Working Title: A Comparison of Approaches for Unplanned Sample Sizes in Phase II Clinical Trials

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ABSTRACT

In this thesis, we develop .....

Chapter 1

Introduction

The introduction will talk about the motivation for the thesis. Introduce some examples of when we would need such methods.

Oncology phase II clinical trials are often used to evaluate the initial effect of a new regimen to determine if to warrant further study in a phase III clinical trial [1, 2, 3]. Simon's two-stage design [2] is a commonly used design in specifying sample sizes and critical values in phase II oncology clinical trials. Koyama and Chen [3] point out that it is common for actual sample sizes of these phase II trials to differ than the planned, pre-specified sample sizes. This could happen because of unanticipated accruement speed, drop-out rates are unexpected, and often multi-center trials can be slow in sharing information ... Currently, when unplanned sample sizes occur, it is common practice to treat the attained sample sizes as planned. Though, when acheived sample sizes differ from planned, hypothesis testing using the attained sample sizes as if they were planned is not valid and hypothesis testing in these cases is not straightforward [1, 3]. Because of these reasons, extensions of Simon's design for hypothesis testing with unplanned sample sizes is important.

Talk about examples here

There have been many attempts to develop Frequentist methods that handle unplanned sample sizes in the second stage while using the planned stage I sample size, but my literature review found that there were only few Frequentist methods to handle unplanned sample sizes in both stage I and stage II. Likelihood based designs, that are able to be an extension of Simon's design, offer a nice solution to this problem because these designs offer flexi-

bility in sample size without inflation of type I error. In this paper, we discuss the different methods for Simon's design when the attained stage II sample size is different than planned and when attained sample sizes in both stages are different than planned. In chapter 4, we review a concrete example from a Likelihood-based clinical trial, and in chapter 5, results of a numerical and theoretical study comparing the Frequentist properties of approaches in the setting where both stages differ **wording** in different settings are presented.

Chapter 2

Background

Simon's design will go here. This section will also talk about extending/shortening a trial (unplanned sample sizes) and how recalculating as if it were the planned design will introduce bias and inflate type I error. Talk about prespecifying (maybe here?)

We will only talk about extensions to Simon's design, hypothesis testing, and only stopping for futility in this paper.

Chapter 3

Unplanned Sample Sizes

This chapter will talk about unplanned sample sizes when only the second stage is different and when both stages can be different. The former will talk about methods such as Koyama and Chen, UMVUE, MLE, etc. The latter will talk about the likelihood design, Chang, adaptation of Chang, and possibly Wu.

3.1 Unplanned Sample Sizes in Second Stage

3.2 Unplanned Sample Sizes in Both Stages

Decide later if subsections are needed.

3.2.1 *Chang et al.* Alternative Designs and Adaptation

Because accruement of patients can often be unexpected in both stages, it's imperative that methods are available to handle situations with attained sample sizes that differ from the planned sample size. Chang *et al* [4] proposed an alternative design that is an extension of Simons two stage design to handle unplanned sample sizes in both the first and second stages. Chang *et al* proposes that type II error probability spent in stage I, based on planned and attained sample size, is ...

Wu *et al* [**?**] also proposed an adjustment to Simons design based on attained sample sizes

in both the first and second stages. Because Wu's methods don't work very well **wording**, we won't consider their method for the remainder of this paper.

3.2.2 Likelihood Design

Likelihood characteristics:

$$LR_n = \frac{L_n(\theta_1)}{L_n(\theta_0)} \in \{[0, 1/k], [1/k, k], [k, \infty)\}$$

Probability of Weak Evidence

$$\gamma_p = P(k_a \leq LR_n \leq K_b | H_p), k_a \leq k_b$$

Probability of Strong Evidence

$$\eta_1 = P(LR_n > k_b | H_1)$$

$$\eta_1 = P(LR_n < k_a | H_0)$$

Probability of Observing Misleading Evidence

$$\tau_0 = P(LR_n > k_b | H_0), \tau_0 \leq 1/k_b$$

$$\tau_1 = P(LR_n < k_a | H_1), \tau_1 \leq k_a$$

$\tau_i = O_p(n^{-1/2})$instead of remaining fixed like type I error

Translating likelihood properties into Simon-like design:

Interim: Translating to successes. This is the region in which we move to stage 2

$$UB_{interim} = \frac{log(k_{bi}) - n_1 log(\frac{1-p_1}{1-p_0})}{log(\frac{p_1(1-p_0)}{p_0(1-p_1)})}$$

$$LB_{interim} = \frac{log(k_{ai}) - n_1 log(\frac{1-p_1}{1-p_0})}{log(\frac{p_1(1-p_0)}{p_0(1-p_1)})}$$

(LB, UB) is the interval for weak evidence. If this was Simon's design, $LB_{interim} = r_1$

Probability of strong, misleading, and weak evidence under the null

$$P(\text{Strong}_{0i}) = B(\lfloor LB_{interim} \rfloor, n_1, p_0)$$

$$P(Misleading_{0i}) = 1 - B(\lfloor UB_{interim} \rfloor, n_1, p_0)$$

$$P(Weak_{0i}) = B(\lfloor UB_{interim} \rfloor, n_1, p_0) - B(\lfloor LB_{interim} \rfloor, n_1, p_0)$$

Probability of strong, misleading, and weak evidence under the alternative

$$P(Strong_{0i}) = 1 - B(\lfloor UB_{interim} \rfloor, n_1, p_1)$$

$$P(Misleading_{0i}) = B(\lfloor LB_{interim} \rfloor, n_1, p_1)$$

$$P(Weak_{0i}) = B(\lfloor UB_{interim} \rfloor, n_1, p_1) - B(\lfloor LB_{interim} \rfloor, n_1, p_1)$$

note: under Simon's, PET = 1-P(Weak)

Translating likelihood properties into Simon-like design:

Final Stage: Translating to successes.

The amount of successes that allow for continuation to the second stage are:

$$(\lfloor LB_{interim}+1\rfloor, \lfloor min(n_1, UB_{interim})\rfloor)$$

Probability of strong, misleading, and weak evidence under H_p

$$P(Weak_p) = \sum_{x=\lfloor LB_{interim}+1\rfloor}^{\lfloor min(n_1,UB_{interim})\rfloor} \Big(b(x,n_1,p_p)\times B(UB_{interim}-x,n-n_1,p_p)\Big) - B(LB_{interim}-x,n-n_1,p_p)$$

$$P(Strong_p) = P(Strong_{0i}) + \sum_{x=\lfloor LB_{interim}+1\rfloor}^{\lfloor min(n_1,UB_{interim})\rfloor} \Big(b(x,n_1,p_0)\times B(LB_{interim}-x,n-n_1,p_0)\Big)$$

$$P(Misleading_p) = P(Misleading_{0i}) + \sum_{x=\lfloor LB_{interim}+1\rfloor}^{\lfloor min(n_1,UB_{interim})\rfloor} \Big(b(x,n_1,p_p)\times (1-B(UB_{interim}-x,n-n_1,p_p)\Big)$$

If we want to translate likelihood design into a Simon's design, we overwrite the LR limits above as:

$$k_{ai} = OR^{r_1}\frac{1-p_1}{1-p_0}^{n_1} = \frac{1-p_0}{1-p_1}^{r_1-n_1}\frac{p_1}{p_0}^{r_1}$$

$$k_a = OR^{r}\frac{1-p_1}{1-p_0}^{n} = \frac{1-p_0}{1-p_1}^{r-n}\frac{p_1}{p_0}^{r}$$

$$k_{bi} = k_b = \infty$$

Chapter 4

Example

Here put the results of comparing the Chang et al paper and adaptation to the protocol of the study. We used Monte Carlo simulation to examine the performance of the study design of Chang et al...

Chapter 5

Results

The findings will be put here - primarily tables covering different combinations of Simon's designs and unplanned sample sizes.

Should maybe talk about how I couldn't replicate some results in the paper.

[3]

REFERENCES

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[3] T. Koyama and H. Chen, "Proper inference from simon's two-stage designs," *Statistics In Medicine*, vol. 27, pp. 3145–3154, 2008.

[4]