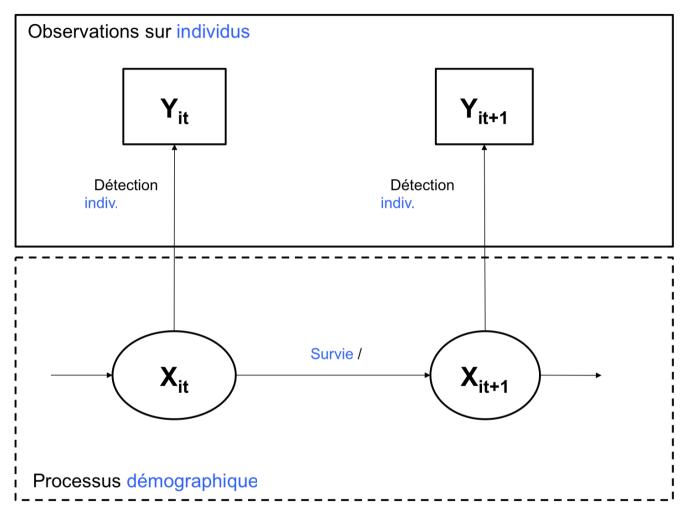
# Local minima and capturerecapture models

Olivier Gimenez

### Multistate capture-recapture models

- Individual data on marked animals/plants
- Repeated sampling in time
- Survival, movement between states
- States = sites, breeding, disease, behavior
- Individual detectability < 1, heterogeneous</li>
- Lebreton, J.-D., Nichols, J.D., Barker, R.J., Pradel, R. & Spendelow, J.A. (2009) Modeling Individual Animal Histories with Multistate Capture-Recapture Models. Advances In Ecological Research, 41, 87–173.

#### CR models are hierarchical



- Gimenez, O., Lebreton, J.-D., Gaillard, J.-M., Choquet, R. & Pradel, R. (2012) Estimating demographic parameters using hidden process dynamic models. TPB, 82, 307–316.
- Gimenez, O., Rossi, V., Choquet, R., Dehais, C., Doris, B., Varella, H., Vila, J.-P. & Pradel, R. (2007) State-space modelling of data on marked individuals. Ecol Mod, 206, 431–438.

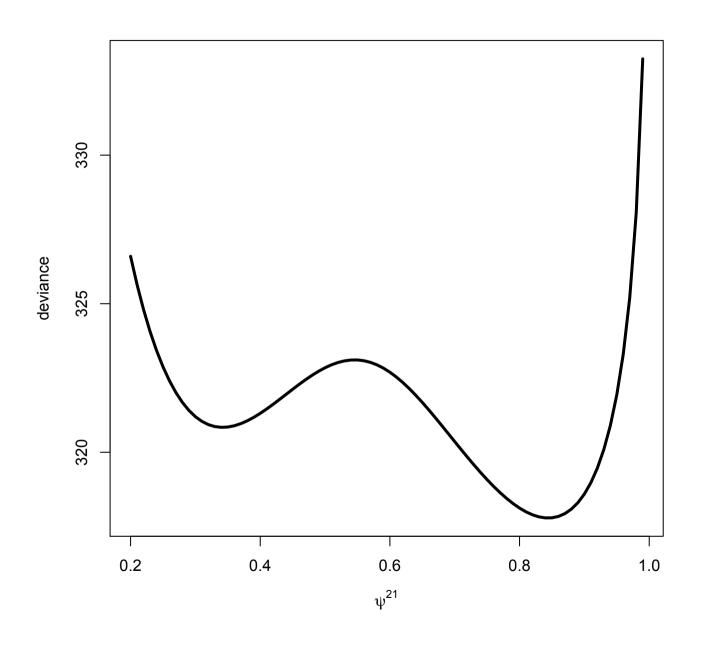
#### Simulated data

- 2 states, 7 occasions
- Survival = 1, detection = 0.6
- Transition 1 -> 2 = 0.6
- Transition 2 -> 1 = 0.85

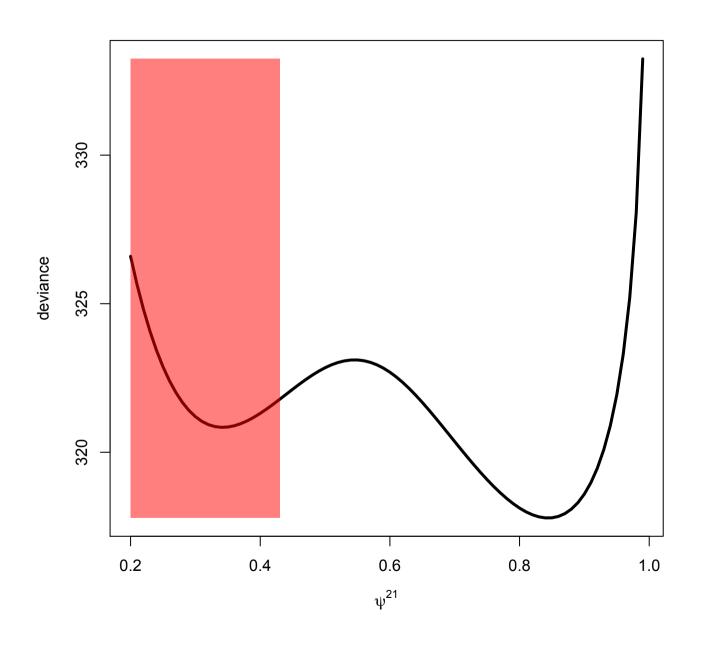
```
2021202 4; 1110101 4;
2020201 4; 1010101 4;
2020202 4; 1010102 4;
2201021 4; 2102011 4;
```

• Courtesy of J. Dupuis; cf. Gimenez, O., Choquet, R., Lamor, L., Scofield, P., Fletcher, D., Lebreton, J.-D. & Pradel, R. (2005) Efficient profile-likelihood confidence intervals for capture-recapture models. Journal of Agricultural, Biological, and Environmental Statistics, 10, 184–196.

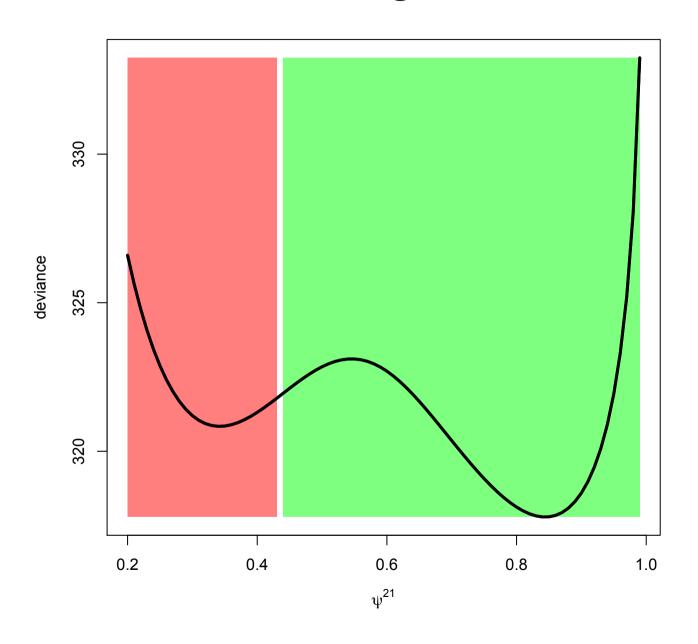
#### Deviance as a function of transition 2->1



#### Initial values lead to local minimum



#### Initial values lead to global minimum



#### Influence of link function?

- By link function, I mean:
   f(ψ) = β and β is estimated on ]-∞,+∞[
- Alternative: constrained optimisation

### Influence of link function?

• Sin link function:  $\Psi^{12} = 0.25$ ;  $\Psi^{21} = 0.34$ !

$$\Psi^{12} = 0.6$$
;  $\Psi^{21} = 0.85$ 

### Influence of link function?

- Sin link function:  $\Psi^{12} = 0.25$ ;  $\Psi^{21} = 0.34$ !
- Logit link function:  $\Psi^{12} = 0.60$ ;  $\Psi^{21} = 0.84$

$$\Psi^{12} = 0.6$$
;  $\Psi^{21} = 0.85$ 

### Quasi-Newton (BFGS) vs. simulated annealing

• Sin link function BFGS:  $\Psi^{12} = 0.25$ ;  $\Psi^{21} = 0.34$ 

$$\Psi^{12} = 0.6$$
;  $\Psi^{21} = 0.85$ 

### Quasi-Newton (BFGS) vs. simulated annealing

- Sin link function BFGS:  $\Psi^{12} = 0.25$ ;  $\Psi^{21} = 0.34$
- Sin link function SA:  $\Psi^{12} = 0.60$ ;  $\Psi^{21} = 0.84$

$$\Psi^{12} = 0.6$$
;  $\Psi^{21} = 0.85$ 

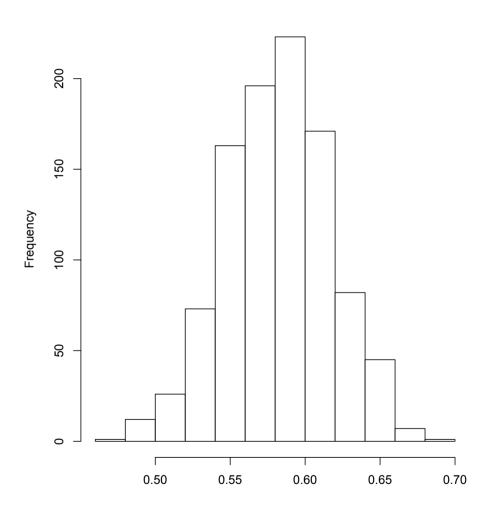
### Quasi-Newton (BFGS) vs. simulated annealing

- Sin link function BFGS:  $\Psi^{12} = 0.25$ ;  $\Psi^{21} = 0.34$
- Sin link function SA:  $\Psi^{12} = 0.60$ ;  $\Psi^{21} = 0.84$
- But: SA is much (much) slower than BFGS

$$\Psi^{12} = 0.6$$
;  $\Psi^{21} = 0.85$ 

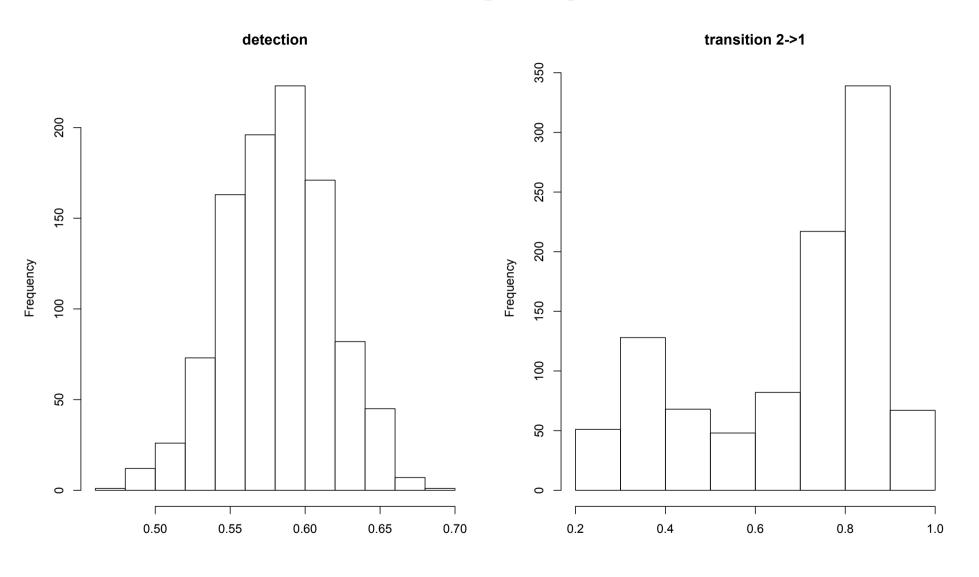
## **MCMC**





detection = 0.6

### **MCMC**



 $\Psi^{21} = 0.85$  (sin link)

## **Implementation**

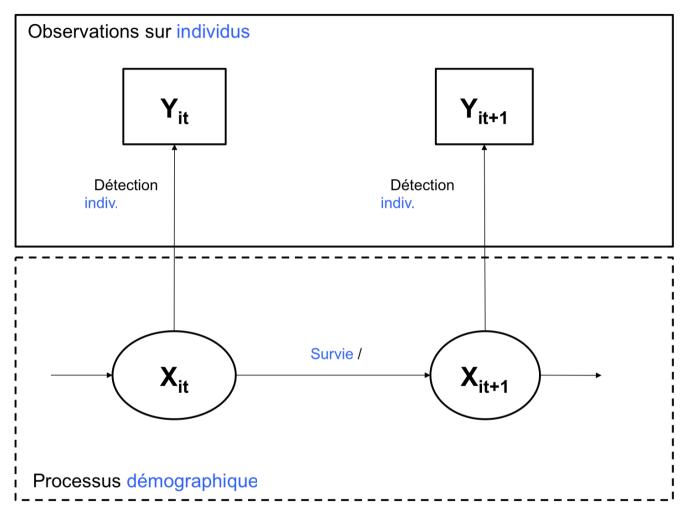
- Mark called from R using package Rmark
- Jags called from R using package R2jags
- Code and slides available on GitHub:

```
https://github.com/oliviergimenez/multistate local minima
```

## **Ongoing work**

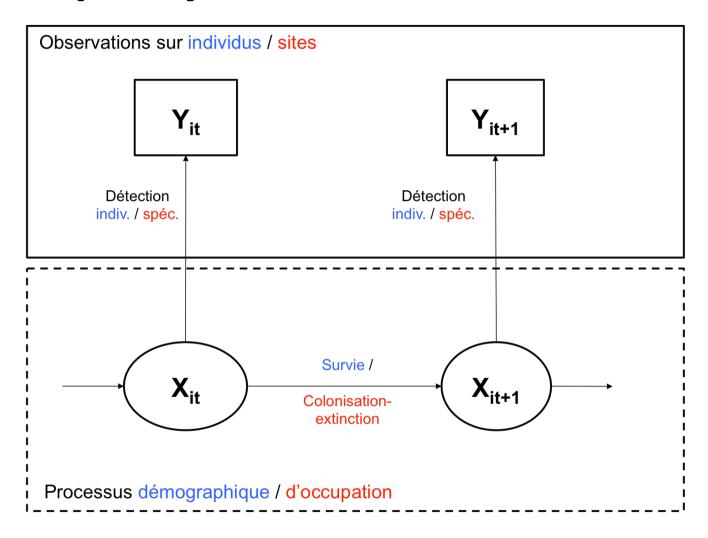
Local minima in dynamic occupancy models?

#### CR models are hierarchical



- Gimenez, O., Lebreton, J.-D., Gaillard, J.-M., Choquet, R. & Pradel, R. (2012) Estimating demographic parameters using hidden process dynamic models. TPB, 82, 307–316.
- Gimenez, O., Rossi, V., Choquet, R., Dehais, C., Doris, B., Varella, H., Vila, J.-P. & Pradel, R. (2007) State-space modelling of data on marked individuals. Ecol Mod, 206, 431–438.

### Occupancy models are hierarchical



• Gimenez, O., Blanc, L., Besnard, A., Pradel, R., Doherty, P.F., Marboutin, E. & Choquet, R. (2014) Fitting occupancy models with E-SURGE: Hidden Markov modelling of presenceabsence data. Methods in Ecology and Evolution, 5, 592–597.

## **Explore other avenues...**

BIOMETRICS 57, 240-244

Minimising model fitting objectives that contain spurious local minima by bootstrap restarting

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#### An escape-from-local minima technique in unconstrained optimization using a grid-like approach and interval equations

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GR 265 04 Rio, Greece,
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Key words: Global Optimization, grid-like technique, interval equations, escape from local minima.

3rd International Conference on Experiments/Process/System Modeling/Sim



#### Journal of Statistical Software

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http://www.istatsoft.org/

Genetic Optimization Using Derivatives: The rgenoud Package for R

Walter R. Mebane, Jr. University of Michigan Jasjeet S. Sekhon UC Berkelev

Regrouping Particle Swarm Optimization: A New Global Optimization Algorithm with Improved Performance Consistency Across Benchmarks

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#### MULTISTART OPTIMIZATION WITH A TRAINABLE DECISION MAKER FOR AVOIDING HIGH-VALUED LOCAL MINIMA

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