## MARSS and Hwange data

24/09/2020

## Read in and visualize data

Prerequisites.

```
library(tidyverse)
theme_set(theme_light())
library(janitor)
library(lubridate)
library(MARSS)
```

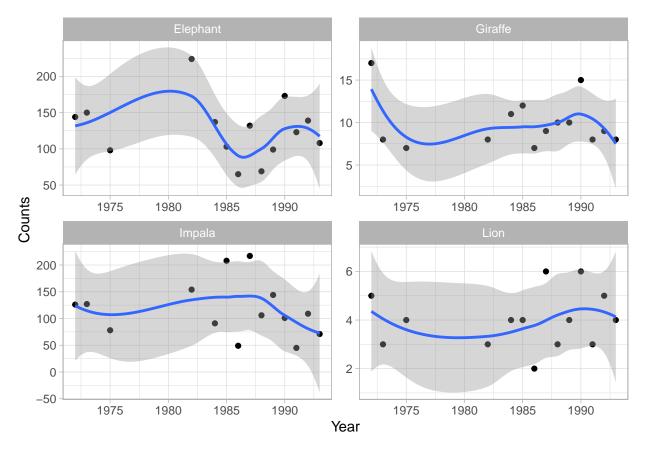
Read in the data.

## 2 Zebra

```
wps7293 <- readxl::read_xls("data/Water point surveys 1972 - 1993 - Total Number.xls") %>% clean_names(
wps2001 <- readxl::read_xls("data/Water point surveys 1994 - 2001 - Detailled.xls") %>% clean_names()
wps2005 <- readxl::read_xls("data/Water point surveys 2002 - 2005 - Detailed.xls") %>% clean_names()
wps7293 %>%
 count(water_point, sort = TRUE)
## # A tibble: 175 x 2
##
     water_point n
##
      <chr>
                  <int>
## 1 NGWESHLA
                    173
## 2 KENNEDY 1
                    172
## 3 KENNEDY 2
                    167
## 4 NYAMANDHLOVU 167
## 5 SAMAVUNDHLA
                    159
## 6 MAKOLOLO I
                    154
## 7 MAKWA
                    150
## 8 BIG TOMS
                    148
## 9 LIVINGI
## 10 MASUMA DAM
## # ... with 165 more rows
wps7293 %>%
  count(species, sort = TRUE)
## # A tibble: 32 x 2
##
      species
                             n
##
      <chr>>
                         <int>
## 1 Elephant
                           802
                           706
```

```
## 3 Kudu
                           697
## 4 Warthog
                           678
## 5 Giraffe
                           588
## 6 Impala
                           585
## 7 Spotted hyaena
                           572
## 8 Sable
                           554
## 9 Buffalo
                           527
## 10 Black Backed Jackal
                           448
## # ... with 22 more rows
wps7293 %>%
count(year, sort = TRUE)
## # A tibble: 14 x 2
##
      year
               n
##
      <dbl> <int>
## 1 1990
             918
## 2 1992
             854
## 3 1988
             820
## 4 1982
             795
## 5 1989
             701
## 6 1991
             696
## 7 1987
             689
## 8 1993
             626
## 9 1985
             556
## 10 1984
             501
## 11 1973
             456
## 12 1975
             357
## 13 1986
             311
## 14 1972
             150
dat <- wps7293 %>%
 filter(species %in% c("Elephant", "Giraffe", "Lion", "Impala")) %>%
  select(year, species, total) %>%
 mutate(species = as_factor(species))
dat
## # A tibble: 2,252 x 3
      year species total
##
      <dbl> <fct>
                    <dbl>
## 1 1972 Elephant
                       24
## 2 1972 Giraffe
## 3 1972 Impala
                        6
## 4 1972 Elephant
                      303
## 5 1972 Giraffe
                       25
## 6 1972 Lion
## 7 1972 Elephant
                      129
## 8 1972 Giraffe
                       10
## 9 1972 Impala
                      511
## 10 1972 Lion
## # ... with 2,242 more rows
```

Plot all data.



## MARSS model in the frequentist framework

We consider a model with the following assumptions: \* All prey species share the same process variance. \* All predator species share the same process variance. \* Prey and predator species have different measurement variances. \* Measurement errors are independent. \* Process errors are independent.

We fit this model with the MARSS package. We need to specify the ingredients first.

```
Q <- matrix(list(0), 4, 4)
diag(Q) <- c("Prey", "Prey", "Prey", "Predator")
R <- matrix(list(0), 4, 4)
diag(R) <- c("Prey", "Prey", "Prey", "Predator")
model.0 <- list(
    B = "unconstrained", U = "zero", Q = Q,</pre>
```

```
Z = "identity", A = "zero", R = R,
 x0 = "unequal", tinitx = 1
model.0
## $B
## [1] "unconstrained"
##
## $U
## [1] "zero"
##
## $Q
##
        [,1]
               [,2]
                      [,3]
                              [,4]
## [1,] "Prey" 0
                      0
## [2,] 0
               "Prey" 0
                              0
                      "Prey" 0
## [3,] 0
               0
## [4,] 0
               0
                      0
                              "Predator"
##
## $Z
## [1] "identity"
##
## $A
## [1] "zero"
## $R
        [,1]
               [,2]
                      [,3]
                              [,4]
## [1,] "Prey" 0
                      0
                              0
               "Prey" 0
                              0
## [2,] 0
                      "Prey" 0
## [3,] 0
               0
## [4,] 0
               0
                      0
                              "Predator"
##
## $x0
## [1] "unequal"
##
## $tinitx
## [1] 1
Then we fit the model.
mod.0 <- dat %>%
  group_by(year, species) %>%
  summarise(mean_biomass = round(mean(total))) %>%
  ungroup() %>%
  pivot_wider(names_from = species, values_from = mean_biomass) %>%
  select(-year) %>%
  t() %>%
  MARSS(model = model.0)
## Stopped at iter=227 in MARSSkem at x0 update.
## There are 0s on R diagonal. x0 assoc with these must be fixed (not estimated)
## when using the EM algorithm. Try method="BFGS". Type MARSSinfo("xORO") for help.
## par, kf, states, iter, loglike are the last values before the error.
## Try control$safe=TRUE which uses a slower but slightly more robust algorithm.
## Use control$trace=1 to generate a more detailed error report. See user guide for insight.
```

We may get the estimates in a more readable format. For example, let's have a look to the interactions. These estimates describe the effect of the density of species j on the per capita growth rate of species i.

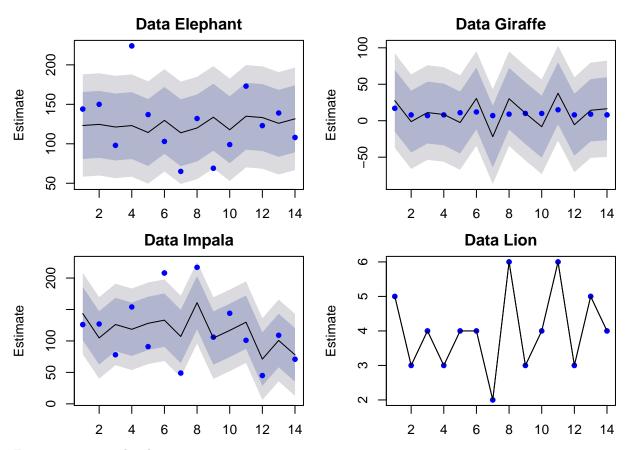
```
B.0 <- coef(mod.0, type = "matrix")$B[1:4, 1:4]
rownames(B.0) <- colnames(B.0) <- c("Elephant", "Giraffe", "Impala", "Lion")
print(B.0, digits = 2)</pre>
```

```
##
            Elephant Giraffe
                                Impala
                                         Lion
                0.604
                                0.1141
                                        11.03
## Elephant
                       -0.775
## Giraffe
               -0.282
                       -1.459
                                0.0186
                                        14.19
## Impala
                0.466
                       -1.159
                                1.0190 -13.40
## Lion
                0.026
                       -0.086 -0.0017
                                         0.43
```

The effect of species j on species i is given by the cell at i-th row and j-th column. The B matrix suggests that Lion has a negative effect on impala and positive on Elephant and Giraffe. In the diagonal, we have the strength of density-dependence: if species i is density-independent, then  $B_{i,i}$  equals 1, like Impala; smaller  $B_{i,i}$  means more density dependence, like Giraffe.

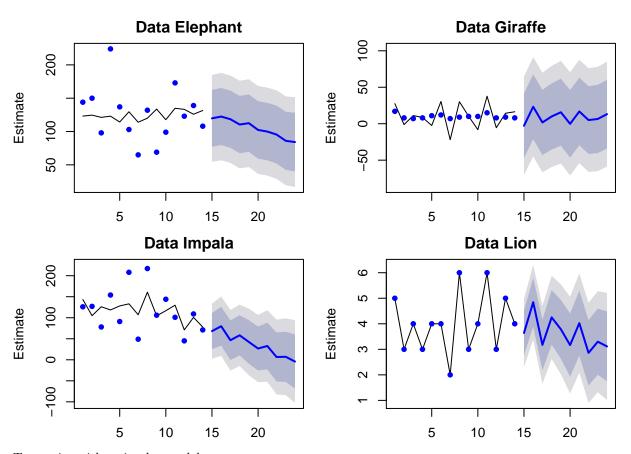
Compare observations to fitted values.

```
fr <- forecast.marssMLE(mod.0, h=0)
plot(fr)</pre>
```



Forecast 10 years ahead.

```
fr <- forecast.marssMLE(mod.0, h = 10)
plot(fr)</pre>
```



Try again, with a simpler model.

```
Q <- matrix(list(0), 4, 4)
diag(Q) <- c("all", "all", "all", "all")
R <- matrix(list(0), 4, 4)
diag(R) <- c("all", "all", "all", "all")
model.0 <- list(
    B = "unconstrained", U = "zero", Q = Q,
    Z = "identity", A = "zero", R = R,
    x0 = "unequal", tinitx = 1
)
model.0</pre>
```

```
## $B
## [1] "unconstrained"
##
## $U
## [1] "zero"
##
## $Q
## [,1] [,2] [,3] [,4]
## [1,] "all" 0 0 0
## [2,] 0 "all" 0
```

```
0 "all" 0
## [3,] 0
## [4,] 0
              0
                    0
                          "all"
##
## $Z
## [1] "identity"
##
## $A
## [1] "zero"
##
## $R
        [,1] [,2] [,3] [,4]
## [1,] "all" 0
                    0
## [2,] 0
              "all" 0
                          0
                    "all" 0
## [3,] 0
              0
## [4,] 0
              0
                    0
                          "all"
##
## $x0
## [1] "unequal"
## $tinitx
## [1] 1
Then we fit the model.
mod.0 <- dat %>%
  group_by(year, species) %>%
  summarise(mean_biomass = round(mean(total))) %>%
  ungroup() %>%
 pivot_wider(names_from = species, values_from = mean_biomass) %>%
  select(-year) %>%
 t() %>%
 MARSS(model = model.0)
## Warning! Reached maxit before parameters converged. Maxit was 500.
## neither abstol nor log-log convergence tests were passed.
##
## MARSS fit is
## Estimation method: kem
## Convergence test: conv.test.slope.tol = 0.5, abstol = 0.001
## WARNING: maxit reached at 500 iter before convergence.
## Neither abstol nor log-log convergence test were passed.
## The likelihood and params are not at the ML values.
## Try setting control$maxit higher.
## Log-likelihood: -213.3287
## AIC: 470.6574
                 AICc: 501.3241
##
##
                  Estimate
## R.all
                  15.33054
## B.(1,1)
                  -0.00245
## B.(2,1)
                  0.02059
## B.(3,1)
                  0.04521
## B.(4,1)
                  -0.01532
```

## B.(1,2)

13.11363

```
## B.(2,2)
                   0.20074
## B.(3,2)
                   9.89028
                   0.72821
## B.(4,2)
## B.(1,3)
                  -0.30259
## B.(2,3)
                   0.03413
## B.(3,3)
                   0.47642
## B.(4,3)
                  -0.00785
## B.(1,4)
                   8.13902
## B.(2,4)
                   0.18946
## B.(3,4)
                 -11.47843
## B.(4,4)
                  -0.16077
## Q.all
                   7.35896
## x0.X.Elephant 143.82620
## x0.X.Giraffe
                  11.54587
## x0.X.Impala
                 125.70464
## x0.X.Lion
                   4.60775
## Initial states (x0) defined at t=1
##
## Standard errors have not been calculated.
## Use MARSSparamCIs to compute CIs and bias estimates.
##
## Convergence warnings
## Warning: the R.all parameter value has not converged.
## Warning: the Q.all parameter value has not converged.
## Warning: the logLik parameter value has not converged.
## Type MARSSinfo("convergence") for more info on this warning.
```

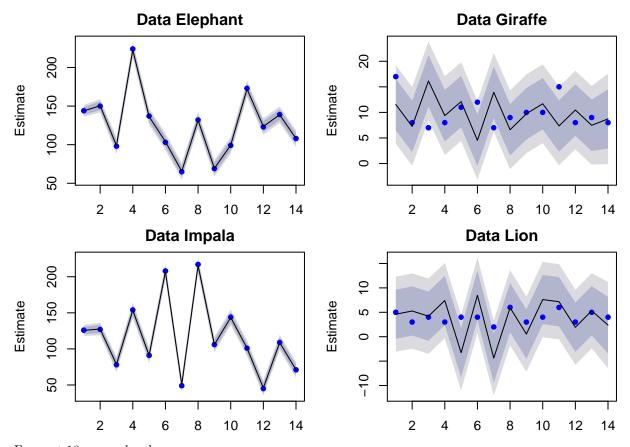
We may get the estimates in a more readable format. For example, let's have a look to the interactions. These estimates describe the effect of the density of species j on the per capita growth rate of species i.

```
B.0 \leftarrow coef(mod.0, type = "matrix") \$B[1:4, 1:4]
rownames(B.0) <- colnames(B.0) <- c("Elephant", "Giraffe", "Impala", "Lion")
print(B.0, digits = 2)
            Elephant Giraffe Impala
##
                                        Lion
## Elephant -0.0024
                        13.11 -0.3026
                                        8.14
## Giraffe
              0.0206
                         0.20 0.0341
                                        0.19
              0.0452
## Impala
                         9.89 0.4764 -11.48
## Lion
             -0.0153
                         0.73 -0.0079 -0.16
```

The effect of species j on species i is given by the cell at i-th row and j-th column. The B matrix suggests that Lion has a negative effect on impala and positive on Elephant and Giraffe. In the diagonal, we have the strength of density-dependence: if species i is density-independent, then  $B_{i,i}$  equals 1, like Impala; smaller  $B_{i,i}$  means more density dependence, like Giraffe.

Compare observations to fitted values.

```
fr <- forecast.marssMLE(mod.0, h=0)
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Forecast 10 years ahead.

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