Stat 292 - Recitation 1

R-Review

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Exercise 1:

Create following sequences.

```
• (100 110 120 130 140 150 160 170 180 190 200)
```

```
• (25 20 15 10 5 0 -5 -10 -15)
```

```
• (-2.0 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 2.0 -2.0 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 2.0)
```

```
• (-5 -5 4 4 -3 -3 2 2 -1 -1 0 0)
```

```
• ("a" "c" "e" "g" "i" "k" "m" "o" "q" "s" "u" "w" "y")
```

```
seq(100, 200, 10)
## [1] 100 110 120 130 140 150 160 170 180 190 200
seq(25, -15, length.out = 9)
## [1] 25 20 15 10 5 0 -5 -10 -15
rep(seq(-2,2,0.5),2)
## [1] -2.0 -1.5 -1.0 -0.5 0.0 0.5 1.0 1.5 2.0 -2.0 -1.5 -1.0 -0.5 0.0 0.5
## [16] 1.0 1.5 2.0
rep(seq(5,0,-1) * c(-1,1),each=2)
## [1] -5 -5 4 4 -3 -3 2 2 -1 -1 0 0
letters[seq(1,length(letters),2)]
```

Exercise 2:

[1] "a" "c" "e" "g" "i" "k" "m" "o" "q" "s" "u" "w" "y"

Part A:

Create following matrices.

$$X = \begin{bmatrix} 1 & 0 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 1 \end{bmatrix}, \quad Y = \begin{bmatrix} 1 & -2 & -2 \\ 0 & 0 & 1 \\ -1 & 5 & 2 \\ 2 & 4 & 6 \end{bmatrix}, \quad Z = \begin{bmatrix} 2 & 1 & 3 \\ 3 & -1 & 5 \\ 4 & -2 & 6 \end{bmatrix}, \quad P = \begin{bmatrix} 5 & 0 & 0 & 0 \\ 0 & 6 & 0 & 0 \\ 0 & 0 & 7 & 0 \\ 0 & 0 & 0 & 8 \end{bmatrix}, \quad K = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

```
X <- matrix(rep(c(1,0,1),3), nrow = 3, byrow = TRUE)
Y <- matrix(c(1,-2,-2,0,0,1,-1,5,2,2,4,6), nrow = 4, byrow = TRUE)
Z <- matrix(c(2,3,4,1,-1,-2,3,5,6), nrow = 3)
P <- diag(5:8)
K <- matrix(1:6, nrow = 2, byrow = T)</pre>
```

Part B:

Calculate following;

- $\bullet X + Z$
- $Z^{-1}X$
- YK^T
- PY
- $\max\{|X|, |Z|, |P|\}$

X + Z

solve(Z) %*% X

Y %*% t(K)

```
## [4,]
           28
                 64
P %*% Y
         [,1] [,2] [,3]
##
## [1,]
            5
                -10
                     -10
## [2,]
                  0
                        6
## [3,]
           -7
                 35
                       14
## [4,]
           16
                 32
                       48
\max(c(\det(X), \det(Z), \det(P)))
## [1] 1680
```

Part C:

Using those matrices;

- Replace [1,1] and [1,2] elements for each matrix with -100 and 100 respectively.
- Create a new matrix called A, by binding X and K properly, check its dimension.
- Create a new matrix called B, by binding Y and P properly, assign row and column names.
- Combine Y, P and K in a list. Add a vector of your 3 favorite TV Shows in your list.
- Create an array whose layers are X and Z.

```
X[1,1:2] <- Y[1,1:2] <- Z[1,1:2] <- P[1,1:2] <- K[1,1:2] <- c(-100,100)

A <- rbind(X,K); dim(A)

## [1] 5 3

B <- cbind(Y,P)
rownames(B) <- paste("row.",1:nrow(B),sep="")
colnames(B) <- paste("col.",1:ncol(B),sep="")

mylist <- list(Y, P, K)
mylist$TvShows <- c("Cennet Mahallesi","Acun Firarda","Çiçek Taksi")

myarray <- array(c(X,Z), dim = c(nrow(X),ncol(X),2))</pre>
```

Exercise 3:

• Read height.txt data into R. Then, write an if statement to group observations based on the following rule. Create another column on your dataframe called 'group'.

```
\mbox{Group1} = \left\{ \begin{array}{ll} \mbox{Group1}, & Height \leq 165 \\ \mbox{Group2}, & Height > 165 & \& & Height < 180 \\ \mbox{Group3}, & Height \geq 180 \end{array} \right.
```

```
## ID Height Group

## 1 1 153 Group1

## 2 2 188 Group3

## 3 3 150 Group1

## 4 4 183 Group3

## 5 5 172 Group2

## 6 6 163 Group1
```

• Print frequency and proportion of each group.

```
table(data$Group)
```

```
##
## Group1 Group2 Group3
## 7 6 7
table(data$Group) / nrow(data)

##
## Group1 Group2 Group3
## 0.35 0.30 0.35
```

Part B:

Write an if statement that prints;

- square of an integer if it is even and less than or equal to 20,
- cube of an integer if it is odd and less than or equal to 20,
- natural logarithm if it is more than 20.

Then, give different integers to see if your if statement works well.

```
myint <- 13
if(myint > 20){
  log(myint)
}else{
```

```
if(myint %% 2 == 0){
    # meaning it is even
    myint^2
}else{
    myint^3
}

## [1] 2197

#ifelse(myint >20, log(myint), ifelse(myint %% 2 == 0, myint^2, myint^3))
```

Exercise 4:

Part A:

Write a while loop that prints out standard random normal numbers (use rnorm()) but stops (breaks) if you get a number bigger than 1.

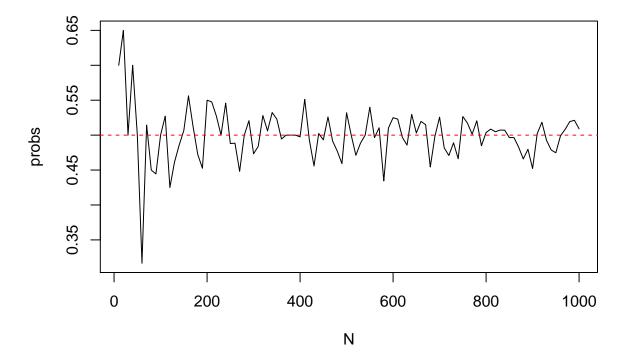
```
while(TRUE){
  x \leftarrow rnorm(1)
  if(x > 1){
    break
  }
 print(x)
}
## [1] -0.4115108
## [1] 0.2522234
## [1] -0.8919211
## [1] 0.4356833
## [1] -1.237538
## [1] -0.2242679
## [1] 0.3773956
## [1] 0.1333364
## [1] 0.8041895
## [1] -0.05710677
## [1] 0.503608
```

Part B:

Consider a coin tossing experiment. Using 'sample' function simulate this experiment. First, 'flip your fair coin' 10 times then increase this number by 10 till you have 1000 flips ($N = 10,20,30,\ldots,990,1000$), and in each step store estimated probabilities in a vector.

After you simulate this experiment, draw a line graph to see if the estimated probability converges to the exact probability as N gets larger.

```
set.seed(12)
probs <- numeric()
N <- seq(10,1000,10)
for(i in 1:length(N)){
   probs[i] <- mean(sample(0:1, replace = T, size = N[i]))
}
plot(x = N, y = probs, type = "l")
abline(h = 0.5, col = "Red", lty = "dashed")</pre>
```



Part C:

Implement a multiplication game. A while loop that gives the user two random numbers from 2 to 12 and asks the user to multiply them. Only exit the loop after five correct answers. Use as.integer(readline()) to get the user's answers.

```
correct_number <- 0
while(correct_number < 5){
    x <- sample(2:12, size = 2, replace = T)
    mult_x <- x[1] * x[2]</pre>
```

Exercise 5:

Part A:

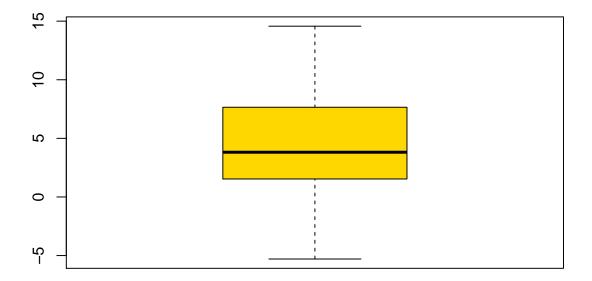
Write an R function which converts given amount of Turkish Lira to the USD, CAD, EURO and GBP.

```
## Amount
## TL 75.000
## USD 9.750
## CAD 12.000
## EURO 8.250
## GBP 7.125
```

Part B:

Write an R function which takes a continuous random sample (vector), calculates basic statistics (mean, median, variance, quartiles (1^{st} and 3^{rd}), skewness, kurtosis, range ...) and stores them in a list; finally returns that list. Also, your function must have an option for a boxplot, if TRUE it will plot a boxplot.

Boxplot



```
## $Mean
## [1] 4.61188
##
```

```
## $Median
## [1] 3.816457
##
## $Variance
## [1] 19.67517
##
## $Quartiles
##
        25%
                  75%
## 1.551665 7.633397
##
## $Range
## [1] 19.86436
##
## $Skewness
## [1] 0.1431411
##
## $Kurtosis
## [1] 2.509511
```

Part C:

Write an R function that given a vector and an integer will return how many times the integer appears inside the vector. (Don't use 'table' command)

[1] "The value 15 appears 1 times in the given vector"

Exercise 6:

Part A:

• Load 'Hitters' data set from 'ISLR' package.

```
library(ISLR)
data("Hitters")
```

• Check structure of the 'Hitters' data set.

```
str(Hitters)
```

```
'data.frame':
                    322 obs. of 20 variables:
                      293 315 479 496 321 594 185 298 323 401 ...
##
    $ AtBat
               : int
    $ Hits
               : int
                      66 81 130 141 87 169 37 73 81 92 ...
    $ HmRun
                      1 7 18 20 10 4 1 0 6 17 ...
##
               : int
                      30 24 66 65 39 74 23 24 26 49 ...
    $ Runs
               : int
##
    $ RBI
                      29 38 72 78 42 51 8 24 32 66 ...
               : int
    $ Walks
                      14 39 76 37 30 35 21 7 8 65 ...
##
               : int
##
    $ Years
               : int
                      1 14 3 11 2 11 2 3 2 13 ...
                      293 3449 1624 5628 396 4408 214 509 341 5206 ...
##
    $ CAtBat
               : int
    $ CHits
                      66 835 457 1575 101 1133 42 108 86 1332 ...
##
               : int
##
    $ CHmRun
               : int
                      1 69 63 225 12 19 1 0 6 253 ...
##
    $ CRuns
                      30 321 224 828 48 501 30 41 32 784 ...
               : int
    $ CRBI
               : int
                      29 414 266 838 46 336 9 37 34 890 ...
##
    $ CWalks
                      14 375 263 354 33 194 24 12 8 866 ...
##
               : Factor w/ 2 levels "A", "N": 1 2 1 2 2 1 2 1 2 1 ...
##
    $ League
    $ Division : Factor w/ 2 levels "E", "W": 1 2 2 1 1 2 1 2 2 1 ...
##
    $ PutOuts
               : int
                      446 632 880 200 805 282 76 121 143 0 ...
                      33 43 82 11 40 421 127 283 290 0 ...
##
    $ Assists
               : int
                      20 10 14 3 4 25 7 9 19 0 ...
##
    $ Errors
               : int
               : num NA 475 480 500 91.5 750 70 100 75 1100 ...
    $ Salary
    $ NewLeague: Factor w/ 2 levels "A","N": 1 2 1 2 2 1 1 1 2 1 ...
```

• Print first 10 Players.

head(Hitters, 10)

```
AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun
## -Andy Allanson
                          293
                                 66
                                         1
                                             30
                                                  29
                                                         14
                                                                 1
                                                                       293
                                                                               66
                                                                                        1
                                         7
## -Alan Ashby
                          315
                                 81
                                             24
                                                  38
                                                         39
                                                                14
                                                                      3449
                                                                             835
                                                                                       69
                                                  72
## -Alvin Davis
                          479
                                130
                                        18
                                             66
                                                         76
                                                                 3
                                                                     1624
                                                                             457
                                                                                       63
## -Andre Dawson
                          496
                                141
                                        20
                                             65
                                                  78
                                                         37
                                                                11
                                                                      5628
                                                                            1575
                                                                                     225
                                                                 2
                                                                                       12
## -Andres Galarraga
                          321
                                 87
                                        10
                                             39
                                                  42
                                                         30
                                                                       396
                                                                             101
```

| ## | -Alfredo Griffin | 594 | 169 | 4 | 74 | 51 | 35 | 11 | 44 | 08 11 | 133 | 19 |
|----|-------------------|--------|---------------|--------|------|------|----------|------|--------|--------|-----|--------|
| | -Al Newman | 185 | 37 | 1 | 23 | 8 | 21 | 2 | | 14 | 42 | 1 |
| ## | -Argenis Salazar | 298 | 73 | 0 | 24 | 24 | | 3 | | | 108 | 0 |
| | -Andres Thomas | 323 | 81 | 6 | 26 | 32 | 8 | 2 | | 41 | 86 | 6 |
| ## | -Andre Thornton | 401 | 92 | 17 | 49 | 66 | 65 | 13 | 52 | 06 13 | 332 | 253 |
| ## | | CRuns | CRBI | CWalks | Leag | ue l | Division | PutC | Outs . | Assist | s E | Errors |
| ## | -Andy Allanson | 30 | 29 | 14 | | Α | E | | 446 | | 33 | 20 |
| ## | -Alan Ashby | 321 | 414 | 375 | | N | W | | 632 | 4 | 13 | 10 |
| ## | -Alvin Davis | 224 | 266 | 263 | | Α | W | | 880 | 8 | 32 | 14 |
| ## | -Andre Dawson | 828 | 838 | 354 | | N | E | | 200 | 1 | L1 | 3 |
| ## | -Andres Galarraga | 48 | 46 | 33 | | N | E | | 805 | 4 | 10 | 4 |
| ## | -Alfredo Griffin | 501 | 336 | 194 | | Α | W | | 282 | 42 | 21 | 25 |
| ## | -Al Newman | 30 | 9 | 24 | | N | E | | 76 | 12 | 27 | 7 |
| ## | -Argenis Salazar | 41 | 37 | 12 | | Α | W | | 121 | 28 | 33 | 9 |
| ## | -Andres Thomas | 32 | 34 | 8 | | N | W | | 143 | 29 | 90 | 19 |
| ## | -Andre Thornton | 784 | 890 | 866 | | Α | Е | | 0 | | 0 | 0 |
| ## | | Salary | ary NewLeague | | | | | | | | | |
| ## | -Andy Allanson | NA | | Α | | | | | | | | |
| ## | -Alan Ashby | 475.0 |) | N | | | | | | | | |
| ## | -Alvin Davis | 480.0 |) | Α | | | | | | | | |
| ## | -Andre Dawson | 500.0 |) | N | | | | | | | | |
| ## | -Andres Galarraga | 91.5 | • | N | | | | | | | | |
| ## | -Alfredo Griffin | 750.0 |) | Α | | | | | | | | |
| ## | -Al Newman | 70.0 |) | Α | | | | | | | | |
| ## | -Argenis Salazar | 100.0 |) | Α | | | | | | | | |
| ## | -Andres Thomas | 75.0 |) | N | | | | | | | | |
| ## | -Andre Thornton | 1100.0 |) | Α | | | | | | | | |
| | | | | | | | | | | | | |

• Who has the highest and lowest salaries?

rownames(Hitters)[which.min(Hitters\$Salary)]

[1] "-BillyJo Robidoux"

rownames(Hitters)[which.max(Hitters\$Salary)]

[1] "-Eddie Murray"

• Check if there are any NA values in the data set. Given the fact that NA values appear only in the Salary column, find out the players whose Salaries are NA.

anyNA(Hitters)

[1] TRUE

• What is the mean 'Hits' for the ones with the highest 10% in Salary. (Remember, there are NA values in Salary, make sure you are dealing with them properly)

```
Hitters_new <- na.omit(Hitters)
Q90 <- quantile(Hitters_new$Salary,0.9)
mean(Hitters_new$Salary > Q90,"Hits"])
```

[1] 143.6667

• What is the correlation between HmRun and Hits?

```
cor(Hitters$Hits, Hitters$HmRun)
```

[1] 0.5621579

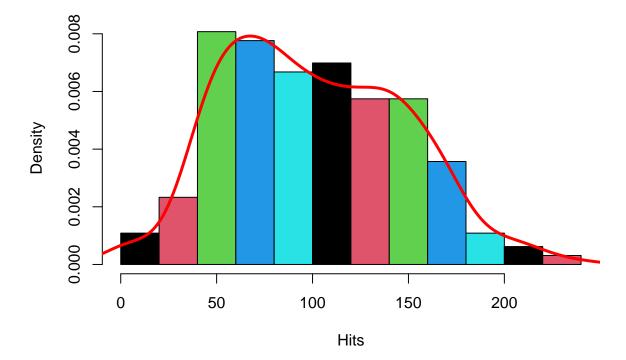
Exercise 7:

Using the same Hitters data set;

• Obtain a histogram of Hits. Give it a proper title and axis names. Also make sure your histogram has a fancy color.

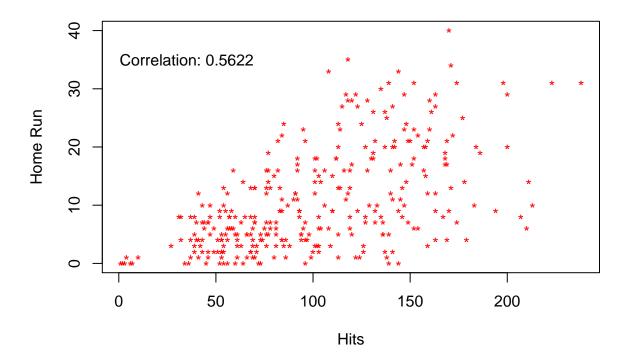
```
hist(Hitters$Hits,
    main = "Distribution of Hits", xlab = "Hits",
    col = c(1,2,3,4,5), prob = T)
lines(density(Hitters$Hits), col = "Red", lwd = 3)
```

Distribution of Hits



• Draw a Scatter Plot for Hits vs HmRun. Give it a proper title, and axis names. Add a text which states the correlation between those two variables.

Hits vs Home Run



• Obtain Boxplots to see the distributions of Runs for each League. Give it a proper title and axis names. Also make sure your Boxplots have fancy colors.

```
boxplot(Hitters$Runs ~ Hitters$League,
    main = "Boxplot of Runs",
    xlab = "Leagues",
    ylab = "Runs",
    col = c("Gold", "Dark Blue"))
```

Boxplot of Runs

