

# FP - Some useful notes

Week 04

**Aula prática nº 4 – Funções**

# Functions

- Natural from maths
- Represent a sequence of actions
  - Using a name
  - With explicit parameters i.e. what you need
  - With explicit result i.e. values after return

# function

This function has no name. It returns a function object which is assigned to the identifier `double`. We can now call it as a normal function. The statement

```
double = lambda x: x * 2
```

is nearly the same as

```
def double(x):  
    return x * 2
```

[https://www.tutorialspoint.com/python/python\\_functions.htm](https://www.tutorialspoint.com/python/python_functions.htm)

<https://www.datacamp.com/community/tutorials/functions-python-tutorial>

# The math inspiration

```
def f(x):  
    return math.sin(x)
```

```
def f(x,y):  
    return x**2 + y**2
```

```
def f(x):  
    return x**2
```

```
def f(x):  
    return math.sqrt(x)
```

```
def f(x):  
    return 1/x
```



# The math inspiration

2. Escreva uma função para calcular o polinómio  $p(x) = x^2 + 2x + 3$  e use-a num programa para calcular e mostrar os valores de  $p(0)$  ,  $p(1)$  ,  $p(2)$  e  $p(p(1))$  . Confira os resultados.

```
def p(x):  
    return x**2 + 2*x + 3
```

```
def pol(a,b,c,x):  
    return a*(x**2) + b*x + c
```

Do you agree?



$P(1) < = > \text{pol}(1,2,3,1)$

# The math inspiration

2. Escreva uma função para calcular o polinómio  $p(x) = x^2 + 2x + 3$  e use-a num programa para calcular e mostrar os valores de  $p(0)$  ,  $p(1)$  ,  $p(2)$  e  $p(p(1))$  . Confira os resultados.

```
def p(x):  
    return x**2 + 2*x + 3
```

```
def pol(a,b,c,x):  
    return a*(x**2) + b*x + c
```

Do you agree?



$p(p(1)) < = > \text{pol}(1,2,3,\text{pol}(1,2,3,1))$

# Factorial (n!)

$$U_0 = 1 \text{ se } n=0$$

$$U_{n+1} = n * U_n \text{ se } n>0$$

```
def factorial( n ):
    if n=0 :
        return 1
    else:
        return n * factorial( n-1)
```

3! < = > factorial( 3 )

# A way to “encapsulate” fixed content...

```
def dc1():  
    message="""  
    As armas e os barões assinalados,  
    Que da ocidental praia Lusitana,  
    Por mares nunca de antes navegados,  
    Passaram ainda além da Taprobana,  
    Em perigos e guerras esforçados,  
    Mais do que prometia a força humana,  
    E entre gente remota edificaram  
    Novo Reino, que tanto sublimaram;  
    """  
    return message
```

```
for i in range(5):  
    print( rc1() )
```

Do you agree?



< = >

```
def c1():  
    message="""  
    As armas e os barões assinalados,  
    Que da ocidental praia Lusitana,  
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    Mais do que prometia a força humana,  
    E entre gente remota edificaram  
    Novo Reino, que tanto sublimaram;  
    """  
    print( message )  
    return
```

```
for i in range(5):  
    c1()
```



# ... and call it using a simple name

```
def dc1():  
    message="""  
    As armas e os barões assinalados,  
    Que da ocidental praia Lusitana,  
    Por mares nunca de antes navegados,  
    Passaram ainda além da Taprobana,  
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    """  
    return message
```

Do you agree?

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    """  
    print( message )  
    return
```

```
for i in range(5) :  
    print( dc1() )
```



```
for i in range(5) :  
    c1()
```

# Functions as chunks of related code...

```
def divRem(a, b):  
    return a//b, a%b
```

```
def printNtimes(msg, n):  
    if n > 0:  
        print(msg)  
        printNtimes(msg, n-1)
```

```
def fullname(first, last):  
    first = first.title()    # title makes  
    last = last.title()  
    return first + " " + last
```

# Referred using a smaller name with parameters

```
def divRem(a, b):  
    return a//b, a%b
```

```
q, r = divRem(13, 4)  
print(q, r)
```

```
def printNtimes(msg, n):  
    if n > 0:  
        print(msg)  
        printNtimes(msg, n-1)
```

```
def fullname(first, last):  
    first = first.title()    # title makes  
    last = last.title()  
    return first + " " + last
```

```
print( fullname("maria", "costa") )  
print( fullname("fernando", "pessoa") )
```

# Lambda

# lambda

**lambda arguments: expression**

- This function can have any number of arguments but only one expression, which is evaluated and returned.
- One is free to use lambda functions wherever function objects are required.
- You need to keep in your knowledge that lambda functions are syntactically restricted to a single expression.
- It has various uses in particular fields of programming besides other types of expressions in functions.

```
# Python code to illustrate cube of a number  
# showing difference between def() and lambda().
```

```
def cube(y):  
    return y*y*y;
```

```
g = lambda x: x*x*x  
print(g(7))
```

```
print(cube(5))
```

```
(lambda x: x * x)(3)
```

[https://www.w3schools.com/python/python\\_lambda.asp](https://www.w3schools.com/python/python_lambda.asp)

<https://realpython.com/python-lambda/>

<https://www.geeksforgeeks.org/python-lambda-anonymous-functions-filter-map-reduce/>

# lambda

## Syntax

As you saw in the previous sections, a lambda form presents syntactic distinctions from a normal function. In particular, a lambda function has the following characteristics:

- It can only contain expressions and can't include statements in its body.
- It is written as a single line of execution.
- It does not support type annotations.
- It can be immediately invoked (IIFE).

```
intervalo1 = lambda a, b : (b,a) if a>b else (a,b)
```

```
intervalo1 = lambda a, b : if a>b : (b,a) else: (a,b)
```



<https://realpython.com/python-lambda/>

# lambda

## Syntax

As you saw in the previous sections, a lambda form presents syntactic distinctions from a normal function. In particular, a lambda function has the following characteristics:

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- It does not support type annotations.
- It can be immediately invoked (IIFE).

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```

```
intervalo1 = lambda a, b : if a>b : (b,a) else: (a,b)
```



<https://realpython.com/python-lambda/>

# Just test

```
my_list = [1, 5, 4, 6, 8, 11, 3, 12]
new_list = list(filter(lambda x: (x%2 == 0) , my_list))
# Output: [4, 6, 8, 12]
print(new_list)
```

```
my_list = [1, 5, 4, 6, 8, 11, 3, 12]
new_list = list(map(lambda x: x * 2 , my_list))
# Output: [2, 10, 8, 12, 16, 22, 6, 24]
print(new_list)
```

```
def myfunc(n):
    return lambda a : a * n

mydoubler = myfunc(2)
mytripler = myfunc(3)

print(mydoubler(11))
print(mytripler(11))
```

<https://www.programiz.com/python-programming/anonymous-function>

[https://www.w3schools.com/python/python\\_lambda.asp](https://www.w3schools.com/python/python_lambda.asp)



# Curiosities: default values

```
#!/usr/bin/python3

# Function definition is here
def printinfo( name, age = 35 ):
    "This prints a passed info into this function"
    print ("Name: ", name)
    print ("Age ", age)
    return

# Now you can call printinfo function
printinfo( age = 50, name = "miki" )
printinfo( name = "miki" )
```

When the above code is executed, it produces the following result –

```
Name: miki
Age  50
Name: miki
Age  35
```

[https://www.tutorialspoint.com/python3/python\\_functions.htm](https://www.tutorialspoint.com/python3/python_functions.htm)

# Curiosities: using parameters names

```
#!/usr/bin/python3

# Function definition is here
def printinfo( name, age ):
    "This prints a passed info into this function"
    print ("Name: ", name)
    print ("Age ", age)
    return

# Now you can call printinfo function
printinfo( age = 50, name = "miki" )
```

When the above code is executed, it produces the following result –

```
Name: miki
Age  50
```

[https://www.tutorialspoint.com/python3/python\\_functions.htm](https://www.tutorialspoint.com/python3/python_functions.htm)

# Functions and parameters

# Function parameters

## Pass by value

### immutable

- *safe from change*, i.e. the contents of objects cannot be changed within a method
- Just copies them... - pass by value
- Basic values
- Int, float

## Pass by reference

### mutable

- objects of which contents can be changed within a method
- Uses reference – send a reference to the data
- “complex” structures
- List, dictionaries...

**Immutable objects can't be changed.**

**Mutable objects can be changed.**

Type	Immutable?
int	Yes
float	Yes
bool	Yes
complex	Yes
tuple	Yes
frozenset	Yes
str	Yes
list	No
set	No
dict	No

<https://realpython.com/pointers-in-python/>

# Function parameters

## Pass by value

### immutable

```
>>> def increment(n):  
...     n += 1  
...     return n  
  
>>> a = 3  
  
>>> a = increment(a)  
# the return value of increment()  
# is captured!  
  
>>> print(a)  
  
a = 4  
  
# a now refers to the new object  
# created by the function
```

## Pass by reference

### mutable

```
>>> def increment(n):  
...     n.append([4])  
  
>>> L = [1, 2, 3]  
  
>>> increment(L)  
  
>>> print(L)  
  
L = [1, 2, 3, 4]    # a changed!
```

# Pass by value

the copier  
i.e. Creates the copy



The original  
i.e. "data"



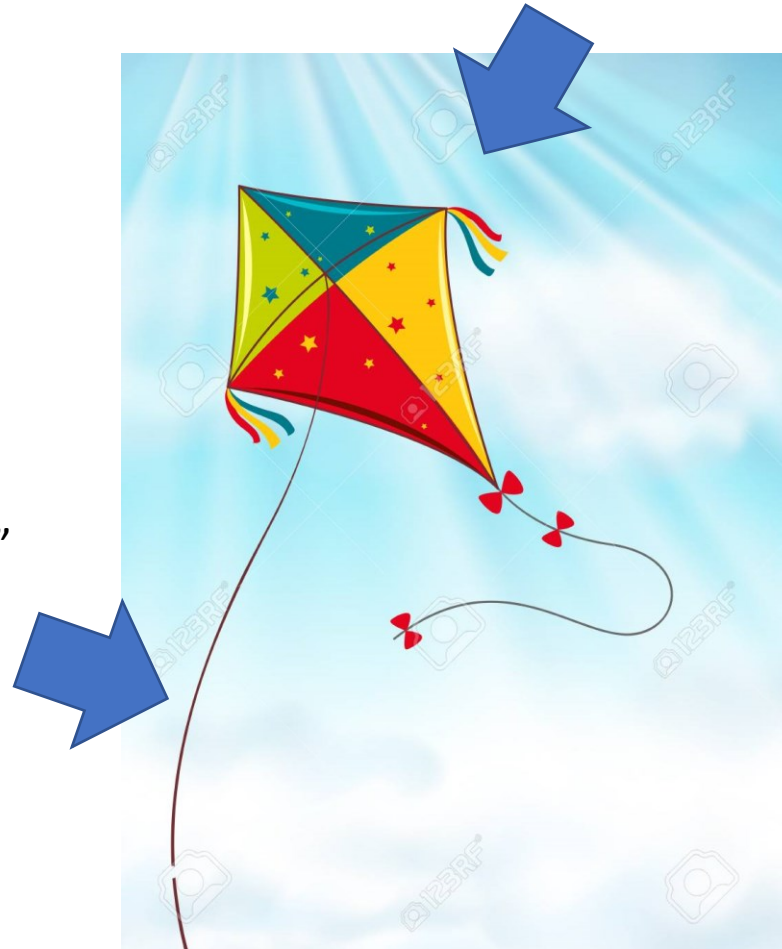
The copy to use  
- No change on original



# Pass by reference

The kite  
i.e. “data”

The reference  
i.e. allows to reach the “data”





# Try this code in pythontutor

```
def changeme( mylist ):  
    mylist.append([1,2,3,4])  
    print("values inside the function", mylist)  
    return
```

```
mylist=[10,20,30]  
changeme( mylist)  
print("values outside the function", mylist)
```

<http://www.pythontutor.com/visualize.html>

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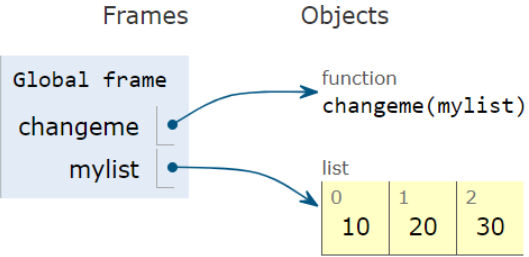
Python 3.6  
([known limitations](#))

```
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2     mylist.append([1,2,3,4])  
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4     return  
5  
→ 6 mylist=[10,20,30]  
→ 7 changeme( mylist)  
8 print("values outside the function", mylist)
```

[Edit this code](#)

→ line that just executed  
→ next line to execute

Print output (drag lower right corner to resize)



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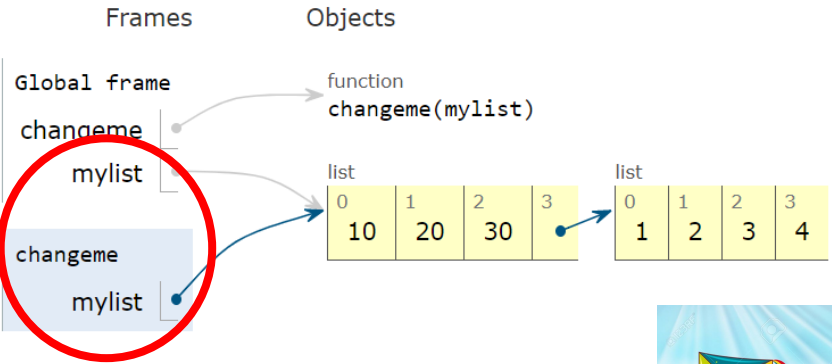
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[Edit this code](#)

→ line that just executed  
→ next line to execute

Print output (drag lower right corner to resize)  
values inside the function [10, 20, 30, [1, 2, 3



Same reference (line to the same “kite” )  
They are the same...



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Python 3.6  
([known limitations](#))

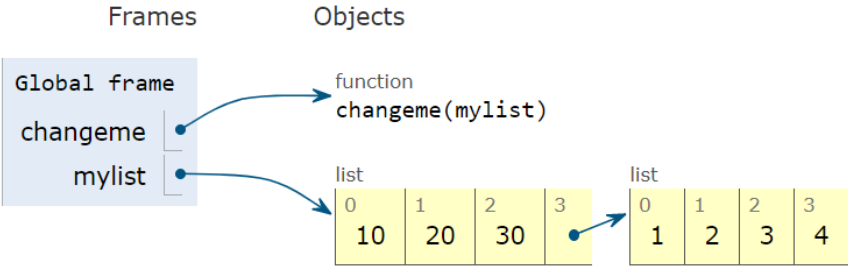
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[Edit this code](#)

→ line that just executed  
→ next line to execute

Print output (drag lower right corner to resize)

```
values inside the function [10, 20, 30, [1, 2, 3  
values outside the function [10, 20, 30, [1, 2,
```



# Try this code in pythontutor

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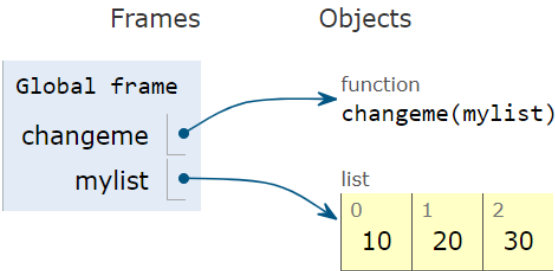
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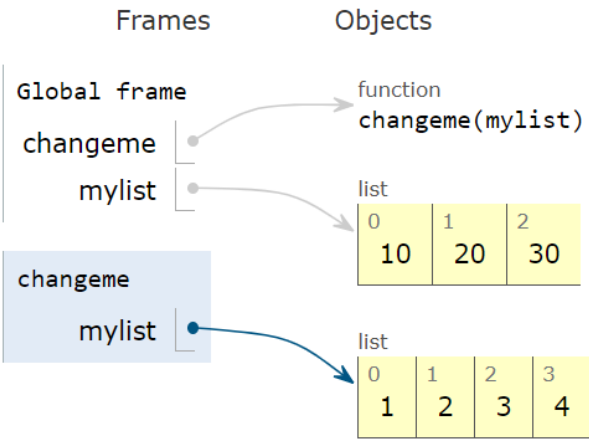
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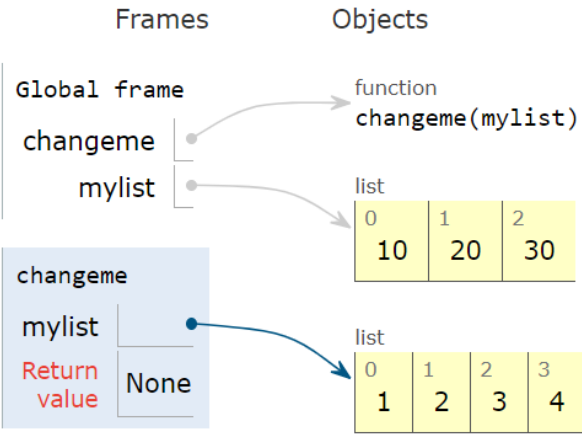
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Print output (drag lower right corner to resize)

values inside the function [1, 2, 3, 4]





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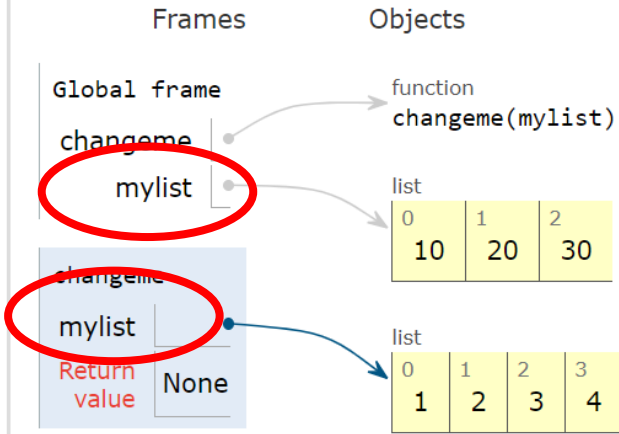
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Print output (drag lower right corner to resize)

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Same name but not the same...  
Not linked to the same “kite”

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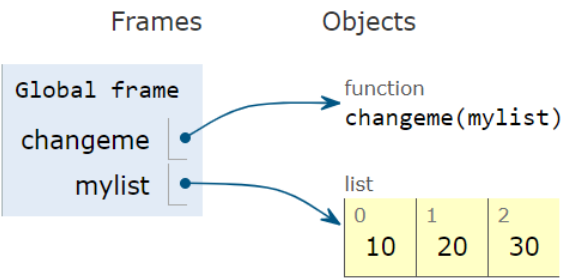
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Print output (drag lower right corner to resize)

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# Pass by reference

All parameters (arguments) in the Python language are passed by reference. It means if you change what a parameter refers to within a function, the change also reflects back in the calling function. For example –

```
#!/usr/bin/python

# Function definition is here
def changeme( mylist ):
    "This changes a passed list into this function"
    mylist = [1,2,3,4]; # This would assign new reference in mylist
    print "Values inside the function: ", mylist
    return

# Now you can call changeme function
mylist = [10,20,30];
changeme( mylist );
print "Values outside the function: ", mylist
```

```
Values inside the function: [1, 2, 3, 4]
Values outside the function: [10, 20, 30]
```

mylist

10	20	30
----	----	----

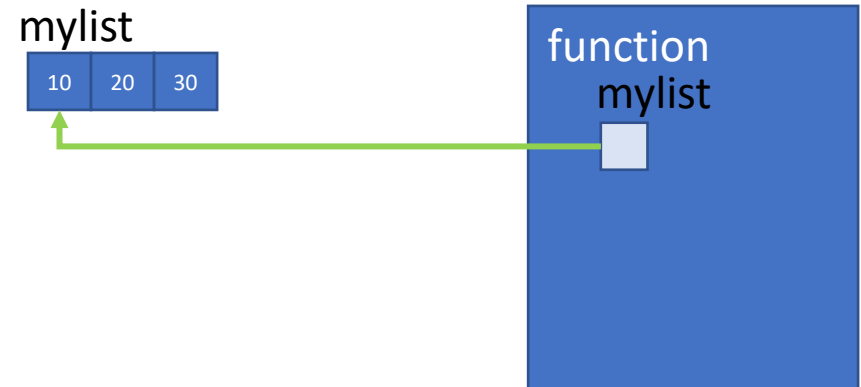
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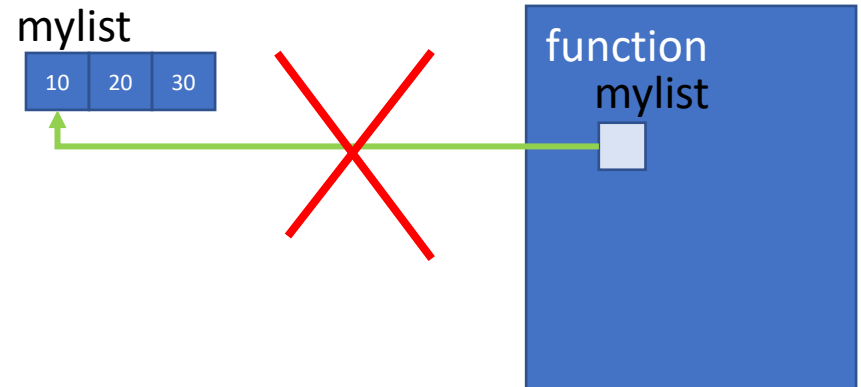
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Loose reference...  
i.e. override the reference  
Loose the original data

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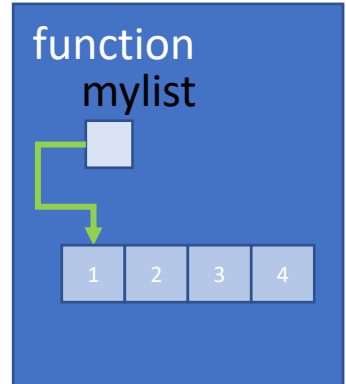
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```

```
Values inside the function: [1, 2, 3, 4]
Values outside the function: [10, 20, 30]
```

mylist

10	20	30
----	----	----



Loose reference...  
i.e. override the reference  
Loose the original data

# The End