

Week 05 - Some ideas and exercises

Mathematical succession

Initial condition

The rule

$$a_1 = 2 \text{ y } a_n = 3a_{n-1}$$

The times= the n ou select

$$a_2 = 3a_1 = 3 \times 2 = 6$$

$$a_3 = 3a_2 = 3 \times 6 = 18$$

$$a_4 = 3a_3 = 3 \times 18 = 54$$

Mathematical succession

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$$a_1 = 2 \text{ y } a_n = 3a_{n-1}$$

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$$a_3 = 3a_2 = 3 \times 6 = 18$$

$$a_4 = 3a_3 = 3 \times 18 = 54$$

aN= ... the initial condition

i=0 # how many times

while I<N : # end when I reaches N

aN1= ... aN ... # the rule

i=i+1 # next index

aN = aN1 # the new becomes the old

Mathematical succession

Initial condition

The rule

$$a_1 = 2 \text{ y } a_n = 3a_{n-1}$$

The times= the n ou select

$$a_2 = 3a_1 = 3 \times 2 = 6$$

$$a_3 = 3a_2 = 3 \times 6 = 18$$

$$a_4 = 3a_3 = 3 \times 18 = 54$$

aN= ... the initial condition

I =0 # how many times

while I<n : # end when I reaches n

aN1= 3 * aN # the rule

i=i+1 # next index

aN = aN1 # the new becamas the old

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
→ 4 while i<n : # end when I reaches n
→ 5     print("termo a({}) é {}".format((i+1),aN))
6     aN1= 3 * aN # the rule
7     i=i+1 # next index
8     aN = aN1 # the new becomes the old
9 print("the end")
```

[Edit this code](#)

→ line that just executed
→ next line to execute

Print output (drag lower right corner to resize)

Frames Objects

Global frame	
i	0
n	5
aN	2

<http://tiny.cc/k8g0tz>

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
4 while i<n : # end when I reaches n
→ 5     print("termo a({}) é {}".format((i+1),aN))
→ 6     aN1= 3 * aN # the rule
7     i=i+1 # next index
8     aN = aN1 # the new becomes the old
9     print("the end")
```

[Edit this code](#)

→ line that just executed
→ next line to execute

Print output (drag lower right corner to resize)

termo a(1) é 2

Frames Objects

Global frame	
i	0
n	5
aN	2

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
➔ 4 while i<n : # end when I reaches n
5     print("termo a({}) é {}".format((i+1),aN))
6     aN1= 3 * aN # the rule
7     i=i+1 # next index
➔ 8     aN = aN1 # the new becomes the old
9     print("the end")
```

[Edit this code](#)

- ➔ line that just executed
- ➔ next line to execute

Print output (drag lower right corner to resize)

termo a(1) é 2

Frames Objects

Global frame	
i	1
n	5
aN	6
aN1	6

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
4 while i<n : # end when I reaches n
5     print("termo a({}) é {}".format((i+1),aN))
6     aN1= 3 * aN # the rule
→ 7     i=i+1 # next index
→ 8     aN = aN1 # the new becomes the old
9     print("the end")
```

[Edit this code](#)

→ line that just executed
→ next line to execute

Print output (drag lower right corner to resize)

```
termo a(1) é 2
termo a(2) é 6
termo a(3) é 18
termo a(4) é 54
termo a(5) é 162
```

Frames Objects

Global frame	
i	5
n	5
aN	162
aN1	486

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
➔ 4 while i<n : # end when I reaches n
5     print("termo a({}) é {}".format((i+1),aN))
6     aN1= 3 * aN # the rule
7     i=i+1 # next index
➔ 8     aN = aN1 # the new becomes the old
9     print("the end")
```

[Edit this code](#)

- ➔ line that just executed
- ➔ next line to execute

Print output (drag lower right corner to resize)

```
termo a(1) é 2
termo a(2) é 6
termo a(3) é 18
termo a(4) é 54
termo a(5) é 162
```

Frames

Objects

Global frame

i	5
n	5
aN	486
aN1	486

Python 3.6
([known limitations](#))

```
1 i =0 # how many times
2 n=5
3 aN= 2 # the initial condition
4 while i<n : # end when I reaches n
5     print("termo a({}) é {}".format((i+1),aN))
6     aN1= 3 * aN # the rule
7     i=i+1 # next index
8     aN = aN1 # the new becomes the old
→ 9 print("the end")
```

[Edit this code](#)

→ line that just executed
→ next line to execute

Print output (drag lower right corner to resize)

```
termo a(2) é 6
termo a(3) é 18
termo a(4) é 54
termo a(5) é 162
the end
```

Frames Objects

Global frame	
i	5
n	5
aN	486
aN1	486

Mathematical succession

Initial condition

The rule

$$a_1 = 2 \text{ y } a_n = 3a_{n-1}$$

The times= the n ou select

$$a_2 = 3a_1 = 3 \times 2 = 6$$

$$a_3 = 3a_2 = 3 \times 6 = 18$$

$$a_4 = 3a_3 = 3 \times 18 = 54$$

aN= ... the initial condition

For I in range(n) # end when I reaches N

while I<N :

aN1= 3 * aN # the rule

i=i+1 # next index

aN = aN1 # the new becamas the old

Python 3.6
([known limitations](#))

```
➔ 1 n=5
   2 aN= 2 # the initial condition
   3 for i in range( n) : # end when i reaches n (0,1,2 , n-1 )
   4 # while I<N :
   5     print("termo a({}) é {}".format((i+1),aN))
   6     aN1= 3 * aN # the rule
   7     # i=i+1 # next index
   8     aN = aN1 # the new becomes the old
   9 print("the end")
```

[Edit this code](#)

- ➡ line that just executed
- ➔ next line to execute

Print output (drag lower right corner to resize)

Frames

Objects

<http://tiny.cc/y8g0tz>

Why loops? Repeat something

Note: this is not a undeniable truth but can help when starting to use loops

Know how many time?

```
fruits = ['banana', 'apple', 'mango']
for fruit in fruits:      # Second Example
    print 'Current fruit :', fruit

print "Good bye!"
```

```
# printing first 20
# whole number
for i in range(20):
    print(i, end = " ")
```

```
fruits = ['banana', 'apple', 'mango']
for index in range(len(fruits)):
    print 'Current fruit :', fruits[index]

print "Good bye!"
```

When you know and for everything else

```
count = 0
while (count < 9):
    print 'The count is:', count
    count = count + 1

print "Good bye!"
```

```
a=int(input("a?"))
mx=a
while a!=0 :
    a=int( input("a?"))
```

Repetition, loops

while loop

Repeats a statement or group of statements while a given condition is TRUE. It tests the condition before executing the loop body.

for loop

Executes a sequence of statements multiple times and abbreviates the code that manages the loop variable.

nested loops

You can use one or more loop inside any another while, for or do..while loop.

https://www.tutorialspoint.com/python/python_loops.htm

https://www.w3schools.com/python/python_while_loops.asp

<https://realpython.com/python-while-loop/>

https://www.tutorialspoint.com/python/python_while_loop.htm

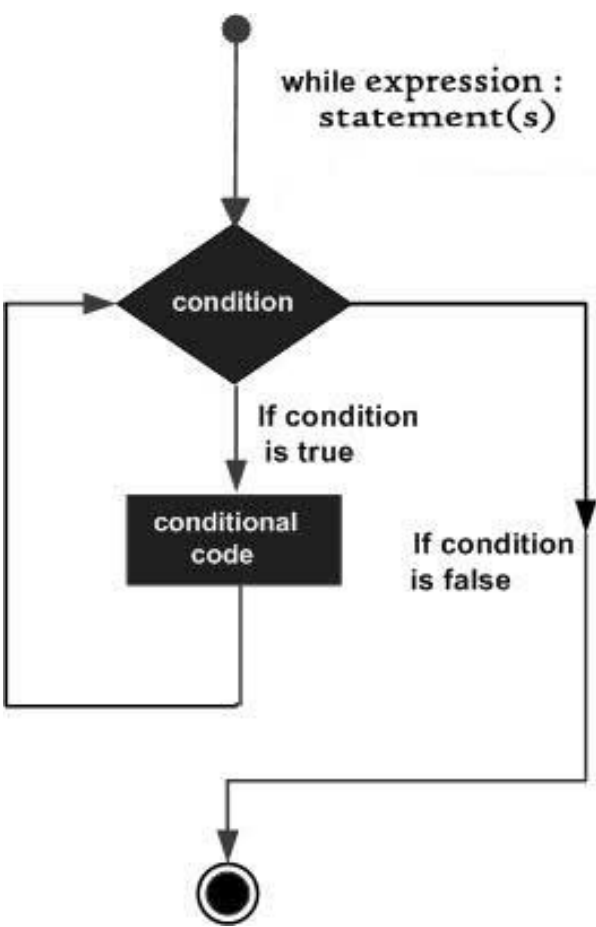
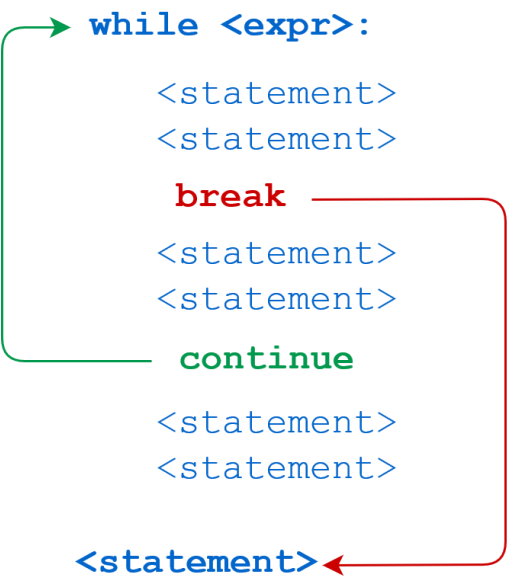
while

```
count = 0
while (count < 9):
    print 'The count is:', count
    count = count + 1

print "Good bye!"
```

<http://tiny.cc/59g0tz>

```
The count is: 0
The count is: 1
The count is: 2
The count is: 3
The count is: 4
The count is: 5
The count is: 6
The count is: 7
The count is: 8
Good bye!
```



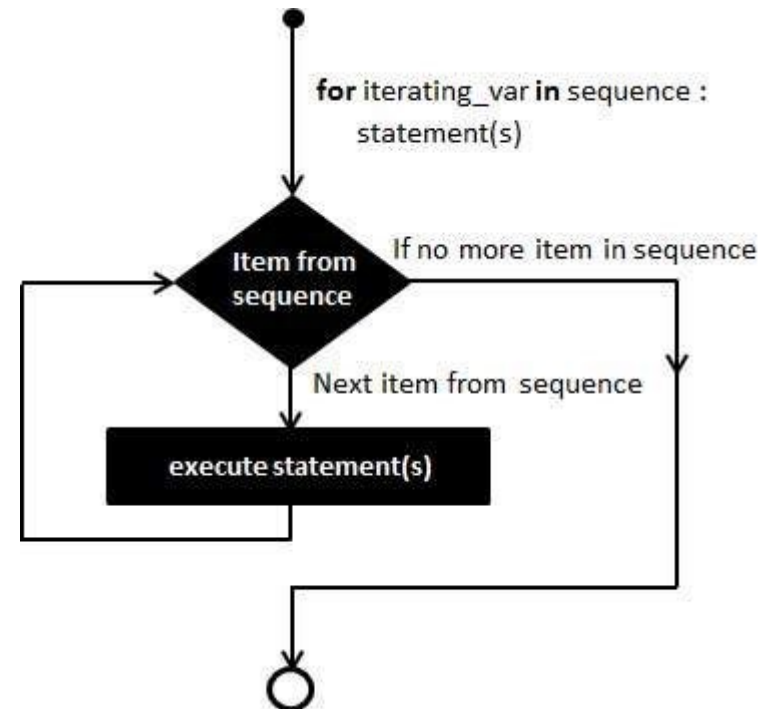
For: collection

```
fruits = ['banana', 'apple', 'mango']  
for fruit in fruits:      # Second Example  
    print 'Current fruit :', fruit  
  
print "Good bye!"
```

<http://tiny.cc/i9g0tz>

```
Current fruit : banana  
Current fruit : apple  
Current fruit : mango  
Good bye!
```

<https://realpython.com/python-for-loop/>

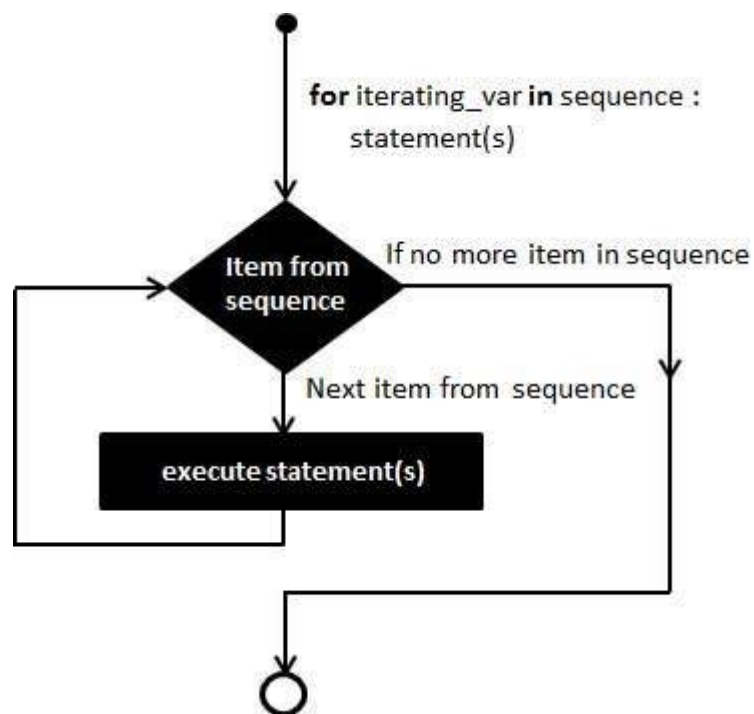


For: ranges

```
fruits = ['banana', 'apple', 'mango']  
for index in range(len(fruits)):  
    print 'Current fruit :', fruits[index]  
  
print "Good bye!"
```

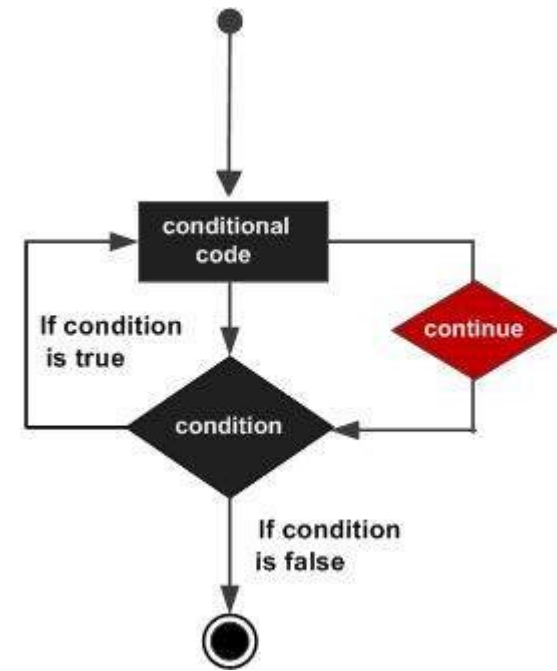
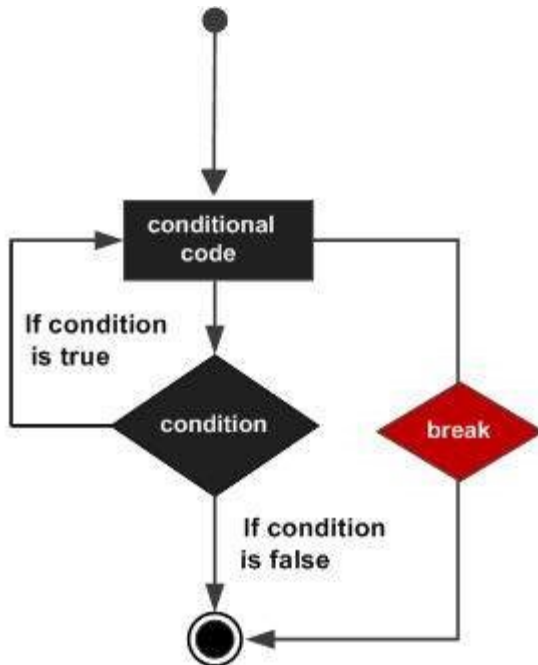
<http://tiny.cc/q9g0tz>

```
Current fruit : banana  
Current fruit : apple  
Current fruit : mango  
Good bye!
```



<https://realpython.com/python-for-loop/>

Break, continue



```

for letter in 'Python':    # First Example
    if letter == 'h':
        break
    print 'Current Letter :', letter
    
```

```

for letter in 'Python':    # First Example
    if letter == 'h':
        continue
    print 'Current Letter :', letter
    
```

https://www.tutorialspoint.com/python/python_continue_statement.htm

https://www.tutorialspoint.com/python/python_break_statement.htm

Nested loops

```
for iterating_var in sequence:  
    for iterating_var in sequence:  
        statements(s)  
statements(s)
```

```
while expression:  
    while expression:  
        statement(s)  
statement(s)
```

https://www.tutorialspoint.com/python3/python_nested_loops.htm

https://www.tutorialspoint.com/python/python_nested_loops.htm

<https://study.com/academy/lesson/nested-loops-in-python-definition-examples.html>

Reading and... stopping

- Reading value
 - “input” from user
`Input(“a?”)`
- Reading values is a repetitive task
`While ... something...`
`Input(“a?”)`
- Usually is non eternal
 - Need to stop on some condition
`While ... something...`
`Input(“a?”)`

Some examples

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
a=int(input("a?"))
```

```
while a!=0 :
```

```
    a=int( input("a?"))
```

<http://tiny.cc/y9g0tz>

Some examples

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
a=int(input("a?"))
```

```
while a!=0 :
```

```
    a=int( input("a?"))
```

Read values (the "a") until a 0 appears

Or

While values != 0 are read ...

Some examples: maximum

a	Mx	
2	2	
4	4	$mx < a$? true
2		
5	5	$mx < a$? true
1		
0		$A == 0$? True

```

A=int( input("a?"))
Mx=a
If a==0 : exit()
If mx<a :
    mx=a
A=int( input("a?"))
If a==0 : exit()
If mx<a :
    mx=a
A=int( input("a?"))
If a==0 : exit()
If mx<a :
    mx=a
    
```


Some examples

Maximum

An element $M \in X$ is a **maximum**
if $x \leq M$ for every $x \in X$.

```
A=int( input("a?"))
```

```
Mx=a
```

```
If a==0 : exit()
```

```
If mx<a :
```

```
    mx=a
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
If mx<a :
```

```
    mx=a
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
If mx<a :
```

```
    mx=a
```

```
A=int( input("a?"))
```

```
If a==0 : exit()
```

```
If mx<a :
```

```
    mx=a
```

```
a=int(input("a?"))
```

```
mx=a
```

```
while a!=0 :
```

```
    If a>mx :
```

```
        mx = a
```

```
a=int( input("a?"))
```

<http://tiny.cc/7ag0tz>

Read values (the "a") until a 0 appears
and finds maximum

Or

While values != 0 are read ...
and finds maximum

Some examples

```
str= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
str=input("a?")
```

```
while str!="":
```

```
    str= input("a?")
```

<http://tiny.cc/eag0tz>

Some examples

```
str= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
A= input("a?")
```

```
If str!="": exit()
```

```
str=input("a?")
```

```
while str!="":
```

```
    str= input("a?")
```

Read string until nothing is entered (empty string "")

Or

Read string while something not empty (!="") is read ...

What does the following code does?

```
a=int( input("a?"))
while a >= 0 :
    a=int(input("a?"))
```

```
a=int( input("a?"))
while a != 0 :
    a=int(input("a?"))
```

```
str=input("a?")
while str!="":
    str= input("a?")
```

Condition on input
As a number
As a string

...

```
a=int( input("a?"))
while a%2== 0 :
    a=int(input("a?"))
```

```
str=input("a?")
while str!="end" :
    str= input("a?")
```

What does the following code does?

Read values while they ≥ 0

```
a=int( input("a?"))
while a $\geq$  0 :
    a=int(input("a?"))
```

Read values while they are $\neq 0$

```
a=int( input("a?"))
while a $\neq$  0 :
    a=int(input("a?"))
```

Read string while they not empty

```
str=input("a?")
while str $\neq$ "" :
    str= input("a?")
```

Condition on input
As a number
As a string

...

```
a=int( input("a?"))
while a $\%2$  $\neq$  0 :
    a=int(input("a?"))
```

Read values while they are even

```
str=input("a?")
while str $\neq$ "end" :
    str= input("a?")
```

Read strings until "end" string is read

Reading values for something

```
a=int(input("a?"))
while a!=0 :
    a=int( input("a?"))
```

The task

```
a=int(input("a?"))
mx=a
while a!=0 :
    If a>mx :
        mx = a
a=int( input("a?"))
```

```
a=int(input("a?"))
mn=a
while a!=0 :
    If a<mn :
        mn = a
a=int( input("a?"))
```

```
a=int(input("a?"))
sum=0
while a>= 0 :
    sum=sum+a
a=int(input("a?"))
```

Reading values for something

```
a=int(input("a?"))
while a!=0 :
    a=int( input("a?"))
```

```
a=int(input("a?"))
```

mx=a

```
while a!=0 :
```

*Read values while they are !=0 and
finds the maximum*

```
a=int( input("a?"))
```

```
a=int(input("a?"))
```

sum=0

```
while a>= 0 :
```

sum=sum+a

```
a=int(input("a?"))
```

The task

*Read values while they are !=0 and
finds the minimum*

```
a=int(input("a?"))
```

mn=a

```
while a!=0 :
```

If a<mn :

mn = a

```
a=int( input("a?"))
```

*Read values while they are >=0 and
finds their sum*

What does the following code does?

The condition
The task

```
a=int(input("a?"))
sum=0
c=0
while a>= 0 :
    sum=sum+a
    c=c+1
    a=int(input("a?"))
avg=sum / c
```

```
a=int(input("a?"))
sum=0
c=0
while True :
    if a==0 :
        break
    sum=sum+a
    c=c+1
    a=int(input("a?"))
avg=sum / c
```


What does the following code does?

The condition

The task

```
a=int(input("a?"))
sum=0
c=0
while a>= 0 :
    sum=sum+a
    c=c+1
    a=int(input("a?"))
avg=sum / c
```

*Read values while they are >=0
and calculates the average of positive values*

```
str=input("a?")
sum=0
c=0
while str!="":
    a=int(str)
    sum=sum+a
    c=c+1
    str= input("a?")
avg=sum / c
```

*Reads values an empty string is read
and calculates the average of all values*

Breaks and continue

```
a=1
sum=0
c=0
while a!=0 :
    a=int(input("a?"))
    if a<0
        continue
    sum=sum+a
    c=c+1
avg=sum / c
```

The condition

The task

```
a=int(input("a?"))
sum=0
c=0
while True :
    if a==0 :
        break
    sum=sum+a
    c=c+1
    a=int(input("a?"))
avg=sum / c
```

Breaks and continue

*Read values while they are !=0
and calculates the average of positive values*

```
a=1
sum=0
c=0
while a!=0 :
    a=int(input("a?"))
    if a<0:
        continue
    sum=sum+a
    c=c+1
avg=sum / c
```

The condition

The task

```
a=int(input("a?"))
sum=0
c=0
while True :
    if a==0 :
        break
    sum=sum+a
    c=c+1
    a=int(input("a?"))
avg=sum / c
```

*Read values while they are !=0
and calculates the average of all values*

What does the following code does?

The condition

The task

<http://tiny.cc/xag0tz>

<http://tiny.cc/8bg0tz>

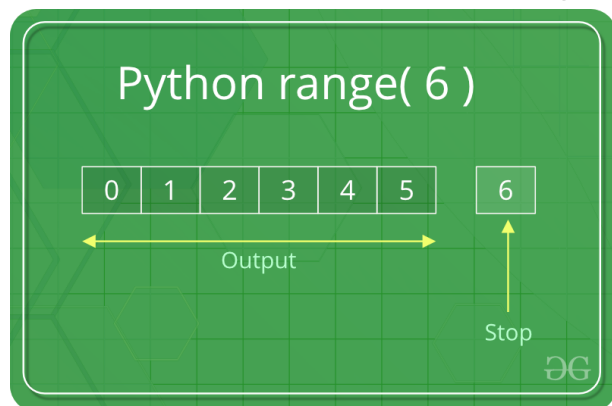
```
a=1
sum=0
c=0
while a!=0 :
    a=int(input("a?"))
    if a<0
        continue
    sum=sum+a
    c=c+1
avg=sum / c
```

```
str=input("a?")
sum=0
c=0
while str!="":
    a=int(str)
    sum=sum+a
    c=c+1
    str= input("a?")
avg=sum / c
```

Question: what with the "avg=sum/c" in ALL previous examples?
Fix it so the code works properly

range

Some help: range



```
for i in range(10):
    print(i, end = " ")
print()
```

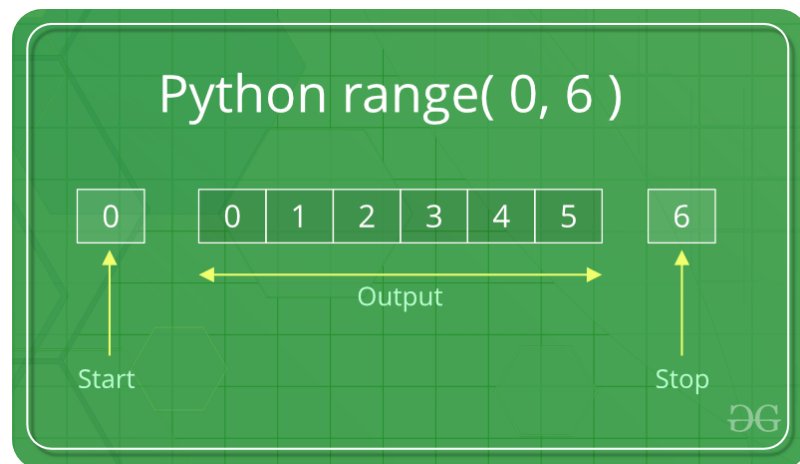
```
# printing first 20
# whole number
for i in range(20):
    print(i, end = " ")
```

```
0 1 2 3 4 5 6 7 8 9
```

```
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19
```

<https://www.geeksforgeeks.org/python-range-function/>

Some help: range



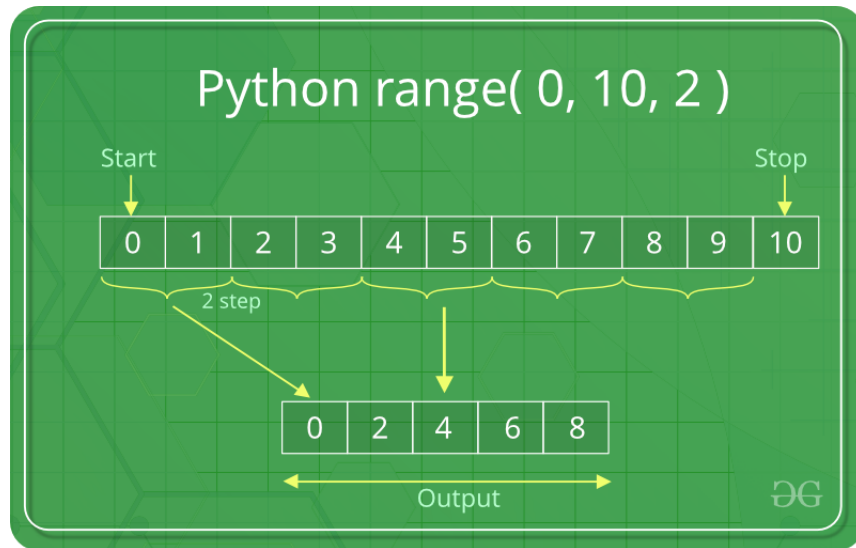
```
for i in range(1, 20):
    print(i, end = " ")
print()
```

```
# printing a natural
# number from 5 to 20
for i in range(5, 20):
    print(i, end = " ")
```

```
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19
5 6 7 8 9 10 11 12 13 14 15 16 17 18 19
```

<https://www.geeksforgeeks.org/python-range-function/>

Some help: range



```
0 3 6 9 12 15 18 21 24 27
0 5 10 15 20 25 30 35 40 45
```

```
for i in range(0, 30, 3):
    print(i, end = " ")
print()
```

```
# using range to print number
# divisible by 5
for i in range(0, 50, 5):
    print(i, end = " ")
```

<https://www.geeksforgeeks.org/python-range-function/>

What does the following code does?

```
i = 2
while(i < 100):
    j = 2
    while(j <= (i/j)):
        if not(i%j): break
        j = j + 1
    if (j > i/j) : print i, " is prime"
    i = i + 1
```

<http://tiny.cc/kgb0tz>

What does the following code does?

```
import sys
for i in range(1,11):
    for j in range(1,11):
        k = i*j
        print (k, end=' ')
    print()
```

<http://tiny.cc/tbg0tz>

```
for a in [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]:
    for b in [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]:
        print("{} x {} = {}".format(a, b, a*b))
```

Some examples

```
>>> # One parameter
>>> for i in range(5):
...     print(i)
...
0
1
2
3
4
>>> # Two parameters
>>> for i in range(3, 6):
...     print(i)
...
3
4
5
>>> # Three parameters
>>> for i in range(4, 10, 2):
...     print(i)
...
4
6
8
>>> # Going backwards
>>> for i in range(0, -10, -2):
...     print(i)
...
0
-2
-4
-6
-8
```

```
>>> my_list = ['one', 'two', 'three', 'four', 'five']
>>> my_list_len = len(my_list)
>>> for i in range(0, my_list_len):
...     print(my_list[i])
...
one
two
three
four
five
```

<https://www.pythoncentral.io/pythons-range-function-explained/>

Define your own range function:

- `Range(end)`
- `Range(start, end)`
- `Range(start, end, step)`

- Note: just print the numbers to the screen

Return the numbers: Just a help

```
l=[]  
for i in range(0,10) :  
    l.append( i )
```

```
list = []          ## Start as the empty list  
list.append('a')   ## Use append() to add elements  
list.append('b')
```

Exercises ...

What does the following code does?

```
import sys
for i in range(1,11):
    for j in range(1,11):
        k = i*j
        print (k, end=' ')
    print()
```

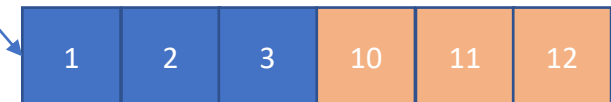
Plot: define arrange...

- Help
 - Loop for numpy.arrange / arrays

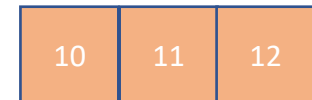
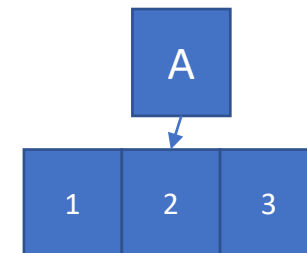
```
import numpy
a = numpy.array([1, 2, 3])
newArray = numpy.append (a, [10, 11, 12])
print(newArray)
```

[1 2 3 10 11 12]

newArray



APPEND



<https://likegeeks.com/numpy-array-tutorial/>

4. Considere a sequência real (U_0, U_1, \dots) onde o primeiro termo é $U_0=100$ e os seguintes são dados por $U_n = 1.01 U_{n-1} - 1.01$. O programa `sequenceUn.py` gera os primeiros 20 termos dessa sequência. Modifique o programa para mostrar todos os termos, enquanto forem positivos. Note que terá que usar uma instrução `while`. No fim, o programa deve dizer quantos termos gerou.
5. Escreva uma função `factorial(n)` que calcule o fatorial de n , definido por $n! = 1 \times 2 \times 3 \times \dots \times n$. Teste a função com diversos valores de n .

9. A sequência de Fibonacci é uma sequência de inteiros na qual cada elemento é igual à soma dos dois anteriores: 0, 1, 1, 2, 3, 5, 8, 13, ..., ou seja, cada termo obtém-se como $F_n = F_{n-1} + F_{n-2}$. Os primeiros valores são definidos como $F_0 = 0$ e $F_1 = 1$. Escreva uma função `Fibonacci(n)` para calcular o n-ésimo número de Fibonacci. *Sugestão: em cada iteração atualize e guarde os dois últimos valores da sequência.*
10. Escreva uma função `isPrime(n)` que devolva `True` se o número n é primo e `False`, caso contrário. Um número N é primo se não tiver divisores além de 1 e de N . *Sugestão: tente dividir o número por 2, por 3, etc. Se encontrar um divisor exato, então o número não é primo.* Teste a função fazendo um programa que percorre todos os números entre 1 e 100 e indique para cada um se é primo ou não.

6. O jogo HiLo consiste em tentar adivinhar um número (inteiro) entre 1 e 100. No início, o programa escolhe um número aleatoriamente. Depois, o utilizador introduz um número e o programa indica se é demasiado alto (High), ou demasiado baixo (Low). Isto é repetido até o utilizador acertar no número. O jogo acaba indicando quantas tentativas foram feitas. O programa `hilo.py` já tem uma instrução para gerar um número aleatório com a função `randrange` do módulo `random`. Complete o programa para fazer o resto do jogo.

Some ideas

- Print all leap years between to given years
- Ler valores até algum ser 0
 - Imprimir máximo, mínimo

The END