, "N")) %>%
  group_by(parameter) %>%
```

## 'summarise()' ungrouping output (override with '.groups' argument)

northern\_norway

# Northern Norway



### Southern Norway: management areas 2, 3, 4 and 5

On applique le modèle exponentiel au dernier regroupement.

```
dat %>%
  filter(region == "2" | region == "3" | region == "4" | region == "5") %>%
```

## 'summarise()' ungrouping output (override with '.groups' argument)

```
bugs.data <- list(
   nyears = 22,
   y = dat1$census,
   harvest = dat1$harvest)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("lambda", "sigmaProc","N", "tauProc")
bugs.chains <- 3
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

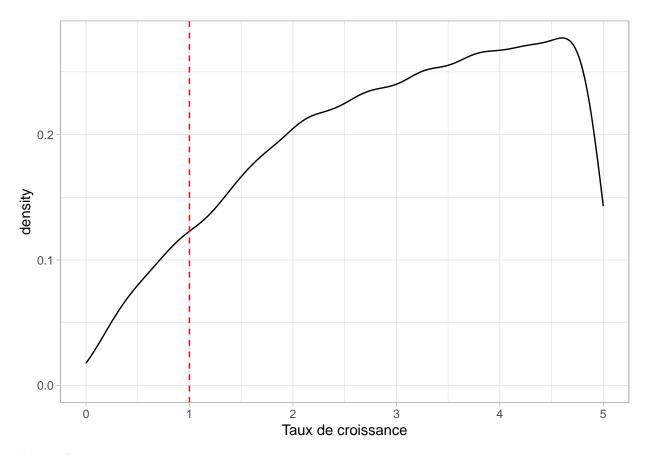
```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 22
## Unobserved stochastic nodes: 24
## Total graph size: 161
##
## Initializing model
```

Jetons un coup d'oeil aux estimations.

```
res <- print(lynx_mod, intervals = c(2.5/100, 50/100, 97.5/100))
```

```
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba4
## 3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
## n.sims = 15000 iterations saved
## mu.vect sd.vect 2.5% 50% 97.5% Rhat n.eff
## N[1] 27.027 5.567 17.217 26.645 38.188 1.001 15000
```

```
## N[2]
             34.026
                      5.807 23.022 34.106 45.649 1.001 15000
## N[3]
             32.802
                      5.772 22.583 32.463 45.166 1.001 5900
                      6.334 28.303 39.305
## N[4]
             39.715
                                           53.038 1.001 11000
## N[5]
             23.610
                      4.834 15.105 23.284
                                            33.995 1.002 2500
## N[6]
             31.804
                      5.789
                             21.530 31.376
                                            44.694 1.001 8500
## N[7]
             28.669
                      5.348 19.139 28.316
                                           39.981 1.001 4900
## N[8]
             18.651
                      4.292 11.224 18.336 27.895 1.001 15000
                      5.038 15.657 24.904 35.120 1.001 10000
## N[9]
             24.848
## N[10]
             33.657
                      5.432
                             23.398 33.341 45.158 1.001 15000
                      5.680
## N[11]
             34.091
                            24.155 33.765 46.254 1.001 15000
## N[12]
             36.983
                      5.673
                            26.359 36.654 49.070 1.001 14000
                      5.918 23.523 33.483 46.444 1.001 7700
## N[13]
             33.932
                      6.490 28.990 40.279 54.691 1.001 15000
## N[14]
             40.706
## N[15]
             38.730
                      6.398 27.465 38.331 52.901 1.001 15000
## N[16]
             34.616
                      5.893
                            24.075 34.276 47.042 1.001 15000
## N[17]
             32.732
                      6.039
                             21.867
                                    32.429
                                            44.906 1.001 15000
## N[18]
             28.988
                      5.656 19.222 28.497
                                            41.683 1.001 15000
## N[19]
             29.944
                      5.681
                            20.112 29.508 42.570 1.001 15000
## N[20]
                     5.344 19.065 28.349
                                            40.104 1.001 7700
             28.678
                     4.680 12.062 19.505
## N[21]
             19.988
                                            30.540 1.001 15000
## N[22]
             25.667
                      5.051 16.708 25.304
                                            36.413 1.001 15000
## lambda
              3.013
                      1.273
                             0.489
                                     3.140
                                             4.910 1.001 12000
                      0.544
## sigmaProc
              3.222
                              2.357
                                             4.488 1.001 10000
                                     3.155
## tauProc
              0.104
                      0.033
                              0.050
                                     0.100
                                             0.180 1.001 10000
## deviance 138.223
                      6.754 126.969 137.569 152.993 1.001 15000
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 22.8 and DIC = 161.0
## DIC is an estimate of expected predictive error (lower deviance is better).
lynx mod$BUGSoutput$sims.matrix %>%
 as_tibble() %>%
# pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
# filter(str_detect(parameter, "lambda")) %>%
 ggplot() +
 aes(x = lambda) +
 geom_density() +
 geom_vline(xintercept = 1, lty = "dashed", color = "red") +
 labs(x = "Taux de croissance")
```



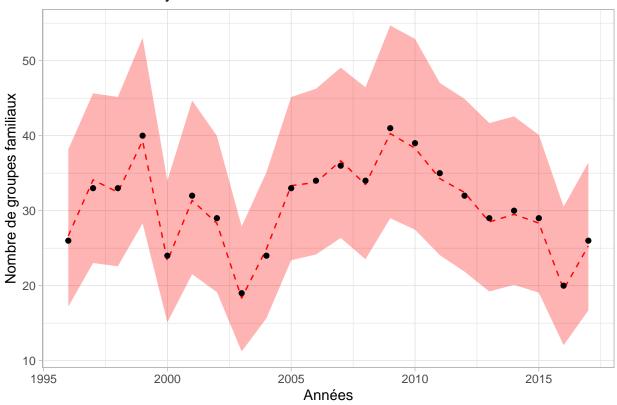
Ensuite les projections.

```
southern_norway <- lynx_mod$BUGSoutput$sims.matrix %>%
  as_tibble() %>%
  pivot_longer(cols = everything(), values_to = "value", names_to = "parameter") %>%
  filter(str_detect(parameter, "N")) %>%
  group_by(parameter) %>%
  summarize(medianN = median(value),
           lci = quantile(value, probs = 2.5/100),
           uci = quantile(value, probs = 97.5/100)) %>%
  mutate(an = parse_number(parameter) + 1995) %>%
  arrange(an) %>%
  ggplot() +
 geom_ribbon(aes(x = an, y = medianN, ymin = lci, ymax = uci), fill = "red", alpha = 0.3) +
  geom_line(aes(x = an, y = medianN), lty = "dashed", color = "red") +
\# geom_point(aes(x = an, y = medianN), color = "red") +
 geom_point(data = bugs.data %>% as_tibble, aes(x = 1995 + 1:unique(nyears), y = y)) +
  labs(y = "Nombre de groupes familiaux",
      x = "Années",
      title = "Northern Norway")
```

## 'summarise()' ungrouping output (override with '.groups' argument)

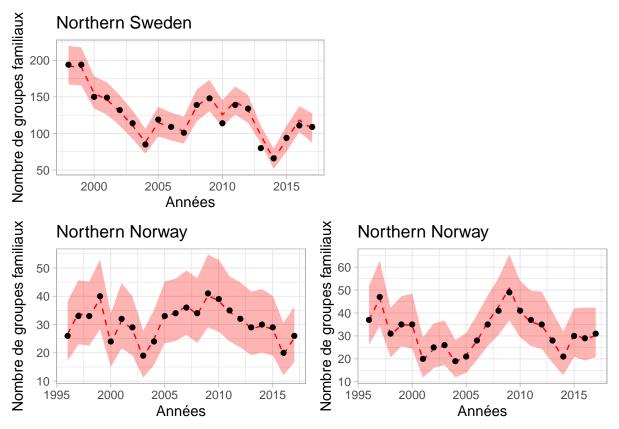
```
southern_norway
```

# Northern Norway



# Tout ensemble - Figure 3 ou presque

```
library(patchwork)
(northern_sweden + grid::textGrob("")) / (southern_norway | northern_norway)
```



Hmm. Si l'on compare à la Figure 3 du papier, on s'aperçoit que l'ajustement du modèle exponentiel aux données est bien meilleur que celui du modèle structuré en âge développé par les auteurs. Ha!

### **Forecasting**

Le modèle décrit l'évolution des effectifs à t en fonction des effectifs à t et permet donc de projeter les effectifs en 2018 en connaissant les effectifs de 2017 la dernière année du suivi, puis ceux de 2019 en utilisant les effectifs prédits pour 2018, et ainsi de suite. A cahque étape, il y a des erreurs qui s'accumulent. L'approche bayésienne a l'avantage de permettre de faire ces prédictions en reportant les incertitudes d'une année à l'autre. C'est ce qui fait des modèles à espace d'états en bayésien un outil très utile pour faire des projections.

Bien. Maintenant dans le modèle utilisé, la variable effectifs prélevés est supposée connue. Il s'agit d'une donnée, et par définition on ne la connait pas dans le futur. Il nous faut donc un modèle sur les effectifs prélevés, comme on en a un sur les effectifs comptés.

Les auteurs proposent le modèle à espace d'états suivant :

$$H_t \sim \text{log-Normale}\left(\max(0, \log(b_0 + b_1 y_{t-1})), \sigma_q^2\right)$$

 $\operatorname{et}$ 

$$q_t \sim \text{Poisson}(H_t)$$

où  $q_t$  est le quota observé au temps t et  $H_t$  l'effectif réel d'animaux prélevés. La prédiction du modèle est  $H_t$  avec une erreur de processus  $\sigma_q^2$ .

On retrouve l'astuce utilisée par Guillaume pour forcer la moyenne de la normale à être supérieure ou égale à 0 avec le  $\max(0, \log)$ .

On a deux scénarios, ou bien un quota proportionnel aux effectifs comptés avec  $b_0 = 0$  (modèle 1 : proportional quota setting strategy), ou bien des prélèvements qui augmentent proportionnellement, avec un

quota nul en-dessous d'un seuil (modèle 2 : threshold quota setting strategy). Ce seuil X se calcule en fixant  $0 = b_0 + b_1 X$  soit  $X = -b_0/b_1$ . J'ai pas tout bien compris encore à ce scénario. Ca deviendra plus clair en essayant d'ajuster les modèles je suppose.

On lit les données spécifique au modèle de décision. On a : \* year – the year of census (February) \* run – the run in the data \* country – code for country; 1 = Sweden and 2 = Norway \* census – number of lynx family groups censused in that year in that region \* quota – the harvest quota for lynx based on the census result of the same year in that region \* quota\_1 – the harvest quota for lynx based on the census result of the year before in the region.

```
dat <- read.csv("eap2063-sup-0004-datas2.csv")

dat %>%
  filter(country == "1") %>%
  select(year, census, quota_1) -> dat_sweden

dat_sweden
```

```
##
      year census quota_1
## 1
      1998
               194
## 2
      1999
               194
                        108
## 3
      2000
               150
                         73
## 4
      2001
               149
                         72
## 5
      2002
               132
                         67
      2003
                         32
## 6
               114
## 7
      2004
                86
                         15
## 8
      2005
                         28
               119
## 9
      2006
               109
                         30
## 10 2007
               102
                         32
## 11 2008
                         99
               140
## 12 2009
               148
                        127
## 13 2010
               114
                         95
## 14 2011
               139
                         86
## 15 2012
               135
                         62
## 16 2013
                80
                         24
## 17 2014
                66
                          0
```

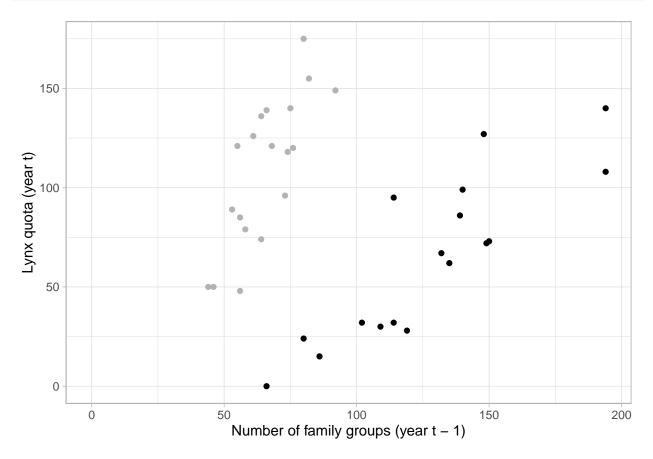
```
dat %%
  filter(country == "2") %>%
  select(year, census, quota_1) -> dat_norway

dat_norway
```

```
##
      year census quota 1
## 1
      1996
                64
                        136
## 2
      1997
                82
                        155
## 3
      1998
                66
                        139
## 4
      1999
                75
                        140
## 5
      2000
                        126
                61
## 6
      2001
                55
                        121
## 7
      2002
                56
                         85
## 8
      2003
                46
                         50
## 9
      2004
                         50
                44
```

```
## 10 2005
                56
                        48
## 11 2006
                64
                        74
## 12 2007
                73
                        96
## 13 2008
                76
                        120
## 14 2009
                92
                        149
## 15 2010
                80
                        175
## 16 2011
                74
                        118
## 17 2012
                68
                        121
## 18 2013
                58
                        79
## 19 2014
                53
                        89
```

```
ggplot() +
  geom_point(data = dat_sweden, aes(x = census, y = quota_1), color = "black") +
  geom_point(data = dat_norway, aes(x = census, y = quota_1), color = "gray70") +
  expand_limits(x = 0, y = 0) +
  labs(x = "Number of family groups (year t - 1)",
      y = "Lynx quota (year t)")
```



# Modèle 1

Commençons par le modèle 1.

```
model1 <- function(){
    # Priors</pre>
```

```
sigmaProc ~ dunif(0, 4)
tauProc <- 1/sigmaProc^2
b[1] ~ dnorm(0, 3)

# Process model
for (t in 1:(nyears)) {
    mu[t] <- log(b[1] * y[t])
    Hproc[t] <- max(0, mu[t])
    H[t] ~ dlnorm(Hproc[t], tauProc)
    }

# Observation model
for (t in 1:nyears) {
    q[t] ~ dpois(H[t])
}</pre>
```

On prépare les données pour la Suède.

```
bugs.data <- list(
   nyears = 17,
   y = dat_sweden$census,
   q = dat_sweden$quota_1)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("b", "sigmaProc","H")
bugs.chains <- 3
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 17
## Unobserved stochastic nodes: 19
## Total graph size: 106
##
## Initializing model
```

Jetons un coup d'oeil aux estimations.

```
print(mod1 sweden, intervals = c(2.5/100, 50/100, 97.5/100))
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba2
   3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
  n.sims = 15000 iterations saved
            mu.vect sd.vect
                                2.5%
                                         50%
                                               97.5% Rhat n.eff
             138.820 11.644 116.906 138.461 162.411 1.001 15000
## H[1]
             107.162 10.212 87.998 106.909 128.201 1.001 6000
## H[2]
## H[3]
             72.540
                      8.450 56.840 72.234 89.975 1.001 15000
## H[4]
                             56.162 71.313
             71.636
                      8.387
                                              88.911 1.001 6800
## H[5]
              66.645
                       8.147
                             51.502 66.326
                                             83.318 1.001 15000
## H[6]
              32.686
                      5.598
                             22.586 32.392
                                              44.500 1.001 4500
## H[7]
              16.515
                      3.928
                              9.734 16.237
                                              25.075 1.001 15000
## H[8]
              28.987
                       5.205 19.569 28.689
                                              39.958 1.001 15000
## H[9]
              30.665
                       5.377
                             20.992 30.360
                                              41.953 1.001 12000
## H[10]
              32.430
                      5.552 22.484 32.116 44.248 1.001 12000
## H[11]
              97.887
                       9.821 79.558 97.614 118.025 1.001 15000
## H[12]
             125.485 11.281 104.591 125.145 148.454 1.001 15000
## H[13]
              93.478
                      9.556 75.486 93.209 113.067 1.001 7000
                      9.131 68.351 84.668 104.115 1.001 15000
## H[14]
              85.160
## H[15]
              61.757
                      7.742 47.618 61.433
                                             77.647 1.001 15000
## H[16]
              24.568
                      4.820
                             16.143 24.252 34.824 1.001 4100
## H[17]
              3.816
                               0.856
                                               8.672 1.001 9600
                       2.041
                                       3.497
               0.402
## b
                       0.079
                               0.264
                                       0.395
                                               0.578 1.001 15000
                                               1.261 1.001 11000
## sigmaProc
               0.775
                       0.200
                               0.479
                                       0.744
## deviance 117.394
                       6.889 105.810 116.757 132.765 1.001 15000
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
##
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 23.7 and DIC = 141.1
## DIC is an estimate of expected predictive error (lower deviance is better).
Le paramètre b_1 est estimé très proche de la valeur qu'on trouve dans le Tableau 4.
mod1 sweden$BUGSoutput$mean$b
## [1] 0.4016313
Idem pour la Norvège. On prépare les données.
bugs.data <- list(</pre>
   nyears = 19,
   y = dat_norway$census,
   q = dat norway$quota 1)
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("b", "sigmaProc","H")
bugs.chains <- 3
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 19
## Unobserved stochastic nodes: 21
## Total graph size: 118
##
## Initializing model
```

Jetons un coup d'oeil aux estimations.

## H[16]

```
print(mod1_norway, intervals = c(2.5/100, 50/100, 97.5/100))
```

```
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba2
## 3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
## n.sims = 15000 iterations saved
            mu.vect sd.vect
                              2.5%
                                       50%
                                            97.5% Rhat n.eff
            131.554 10.999 110.967 131.229 154.279 1.001 5700
## H[1]
## H[2]
            152.424 11.889 130.139 152.145 176.567 1.001 15000
## H[3]
            134.849 11.144 114.036 134.445 157.925 1.001 14000
## H[4]
            137.562 11.180 116.786 137.159 160.529 1.001 15000
## H[5]
            121.949 10.518 102.434 121.539 143.839 1.001 15000
## H[6]
            ## H[7]
             85.564
                     8.646
                           69.626 85.283 103.406 1.001 15000
## H[8]
             54.541
                     6.714
                            41.857
                                   54.317
                                           68.301 1.001 15000
## H[9]
             54.072
                     6.667
                            41.707
                                   53.782
                                           67.759 1.001 15000
## H[10]
             55.497
                     7.089 42.489 55.279
                                           69.916 1.001 15000
## H[11]
             78.110
                     8.295
                            62.628 77.861 95.160 1.001 15000
                     9.268 81.272 98.154 117.447 1.001 13000
## H[12]
             98.468
## H[13]
            119.852 10.236 100.565 119.638 140.342 1.001 15000
            148.542 11.684 126.391 148.401 171.981 1.001 11000
## H[14]
## H[15]
            169.836 12.555 146.086 169.553 195.171 1.001 15000
```

```
## H[17]
           ## H[18]
            81.017 8.326 65.595 80.735 98.042 1.001 6900
## H[19]
            88.024
                   8.613 71.970 87.767 105.559 1.001 11000
             1.560
                   0.101
                            1.360
                                          1.758 1.001 15000
## b
                                   1.560
## sigmaProc
             0.262
                    0.058
                            0.170
                                   0.255
                                          0.397 1.001 15000
## deviance 142.562
                   6.433 132.069 141.859 156.892 1.001 15000
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 20.7 and DIC = 163.3
## DIC is an estimate of expected predictive error (lower deviance is better).
```

Le paramètre  $b_1$  est estimé proche de la valeur qu'on trouve dans le Tableau 4.

```
mod1_norway$BUGSoutput$mean$b
```

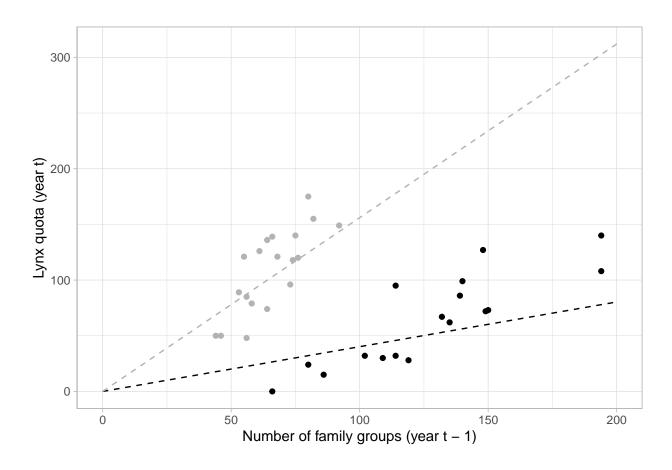
#### ## [1] 1.559921

Graphiquement, on obtient.

```
swgrid <- seq(0, 200, length.out = length(dat_sweden$census))
nwgrid <- seq(0, 200, length.out = length(dat_norway$census))
ggplot() +
    geom_point(data = dat_sweden, aes(x = census, y = quota_1), color = "black") +
    geom_point(data = dat_norway, aes(x = census, y = quota_1), color = "gray70") +
    geom_line(data = dat_sweden, aes(x = swgrid, y = mod1_sweden$BUGSoutput$mean$b * swgrid), color = "bl
    geom_line(data = dat_norway, aes(x = nwgrid, y = mod1_norway$BUGSoutput$mean$b * nwgrid), color = "gr
    expand_limits(x = 0, y = 0) +
    labs(x = "Number of family groups (year t - 1)",
        y = "Lynx quota (year t)")</pre>
```

## Warning in mod1\_sweden\$BUGSoutput\$mean\$b \* swgrid: Recycling array of length 1 in array-vector arith
## Use c() or as.vector() instead.

## Warning in mod1\_norway\$BUGSoutput\$mean\$b \* nwgrid: Recycling array of length 1 in array-vector arith
## Use c() or as.vector() instead.



#### Modèle 2

On écrit le modèle. La différence avec le modèe 1 est qu'on estime une ordonnée à l'origine.

```
model2 <- function(){</pre>
  # Priors
  sigmaProc ~ dunif(0, 4)
  tauProc <- 1/sigmaProc^2</pre>
  b[1] ~ dnorm(0, 1000)
  b[2] ~ dnorm(0, 1000)
  # Process model
  for (t in 1:(nyears)) {
    mu[t] \leftarrow log(b[1] + b[2] * y[t])
     mu[t] \leftarrow log(b[1] + b[2] * y[t]) * index[t]
     index[t] \leftarrow -1000 * step(y[t] + b[1] / b[2]) # step(x) = 1 if x >= 0
     index[t] \leftarrow step(q[t]) \# step(x) = 1 \ if \ x \ge 0
     mu[t] \leftarrow log(b[1] + b[2] * y[t])
    Hproc[t] <- max(0, mu[t])</pre>
    H[t] ~ dlnorm(Hproc[t], tauProc)
# les lignes de code suivantes donnent un ajustement pas mal, mais
# sauf qu'à l'approche de census == 0 on a harvest == 0
   Hproc[t] \leftarrow log(b[1] + b[2] * y[t])
   H[t] ~ dlnorm(Hproc[t], tauProc)
    }
```

```
# Observation model
for (t in 1:nyears) {
   q[t] ~ dpois(H[t])
}
```

On prépare les données pour la Suède.

```
bugs.data <- list(
    nyears = 17,
    y = dat_sweden$census,
    q = dat_sweden$quota_1)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("b", "sigmaProc")
bugs.chains <- 3
bugs.inits <- function(){
    list(
    )
}</pre>
```

Allez zooh, on lance la machine!

```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 17
## Unobserved stochastic nodes: 20
## Total graph size: 122
##
## Initializing model
```

Jetons un coup d'oeil aux estimations.

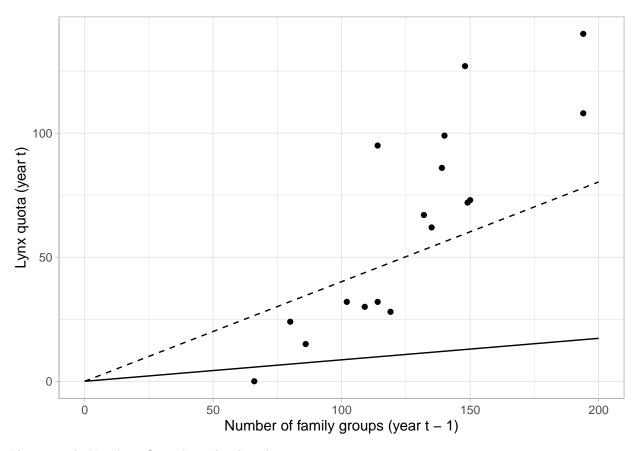
```
print(mod2_sweden, intervals = c(2.5/100, 50/100, 97.5/100))
```

```
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba3
## 3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
## n.sims = 15000 iterations saved
```

```
97.5% Rhat n.eff
##
           mu.vect sd.vect
                             2.5%
                                      50%
## b[1]
            0.001 0.032 -0.062 0.001 0.063 1.001 9200
                            0.042
## b[2]
              0.087
                      0.024
                                      0.086 0.136 1.001 9900
                      0.485 1.210
                                      1.885
                                              3.114 1.001 15000
## sigmaProc 1.956
## deviance 111.594
                     5.872 101.977 110.971 124.688 1.001 9800
##
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
##
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 17.2 and DIC = 128.8
## DIC is an estimate of expected predictive error (lower deviance is better).
Les paramètres b sont estimés comme suit.
mod2_sweden$BUGSoutput$mean$b
## [1] 0.0005412535 0.0865190161
Le ratio se calcule comme suit.
- mod2_sweden$BUGSoutput$mean$b[1] / mod2_sweden$BUGSoutput$mean$b[2]
## [1] -0.006255891
lm(q ~ y, data = bugs.data)
##
## Call:
## lm(formula = q ~ y, data = bugs.data)
## Coefficients:
## (Intercept)
##
      -64.757
                    1.009
glm(q ~ y, data = bugs.data, family = "poisson")
## Call: glm(formula = q ~ y, family = "poisson", data = bugs.data)
## Coefficients:
## (Intercept)
      2.10350
                   0.01504
##
##
## Degrees of Freedom: 16 Total (i.e. Null); 15 Residual
## Null Deviance:
                       481.8
## Residual Deviance: 178.1
                              AIC: 276
```

Graphiquement, on obtient.

## Warning in mod1\_sweden\$BUGSoutput\$mean\$b \* swgrid: Recycling array of length 1 in array-vector arith
## Use c() or as.vector() instead.



Idem pour la Norvège. On prépare les données.

```
bugs.data <- list(
    nyears = 19,
    y = dat_norway$census,
    q = dat_norway$quota_1)</pre>
```

On précise les paramètres à estimer et le nombre de chaines de MCMC (j'en prends trois ici).

```
bugs.monitor <- c("b", "sigmaProc","H")
bugs.chains <- 3
bugs.inits <- function(){
    list(</pre>
```

```
)
}
```

Allez zooh, on lance la machine!

```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 19
## Unobserved stochastic nodes: 22
## Total graph size: 136
##
## Initializing model
```

Jetons un coup d'oeil aux estimations.

```
print(mod2\_norway, intervals = c(2.5/100, 50/100, 97.5/100))
```

```
## Inference for Bugs model at "/var/folders/r7/j0wqj1k95vz8w44sdxzm986c0000gn/T//RtmpZaM5Ca/model3dba5
   3 chains, each with 1e+05 iterations (first 50000 discarded), n.thin = 10
   n.sims = 15000 iterations saved
##
##
            mu.vect sd.vect
                                       50%
                                             97.5% Rhat n.eff
                              2.5%
## H[1]
            135.692 11.600 113.919 135.380 159.185 1.001 15000
## H[2]
            154.654 12.376 131.473 154.214 180.212 1.001 15000
            138.665 11.766 116.793 138.306 162.531 1.001 15000
## H[3]
            139.543 11.704 117.552 139.355 163.182 1.001 15000
## H[4]
## H[5]
            125.724 11.270 104.445 125.397 148.736 1.001 15000
## H[6]
            120.823 10.938 100.586 120.514 143.319 1.001 10000
## H[7]
             84.684
                     9.203 67.455 84.328 103.645 1.001 15000
## H[8]
             49.716
                     7.025
                            36.852 49.398
                                           64.364 1.001 15000
## H[9]
             49.721
                                    49.358
                      7.075
                            36.817
                                            64.835 1.001 12000
## H[10]
             47.800
                      6.980
                            35.223 47.436
                                            62.252 1.001 15000
## H[11]
             73.576
                      8.579
                            57.782
                                    73.234
                                            91.432 1.001 13000
## H[12]
             95.763
                      9.684
                            77.783 95.426 115.330 1.001 14000
## H[13]
            119.511
                     10.990
                            99.042 119.257 141.878 1.001 15000
## H[14]
            148.676 12.280 125.624 148.415 173.373 1.001 15000
## H[15]
            174.670 13.356 149.538 174.325 201.547 1.001 15000
## H[16]
            ## H[17]
            120.656 11.072
                            99.777 120.354 143.377 1.001 15000
## H[18]
             78.717
                      8.875 62.031
                                   78.453 97.045 1.001 7800
## H[19]
             88.776
                      9.418 71.326 88.446 108.044 1.001 12000
              0.002
                      0.032 -0.061
                                     0.002
                                            0.064 1.001 15000
## b[1]
```

```
## b[2]
              0.082
                      0.023
                              0.040
                                      0.081
                                              0.131 1.001 9600
              3.070 0.467
                              2.202
                                      3.065
                                              3.910 1.001 15000
## sigmaProc
## deviance 141.936
                     6.244 131.657 141.298 156.111 1.001 15000
##
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 19.5 and DIC = 161.4
## DIC is an estimate of expected predictive error (lower deviance is better).
```

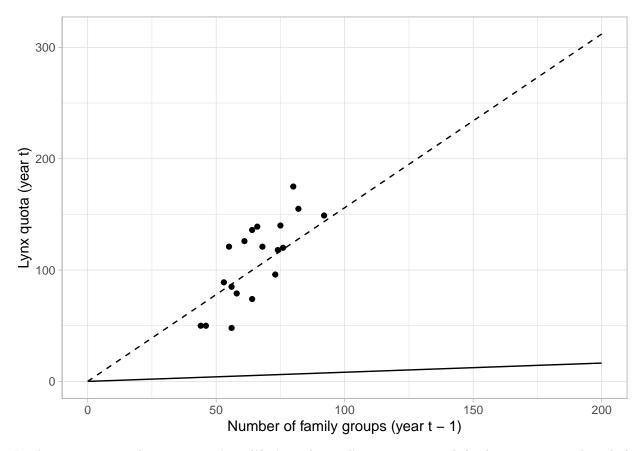
Le paramètre  $b_1$  est estimé proche de la valeur qu'on trouve dans le Tableau 4.

```
mod2_norway$BUGSoutput$mean$b
```

```
## [1] 0.001526982 0.082346563
```

Graphiquement, on obtient.

## Warning in mod1\_norway\$BUGSoutput\$mean\$b \* nwgrid: Recycling array of length 1 in array-vector arith
## Use c() or as.vector() instead.



Je n'arrive pas reproduire ce satané modèle à seuil avec l'intercept non-nul, les lignes en trait plein de la figure 4 du papier. Grrrr. On arrive aux estimations du Tableau 3 via une simple régression hein, donc c'est pas bien grave.