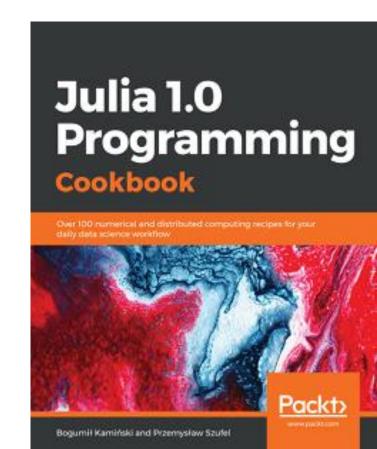
Parallel and distributed computing with Julia

Przemysław Szufel, PhD Warsaw School of Economics

https://szufel.pl/

https://szufel.pl/SCF2019.zip

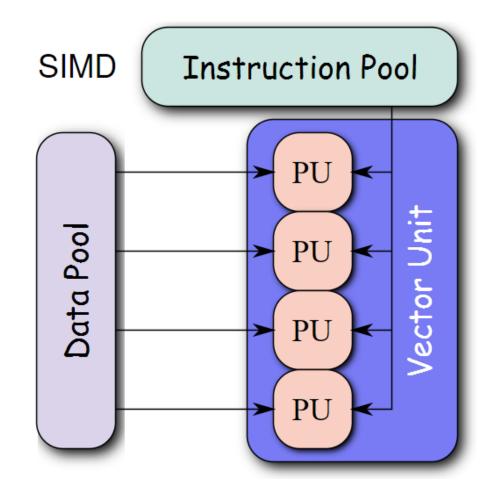


Parallelization options in programming languages

- Single instruction, multiple data (SIMD)
- Green-threads
- Multi-threading
 - Language
 - Libraries
- Multi-processing
 - single machine
 - distributed (cluster)
 - distributed (cluster) via external tools

SIMD

 Single instruction, multiple data (SIMD) describes computers with multiple processing elements that perform the same operation on multiple data points simultaneously. Such machines exploit data level parallelism, but not concurrency: there are simultaneous (parallel) computations, but only a single process (instruction) at a given moment.



Source: https://en.wikipedia.org/wiki/SIMD

Data level parallelism

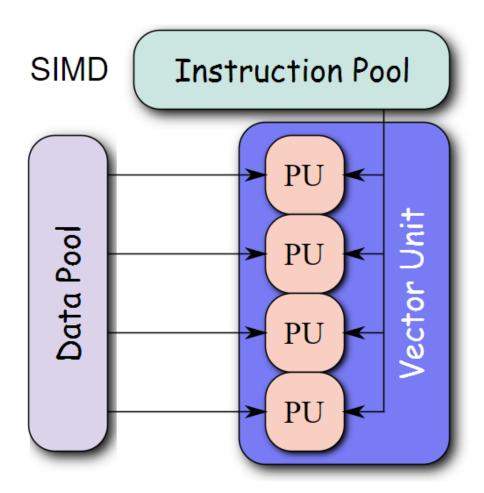


Image source: https://en.wikipedia.org/wiki/SIMD

```
#1_dot_simd.jl
function dot1(x, y)
    s = 0.0
    for i in 1:length(x)
        @inbounds s += x[i]*y[i]
    end
end
function dot2(x, y)
    s = 0.0
    @simd for i in 1:length(x)
        @inbounds s += x[i]*y[i]
    end
end
```

Dot product: output

```
$ julia 1_dot_simd.jl
113.066 ns (0 allocations: 0 bytes)
21.760 ns (0 allocations: 0 bytes)
```

Green threading

• In computer programming, green threads are threads that are scheduled by a runtime library or virtual machine (VM) instead of natively by the underlying operating system. Green threads emulate multithreaded environments without relying on any native OS capabilities, and they are managed in user space instead of kernel space, enabling them to work in environments that do not have native thread support.

A simple web server with green threading

2_webserver.jl

```
server = Sockets.listen(8080)
while true
  sock = Sockets.accept(server)
  @async begin
    data = readline(sock)
    print("Got request:\n", data, "\n")
    cmd = split(data, " ")[2][2:end]
    println(sock, "\nHTTP/1.1 200 OK\nContent-Type: text/html\n")
    println(sock, string("<html><body>", cmd, "=",
                eval(Meta.parse(cmd)), "</body></html>"))
    close(sock)
  end
end
```

Comparison of parallelism types

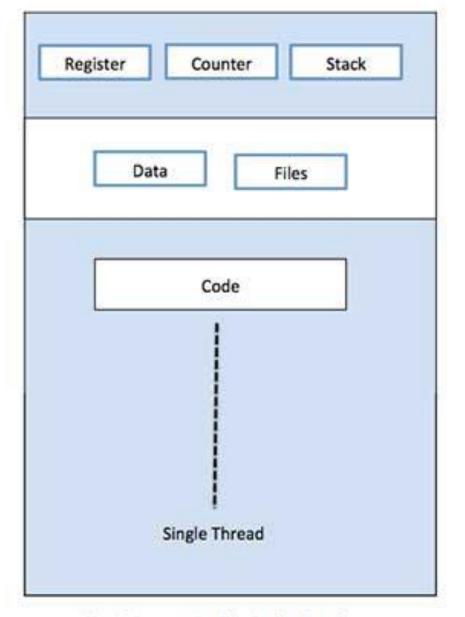
Threading

- Single process (cheap)
- Shared memory
- Number of threads running simultaneously limited by number of processors
- Possible issues with locking and false sharing

Multiprocessing

- Multiple processes
- Separate memory
- Number of processes running simultaneously limited by cluster size
- Possible issues if inter-process communication is needed

Threading



Register Register Register Counter Counter Counter Stack Stack Stack Data Files Code First Thread Second Thread Third Thread

Single Process P with single thread

Single Process P with three threads

Simple example — threading 3_sum_thread.jl

Single threaded

```
function ssum(x)
    r, c = size(x)
   y = zeros(c)
    for i in 1:c
        for j in 1:r
            y[i] += x[j, i]
        end
    end
end
```

Multithreading

```
function tsum(x)
    r, c = size(x)
    y = zeros(c)
    Threads.@threads for i in 1:c
        for j in 1:r
            y[i] += x[j, i]
        end
    end
    У
end
```

Sum: output

```
$ ./3 run sum thread.sh
threads: 1
  0.963284 seconds (28.38 k allocations: 1.619 MiB)
  0.878460 seconds (6 allocations: 156.484 KiB)
  1.782968 seconds (53.94 k allocations: 2.891 MiB)
  1.764061 seconds (7 allocations: 156.531 KiB)
threads: 2
  0.799932 seconds (28.38 k allocations: 1.619 MiB)
  0.813326 seconds (6 allocations: 156.484 KiB)
  0.925774 seconds (53.94 k allocations: 2.891 MiB)
  0.891011 seconds (7 allocations: 156.531 KiB)
threads: 4
  0.779453 seconds (28.38 k allocations: 1.619 MiB)
  0.828074 seconds (6 allocations: 156.484 KiB)
  0.555077 seconds (53.94 k allocations: 2.891 MiB)
  0.556130 seconds (7 allocations: 156.531 KiB)
```

delta is compilation time

Threading: synchronization 4_locking.jl

Increment x 10 7 times using threads:

- Atomic operations
- SpinLock (busy waiting)
- Mutex (OS provided lock)

```
$ ./4_run_locking.sh
```

Locking: output on c4.4xlarge (16 vCPU) 16 threads

```
f_bad
                                                                             f_bad
10000000
                                                                              950043
  0.498997 seconds (10.01 M allocations: 153.318 MiB, 49.89% gc time)
                                                                               0.449196 seconds (1.63 M allocations: 27.759 MiB)
10000000
                                                                              630661
  0.198711 seconds (10.00 M allocations: 152.580 MiB, 3.04% gc time)
                                                                               0.922549 seconds (1.52 M allocations: 26.963 MiB, 61.86% gc time)
                                                                              f atomic
f atomic
10000000
                                                                              10000000
  0.082628 seconds (7.54 k allocations: 403.376 KiB)
                                                                               0.217921 seconds (7.54 k allocations: 403.376 KiB)
10000000
                                                                              10000000
  0.059487 seconds (11 allocations: 288 bytes)
                                                                               0.187748 seconds (12 allocations: 688 bytes)
                                                                             f spin
f spin
10000000
                                                                             10000000
  0.286315 seconds (10.01 M allocations: 153.074 MiB, 2.25% gc time)
                                                                               2.238537 seconds (10.01 M allocations: 153.074 MiB, 15.81% gc time)
10000000
                                                                              10000000
  0.257490 seconds (10.00 M allocations: 152.580 MiB, 1.52% gc time)
                                                                               1.602330 seconds (10.00 M allocations: 152.581 MiB, 19.85% gc time)
f_mutex
                                                                             f mutex
10000000
                                                                              10000000
  0.557977 seconds (10.01 M allocations: 153.260 MiB, 1.17% gc time)
                                                                               4.862945 seconds (10.01 M allocations: 153.260 MiB, 3.67% gc time)
10000000
                                                                              10000000
  0.491197 seconds (10.00 M allocations: 152.580 MiB, 1.02% gc time)
                                                                               4.662214 seconds (10.00 M allocations: 152.580 MiB)
```

```
5_rand_process.jl
```

```
function s_rand()
    n = 10^{4}
    x = 0.0
    for i in 1:n
        x += sum(rand(10^4))
    end
    x / n
end
@time s_rand()
@time s_rand()
```

```
function p_rand()
    n = 10 \land 4
    x = @distributed (+) for i in 1:n
         sum(rand(10^4))
    end
    x / n
end
@time p_rand()
@time p_rand()
```

\$ julia -p \$(nproc) rand_process.jl

using Distributed

Rand: output

```
$ 3_rand/run_rand_process.sh
0.381071 seconds (46.21 k allocations: 765.124 MiB, 37.20% gc time)
0.161149 seconds (20.00 k allocations: 763.703 MiB, 9.64% gc time)
1.661893 seconds (230.81 k allocations: 12.494 MiB, 0.15% gc time)
0.092413 seconds (1.89 k allocations: 155.766 KiB)
delta is compilation and process spawning time
```

Parallelizing Julia code

- @parallel
- @spawnat
- @everywhere
- @async
- @sync
- fetch()

Typical pattern for distributed simulation

```
using Distributed
addprocs(4);
@everywhere include("sim file.jl")
function init()
   Random.seed! (myid())
end
@sync for wid in workers()
    @async fetch(@spawnat wid init())
end
```

Writing distributed loops

```
data = @distributed (vcat) for i = 1:10000
    some param A = rand()
    some param B = rand()
    res 1, res 2, res 3 = run sim();
    (sim stats(res 1, res 2, res 3)...,
    some param A,
    some param B,
    myid())
end
```

Typical computation distribution pattern

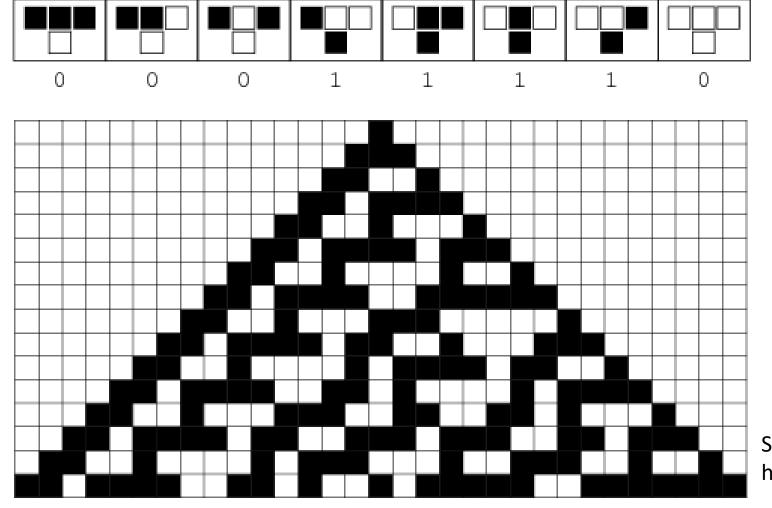
```
@everywhere function f()
     # do something
     return sum(rand(10000))
end
@sync for w in workers()
     @async begin
          res = @spawnat w f()
          values[w-1]=fetch(res)
     end
end
```

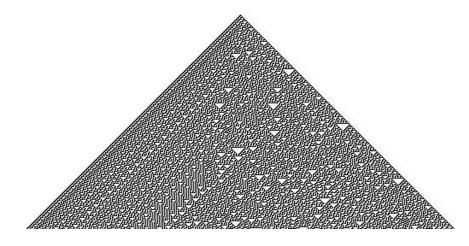
Sending data across cluster nodes

```
@everywhere using ParallelDataTransfer
sendto(workerid, vara = vara)
sendto([workerid1, workerid2], varb = varb)
```

Cellular automaton

rule 30

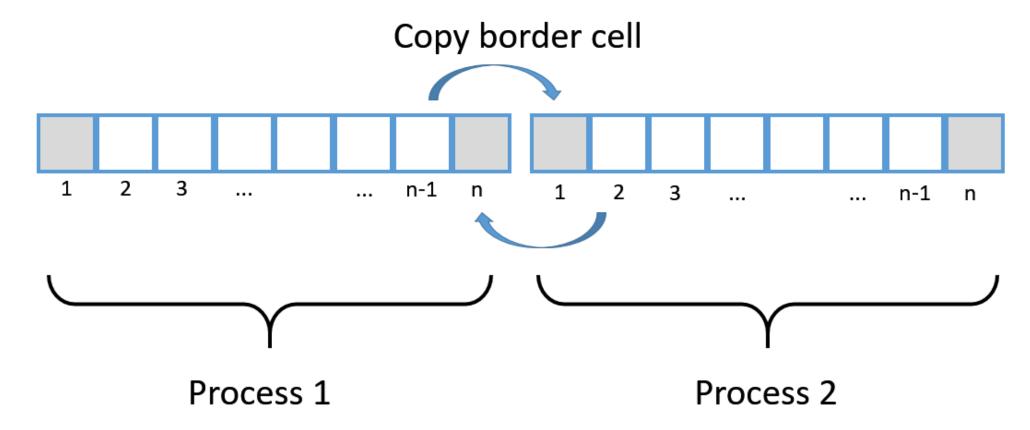




Source: http://mathworld.wolfram.com/Rule30.html

Distributed cellular automaton

Distributing data among worker processes



6_cellular_automaton.jl

```
using Distributed
@everywhere using ParallelDataTransfer
@everywhere function rule30(ca::Array{Bool})
  lastv = ca[1]
  for i in 2:(length(ca)-1)
    current = ca[i]
    ca[i] = xor(lastv, ca[i] | | ca[i+1])
    lastv = current
  end
end
```

```
function runca(steps::Int, visualize::Bool)
  @sync for w in workers()
    @async @fetchfrom w fill!(caa, false)
  end
  @fetchfrom wks[Int(nwks/2)+1] caa[2]=true
  visualize && printsimdist(workers())
  for i in 1:steps
    @sync for w in workers()
      @async @fetchfrom w getsetborder(caa, neighbours)
    end
    @sync for w in workers()
      @async @fetchfrom w rule30(caa)
    end
    visualize && printsimdist(workers())
  end
end
```

Running 6_cellular_automaton.jl

```
wks = workers()
nwks = length(wks)
for i in 1:nwks
  sendto(wks[i],neighbours = (i==1? wks[nwks]: wks[i-1],
                  i==nwks ? wks[1] : wks[i+1]))
  fetch(@defineat wks[i] const caa = zeros(Bool, 15+2));
end
runca(20,true)
```

Typical approach for distributed processing

- Define a "reasonably large" work package
 - In our case one job is 1,000 sudoku problems (~10 seconds)
 - We have 100 such jobs (~20 mins on a single core)
- Julia distributed cluster manager

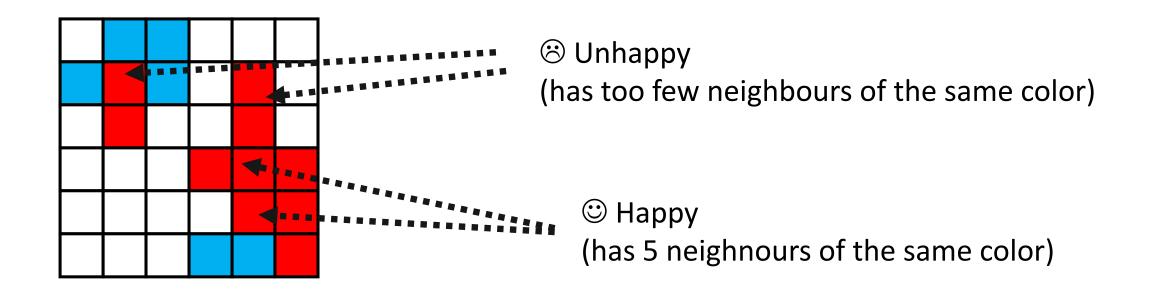
Julia cluster specification file and running distributed clusters

```
$ more machinefile julia
4*ubuntu@172.31.10.229
4*ubuntu@172.31.11.44
4*ubuntu@172.31.0.243
4*ubuntu@172.31.13.134
4*ubuntu@172.31.14.219
$ julia --machinefile machinefile julia program.jl
# REQUIRES PASSWORDLESS SSH TO BE CONFIGURED!
```

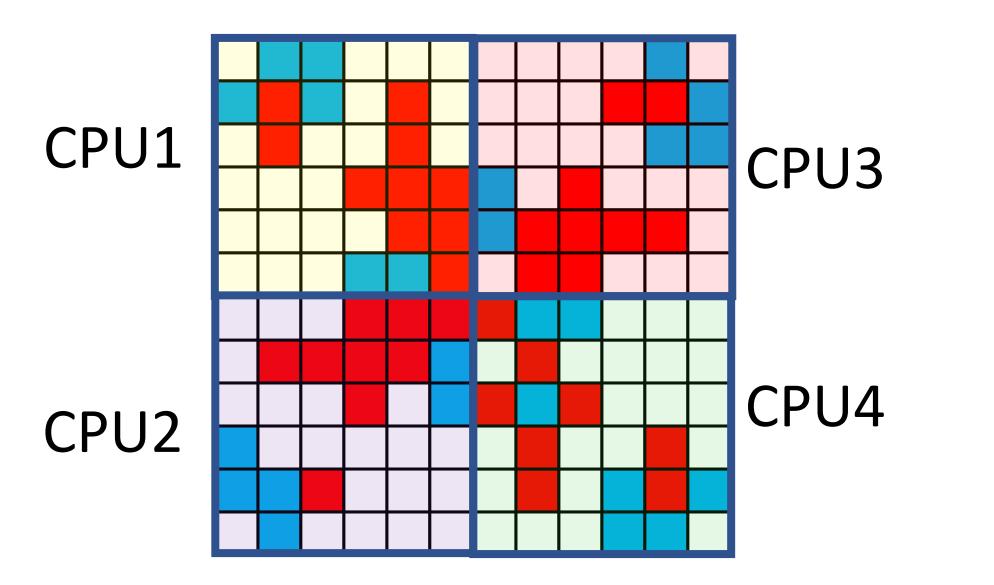
Use case scenario I: Performance of distributed code in Julia Cray vs AWS

Schelling (1974) segregation model

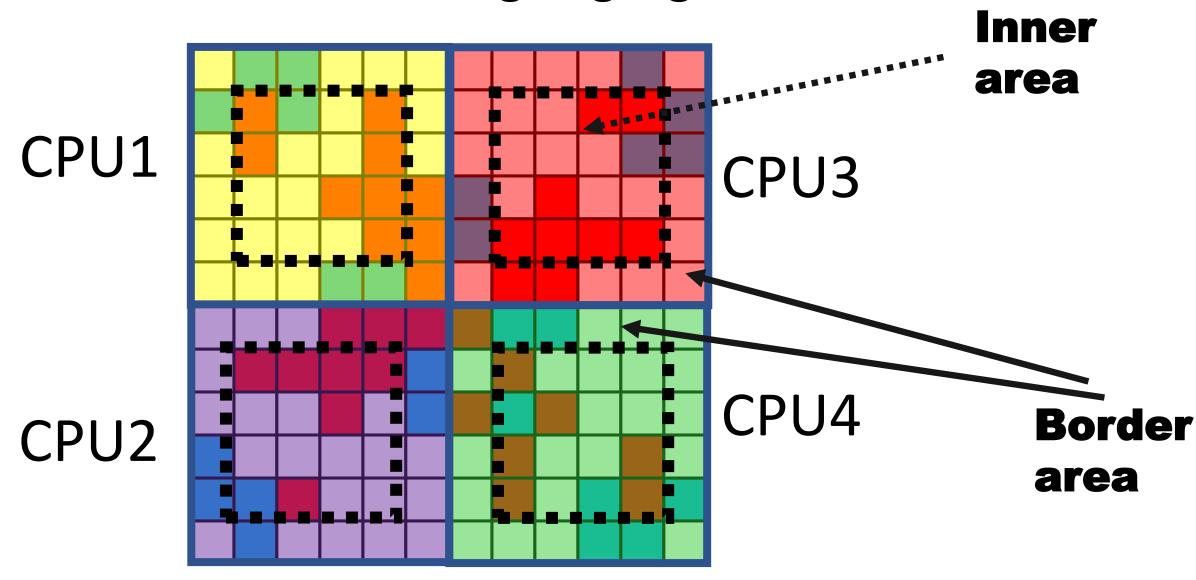
- Agents occupy cells of rectangular space
- Two types of agents (e.g. blue and red)
- When not happy with their neighbours randomly relocate



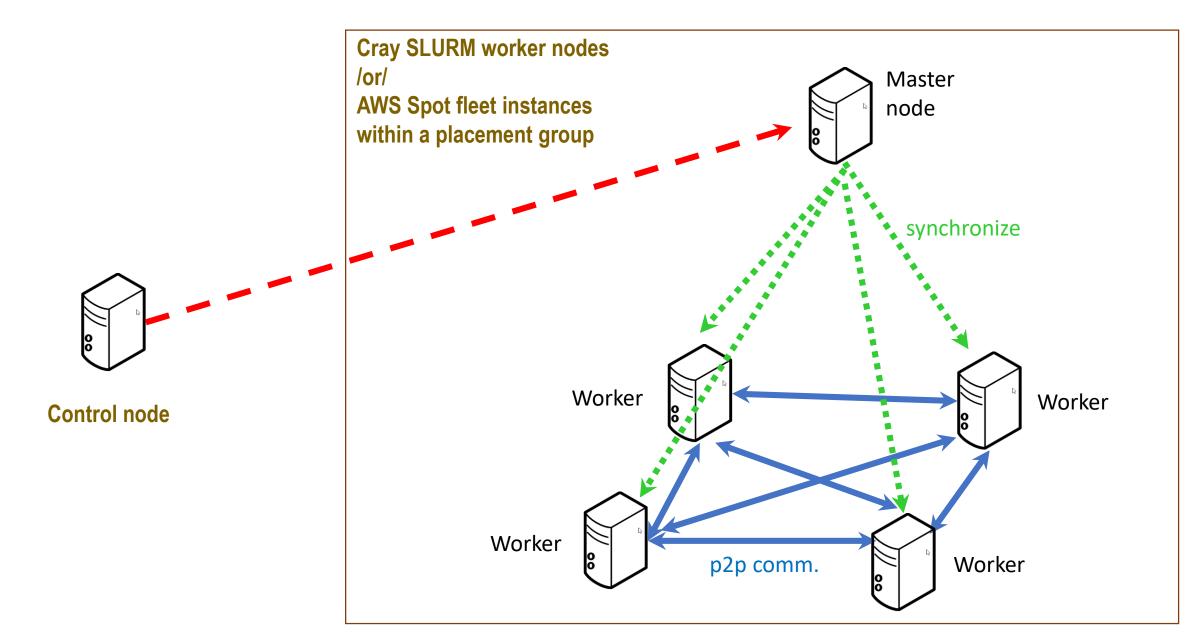
Distributed Schelling segregation model



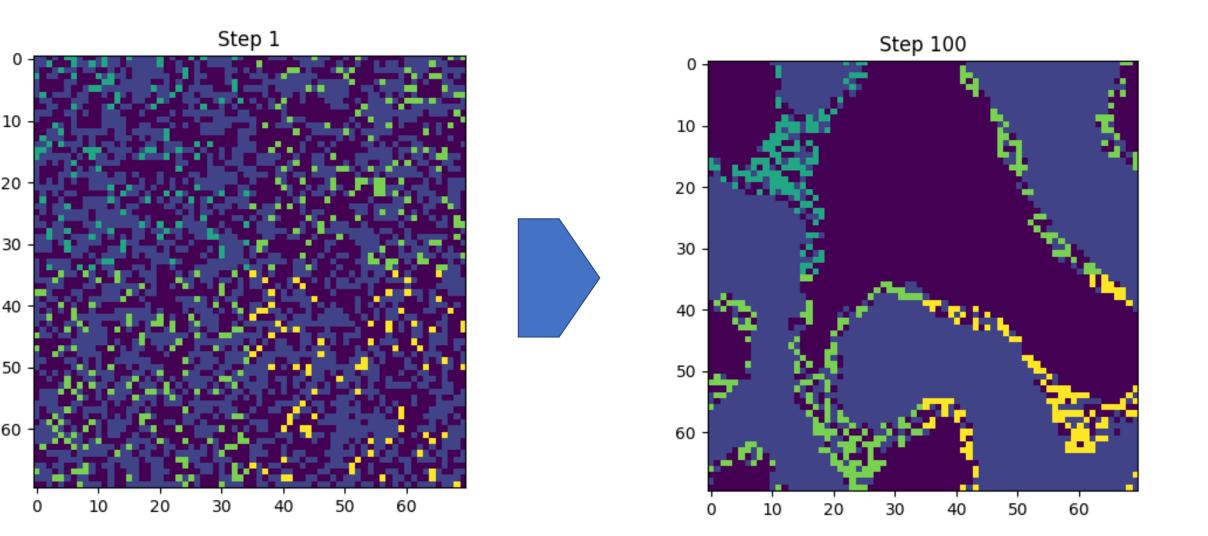
Distributed Schelling segregation model



Distributed simulation architecture

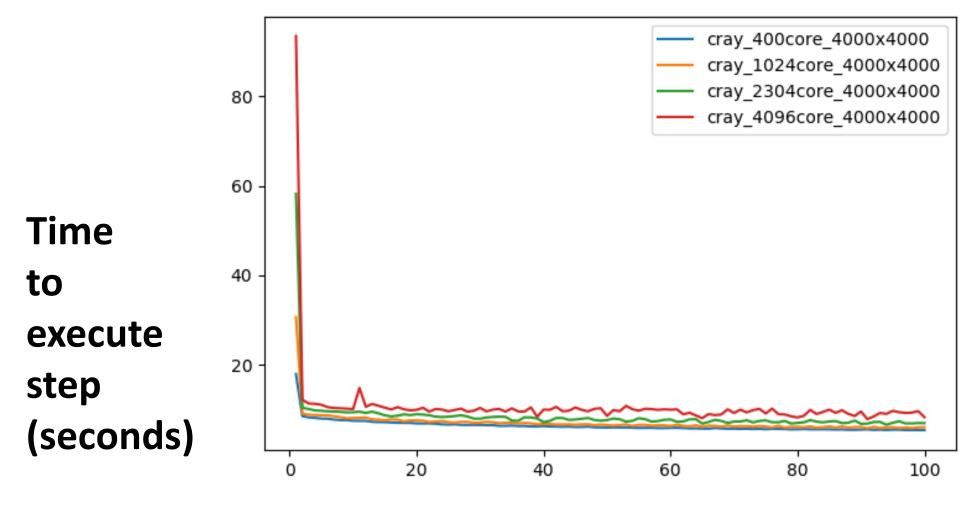


Parallelized Schelling model (2x2)



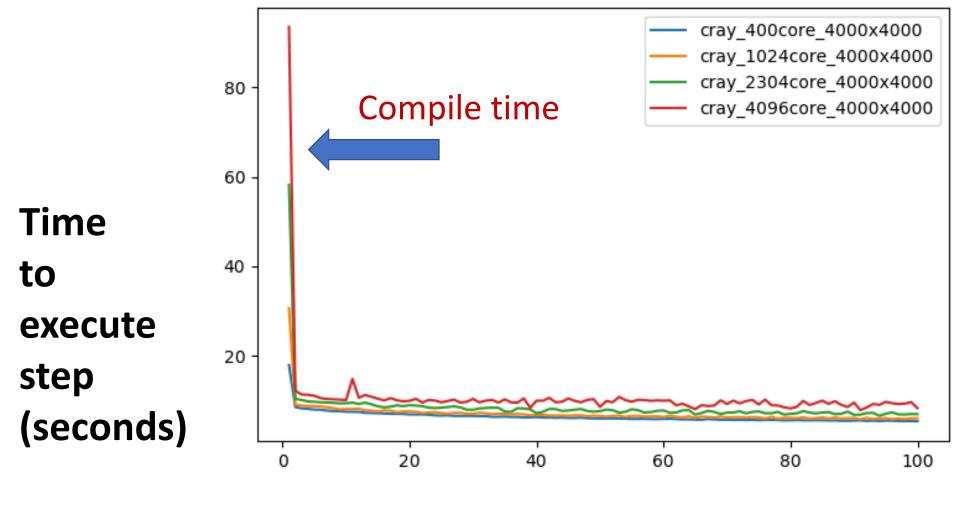
Parralelizing Julia on Cray with SLURM

Typical Julia performance pattern



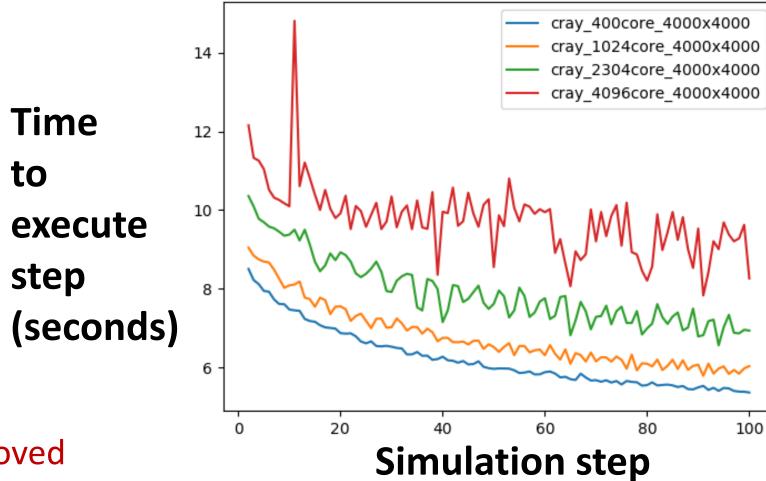
Simulation step

Typical Julia performance pattern



Simulation step

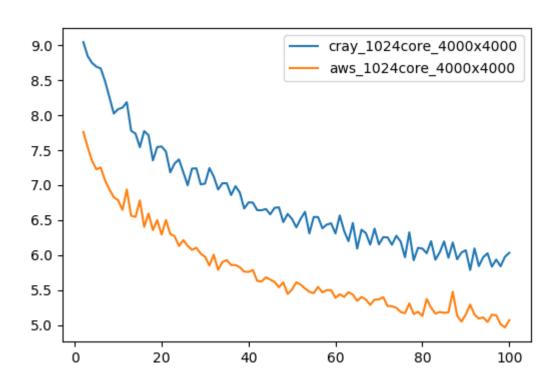
Distributed simulation scalability

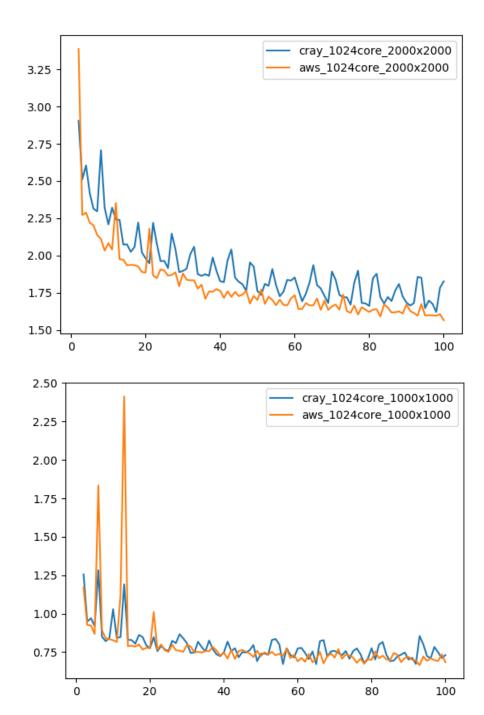


Note:

The first step has been removed

Cray vs AWS Spot Fleet

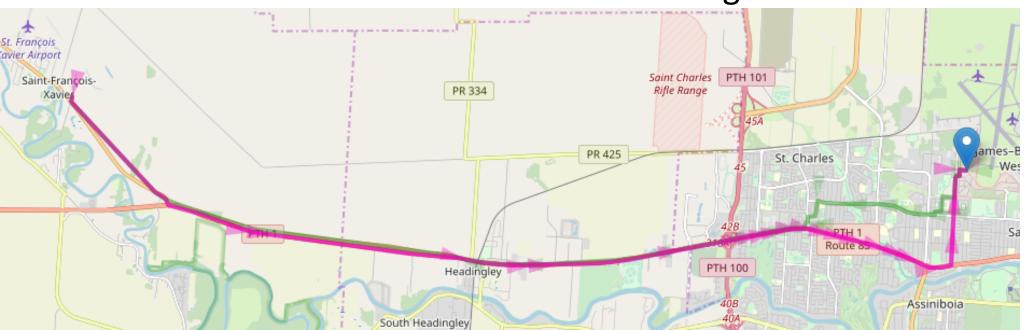




Use Case Scenario II Agent-based simulation of cities https://github.com/pszufe/OpenStreetMapX.jl

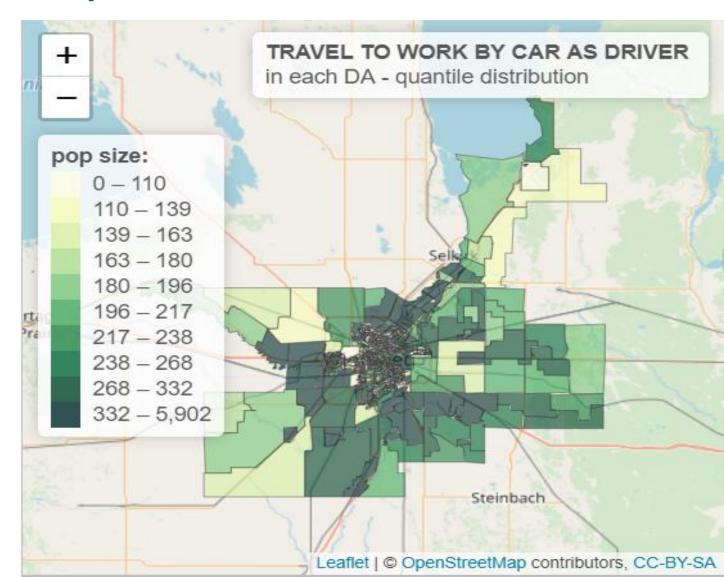
Project goals....

- A multi-agent simulation framework (Open Source) for modelling commuters' behavior within a city
 - individual travel patterns
 - sociodemographic profiles of commuters
 - exchange of information between travelling agents
- The simulation results have been validated against real traffic data

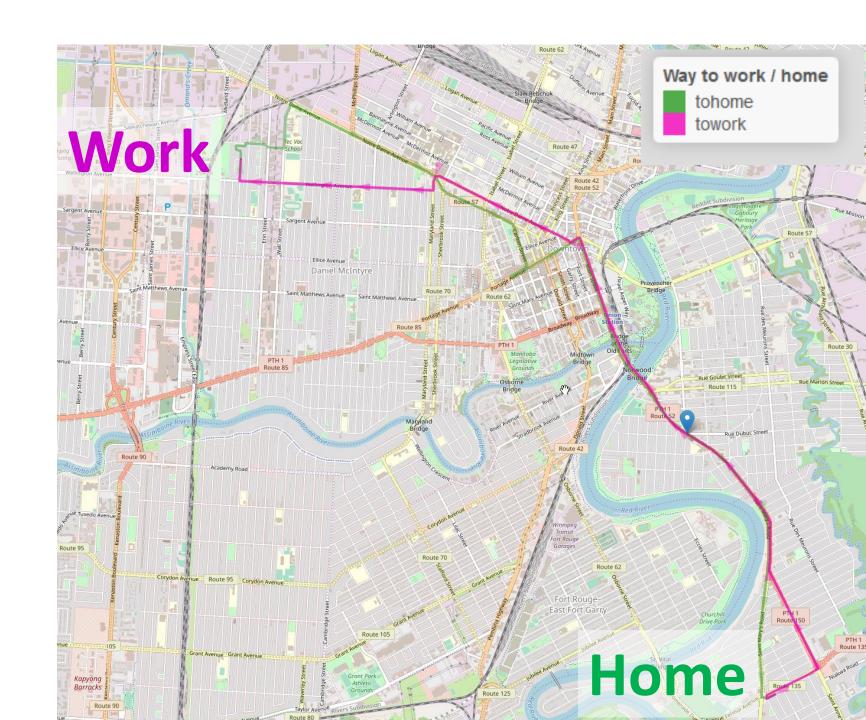


The modelled city – available data

- Winnipeg CMA,
 Canada
- population~1'000'000
- 1'200
 dissemination
 areas



A single simulated commuter's behavior...



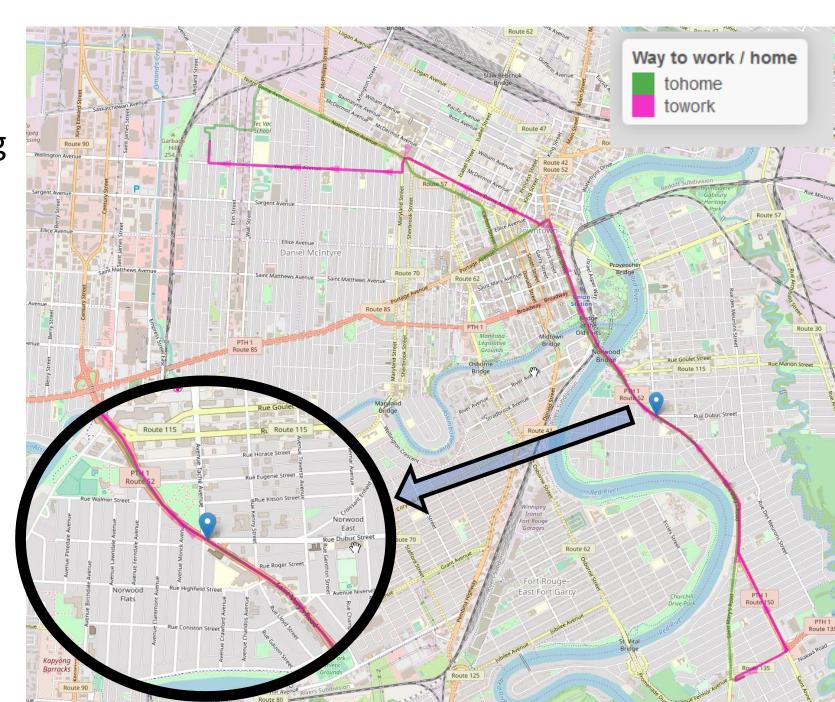
Simulation model travel destinations and commuters' behavior

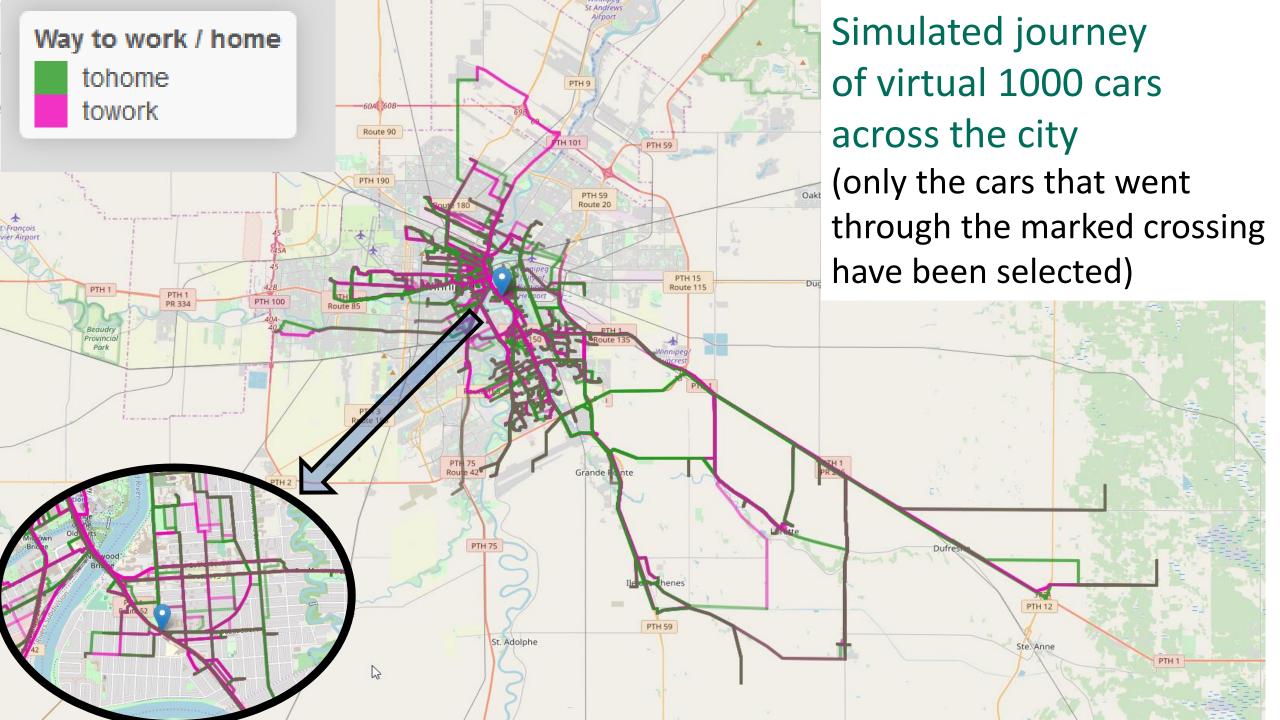


Each agent makes individual travel decisions on the base of her sociodemographic profile

Questions

- How many people went to the given road crossing
- Who are those people?Reach? Poor?Immigrants?
- If a place an advertising billboard – who is going to see it?
- What business makes sense in this area



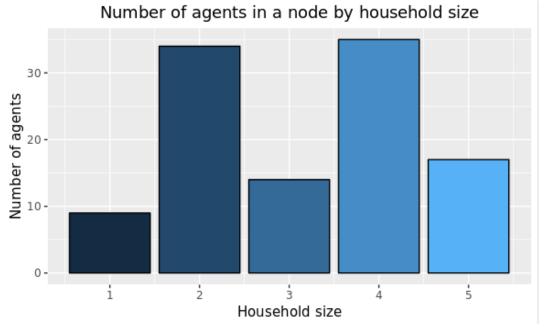


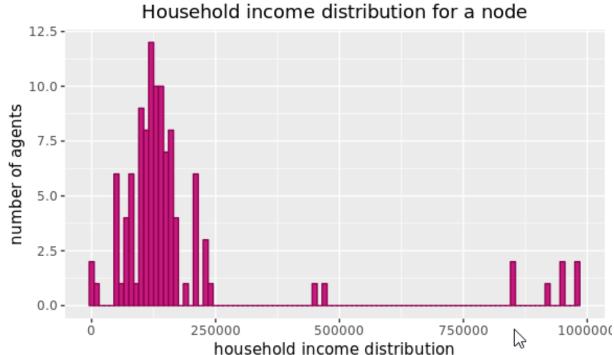
Sample simulation data

NODE_ID	longitude	latitude	DA_home	DA_work	gender	age	marital_	st work_ind	househol	household	no_of_ch	i children_	imigrant	imigrant_	imigrant_i	id
369306773	-97.1122	49.90696	46110714	46110684	⊭ M	69	true	Retail Trac	89138	2	C	0 Int64[]	true	Before 20	Eastern E	2001000028
369306773	-97.1122	49.90696	46110230	46111151	∠ <mark>M</mark>	28	false	Wholesale	65454	. 1	C	0 Int64[]	true	2012 To P	r Central A	r 2001000030
369306773	-97.1122	49.90696	46110803	46111177	/ F	22	false	Retail Trac	48281	. 2	1	1 [5]	true	2006 To 20	Northern	2001000035
369306773	-97.1122	49.90696	46110845	46110632	4 M	52	true	Manufacti	63822	. 1	C	0 Int64[]	false			2001000103
369306773	-97.1122	49.90696	46110795	46110162	4 F − − − − − − − − − − − − − − − − − − −	36	true	Transporta	32480	1	C	0 Int64[]	false			2001000289
369306773	-97.1122	49.90696	46110869	46110100	/ F	20	false	Finance A	82354	2	C	0 Int64[]	false			2001000318
369306773	-97.1122	49.90696	46110801	46110117	/ M	60	false	Arts, Ente	621011	. 3	C	0 Int64[]	false			2001000403
369306773	-97.1122	49.90696	46110701	46110669	/ M	41	false	Public Adı	99562	. 2	1	1 [18]	false			2001000525
369306773	-97.1122	49.90696	46110735	46110075	M	41	false	Retail Trac	909754	2	1	1 [14]	false			2001000529
369306773	-97.1122	49.90696	46110845	46110667	/ M	51	false	Retail Trac	95722	3	C	0 Int64[]	false			2001000736
369306773	-97.1122	49.90696	46120046	46110669	/ M	53	true	Health Car	84334	3	C	0 Int64[]	false			2001000773
369306773	-97.1122	49.90696	46110802	46110144	⊭ M	44	true	Public Adı	42891	. 4	C	0 Int64[]	false			2001000948
369306773	-97.1122	49.90696	46111151	46110145	M	37	true	Finance A	118452	. 1	C	0 Int64[]	true	2012 To P	r Southeast	t 2002000044
369306773	-97.1122	49.90696	46110851	46111177	/ M	55	false	Health Car	62681	. 3	C	0 Int64[]	false			2002000060
369306773	-97.1122	49.90696	46110453	46110683	<i>i</i> F	34	true	Real Estat	29972	. 5	C	0 Int64[]	false			2002000172
369306773	-97.1122	49.90696	46110875	46110145	<i>J</i> F	32	true	Retail Trac	50486	3	1	1 [46]	false			2002000265
369306773	-97.1122	49.90696	46110853	46110631	∡ F	25	false	Public Adı	52526	1	C	0 Int64[]	false			2002000318
369306773	-97.1122	49.90696	46120053	46110669	<i>J</i> F	38	true	Manufacti	119023	2	C	0 Int64[]	false			2002000336
	1		1						-							

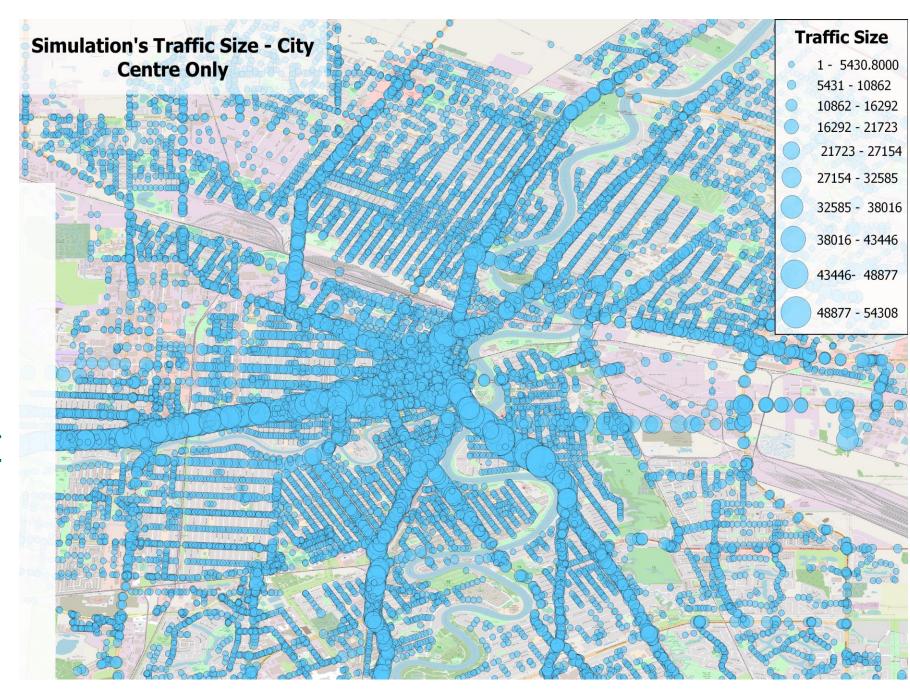
Outcome: Sociodemographic profiles available for each intersection within the city



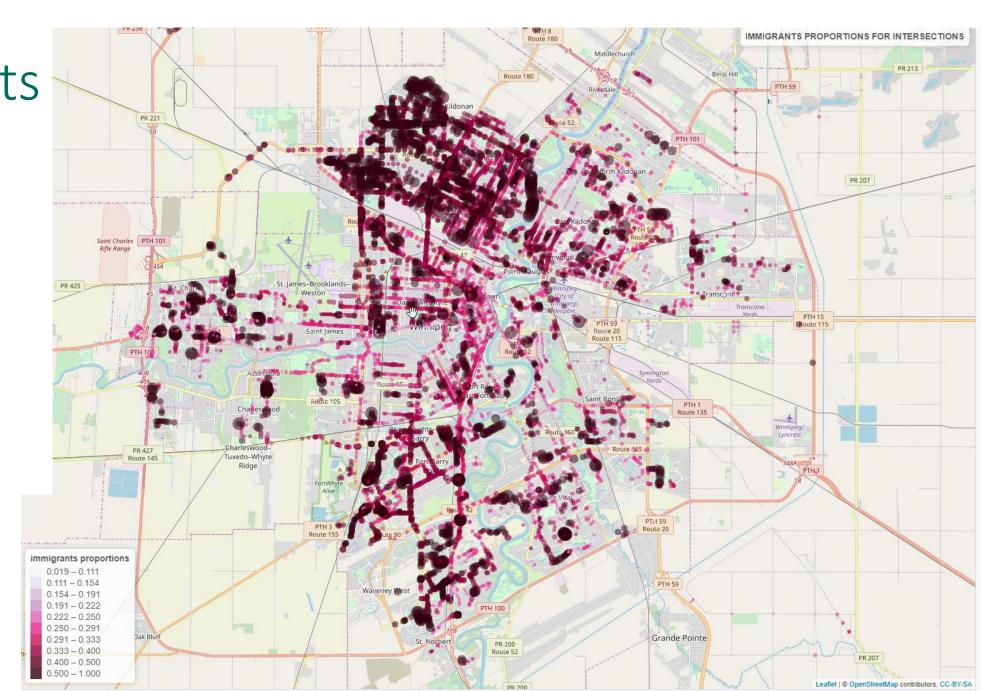




Simulated aggregated traffic on street crossing in the city center



Percentage of immigrants passing through each intersection within the city



Conclusions

- Julia
- PROs
 - distributed computing
 - high performance computing
 - scientific computing
- CONs
 - data visualization layer still under development