

# Package ‘abc.n’

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**Title** abc.n

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**Depends** R (>= 2.10)

**Description** tools for ABC based on n summary values

**License** GPL (>=2)

**LazyLoad** yes

**Collate** ‘nabc\_functions.R’ ‘KLdiv\_functions.R’

## R topics documented:

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|             |   |
|-------------|---|
| dMuTOST_lkl | <i>Compute the density of the (possible truncated) summary likelihood for population means of normal summary values</i> |
|-------------|---|

---

## Description

Compute the density of the (possible truncated) summary likelihood for population means of normal summary values

## Usage

```
dMuTOST_lkl(rho, n.of.x, s.of.x, norm = 1,
  support = c(-Inf, Inf), log = FALSE)
```

## Arguments

|         |  |
|---------|--|
| rho     | vector of quantile   |
| norm    | normalization constant for the truncated summary likelihood (must be $\leq 1$ ). |
| support | vector of dimension 2. Support of the truncated summary likelihood.              |
| log     | logical; if TRUE, densities d are given as $\log(d)$ .                           |
| n.of.x  | number of observed summary values  |
| s.of.x  | standard deviation of observed summary values                                    |

## Note

Given norm, the support is equal to  $s.of.x/\sqrt{n.of.x} \times qt(c(1-norm, 1+norm)/2, n.of.x-1)$

---

|             |  |
|-------------|--|
| dMuTOST_pow | <i>Compute the density of the (possible truncated) power of the equivalence test for population means of normal summary values</i> |
|-------------|--|

---

**Description**

Compute the density of the (possible truncated) power of the equivalence test for population means of normal summary values

**Usage**

```
dMuTOST_pow(rho, df, s.of.T, tau.u, alpha, norm = 1,
            support = c(-Inf, Inf), log = FALSE)
```

**Arguments**

|         |  |
|---------|--|
| rho     | vector of quantile   |
| norm    | normalization constant for the truncated power function.   |
| support | vector of dimension 2. Support of the truncated power function.  |
| log     | logical; if TRUE, densities d are given as log(d).   |
| tau.u   | upper tolerance of the equivalence region. If <code>calibrate.tau.u==TRUE</code> , it's just a guess on an upper bound on the upper tolerance of the equivalence region. |
| alpha   | level of the equivalence test  |
| df      | degrees of freedom of the simulated summary values   |
| s.of.T  | standard deviation of the test statistic   |

**Note**

If `norm = x`, the summary likelihood is truncated such that `HPD = x` and then renormalized.

---

|                            |  |
|----------------------------|--|
| integrand_KL_divergence_1D | <i>Integrand of the Kullback-Leibler divergence <math>D(P  Q)</math> for generic distributions</i> |
|----------------------------|--|

---

**Description**

Integrand of the Kullback-Leibler divergence  $D(P||Q)$  for generic distributions

**Usage**

```
integrand_KL_divergence_1D(x, dP, dQ, P_arg, Q_arg)
```

**Arguments**

|              |   |
|--------------|---|
| x            | value at which integrand is evaluated. Can be a vector.   |
| dP, dQ       | name of the functions that compute the density of P and Q |
| P_arg, Q_arg | list of arguments for dP and dQ                           |

---

KL\_divergence\_chisqstretch

*Compute Kullback-Leibler divergence between the summary likelihood and the power function of mutost after calibration of tau.u*

---

## Description

Compute Kullback-Leibler divergence between the summary likelihood and the power function of mutost after calibration of tau.u

## Usage

```
KL_divergence_chisqstretch(n.of.x, s.of.x, n.of.y,
  s.of.y, mx.pw, calibrate.tau.u = F, tau.u, alpha,
  lkl_norm = 1, lkl_support = c(-Inf, Inf), for.mle = 0,
  debug = 0, plot = F)
```

## Arguments

|                 |  |
|-----------------|--|
| n.of.x          | number of observed summary values  |
| s.of.x          | standard deviation of observed summary values  |
| n.of.y          | number of simulated summary values   |
| s.of.y          | standard deviation of simulated summary values   |
| mx.pw           | maximum power at the point of reference (rho.star=0) (only when calibrate.tau.u==TRUE).  |
| calibrate.tau.u | if TRUE the upper tolerance of the equivalence region (tau.u) is calibrated so that power at the point of reference is equal to mx.pw                      |
| tau.u           | upper tolerance of the equivalence region. If calibrate.tau.u==TRUE, it's just a guess on an upper bound on the upper tolerance of the equivalence region. |
| alpha           | level of the equivalence test  |
| lkl_norm        | normalization constant for truncated summary likelihood. Default=1   |
| lkl_support     | support of truncated summary likelihood. Default=c(-Inf,Inf).  |
| debug           | flag if C implementation is used   |
| plot            | whether to plot the two distributions  |

## Value

|                    |   |
|--------------------|---|
| vector of length 3 |   |
| KL_div             | the Kullback Leibler divergence                             |
| tau.u              | upper tolerance of the equivalence region                   |
| pw.cmx             | actual maximum power associated with the equivalence region |

## Note

If calibrate.tau.u==TRUE

**Examples**

```
KL_divergence_mutost(n.of.x=60,s.of.x=0.1,n.of.y=60,s.of.y=0.3, mx.pw=0.9,
  calibrate.tau.u=T, tau.u=1, alpha=0.01, lkl_normplot=T)
```

---

|                      |   |
|----------------------|---|
| KL_divergence_mutost | <i>Compute Kullback-Leibler divergence between the summary likelihood and the power function of mutost after calibration of tau.u</i> |
|----------------------|---|

---

**Description**

Compute Kullback-Leibler divergence between the summary likelihood and the power function of mutost after calibration of tau.u

**Usage**

```
KL_divergence_mutost(n.of.x, s.of.x, n.of.y, s.of.y,
  mx.pw, alpha, calibrate.tau.u = F, tau.u,
  pow_scale = 1.5, debug = 0, plot = F)
```

**Arguments**

|                 |  |
|-----------------|--|
| n.of.x          | number of observed summary values  |
| s.of.x          | standard deviation of observed summary values  |
| n.of.y          | number of simulated summary values   |
| s.of.y          | standard deviation of simulated summary values   |
| mx.pw           | maximum power at the point of reference (rho.star=0) (only when calibrate.tau.u==TRUE).  |
| alpha           | level of the equivalence test  |
| calibrate.tau.u | if TRUE the upper tolerance of the equivalence region (tau.u) is calibrated so that power at the point of reference is equal to mx.pw                      |
| tau.u           | upper tolerance of the equivalence region. If calibrate.tau.u==TRUE, it's just a guess on an upper bound on the upper tolerance of the equivalence region. |
| pow_scale       | scale for the support of the standardized power. The power is truncated between pow_scale*[-tau.u, tau.u] and then standardized.                           |
| debug           | flag if C implementation is used   |
| plot            | whether to plot the two distributions  |

**Value**

|                    |   |
|--------------------|---|
| vector of length 3 |   |
| KL_div             | the Kullback Leibler divergence                             |
| tau.u              | upper tolerance of the equivalence region                   |
| pw.cmx             | actual maximum power associated with the equivalence region |

**Examples**

```
KL_divergence_mutost(n.of.x=60,s.of.x=0.1,n.of.y=60,s.of.y=0.3, mx.pw=0.9,
  alpha=0.01, calibrate.tau.u=T, tau.u=1, plot=T)
```

---

KL\_divergence\_mutost\_optimize\_n.of.y

*A wrapper to minimize KL\_divergence\_mutost over n.of.y using the function optimize*

---

### Description

A wrapper to minimize KL\_divergence\_mutost over n.of.y using the function optimize

### Usage

```
KL_divergence_mutost_optimize_n.of.y(n.of.y, n.of.x,
  s.of.x, s.of.y, mx.pw, alpha, calibrate.tau.u, tau.u,
  debug = 0, plot = F)
```

### Arguments

|                 |  |
|-----------------|--|
| n.of.y          | number of simulated summary values   |
| n.of.x          | number of observed summary values  |
| s.of.x          | standard deviation of observed summary values  |
| s.of.y          | standard deviation of simulated summary values   |
| mx.pw           | maximum power at the point of reference (rho.star=0) (only when calibrate.tau.u==TRUE).  |
| alpha           | level of the equivalence test  |
| calibrate.tau.u | if TRUE the upper tolerance of the equivalence region (tau.u) is calibrated so that power at the point of reference is equal to mx.pw                      |
| tau.u           | upper tolerance of the equivalence region. If calibrate.tau.u==TRUE, it's just a guess on an upper bound on the upper tolerance of the equivalence region. |
| debug           | flag if C implementation is used   |
| plot            | whether to plot the two distributions  |

---

KL\_divergence\_mutost\_optimize\_tau.u

*A wrapper to minimize KL\_divergence\_mutost over tau.u using the function optimize*

---

### Description

A wrapper to minimize KL\_divergence\_mutost over tau.u using the function optimize

### Usage

```
KL_divergence_mutost_optimize_tau.u(tau.u, n.of.x,
  s.of.x, n.of.y, s.of.y, mx.pw, alpha,
  calibrate.tau.u = F, debug = 0, plot = F)
```

**Arguments**

|                              |  |
|------------------------------|--|
| <code>tau.u</code>           | upper tolerance of the equivalence region. If <code>calibrate.tau.u==TRUE</code> , it's just a guess on an upper bound on the upper tolerance of the equivalence region. |
| <code>n.of.x</code>          | number of observed summary values  |
| <code>s.of.x</code>          | standard deviation of observed summary values  |
| <code>n.of.y</code>          | number of simulated summary values   |
| <code>s.of.y</code>          | standard deviation of simulated summary values   |
| <code>mx.pw</code>           | maximum power at the point of reference ( $\rho_{\text{star}}=0$ ) (only when <code>calibrate.tau.u==TRUE</code> ).  |
| <code>alpha</code>           | level of the equivalence test  |
| <code>calibrate.tau.u</code> | if TRUE the upper tolerance of the equivalence region ( <code>tau.u</code> ) is calibrated so that power at the point of reference is equal to <code>mx.pw</code>        |
| <code>debug</code>           | flag if C implementation is used   |
| <code>plot</code>            | whether to plot the two distributions  |

---

`nabc.acf.equivalence`    *Perform the asymptotic equivalence test for autocorrelations at lag 1*

---

**Description**

Perform the asymptotic equivalence test for autocorrelations at lag 1

**Usage**

```
nabc.acf.equivalence(sim, obs, args = NA,
  verbose = FALSE, alpha = 0, leave.out = 0,
  normal.test = "sf.test")
```

**Arguments**

|                          |   |
|--------------------------|---|
| <code>sim</code>         | simulated summary values  |
| <code>obs</code>         | observed summary values   |
| <code>args</code>        | argument that contains the equivalence region and the level of the test (see Examples). This is the preferred method for specifying arguments and overwrites the dummy default values |
| <code>verbose</code>     | flag if detailed information on the computations should be printed to standard out  |
| <code>alpha</code>       | level of the equivalence test   |
| <code>leave.out</code>   | thinning, how many values in the pair sequence $(x_i, x_{i-1})$ should be left out. Defaults to zero.   |
| <code>normal.test</code> | name of function with which normality of the summary values is tested   |

**Value**

vector containing

|        |   |
|--------|---|
| error  | test statistic. Here, instead of T we return the p-value of the TOST. |
| cil    | lower ABC tolerance. Here, instead of $c^-$ we return 0.              |
| cir    | upper ABC tolerance. Here, instead of $c^+$ we return 'alpha'.        |
| al     | free entry. Here set to $c^-$ .                                       |
| ar     | free entry. Here set to $c^+$ .                                       |
| mx.pw  | Maximum power at the point of equality                                |
| rho.mc | sample estimate of 'rho'  |

**Examples**

```
leave.out<- 2
tau.u<- 0.09
alpha<- 0.01
n<- 5e3
sigma<- 1
a<- 0.1
args<- paste("acfequiv",leave.out,tau.u,alpha,sep='/')
x<-rnorm(n+1,0,sigma)
x<- x[-1] + x[-(n+1)]*a
y<-rnorm(n+1,0,sigma)
y<- y[-1] + y[-(n+1)]*a
nabc.acf.equivalence(y,x,args)
```

---

nabc.acf.equivalence.abctol

*Compute the ABC tolerances of the asymptotic equivalence test for autocorrelations at lag 1*

---

**Description**

Compute the ABC tolerances of the asymptotic equivalence test for autocorrelations at lag 1

**Usage**

```
nabc.acf.equivalence.abctol(tau.l, tau.u, n, alpha)
```

**Arguments**

|       |  |
|-------|--|
| tau.l | lower tolerance of the equivalence region  |
| tau.u | upper tolerance of the equivalence region  |
| n     | number of pairs $(x_i, x_{i-1})$ after thinning of the time series $x_1, x_2, \dots$ |
| alpha | level of the equivalence test  |

**Value**

vector of length 2, first entry is lower ABC tolerance, second entry is upper ABC tolerance



**Examples**

```
tau.u<- 0.09
tau.l<- -tau.u
sim.n<-5e3
leave.out<- 2
nabc.acf.equivalence.abctol(tau.l, tau.u, floor(sim.n / (1+leave.out)), 0.01)
```

---

nabc.acf.equivalence.cor

*Compute the autocorrelation in a time series along with some other info*

---

**Description**

Compute the autocorrelation in a time series along with some other info

**Usage**

```
nabc.acf.equivalence.cor(x, leave.out = 0)
```

**Arguments**

|           |  |
|-----------|--|
| x         | time series (simply vector)  |
| leave.out | thinning, how many values in the pair sequence (x <sub>i</sub> ,x <sub>i-1</sub> ) should be left out. Defaults to zero. |

**Value**

|     |  |
|-----|--|
| cor | autocorrelation in the thinned sequence                            |
| z   | Z-transformation of the autocorrelation (this is atanh of "cor")   |
| n   | Number of pairs (x <sub>i</sub> ,x <sub>i-1</sub> ) after thinning |

**Examples**

```
nabc.acf.equivalence.cor(rnorm(100,0,1), leave.out=2)
```

---

nabc.acf.equivalence.pow

*Compute power of the asymptotic equivalence test for autocorrelations at lag 1*

---

**Description**

Compute power of the asymptotic equivalence test for autocorrelations at lag 1

**Usage**

```
nabc.acf.equivalence.pow(rho, tau.u, alpha, s)
```

**Arguments**

|       |  |
|-------|--|
| rho   | true difference in simulated and observed autocorrelation at lag 1 |
| tau.u | upper tolerance of the equivalence region                          |
| alpha | level of the equivalence test                                      |
| s     | standard deviation of the test statistic                           |

**Value**

power of the asymptotic test. this is approximate because the test is asymptotic

**Examples**

```
tau.u<- 0.09
tau.l<- -tau.u
sim.n<-5e3
rho<- seq(tau.l,tau.u,0.001)
pw<- nabc.acf.equivalence.pow(rho, tau.u, alpha, 1/sqrt(floor(sim.n/3)-3))
```

---

nabc.acf.equivalence.tau.lowup

*Calibrate the equivalence region of the asymptotic equivalence test for autocorrelations at lag 1 for given maximum power*

---

**Description**

Calibrate the equivalence region of the asymptotic equivalence test for autocorrelations at lag 1 for given maximum power

**Usage**

```
nabc.acf.equivalence.tau.lowup(mx.pw, tau.up.ub, n,
  alpha, rho.star = 0, tol = 1e-05, max.it = 100)
```

**Arguments**

|           |  |
|-----------|--|
| mx.pw     | maximum power at the point of reference (rho.star).  |
| tau.up.ub | guess on an upper bound on the upper tolerance of the equivalence region                                       |
| n         | number of pairs ( $x_i, x_{i-1}$ ) after thinning of the time series $x_1, x_2, \dots$                         |
| alpha     | level of the equivalence test  |
| rho.star  | point of reference. Defaults to the point of equality rho.star=0.  |
| tol       | this algorithm stops when the actual maximum power is less than 'tol' from 'mx.pw'                             |
| max.it    | this algorithm stops prematurely when the number of iterations to find the equivalence region exceeds 'max.it' |

**Value**

vector of length 4

- |   |   |
|---|---|
| 1 | lower tolerance of the equivalence region                   |
| 2 | upper tolerance of the equivalence region                   |
| 3 | actual maximum power associated with the equivalence region |
| 4 | error ie $\text{abs}(\text{actual power} - \text{mx.pw})$   |

**Examples**

```
tau.u<- 0.09
tau.l<- -tau.u
sim.n<-5e3
leave.out<- 2
nabc.acf.equivalence.tau.lowup(0.9, 2, floor(sim.n / (1+leave.out)), 0.01)
```

---

|                   |   |
|-------------------|---|
| nabc.chisqstretch | <i>Perform the exact test for dispersion equivalence when the summary values are normally distributed</i> |
|-------------------|---|

---

**Description**

Perform the exact test for dispersion equivalence when the summary values are normally distributed

**Usage**

```
nabc.chisqstretch(sim, obs.mc, args = NA,
  verbose = FALSE, tau.l = 1, tau.u = 1, guess.tau.l = 0,
  alpha = 0, normal.test = "sf.test", for.mle = 0)
```

**Arguments**

- |             |   |
|-------------|---|
| sim         | simulated summary values  |
| obs.mc      | variance of the observed summary values   |
| args        | argument that contains the equivalence region and the level of the test (see Examples). This is the preferred method for specifying arguments and overwrites the dummy default values |
| verbose     | flag if detailed information on the computations should be printed to standard out  |
| tau.l       | lower tolerance of the equivalence region   |
| tau.u       | upper tolerance of the equivalence region   |
| guess.tau.l | guess on the lower tolerance of the equivalence region. Used when the tolerances are annealed and calibration is numerically unstable.  |
| alpha       | level of the equivalence test   |
| leave.out   | thinning, how many values in the pair sequence $(x_i, x_{i-1})$ should be left out. Defaults to zero.   |
| normal.test | name of function with which normality of the summary values is tested   |
| for.mle     | calibrate so that the mode of the power is at the MLE   |

**Value**

vector containing

|        |   |
|--------|---|
| error  | test statistic, here $\text{var}(\text{sim})/\text{obs.mc}$ |
| cil    | lower ABC tolerance $c^-$                                   |
| cir    | upper ABC tolerance $c^+$                                   |
| mx.pw  | Maximum power at the point of equality                      |
| rho.mc | $\log(\text{var}(\text{sim}) / \text{obs.mc})$              |

**Examples**

```
alpha<- 0.01; xn<- yn<- 60; xsigma2<- 1; tau.u<- 2.2
tau.l<- nabc.chisqstretch.tau.low(tau.u, yn-1, alpha)
args<- paste("chisqstretch",tau.l,tau.u,alpha,sep='/')
x<- rnorm(xn,0,sd=sqrt(xsigma2))
y<- rnorm(yn,0,sd=sqrt(xsigma2))
nabc.chisqstretch(y, var(x), args=args, verbose= 0)
```

---

nabc.chisqstretch.n.of.y

*Calibrate the number of simulated summary values and the equivalence region for the test of dispersion equivalence*

---

**Description**

Calibrate the number of simulated summary values and the equivalence region for the test of dispersion equivalence

**Usage**

```
nabc.chisqstretch.n.of.y(n.of.x, s.of.Sx, mx.pw, alpha,
  tau.u.ub = 2, tol = 1e-05, max.it = 100, for.mle = 0)
```

**Arguments**

|           |   |
|-----------|---|
| n.of.x    | number of observed summary values   |
| s.of.Sx   | standard deviation in the observed summary likelihood   |
| mx.pw     | maximum power at the point of reference (rho.star).   |
| alpha     | level of the equivalence test   |
| tau.up.ub | guess on an upper bound on the upper tolerance of the equivalence region  |
| tol       | this algorithm stops when the actual variation in the ABC approximation to the summary likelihood is less than 'tol' from 's.of.Sx*s.of.Sx' |
| max.it    | this algorithm stops prematurely when the number of iterations to calibrate the number of simulated data points exceeds 'max.it'            |
| for.mle   | calibrate so that the mode of the power is at the MLE   |

**Value**

vector of length 8

- |   |  |
|---|--|
| 1 | number of simulated summary values   |
| 2 | lower tolerance of the equivalence region  |
| 3 | upper tolerance of the equivalence region  |
| 4 | lower ABC tolerance $c^-$  |
| 5 | upper ABC tolerance $c^+$  |
| 6 | actual variation of the power  |
| 7 | actual maximum power associated with the equivalence region  |
| 8 | error ie $\text{abs}(\text{actual variation} - \text{variation in the observed summary likelihood})$ |

**Examples**

```
xn<- 60; alpha <- 0.01; prior.u <- 3; prior.l <- 1/3; tau.u<- 2.5; xsig2 <- 1
#summary likelihood of sigma2 given sample mean and sum of squares
th <- seq(prior.l,prior.u,length.out=1e3)
shape <- (xn-2)/2
scale <- xsig2*xn*xn/(xn-1)/2
y <- densigamma(th, shape, scale)
var.Sx <- scale*scale/((shape-1)*(shape-1)*(shape-2))
#abc approximation to summary likelihood
nabc.chisqstretch.n.of.y(xn, sqrt(var.Sx), 0.9, alpha, tau.u.ub=tau.u)
yn <- tmp[1]
tau.l <- tmp[2]
tau.u <- tmp[3]
c.l <- tmp[4]
c.u <- tmp[5]
y2 <- nabc.chisqstretch.pow(th, yn-1, yn-1, c.l, c.u)
#plot the summary likelihood and the abc approximation
plot(th,y/mean(y),ylim=range(c(y/mean(y),y2/mean(y2))),type='l')
lines(th,y2/mean(y2),col="blue")
```

---

nabc.chisqstretch.n.of.y.KL

*Calibrate the number of simulated summary values and the equivalence region for the test of dispersion equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.*

---

**Description**

Calibrate the number of simulated summary values and the equivalence region for the test of dispersion equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.

**Usage**

```
nabc.chisqstretch.n.of.y.KL(n.of.x, s.of.x, n.of.y,
  s.of.y, mx.pw, alpha, tau.u.ub = 2, for.mle = 0,
  max.it = 100, debug = 0, plot = F)
```

**Arguments**

|        |  |
|--------|--|
| plot   | if TRUE, the summary likelihood and abc approximation are plotted  |
| max.it | this algorithm stops prematurely when the number of iterations to calibrate the number of simulated data points exceeds 'max.it' |
| debug  | Flag if C implementation is used.  |
| n.of.x | number of observed summary values  |
| s.of.x | standard deviation of observed summary values  |
| n.of.y | number of simulated summary values   |
| s.of.y | standard deviation of simulated summary values   |
| mx.pw  | maximum power at the point of reference (rho.star=0) (only when calibrate.tau.u==TRUE).  |
| alpha  | level of the equivalence test  |

**Value**

|        |   |
|--------|---|
|        | vector of length 4  |
| n.of.y | number of simulated summary values                          |
| KL_div | the Kullback Leibler divergence                             |
| tau.u  | upper tolerance of the equivalence region                   |
| pw.cmx | actual maximum power associated with the equivalence region |

---

nabc.chisqstretch.pow *Compute power of the exact equivalence test for dispersion*

---

**Description**

Compute power of the exact equivalence test for dispersion

**Usage**

```
nabc.chisqstretch.pow(rho, scale, df, cl, cu)
```

**Arguments**

|       |   |
|-------|---|
| rho   | true ratio in simulated variance / observed variance                        |
| scale | scaling of T apart from rho, either n-1 for unbiased ABC or n for exact MAP |
| df    | degrees of freedom  |
| cl    | lower ABC tolerance   |
| cu    | upper ABC tolerance   |

**Value**

power of the exact test. this is exact.

**Examples**

```
alpha<- 0.01
tau.up<- 1.09
yn<- 5e3
tau.low<- nabc.chisqstretch.tau.low(tau.up, yn-1, alpha)
rej<- .Call("abcScaledChiSq",c(yn-1,yn-1,tau.low,tau.up,alpha,1e-10,100,0.05) )
rho<- seq(tau.low,tau.up,by=0.001)
nabc.chisqstretch.pow(rho,yn-1,yn-1,rej[1],rej[2])
```

---

nabc.chisqstretch.tau.low

*Calibrate the lower tolerance interval of the equivalence region for the test of dispersion equivalence*

---

**Description**

Calibrate the lower tolerance interval of the equivalence region for the test of dispersion equivalence

**Usage**

```
nabc.chisqstretch.tau.low(tau.up, df, alpha,
  rho.star = 1, tol = 1e-05, max.it = 100, for.mle = 0)
```

**Arguments**

|          |  |
|----------|--|
| tau.up   | upper tolerance of the equivalence region  |
| df       | degrees of freedom   |
| alpha    | level of the equivalence test  |
| rho.star | point of reference. Defaults to the point of equality rho.star=1   |
| tol      | this algorithm stops when the actual point of reference is less than 'tol' from 'rho.star'                     |
| max.it   | this algorithm stops prematurely when the number of iterations to find the equivalence region exceeds 'max.it' |
| for.mle  | calibrate so that the mode of the power is at the MLE  |

**Value**

tau.low, lower tolerance of the equivalence region

**Examples**

```
tau.u<- 2.2
yn<- 60
tau.l<- nabc.chisqstretch.tau.low(tau.u, yn-1, 0.01)
```

---

nabc.chisqstretch.tau.lowup

*Calibrate the equivalence region for the test of dispersion equivalence for given maximum power*

---

## Description

Calibrate the equivalence region for the test of dispersion equivalence for given maximum power

## Usage

```
nabc.chisqstretch.tau.lowup(mx.pw, tau.up.ub, df, alpha,
  rho.star = 1, tol = 1e-05, max.it = 100, for.mle = 0)
```

## Arguments

|           |  |
|-----------|--|
| mx.pw     | maximum power at the point of reference (rho.star).  |
| tau.up.ub | guess on an upper bound on the upper tolerance of the equivalence region                                       |
| df        | degrees of freedom   |
| alpha     | level of the equivalence test  |
| rho.star  | point of reference. Defaults to the point of equality rho.star=1.  |
| tol       | this algorithm stops when the actual maximum power is less than 'tol' from 'mx.pw'                             |
| max.it    | this algorithm stops prematurely when the number of iterations to find the equivalence region exceeds 'max.it' |
| for.mle   | calibrate so that the mode of the power is at the MLE  |

## Value

vector of length 6

|   |   |
|---|---|
| 1 | lower tolerance of the equivalence region                   |
| 2 | upper tolerance of the equivalence region                   |
| 3 | actual maximum power associated with the equivalence region |
| 4 | error ie abs(actual power - mx.pw)                          |
| 5 | lower point of critical region                              |
| 6 | upper point of critical region                              |

## Examples

```
yn<- 60
nabc.chisqstretch.tau.lowup(0.9, 2.5, yn-1, 0.01)
```



---

|                  |  |
|------------------|--|
| NABC.DEFAULT.ANS | <i>this file contains all R functions of the abc-n package</i> |
|------------------|--|

---

**Description**

this file contains all R functions of the abc-n package

**Usage**

```
NABC.DEFAULT.ANS
```

**Format**

```
Named num [1:17] 0 50 1 NA NA NA 0 0 0 0 ... - attr(*, "names")= chr [1:17] "lkl" "error" "pval"
"link.mc.obs" ...
```

---

|                      |   |
|----------------------|---|
| nabc.exprho.at.theta | <i>Estimate summary parameter errors rho from unbiased Monte Carlo estimates rho.mc for all proposed theta including rejections</i> |
|----------------------|---|

---

**Description**

Estimate summary parameter errors rho from unbiased Monte Carlo estimates rho.mc for all proposed theta including rejections

**Usage**

```
nabc.exprho.at.theta(df, theta.names, rho.names,
  thin = 1)
```

**Arguments**

|             |  |
|-------------|--|
| df          | data frame with all proposed theta and corresponding rho.mc for each summary of interest |
| theta.names | vector of theta names (columns in df)  |
| rho.names   | vector of rho names (columns in df)  |
| thin        | thinning factor in case there are many rows in df  |

**Value**

matrix containing the estimated rho (per column). The ith row corresponds to the ith theta in df.

---

|                   |  |
|-------------------|--|
| nabc.generic.tost | <i>Perform a generic two one sided test. This is an internal function.</i> |
|-------------------|--|

---

**Description**

Perform a generic two one sided test. This is an internal function.

**Usage**

```
nabc.generic.tost(tost.args, tau.l, tau.u, alpha,
  tost.distr = "t")
```

**Arguments**

|            |                                       |
|------------|---------------------------------------|
| tost.args  | vector of arguments for generic TOST  |
| tau.l      | lower tolerance of equivalence region |
| tau.u      | upper tolerance of equivalence region |
| alpha      | level of equivalence test             |
| tost.distr | name of distribution of tost          |

**Value**

vector of length 7

---

|                    |  |
|--------------------|--|
| nabc.get.pfam.pval | <i>Test if summary values are normally distributed</i> |
|--------------------|--|

---

**Description**

Test if summary values are normally distributed

**Usage**

```
nabc.get.pfam.pval(x, normal.test)
```

**Arguments**

|             |   |
|-------------|---|
| x           | summary values  |
| normal.test | name of function with which normality of the summary values is tested |

**Value**

p value of the test

**Examples**

```
nabc.get.pfam.pval(rnorm(1e4), "shapiro.test")
```

---

nabc.mutost.onesample *Perform the exact TOST for location equivalence when the summary values are normally distributed*

---

## Description

Perform the exact TOST for location equivalence when the summary values are normally distributed

## Usage

```
nabc.mutost.onesample(sim, obs, obs.n = NA, obs.sd = NA,
  args = NA, verbose = FALSE, tau.u = 0, tau.l = -tau.u,
  alpha = 0, mx.pw = 0.9, annealing = 1,
  normal.test = "sf.test", plot = 0, legend.txt = "")
```

## Arguments

|             |   |
|-------------|---|
| sim         | simulated summary values  |
| obs         | observed summary values   |
| args        | argument that contains the equivalence region and the level of the test (see Examples). This is the preferred method for specifying arguments and overwrites the dummy default values |
| verbose     | flag if detailed information on the computations should be printed to standard out  |
| s.of.x      | standard deviation of the observed summary values   |
| tau.u       | upper tolerance of the equivalence region   |
| tau.l       | lower tolerance of the equivalence region   |
| alpha       | level of the equivalence test   |
| mx.pw       | maximum power at the point of equality  |
| annealing   | inflation factor of tolerances of the equivalence region  |
| normal.test | name of function with which normality of the summary values is tested   |

## Value

|                   |  |
|-------------------|--|
| vector containing |  |
| error             | test statistic, here p-value of TOST   |
| cil               | lower ABC tolerance, here 0            |
| cir               | upper ABC tolerance, here alpha        |
| mx.pw             | Maximum power at the point of equality |
| rho.mc            | mean(sim) - obs.mean                   |

## Examples

```
tau.u<- 0.5; tau.l<- -tau.u; alpha<- 0.01; xn<- yn<- 60; xmu<- ymu<- 0.5; xsigma2<- ysigma2<- 2
args<- paste("mutost",1,tau.u,alpha,sep='/')
x<- rnorm(xn,xmu,sd=sqrt(xsigma2))
y<- rnorm(yn,ymu,sd=sqrt(ysigma2))
nabc.mutost.onesample(y, x, args= args, verbose= 0)
```

---

nabc.mutost.onesample.n.of.y

*Calibrate the number of simulated summary values and the equivalence region for the test of location equivalence*

---

## Description

Calibrate the number of simulated summary values and the equivalence region for the test of location equivalence

## Usage

```
nabc.mutost.onesample.n.of.y(n.of.x, s.of.Sx, mx.pw,
  s.of.y, alpha, tau.u.ub = 2, tol = 1e-05, max.it = 100,
  debug = 0)
```

## Arguments

|           |   |
|-----------|---|
| n.of.x    | number of observed summary values   |
| s.of.Sx   | standard deviation in the observed summary likelihood   |
| mx.pw     | maximum power at the point of reference (rho.star).   |
| s.of.y    | standard deviation in the simulated summary values  |
| alpha     | level of the equivalence test   |
| tau.up.ub | guess on an upper bound on the upper tolerance of the equivalence region  |
| tol       | this algorithm stops when the actual variation in the ABC approximation to the summary likelihood is less than 'tol' from 's.of.Sx*s.of.Sx' |
| max.it    | this algorithm stops prematurely when the number of iterations to calibrate the number of simulated data points exceeds 'max.it'            |
| debug     | Flag if C implementation is used.   |

## Value

vector of length 6

|   |   |
|---|---|
| 1 | number of simulated summary values  |
| 2 | lower tolerance of the equivalence region                                     |
| 3 | upper tolerance of the equivalence region                                     |
| 4 | actual variation of the power   |
| 5 | actual maximum power associated with the equivalence region                   |
| 6 | error ie abs(actual variation - variation in the observed summary likelihood) |

## Examples

```
prior.u<- 2; prior.l<- -prior.u; tau.u<- 0.75; xn<- yn<- 60; xmu<- 0.5; xsigma2<- ysigma2<- 2; alpha<- 0.0
rho<- seq(prior.l,prior.u,length.out=1e3)
#summary likelihood
y<-dnorm(rho,0,sqrt(xsigma2/xn))
y<- y / diff(pnorm(c(prior.l,prior.u),0,sqrt(xsigma2/xn)))
#abc approximation to summary likelihood based on equivalence test
tmp <- nabc.mutost.onesample.n.of.y(xn, sqrt(xsigma2/xn), 0.9, sqrt(ysigma2), alpha, tau.u.ub=2*tau.u )
yn <- tmp[1]
tau.u <- tmp[3]
y2<- nabc.mutost.pow(rho, yn-1, tau.u, sqrt(ysigma2/yn), alpha)
rho2<- rho[which(y2!=0)]
y2<- y2[which(y2!=0)]
y2<- y2/sum(diff(rho2)*y2[-1])
#plot summary likelihood and abc approximation thereof
plot(1,1,type='n',xlim=range(rho),ylim=range(c(y,y2)),xlab=expression(rho))
lines(rho,y,col="red")
lines(rho2,y2,col="blue")
abline(v=0,col="red")
```

---

nabc.mutost.onesample.n.of.y.KL

*Calibrate the number of simulated summary values and the equivalence region for the test of location equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.*

---

## Description

Calibrate the number of simulated summary values and the equivalence region for the test of location equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.

## Usage

```
nabc.mutost.onesample.n.of.y.KL(n.of.x, s.of.x, n.of.y,
  s.of.y, mx.pw, alpha, tau.u.ub = 2, max.it = 100,
  debug = 0, plot = F)
```

## Arguments

|        |  |
|--------|--|
| plot   | if TRUE, the summary likelihood and abc approximation are plotted  |
| max.it | this algorithm stops prematurely when the number of iterations to calibrate the number of simulated data points exceeds 'max.it' |
| debug  | Flag if C implementation is used.  |
| n.of.x | number of observed summary values  |
| s.of.x | standard deviation of observed summary values  |
| n.of.y | number of simulated summary values   |
| s.of.y | standard deviation of simulated summary values   |
| mx.pw  | maximum power at the point of reference (rho.star=0) (only when calibrate.tau.u==TRUE).  |
| alpha  | level of the equivalence test  |

**Value**

vector of length 4

|        |   |
|--------|---|
| n.of.y | number of simulated summary values                          |
| KL_div | the Kullback Leibler divergence                             |
| tau.u  | upper tolerance of the equivalence region                   |
| pw.cmx | actual maximum power associated with the equivalence region |

**Examples**

```
xn <- 60
yn <- xn
xmean <- 2
xsigma <- 2
ymean <- 2
ysigma <- 3

obs <- rnorm(xn, xmean, xsigma)
obs <- (obs - mean(obs))/sd(obs) * xsigma + xmean
sim <- rnorm(yn, ymean, ysigma)

n.of.x <- xn
s.of.x <- sd(obs)
n.of.y <- yn
s.of.y <- sd(sim)
mx.pw <- 0.9
alpha <- 0.01
tau.u.ub <- 2

#compute the Kullback-Leibler divergence between the summary likelihood and the power; and plot.
KL_divergence_mutost(n.of.x, s.of.x, n.of.y, s.of.y, mx.pw, alpha, calibrate.tau.u = T, tau.u = tau.u.ub,
plot = T)

#adjust n.of.y to minimize the Kullback-Leibler divergence, and plot result.
nabc.mutost.onesample.n.of.y.KL(n.of.x, s.of.x, n.of.y, s.of.y, mx.pw, alpha, plot = T)
```

---

nabc.mutost.onesample.tau.lowup.KL

*Calibrate the equivalence region for the test of location equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.*

---

**Description**

Calibrate the equivalence region for the test of location equivalence by minimising the Kullback-Leibler divergence between the power function and the summary likelihood.

**Usage**

```
nabc.mutost.onesample.tau.lowup.KL(n.of.x, s.of.x,
  n.of.y, s.of.y, mx.pw, alpha, tau.u.lb = 0,
  max.it = 100, debug = 0, plot = F)
```

**Arguments**

|        |  |
|--------|--|
| plot   | if TRUE, the summary likelihood and abc approximation are plotted  |
| max.it | this algorithm stops prematurely when the number of iterations to calibrate the number of simulated data points exceeds 'max.it' |
| debug  | Flag if C implementation is used.  |
| n.of.x | number of observed summary values  |
| s.of.x | standard deviation of observed summary values  |
| n.of.y | number of simulated summary values   |
| s.of.y | standard deviation of simulated summary values   |
| mx.pw  | maximum power at the point of reference ( $\rho.\text{star}=0$ ) (only when <code>calibrate.tau.u==TRUE</code> ).                |
| alpha  | level of the equivalence test  |

**Value**

|                    |   |
|--------------------|---|
| vector of length 4 |   |
| n.of.y             | number of simulated summary values                          |
| KL_div             | the Kullback Leibler divergence                             |
| tau.u              | upper tolerance of the equivalence region                   |
| pw.cmx             | actual maximum power associated with the equivalence region |

**Examples**

```
prior.u<- 2; prior.l<- -prior.u; tau.u<- 0.75; xn<- yn<- 60; xmu<- 0.5;
xsigma2<- ysigma2<- 2; alpha<- 0.01
rho<- seq(prior.l,prior.u,length.out=1e3)
#summary likelihood
y<-dnorm(rho,0,sqrt(xsigma2/xn))
y<- y / diff(pnorm(c(prior.l,prior.u),0,sqrt(xsigma2/xn)))
#abc approximation to summary likelihood based on equivalence test
tmp <- nabc.mutost.onesample.n.of.y.KL(xn, sqrt(xsigma2/xn), yn,
sqrt(ysigma2),0.9, alpha, tau.u.ub=2*tau.u,plot=T)
yn <- tmp["n.of.y"]
tau.u <- tmp["tau.u"]
y2<- nabc.mutost.pw(rho, yn-1, tau.u, sqrt(ysigma2/yn), alpha)
rho2<- rho[which(y2!=0)]
y2<- y2[which(y2!=0)]
y2<- y2/sum(diff(rho2)*y2[-1])
#plot summary likelihood and abc approximation thereof
plot(1,1,type='n',xlim=range(rho),ylim=range(c(y,y2)),xlab=expression(rho))
lines(rho,y,col="red")
lines(rho2,y2,col="blue")
abline(v=0,col="red")
```

---

```
nabc.mutost.onesample.tau.lowup.pw
```

*Calibrate the equivalence region for the test of location equivalence for given maximum power*

---

## Description

Calibrate the equivalence region for the test of location equivalence for given maximum power

## Usage

```
nabc.mutost.onesample.tau.lowup.pw(mx.pw, df, s.of.T,
  tau.up.ub, alpha, rho.star = 0, tol = 1e-05,
  max.it = 100, debug = 0)
```

## Arguments

|                        |  |
|------------------------|--|
| <code>mx.pw</code>     | maximum power at the point of reference ( <code>rho.star</code> ).   |
| <code>df</code>        | degrees of freedom   |
| <code>s.of.T</code>    | standard deviation of the test statistic   |
| <code>tau.up.ub</code> | guess on an upper bound on the upper tolerance of the equivalence region                                       |
| <code>alpha</code>     | level of the equivalence test  |
| <code>rho.star</code>  | point of reference. Defaults to the point of equality <code>rho.star=0</code> .                                |
| <code>tol</code>       | this algorithm stops when the actual maximum power is less than 'tol' from 'mx.pw'                             |
| <code>max.it</code>    | this algorithm stops prematurely when the number of iterations to find the equivalence region exceeds 'max.it' |
| <code>debug</code>     | Flag if C implementation is used.  |

## Value

vector of length 4

|   |   |
|---|---|
| 1 | lower tolerance of the equivalence region                   |
| 2 | upper tolerance of the equivalence region                   |
| 3 | actual maximum power associated with the equivalence region |
| 4 | error ie <code>abs(actual power - mx.pw)</code>             |

## Examples

```
yn<- 60; ysigma2<- 1; alpha<- 0.01
nabc.mutost.onesample.tau.lowup.pw(0.9, yn-1, sqrt(ysigma2/yn), 2, alpha )
```



---

nabc.mutost.onesample.tau.lowup.var

*Calibrate the equivalence region for the test of location equivalence for given variance of the summary likelihood*

---

## Description

Calibrate the equivalence region for the test of location equivalence for given variance of the summary likelihood

## Usage

```
nabc.mutost.onesample.tau.lowup.var(s.of.Sx, df, s.of.T,
  tau.up.ub, alpha, rho.star = 0, tol = 1e-05,
  max.it = 100, debug = 0)
```

## Arguments

|           |  |
|-----------|--|
| s.of.Sx   | standard deviation of the summary likelihood   |
| df        | degrees of freedom   |
| s.of.T    | standard deviation of the test statistic   |
| tau.up.ub | guess on an upper bound on the upper tolerance of the equivalence region                                       |
| alpha     | level of the equivalence test  |
| rho.star  | point of reference. Defaults to the point of equality rho.star=0.  |
| tol       | this algorithm stops when the actual maximum power is less than 'tol' from 'mx.pw'                             |
| max.it    | this algorithm stops prematurely when the number of iterations to find the equivalence region exceeds 'max.it' |
| debug     | Flag if C implementation is used.  |

## Value

vector of length 4

|   |   |
|---|---|
| 1 | lower tolerance of the equivalence region                 |
| 2 | upper tolerance of the equivalence region                 |
| 3 | actual variance associated with the power                 |
| 4 | error ie abs(actual var(power) - var(summary likelihood)) |

## Examples

```
yn<- 60; ysigma2<- 1; alpha<- 0.01
nabc.mutost.onesample.tau.lowup.var(0.002, yn-1, sqrt(ysigma2/yn), 2, alpha )
```

---

|                 |  |
|-----------------|--|
| nabc.mutost.pow | <i>Compute power of the equivalence test for population means of normal summary values</i> |
|-----------------|--|

---

**Description**

Compute power of the equivalence test for population means of normal summary values

**Usage**

```
nabc.mutost.pow(rho, df, tau.u, s.of.T, alpha,  
  rtn.fun = FALSE, force = FALSE)
```

**Arguments**

|         |   |
|---------|---|
| rho     | true difference in simulated and observed population means                      |
| df      | degrees of freedom of the simulated summary values                              |
| tau.u   | upper tolerance of the equivalence region                                       |
| s.of.T  | standard deviation of the test statistic  |
| alpha   | level of the equivalence test   |
| rtn.fun | indicator if a function to compute the power should be returned. Defaults to 0. |
| force   | if TRUE, enforce power computation outside of acceptance region                 |

**Value**

approximate power of the exact test. this is approximate because the standard deviation of the normal model for the simulated summary values is not known.

**Examples**

```
prior.u<- 5; prior.l<- -prior.u; tau.u <- 0.75; yn<- 60; ysigma2<- 1; alpha<- 0.01  
rho <- seq(prior.l,prior.u,length.out=1e3)  
nabc.mutost.pow(rho, yn-1, tau.u, sqrt(ysigma2/yn), alpha)
```

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