

## Homework I: Graph Theory

### Vertex and edge sets

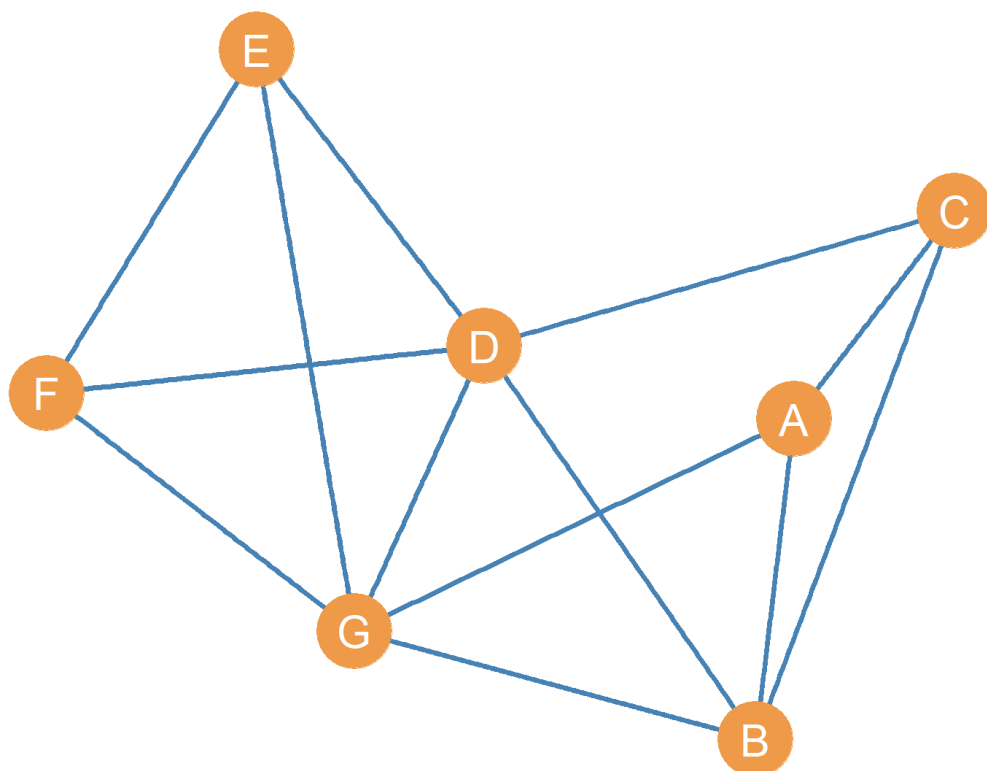
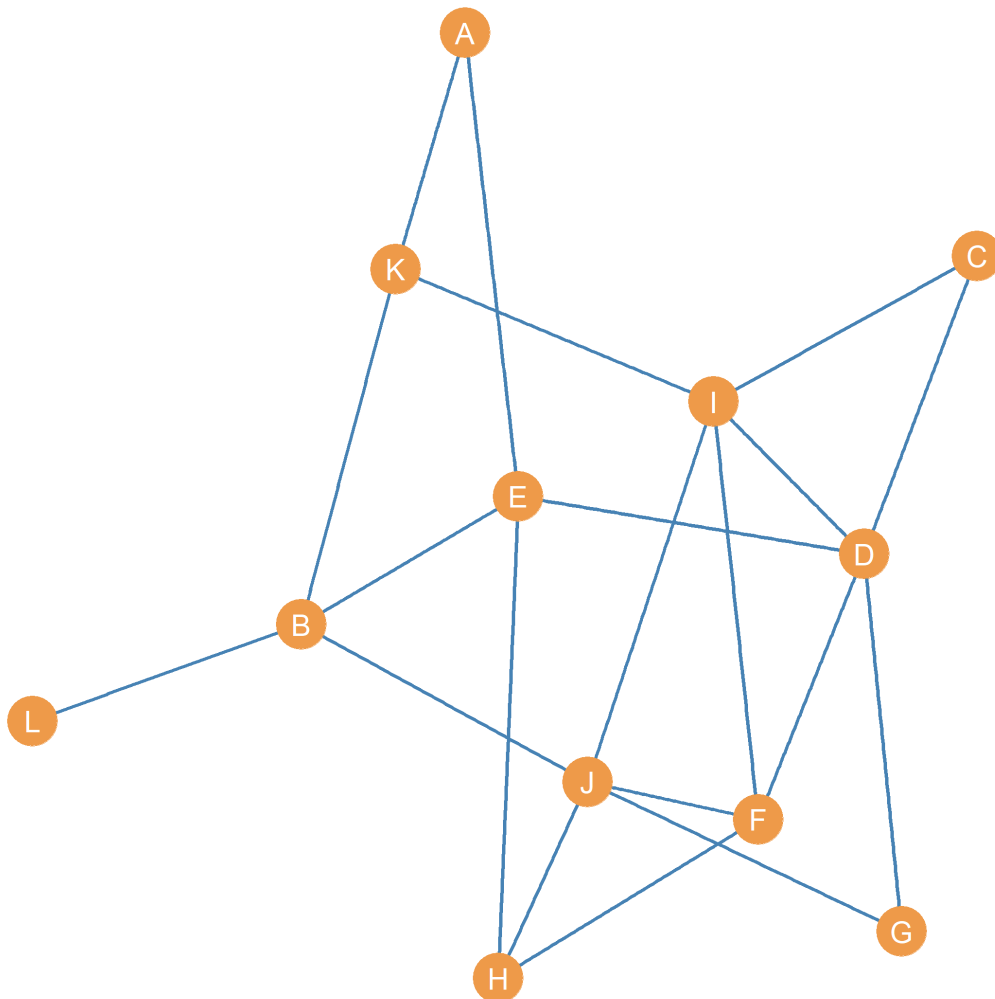


Figure 1: A simple graph.

Consider the graph shown in [Figure 1](#):

1. Write down the **vertex set** of the graph:
2. Write down the **edge set** of the graph:

## Node Neighborhoods



*Figure 2: Another simple graph.*

Consider the graph shown in [Figure 2](#):

1. Write down the **neighborhood** of node *D*
2. Write down the **neighborhood** of node *K*

3. What is the **intersection** of the neighborhoods of nodes  $D$  and  $I$ ?
4. What is the **intersection** of the neighborhoods of nodes  $E$  and  $F$ ?
5. What is the **union** of the neighborhoods of nodes  $H$  and  $J$ ?

### Node Degree

Consider the graph shown in [Figure 2](#):

1. What is the **degree** of node  $B$ ?
2. What is(are) the node(s) with the largest **degree**?
3. What is(are) the node(s) with the smallest **degree**?

### Subgraphs

1. Go back to [Figure 1](#). Draw the **node-deleted** subgraph of this graph that *excludes* nodes  $D$  and  $G$

