Day10

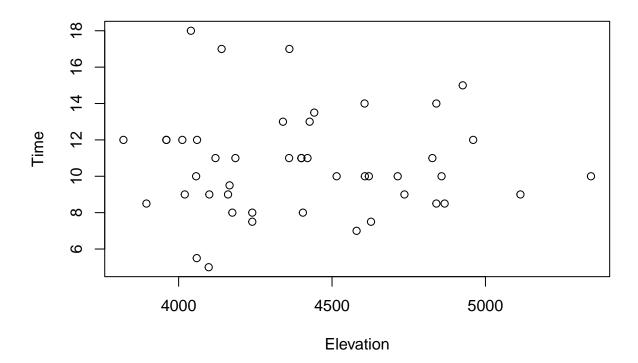
Olivia Wu

2024-03-19

Problem 4.2

a) The correlation coefficient between these two variables is 0.016, which is extremely small. Additionally, the scatterplot shows a very weak linear relationship with no clear direction.

[1] -0.0162768



b) The p-value of Elevation is 0.016 < 0.05, so it is significant. Both predictors can explain the model because they each have small p-values. The \mathbb{R}^2 is larger for the two-predictor model.

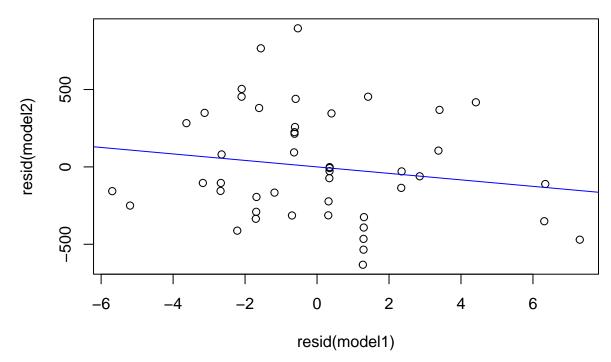
##

Call:

```
## lm(formula = Time ~ Elevation + Length, data = HP)
##
## Residuals:
               1Q Median
##
      Min
                              3Q
                                     Max
## -2.5924 -0.8050 -0.1959 0.6380 3.8432
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 8.0753787 2.5327132
                                    3.188 0.00267 **
## Elevation
             -0.0014483 0.0005805 -2.495 0.01653 *
## Length
              ## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.37 on 43 degrees of freedom
## Multiple R-squared: 0.7703, Adjusted R-squared: 0.7596
## F-statistic: 72.09 on 2 and 43 DF, p-value: 1.844e-14
##
## Call:
## lm(formula = Time ~ Elevation, data = HP)
## Residuals:
               1Q Median
                              3Q
## -5.6912 -1.6985 -0.5639 1.2963 7.3015
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 11.2113764 5.1953800
                                     2.158
                                            0.0364 *
## Elevation
             -0.0001269 0.0011756 -0.108
                                            0.9145
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.826 on 44 degrees of freedom
## Multiple R-squared: 0.0002649, Adjusted R-squared: -0.02246
## F-statistic: 0.01166 on 1 and 44 DF, p-value: 0.9145
##
## Call:
## lm(formula = Time ~ Length, data = HP)
## Residuals:
##
      Min
               1Q Median
                              3Q
                                     Max
## -2.4491 -0.6687 -0.0122 0.5590 4.0034
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.04817
                         0.80371
                                   2.548 0.0144 *
                         0.06162 11.105 2.39e-14 ***
## Length
               0.68427
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.449 on 44 degrees of freedom
## Multiple R-squared: 0.737, Adjusted R-squared: 0.7311
```

```
## F-statistic: 123.3 on 1 and 44 DF, p-value: 2.39e-14
```

c) There is a negative association between the two models, which suggests that adding Elevation is signifi-



cant.

Problem 4.3

a) The best predictors would be ERA, WHIP, HitsAllowed, StrikeOuts, Runs, and more.

```
##
             League BattingAverage
                                                                      Doubles
                                                   Hits
                                                                HR
                                         Runs
                         0.3433983 0.5400781 0.2895004 0.3637802 0.09226302
## [1,] -0.09477801
           Triples
                        RBI
                                     SB
                                              OBP
                                                         SLG
##
                                                                    ERA HitsAllowed
## [1,] -0.2660382 0.544065 -0.2539841 0.6012836 0.4433713 -0.7978057
                                                                           -0.765045
             Walks StrikeOuts
                                   Saves
## [1,] -0.4079906  0.5561356  0.5034185 -0.7782017
```

If we start with ERA, we get:

$$WinPct = \beta_0 + \beta_1 ERA + \beta_2 Runs + \beta_3 Saves + \beta_4 WHIP + \epsilon$$

The \mathbb{R}^2 values is 0.8863.

```
##
## Call:
## Im(formula = MLB$WinPct ~ ERA + Runs + Saves + WHIP, data = MLmod)
```

```
##
## Coefficients:
  (Intercept)
                                    Runs
                                                Saves
                                                              WHIP
     0.5159838
                 -0.0363571
                               0.0005187
                                            0.0026427
                                                        -0.2657969
##
##
## Call:
## lm(formula = MLB$WinPct ~ ERA + Runs + Saves + WHIP, data = MLmod)
## Residuals:
##
                          Median
                                        30
         Min
                    1Q
                                                 Max
  -0.051472 -0.017986 -0.001991 0.017048
                                            0.047963
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.160e-01 1.186e-01
                                       4.351 0.000201 ***
                           2.626e-02
                                      -1.385 0.178402
## ERA
               -3.636e-02
## Runs
                5.187e-04
                          7.764e-05
                                       6.681 5.31e-07 ***
                2.643e-03 6.788e-04
                                       3.893 0.000652 ***
## Saves
## WHIP
               -2.658e-01 1.275e-01 -2.085 0.047457 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02404 on 25 degrees of freedom
## Multiple R-squared: 0.8863, Adjusted R-squared: 0.8681
## F-statistic: 48.7 on 4 and 25 DF, p-value: 1.91e-11
```

- b) The first time around, we drop Doubles. The second time, we drop SB. Then StrikeOuts,SLG, Triples, HR, RBI, ERA, OBP, HitsAllowed, Walks, and Hits. The final predictors or Saves, WHIP, Runs, and BattingAverage. The final R^2 is 0.8836.
 - c) The output shows the best predictors are Runs, Doubles, Saves, and WHIP. \mathbb{R}^2 is 0.885.

```
## Subset selection object
## Call: regsubsets.formula(MLB$WinPct ~ ., nbest = 1, data = MLmod)
## 17 Variables (and intercept)
##
                  Forced in Forced out
## League
                      FALSE
                                  FALSE
                       FALSE
                                  FALSE
## BattingAverage
## Runs
                      FALSE
                                  FALSE
## Hits
                      FALSE
                                  FALSE
## HR
                      FALSE
                                  FALSE
## Doubles
                      FALSE
                                  FALSE
                      FALSE
## Triples
                                  FALSE
## RBI
                      FALSE
                                  FALSE
                      FALSE
## SB
                                  FALSE
## OBP
                      FALSE
                                  FALSE
## SLG
                      FALSE
                                  FALSE
## ERA
                      FALSE
                                  FALSE
## HitsAllowed
                      FALSE
                                  FALSE
## Walks
                      FALSE
                                  FALSE
## StrikeOuts
                      FALSE
                                  FALSE
## Saves
                      FALSE
                                  FALSE
## WHIP
                      FALSE
                                  FALSE
```

```
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
           League BattingAverage Runs Hits HR Doubles Triples RBI SB OBP SLG
     (1)""
                                11 11
## 1
                                                              . . . . . . . . .
     (1)""
                                "*"
                                     11 11
                                          11 11 11 11
## 2
## 3 (1)""
## 4 (1)""
                  11 11
                                     11 11
                                          " " "*"
                                                      11 11
                                                              . . . . . . . . . .
     (1)""
                                "*"
## 5
## 6
     (1)""
## 7 (1)""
                                                             . . . . . . . . .
                  "*"
                                          11 11 11 11
                                                              ## 8 (1)""
           ERA HitsAllowed Walks StrikeOuts Saves WHIP
## 1
    (1)"*"""
                          11 11
                                11 11
                                           11 11
## 2 (1) "*" "
                           11 11
                                11 11
## 3 (1)""""
                           11 11
                                11 11
                                           "*"
## 4 (1)""""
                           11 11
                                           "*"
## 5 (1)""""
                           11 11
## 6 (1) " " " "
                          "*"
                                11 11
                                           "*"
                                                 "*"
## 7 (1) " " *"
                           "*"
                                11 11
## 8 (1)""*"
                                           "*"
                           "*"
                                                 "*"
##
## Call:
## lm(formula = MLB$WinPct ~ Runs + Doubles + Saves + WHIP, data = MLmod)
## Residuals:
                   1Q
                        Median
## -0.041565 -0.012093 -0.002165 0.014349 0.042894
##
## Coefficients:
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.6216851 0.1226586
                                     5.068 3.12e-05 ***
               0.0006352 0.0001040
                                     6.110 2.19e-06 ***
## Runs
## Doubles
              -0.0004463
                         0.0002841
                                    -1.571 0.12876
## Saves
              0.0025272
                         0.0006910
                                     3.658 0.00119 **
## WHIP
              ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0238 on 25 degrees of freedom
## Multiple R-squared: 0.8885, Adjusted R-squared: 0.8707
## F-statistic: 49.82 on 4 and 25 DF, p-value: 1.486e-11
 d) The C_p for each model is 11.11, 11.885, and 10.537.
## [1] 5.00000 11.10941
## [1]
      5.00000 11.83185
      5.00000 10.48566
## [1]
```

e) I would use the third model because it has the lowest C_p and highest \mathbb{R}^2 .