

# USENSYS - Electric Power Sector

## renewables balancing version (6.0)

@olugovoy

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<b>Release notes:</b>	
• <b>v6.0</b> (Apr 11, 2020)	
– Rediced time resolution for supply commodities to improve performance.	

- Added capacity constraints to control resource availability of solar and wind energy.
- The temporary solution for large data files: usensys-balancing-model-data.
- **v5.0** (Feb 22, 2020)
  - Small adjustment according to the newer version of the *energyRt* package (v0.0.4).
  - Investment costs of UHVDC lines increased (+50% for land, an assumption).
  - Concevative storage costs for all scenarios.
  - 100 interregional UHVDC power lines (vs. 80+ in previous version).
- ...
- **v1.0** (May 4, 2019)
  - First version. First set of scenarios.
  - Exogenous trade routes.

```
## Loading required package: sp
## Loading required package: parallel
## Loading required package: ggplot2
##
## Loading package: energyRt
## Energy technology modeling toolbox in R
## Version: 0.01.07.9000-beta (development version from GitHub)
## <http://www.energyrt.org>
##
##
## Attaching package: 'lubridate'
## The following object is masked from 'package:base':
##
##     date
##
## -- Attaching packages ----- tidyverse 1.3.0 --
## v tidyr    1.0.2      v dplyr    0.8.5
## v readr    1.3.1      v stringr 1.4.0
## v purrr    0.3.3      v forcats 0.5.0
##
## -- Conflicts ----- tidyverse_conflicts() --
## x lubridate::as.difftime() masks base::as.difftime()
## x lubridate::date()       masks base::date()
## x dplyr::filter()         masks stats::filter()
## x lubridate::intersect()  masks base::intersect()
## x dplyr::lag()            masks stats::lag()
## x lubridate::setdiff()    masks base::setdiff()
## x lubridate::union()      masks base::union()
```

## Overview

The *renewables balancing* version of USENSYS (*USENSYS\_RENBAL*) has a relatively high temporal resolution to better represent the potential of intermittent wind and solar power generation. Given hourly weather data by regions, the model optimizes the allocation of generating capacities, energy storage, long-distance electric power grid, and the structure of demand across regions based on minimal costs. The full year of hourly data (8760 hours) by 49 regions provide a good (for the capacity expansion class of models) approximation of a power system with intermittent resources. Though the additional granularity increases

the computational burden. Therefore the model horizon is reduced to one year. Depending on scenario, the solution time varies from 1 to 24+ hours on 6-core, 5GHz Intel processor, 64Gb RAM, using GAMS/CPLEX.

#### The main features of the version of the model:

- \* 49 regions (48 lower states and District of Columbia);
- \* 1 year, 8760 hours (24x365);
- \* estimated demand for electricity in 2018 (monthly data by states, disaggregated by hours using national load curve - to be improved on further steps);
- \* Main technologies: - solar PV arrays and wind farms,
  - hourly electricity storage ( $\geq 1$  hour),
  - seasonal electricity storage ( $\geq 1$  day),
  - endogenous interregional grid (UHV power lines and converter stations),
- \* MERRA-2 weather data (see below the aggregation procedure);
- \* Demand options:
  - fully exogenous demand (fixed in time and by regions),
  - static demand with optimized location (fixed in time, endogenous location),
  - time-shiftable demand within a day (24 calendar hours), fixed or optimized location,
  - demand technologies with flexible consumption and restrictions on annual capacity utilization ("power-to-X").
- \* Various policy and resource constraints.

The script below defines the model objects (regions, technologies, commodities, HVDC power lines, demand options, time resolution). The objects can be combined to define scenarios. The result of the entire script is saved in the `USENSYS$file` file. To change any parameters or costs, make the intended modification and rerun this script.

## Map data

GIS information is used for evaluation of renewables potentials by the model regions, for estimation of distances between regions for electric power lines, and for graphical output.

Map objects: **usa49reg** - lower 48 states + DC, spatial polygon data frame format;

**usa49r** - lower 48 states + DC, data frame format.

code

```
if (!file.exists("data/maps/usa49reg.RData")) {
  stop("US map data is not found. Follow the steps in 'usa_maps.R'")
} else {
  load("data/maps/usa49reg.RData")
}

b <- ggplot(usa49r, aes(long,lat, group = group, fill = id)) +
  geom_polygon(aes(fill = id), colour = rgb(1,1,1,.2)) +
  # geom_polygon(aes(fill = id), colour = "white", size = .75) +
  labs(fill = "Region") +
  coord_fixed(1.45) +
  # scale_fill_brewer(palette = "Paired") +
  # coord_quickmap() +
  theme_void() +
  theme(legend.position="none")

# Names of the regions in the model and the map-data
(reg_names <- unique(as.character(usa49reg@data$region)))

## [1] "WA" "MT" "ME" "ND" "SD" "WY" "WI" "ID" "VT" "MN" "OR" "NH" "IA" "MA" "NE"
## [16] "NY" "PA" "CT" "RI" "NJ" "IN" "NV" "UT" "CA" "OH" "IL" "DC" "DE" "WV" "MD"
```

```
## [31] "CO" "KY" "KS" "VA" "MO" "AZ" "OK" "NC" "TN" "TX" "NM" "AL" "MS" "GA" "SC"
## [46] "AR" "LA" "FL" "MI"
```

```
(reg_names_in_gis <- as.character(usa49reg@data$region))
```

```
## [1] "WA" "MT" "ME" "ND" "SD" "WY" "WI" "ID" "VT" "MN" "OR" "NH" "IA" "MA" "NE"
## [16] "NY" "PA" "CT" "RI" "NJ" "IN" "NV" "UT" "CA" "OH" "IL" "DC" "DE" "WV" "MD"
## [31] "CO" "KY" "KS" "VA" "MO" "AZ" "OK" "NC" "TN" "TX" "NM" "AL" "MS" "GA" "SC"
## [46] "AR" "LA" "FL" "MI"
```

```
# Number of regions
```

```
(nreg <- length(reg_names))
```

```
## [1] 49
```

```
(nreg_in_gis <- length(usa49reg@data$region))
```

```
## [1] 49
```

```
# Neighbor regions
```

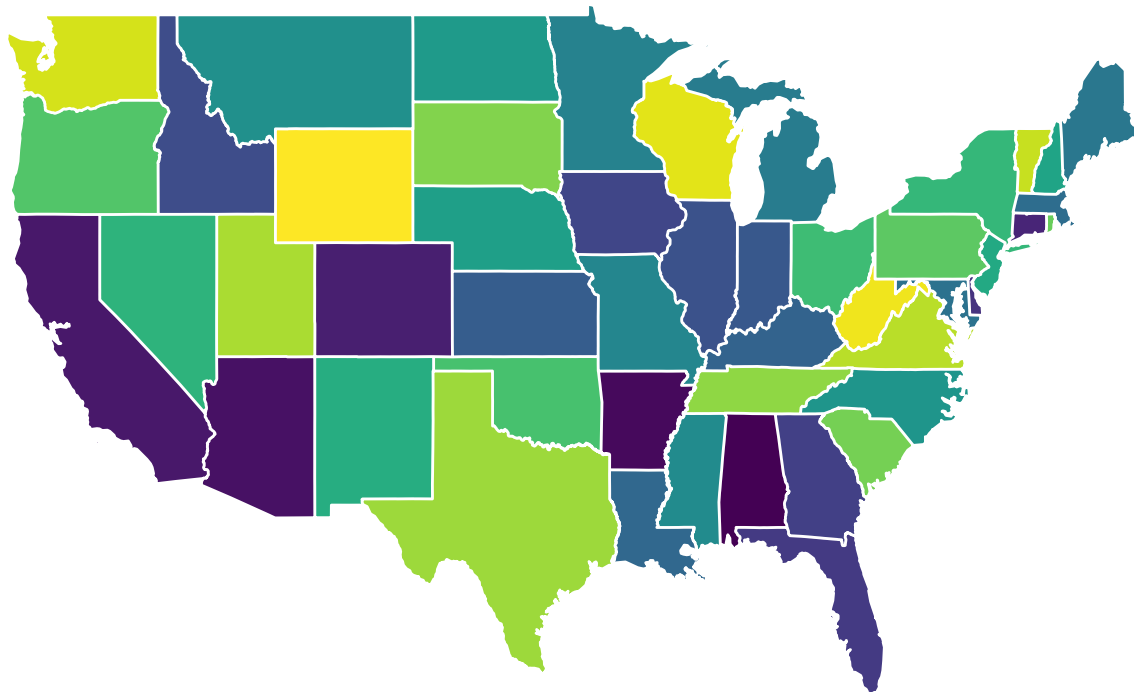
```
nbr <- spdep::poly2nb(usa49reg)
```

```
names(nbr) <- usa49reg@data$region
```

```
# Geographic centers of the regions
```

```
reg_centers <- getCenters(usa49reg)
```

```
mobj <- c(mobj, "usa49r", "usa49reg", "reg_names", "reg_names_in_gis",
          "nreg", "nreg_in_gis", "nbr", "reg_centers")
```



## Sub-annual time resolution (time-slices)

The sub-annual time in the model has two levels:

- the day of the year (*YDAY*), from 1 to 365;
- the hour (1 to 24).

The total number of time-slices (sub-annual time steps) is 8760. Every time-slice is named according to the format "*dNNN\_hNN*", where *NNN* - a day number in a year, *NN* - an hour in 24h format.

code

```
# A list with two levels slices
timeslices365 <- list(
  YDAY = paste0("d", formatC(1:365, width = 3, flag = "0")),
  HOUR = paste0("h", formatC(0:23, width = 2, flag = "0"))
)

# Function to convert data-time object into names of time-slices.
datetime2tsdh <- function(dt) {
  paste0("d", formatC(yday(dt), width = 3, flag = "0"), "_",
    "h", formatC(hour(dt), width = 2, flag = "0"))
}

# check
datetime2tsdh(today("EST"))

## [1] "d106_h00"

# Function to coerse time-slices names into data-time format, for a given year and time-zone.
tsdh2datetime <- function(tslice, year = 2018, tz = "EST") {
  DAY <- as.integer(substr(tslice, 2, 4)) - 1
  HOUR <- as.integer(substr(tslice, 7, 8))
  lubridate::ymd_h(paste0(year, "-01-01 0"), tz = tz) + days(DAY) + hours(HOUR)
}

# check
tsdh2datetime("d365_h23")

## [1] "2018-12-31 23:00:00 EST"

# data.frame object with names of the final time-slices in the model
# and releted data-time information
slc365 <- tibble(
  slice = kronecker(timeslices365$YDAY, timeslices365$HOUR, FUN = "paste", sep = "_")
)

# add date-time info
slc365$yday <- substr(slc365$slice, 1, 4)
slc365$shour <- substr(slc365$slice, 6, 8)
slc365$yday <- as.integer(substr(slc365$slice, 2, 4))
slc365$hour <- as.integer(substr(slc365$slice, 7, 8))
slc365$datetime <- tsdh2datetime(slc365$slice)
slc365$month <- month(slc365$datetime)
slc365$week <- week(slc365$datetime)
head(slc365)

## # A tibble: 6 x 8
##   slice    syday shour  yday  hour datetime      month  week
##   <chr>    <chr> <chr> <int> <int> <dtm>      <dbl> <dbl>
## 1 d001_h00 d001  h00      1      0 2018-01-01 00:00:00      1      1
```

```
## 2 d001_h01 d001 h01      1      1 2018-01-01 01:00:00      1      1
## 3 d001_h02 d001 h02      1      2 2018-01-01 02:00:00      1      1
## 4 d001_h03 d001 h03      1      3 2018-01-01 03:00:00      1      1
## 5 d001_h04 d001 h04      1      4 2018-01-01 04:00:00      1      1
## 6 d001_h05 d001 h05      1      5 2018-01-01 05:00:00      1      1
```

```
tail(slc365)
```

```
## # A tibble: 6 x 8
##   slice    syday shour  yday  hour datetime      month  week
##   <chr>    <chr> <chr> <int> <int> <dtm>      <dbl> <dbl>
## 1 d365_h18 d365  h18    365    18 2018-12-31 18:00:00     12    53
## 2 d365_h19 d365  h19    365    19 2018-12-31 19:00:00     12    53
## 3 d365_h20 d365  h20    365    20 2018-12-31 20:00:00     12    53
## 4 d365_h21 d365  h21    365    21 2018-12-31 21:00:00     12    53
## 5 d365_h22 d365  h22    365    22 2018-12-31 22:00:00     12    53
## 6 d365_h23 d365  h23    365    23 2018-12-31 23:00:00     12    53
```

```
mobj <- c(mobj, "timeslices365", "datetime2tsdh", "tsdh2datetime", "slc365")
```

## Commodities

Declaration of the model commodities.

code

```
ELC <- newCommodity(
  name = 'ELC',
  description = "Generic electricity",
  slice = "HOURLY")
SOL <- newCommodity(
  name = 'SOL',
  description = "Solar energy",
  slice = "ANNUAL")
WIN <- newCommodity(
  name = 'WIN',
  description = "Wind energy, onshore",
  slice = "ANNUAL")
WFF <- newCommodity(
  name = 'WFF',
  description = "Wind energy, offshore",
  slice = "ANNUAL")
UHV <- newCommodity(
  name = 'UHV',
  description = "Ultra High Voltage electricity, DC",
  slice = "HOURLY")
```

## Demand

The final demand for electricity can be specified by hours as an exogenous load curve for each region of the model, or with temporal and/or spatial flexibility. The flexibility of demand might be achieved in several ways, as discussed below.

## Exogenous load curve

Hourly demand by states (the current version applies an aggregated national load curve for every region – to be updated with the actual consumption data).

code

```
## [1] 40630      2

## # A tibble: 6 x 2
##   datetime      MWh
##   <chr>         <dbl>
## 1 02/18/2020 02H 470820
## 2 02/18/2020 01H 471417
## 3 02/18/2020 00H 463638
## 4 02/17/2020 23H 450007
## 5 02/17/2020 22H 441414
## 6 02/17/2020 21H 438162

##   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##   2015    2016    2017    2017    2018    2020

## [1] 8760      7

## # A tibble: 8,760 x 7
##   datetime      MWh datetime_EST      year slice      month hGWh
##   <chr>         <dbl> <dtm>         <dbl> <chr>      <dbl> <dbl>
## 1 01/1/2018 00H 562684 2018-01-01 00:00:00 2018 d001_h00      1 563.
## 2 01/1/2018 01H 566264 2018-01-01 01:00:00 2018 d001_h01      1 566.
## 3 01/1/2018 02H 565612 2018-01-01 02:00:00 2018 d001_h02      1 566.
## 4 01/1/2018 03H 556869 2018-01-01 03:00:00 2018 d001_h03      1 557.
## 5 01/1/2018 04H 545727 2018-01-01 04:00:00 2018 d001_h04      1 546.
## 6 01/1/2018 05H 536422 2018-01-01 05:00:00 2018 d001_h05      1 536.
## 7 01/1/2018 06H 526434 2018-01-01 06:00:00 2018 d001_h06      1 526.
## 8 01/1/2018 07H 520531 2018-01-01 07:00:00 2018 d001_h07      1 521.
## 9 01/1/2018 08H 516766 2018-01-01 08:00:00 2018 d001_h08      1 517.
## 10 01/1/2018 09H 513790 2018-01-01 09:00:00 2018 d001_h09      1 514.
## # ... with 8,750 more rows

## [1] 4067.913

##   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##   321.2  411.8  449.6  464.4  506.1  709.6

## Joining, by = "month"

## # A tibble: 12 x 2
##   month msum
##   <dbl> <dbl>
## 1     1     1
## 2     2     1
## 3     3     1
## 4     4     1
## 5     5     1
## 6     6  1.00
## 7     7  1.00
## 8     8     1
## 9     9     1
```

```

## 10    10    1
## 11    11    1
## 12    12    1

## # A tibble: 588 x 6
##   YEAR MONTH STATE `TYPE OF PRODUCER` `ENERGY SOURCE` `GENERATION`r\n(Mega~
##   <dbl> <dbl> <chr> <chr> <chr> <dbl>
## 1 2018      1 AL    Total Electric Power~ Total 13310533
## 2 2018      1 AR    Total Electric Power~ Total 6177100
## 3 2018      1 AZ    Total Electric Power~ Total 8208302
## 4 2018      1 CA    Total Electric Power~ Total 14461936
## 5 2018      1 CO    Total Electric Power~ Total 4681142
## 6 2018      1 CT    Total Electric Power~ Total 3470117
## 7 2018      1 DC    Total Electric Power~ Total 6937
## 8 2018      1 DE    Total Electric Power~ Total 540139
## 9 2018      1 FL    Total Electric Power~ Total 19687966
## 10 2018      1 GA    Total Electric Power~ Total 12103582
## # ... with 578 more rows

## [1] 4161.304

## [1] 4067.913

## [1] 49

## Joining, by = "month"

## [1] TRUE

## [1] 4161304

## [1] 4067913

## [1] 4161304

##   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.00368 4.02346 7.50708 9.69458 12.62367 88.11843

## [1] 429240      4

## [1] 49

##   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.00368 4.02346 7.50708 9.69458 12.62367 88.11843

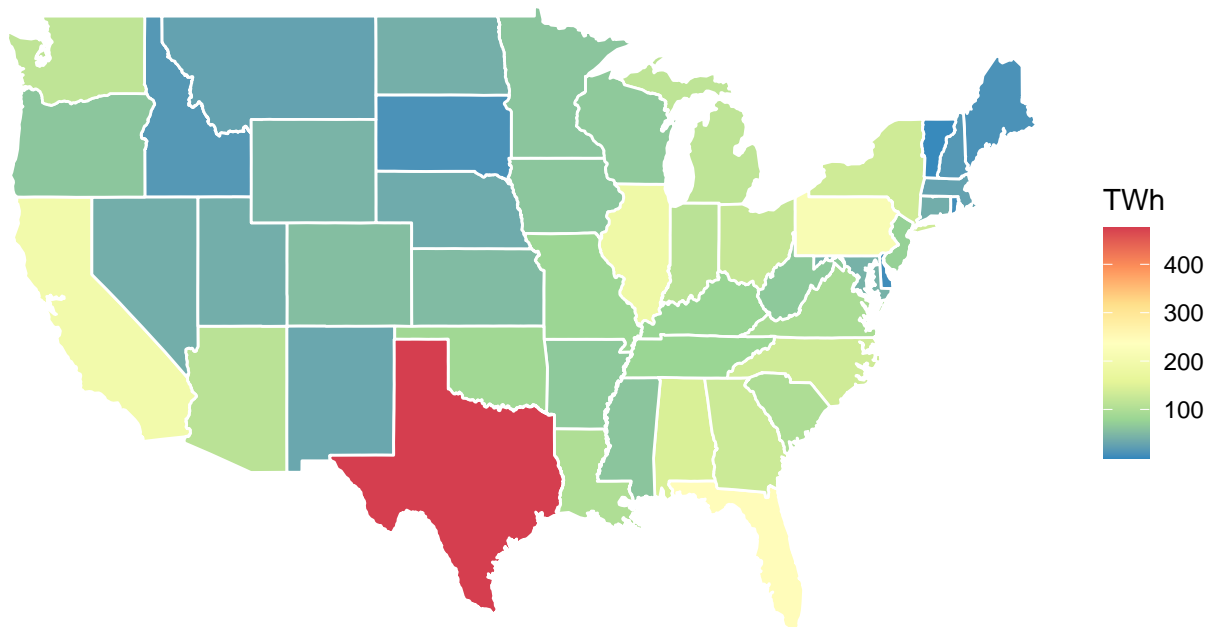
## Warning: Column `region`/`id` joining character vector and factor, coercing into
## character vector

## # A tibble: 11,481 x 8
##   region TWh long lat order hole piece group
##   <chr> <dbl> <dbl> <dbl> <int> <lgl> <fct> <fct>
## 1 AL    145. -85.1 32.0     1 FALSE 1 AL.1
## 2 AL    145. -85.1 31.9     2 FALSE 1 AL.1
## 3 AL    145. -85.1 31.9     3 FALSE 1 AL.1
## 4 AL    145. -85.1 31.8     4 FALSE 1 AL.1
## 5 AL    145. -85.1 31.8     5 FALSE 1 AL.1
## 6 AL    145. -85.1 31.7     6 FALSE 1 AL.1
## 7 AL    145. -85.1 31.7     7 FALSE 1 AL.1
## 8 AL    145. -85.1 31.7     8 FALSE 1 AL.1
## 9 AL    145. -85.1 31.6     9 FALSE 1 AL.1
## 10 AL   145. -85.0 31.6    10 FALSE 1 AL.1

```



```
## # ... with 11,471 more rows
## Saving 6.5 x 4.5 in image
```



## “Flat” load curve

```
code
```

```
## [1] 429240      4
## [1] 2018
## [1] 49
## [1] 8760
## # A tibble: 49 x 3
## # Groups:   region [49]
##   region year    GWh
##   <chr> <int> <dbl>
## 1 AL    2018 144989.
## 2 AR    2018  67134.
## 3 AZ    2018 112303.
## 4 CA    2018 197227.
## 5 CO    2018  56010.
## 6 CT    2018  39042.
## 7 DC    2018    79.5
## 8 DE    2018   6014.
```

```
## 9 FL      2018 244898.
## 10 GA     2018 130061.
## # ... with 39 more rows
## [1] 4161304
```

## Demand-side technology with flexible load

Any technology with seasonally and hourly flexible load, for example Power-to-X (P2X).

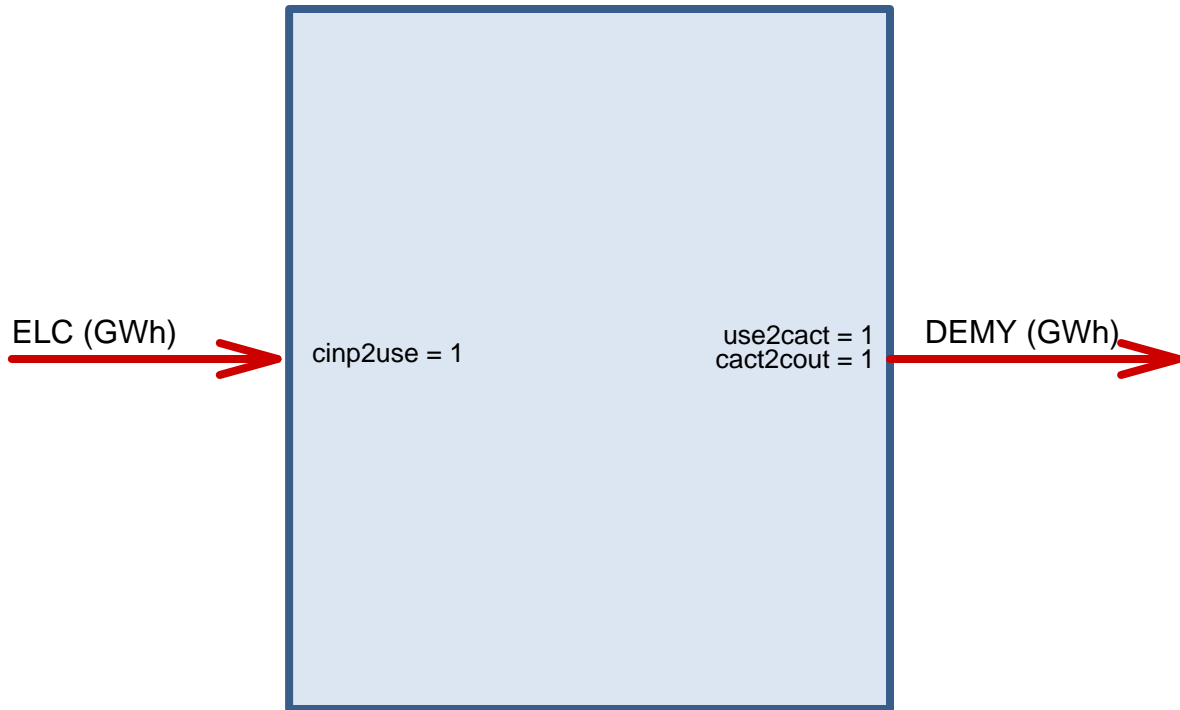
code

```
DEM35 <- newCommodity(
  "DEM35",
  description = "",
  slice = "HOURLY")

ELC2DEM35 <- newTechnology(
  name = "ELC2DEM35",
  description = "Demand-side technology with 35% lower bound on annual load",
  # region = reg_names,
  input = list(
    comm = "ELC",
    unit = "GWh"
  ),
  output = list(
    # comm = "DEM35",
    comm = "DEMY",
    unit = "GWh"
  ),
  cap2act = 24*365,
  afs = list(
    slice = "ANNUAL",
    # The technology cannot have less than 35% annual load (in each region)
    afs.lo = .35
  ),
  # invcost = list(
  #   invcost = 1 # arbitrary small number for tracking
  # ),
  varom = list(varom = convert("cents/kWh", "MUSD/GWh", 10)),
  # olife = list(olife = 100),
  slice = "HOURLY"
)
draw(ELC2DEM35)
```

## ELC2DEM35

Demand-side technology with 35% lower bound on annual load



```
ELC2DEM35CAP <- newConstraintS(
  name = "ELC2DEM35CAP",
  eq = ">=",
  type = "capacity",
  for.each = list(
    year = USENSYS$modelYear,
    tech = "ELC2DEM35"),
  for.sum = list(
    region = reg_names
  ),
  rhs = round(elc_dem_fx_y_GWh / 24 / 365 * 0.25)) # limit on capacity

DEM35EXP <- newExport(
  name = "DEM35EXP",
  description = "Annual demand for technologies with 35% annual load",
  commodity = "DEM35",
  exp = list(
    price = convert("cents/kWh", "MUSD/GWh", 1) # sell for 1 cent
  )
)
```

### Optimized location

code

```

DEM100 <- newCommodity("DEM100", slice = "HOURL")

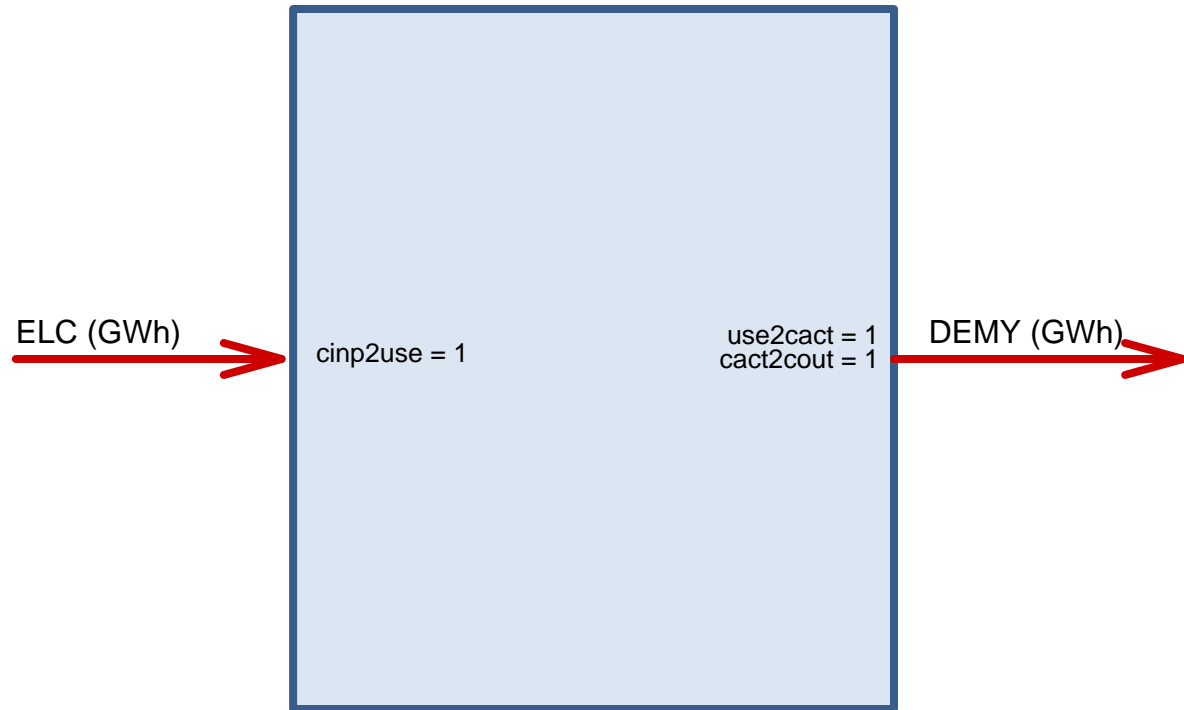
DEMY <- newCommodity("DEMY", slice = "ANNUAL")

ELC2DEM100 <- newTechnology(
  name = "ELC2DEM100",
  description = "Tech for allocatable static demand 1x",
  input = list(
    comm = "ELC",
    unit = "GWh"
    # unit = "PJ"
  ),
  output = list(
    # comm = "DEM100",
    comm = "DEMY",
    unit = "GWh"
    # unit = "PJ"
  ),
  cap2act = 24*365,
  # afs = list(
  #   slice = "ANNUAL",
  #   afs.lo = 1
  # ),
  af = list(
    af.lo = 1
  ),
  slice = "HOURL"
)
draw(ELC2DEM100)

```

## ELC2DEM100

Tech for allocatable static demand 1x



```

CELC2DEM100CAPFX <- newConstraintS(
  name = "CELC2DEM100CAPFX",
  eq = ">=",
  type = "capacity",
  for.each = list(
    year = 2018,
    tech = "ELC2DEM100"),
  for.sum = list(
    region = reg_names
  ),
  rhs = round(elc_dem_fx_y_GWh / 24 / 365 * .5)) # limit on capacity

CELC2DEM100CAPUP <- newConstraintS(
  name = "CELC2DEM100CAPUP",
  eq = "<=",
  type = "capacity",
  for.each = list(
    year = 2018,
    region = reg_names,
    tech = "ELC2DEM100"),
  rhs = CELC2DEM100CAPFX@defVal/10) # at least 10 regions

DEM100DEXP <- newExport(
  name = "DEM100DEXP",
  description = "Flexible demand",

```

```

commodity = "DEM100",
exp = list(
  price = convert("cents/kWh", "MUSD/GWh", 10) # sell for 1 cent
)
)

```

## Intraday, 24h flexible demand (DSM)

code

```

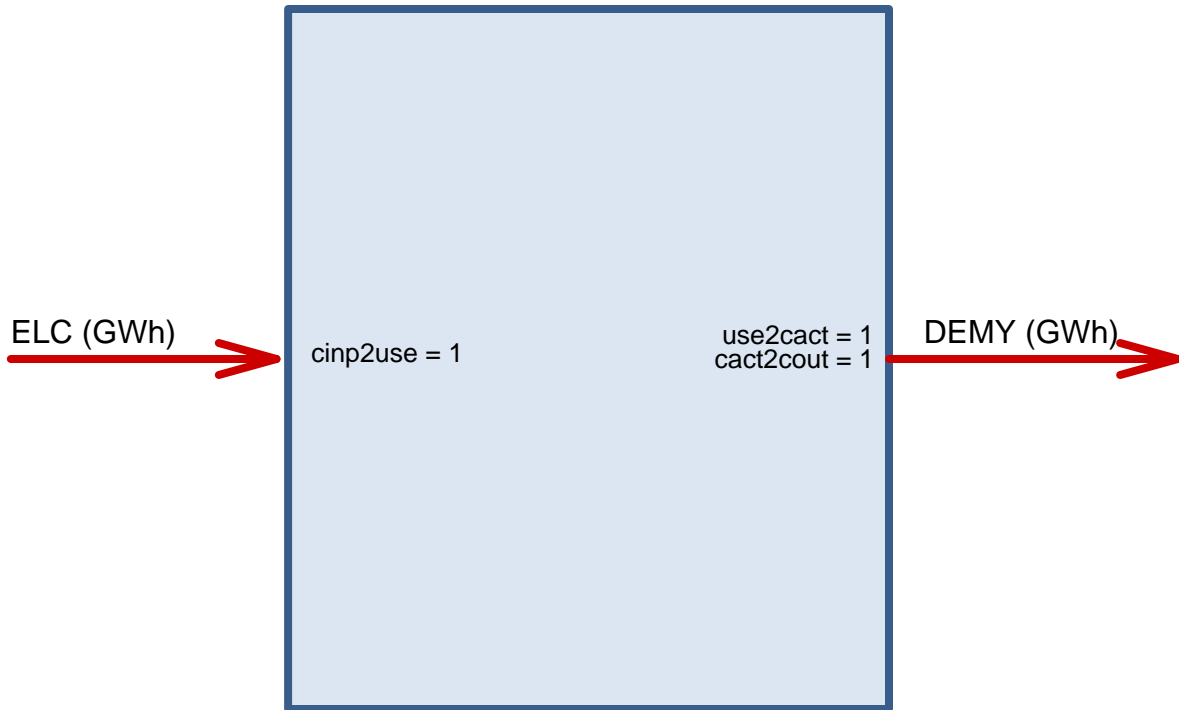
DSMD <- newCommodity("DSMD", slice = "YDAY")

ELC2DSMD <- newTechnology(
  name = "ELC2DSMD",
  description = "Tech to convert ELC from HOUR to YDAY",
  input = list(
    comm = "ELC",
    unit = "GWh"
    # unit = "PJ"
  ),
  output = list(
    # comm = "DSMD",
    comm = "DEMY",
    unit = "GWh"
    # unit = "PJ"
  ),
  # cap2act = 31.536, #convert("GWh", "PJ", 24 * 365),
  cap2act = 24*365,
  afs = list(
    # slice = "MONTH",
    slice = timeslices365$YDAY,
    ## The technology should be x% operational in every region where exists
    ## < 1 allows some seasonality if export-demand is used for DSMD,
    ## but shouldn't affect anything if demand is used for DSMD
    afs.lo = rep(9/24, length(timeslices365$YDAY))
  ),
  # invcost = list(
  #   invcost = 1 # arbitrary small number for tracking
  # )
  # varom = list(varom = convert("USD/kWh", "MUSD/PJ", .01)),
  varom = list(varom = convert("cents/kWh", "MUSD/GWh", 5)),
  # stock = data.frame(
  #   region = elc_dem_fx_reg_y$region,
  #   stock = elc_dem_fx_reg_y$GWh/365/24 * 0.25 # 25% additional to the static demand
  # ),
  # end = list(
  #   end = 2010
  # ),
  slice = "HOUR"
)
# ELC2DSMD@stock$stock <- ELC2DSMD@stock$stock / ELC2DSMD@afs$afs.lo[1] # Adjust capacity
draw(ELC2DSMD)

```

## ELC2DSMD

Tech to convert ELC from HOUR to YDAY



```

# DSMDEXP <- newExport(
#   name = "DSMDEXP",
#   description = "Flexible demand",
#   commodity = "DSMD",
#   exp = list(
#     price = convert("cents/kWh", "MUSD/GWh", 5) # sell for 1 cent
#   )
# )
#
elc_gen_2018_reg_y <- elc_gen_2018 %>%
  group_by(region) %>%
  summarise(GWh = sum(GWh))

DEMYEXP <- newExport(
  name = "DEMYEXP",
  # description = "Flexible demand",
  commodity = "DEMY",
  exp = data.frame(
    slice = "ANNUAL",
    region = elc_gen_2018_reg_y$region,
    # exp.up = elc_gen_2018_reg_y$GWh,
    exp.fx = elc_gen_2018_reg_y$GWh,
    price = convert("cents/kWh", "MUSD/GWh", 15)
  )
)
  
```

## Weather factors

Hourly weather information is used to estimate the output of intermittent renewables, solar PVs and wind turbines. The weather information is supplied as multipliers to availability factors of the generating technologies. I.e. availability of solar energy can be estimated based on the solar radiation (flux) data, or actual output of the technology (PV) expected under complex weather data (direct and indirect solar irradiance, temperature, and/or clouds etc.). The estimation can be done on grid data, then aggregated using potentially perspective and available locations for the installation of the solar arrays. Here, for simplicity, we estimate availability of the solar resource based on NASA's "surface net downward shortwave flux" (SWGNT, Watts per square meter), assuming that the full capacity of PV arrays is achieved at 800 W/m<sup>2</sup> level of the flux. This estimate is certainly not the best one, can be improved.

The estimated factors are aggregated for all available locations by states (which implies that allocation of PVs capacity is assumed to be evenly distributed across all the territory in each state).

For wind energy, wind-power curves are used to estimate potential output of wind-mills across locations with the best potential of wind energy.

## Land assumptions based on MERRA-2 data

1 degree of latitude is about 111 km |  $\times 0.625 = \sim 69$  km

1 degree of latitude at  $\sim 20$ -50 degree is  $\sim 100$ -70km |  $\times 0.5 = \sim 35$ -50km

1 cell of NASA grid is from 3569 to 5069 == 2415 (North) to 3450 (South) sq.km

we can take 3000 sq.km as approximation for all locations

## Solar availability factors

code

### Land requirements for solar PVs

1sq.m PV requires  $\sim 2.5$ sq.m of land

$1.046 \times 1.558$  PV panel 345 Watt / 1.63 m<sup>2</sup>  $\sim 200$  Watt/m<sup>2</sup> ==  $.2$  GW/km<sup>2</sup> / 2.5 =  $.08$  GW/km<sup>2</sup> = 80GW/1000km<sup>2</sup>

Spacing  $\sim .08$  GW per sq.km assuming PV efficiency = 0.2

Increase of PV efficiency will require less space ( $0.08 \times 1.5 = 0.12$ GW for 30% efficiency and 0.16GW for 40% PV efficiency)

```
# Share of land in every region which potentially can be used for PVs:
PV_coverage_share_max <- 0.1 # an assumption (almost unrestricted case)
PV_GW_max <- .08 * 3000 * PV_coverage_share_max # per one MERRA-2 grid cell

# MERRA-2 data:
# https://gmao.gsfc.nasa.gov/reanalysis/MERRA-2/data_access/
# here we use data for one year only
load("data/MERRA2/nasa_sol_US49.RData")
gsol
```

```
## # A tibble: 22,916,160 x 11
```

```
##   datetime          loc_id SWGDN SWGNT   lon   lat region  hour month mdays
##   <dtm>             <int> <dbl> <dbl> <dbl> <dbl> <fct>  <int> <fct> <int>
## 1 2017-01-01 00:30:00 133216     0     0 -80.6  25.5 FL        0 Janu~    31
## 2 2017-01-01 00:30:00 133765     0     0 -97.5  26   TX        0 Janu~    31
## 3 2017-01-01 00:30:00 133791     0     0 -81.2  26   FL        0 Janu~    31
## 4 2017-01-01 00:30:00 133792     0     0 -80.6  26   FL        0 Janu~    31
## 5 2017-01-01 00:30:00 134339     0     0 -98.8  26.5 TX        0 Janu~    31
```

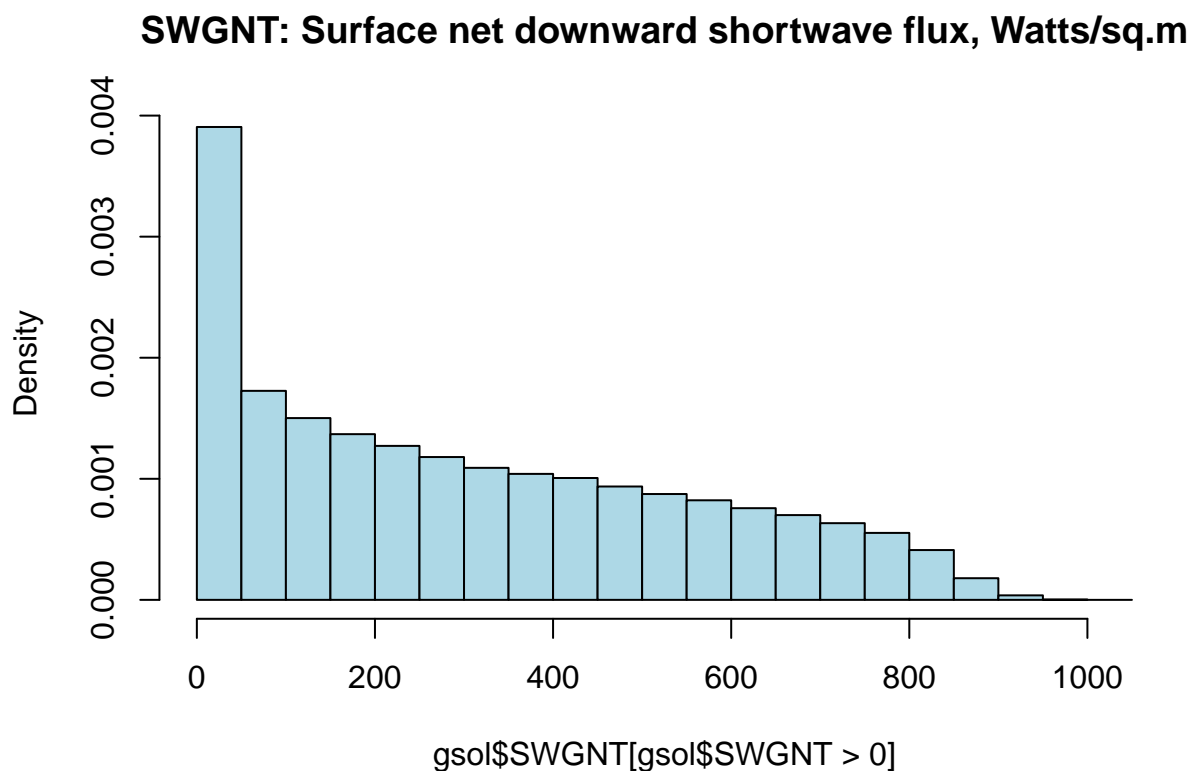


```
## 6 2017-01-01 00:30:00 134340      0      0 -98.1  26.5 TX      0 Janu~   31
## 7 2017-01-01 00:30:00 134341      0      0 -97.5  26.5 TX      0 Janu~   31
## 8 2017-01-01 00:30:00 134366      0      0 -81.9  26.5 FL      0 Janu~   31
## 9 2017-01-01 00:30:00 134367      0      0 -81.2  26.5 FL      0 Janu~   31
## 10 2017-01-01 00:30:00 134368      0      0 -80.6  26.5 FL      0 Janu~   31
## # ... with 22,916,150 more rows, and 1 more variable: yday <dbl>
```

```
summary(gsol$SWGNT)
```

```
##      Min.   1st Qu.   Median     Mean  3rd Qu.     Max.
##      0.000    0.000    7.051  167.446  294.875 1011.000
```

```
hist(gsol$SWGNT[gsol$SWGNT > 0], col = "lightblue", probability = T,
     main = "SWGNT: Surface net downward shortwave flux, Watts/sq.m")
```

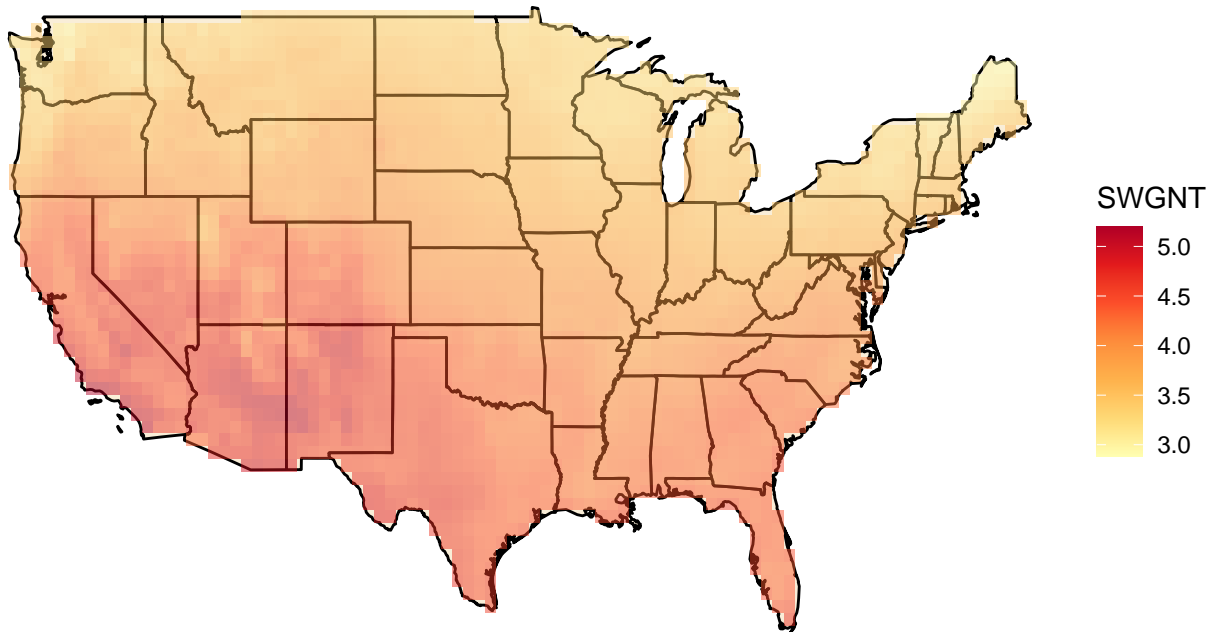


```
# Annual aggregate, kWh/day
ysol <- group_by(gsol, loc_id, lat, lon, region) %>%
  summarise(SWGNT = sum(SWGNT)/365/1e3)

# Max capacity by MERRA-2 locations
PV_GW_max_reg <- ysol %>%
  group_by(region) %>%
  summarise(GW_up = PV_GW_max * n())

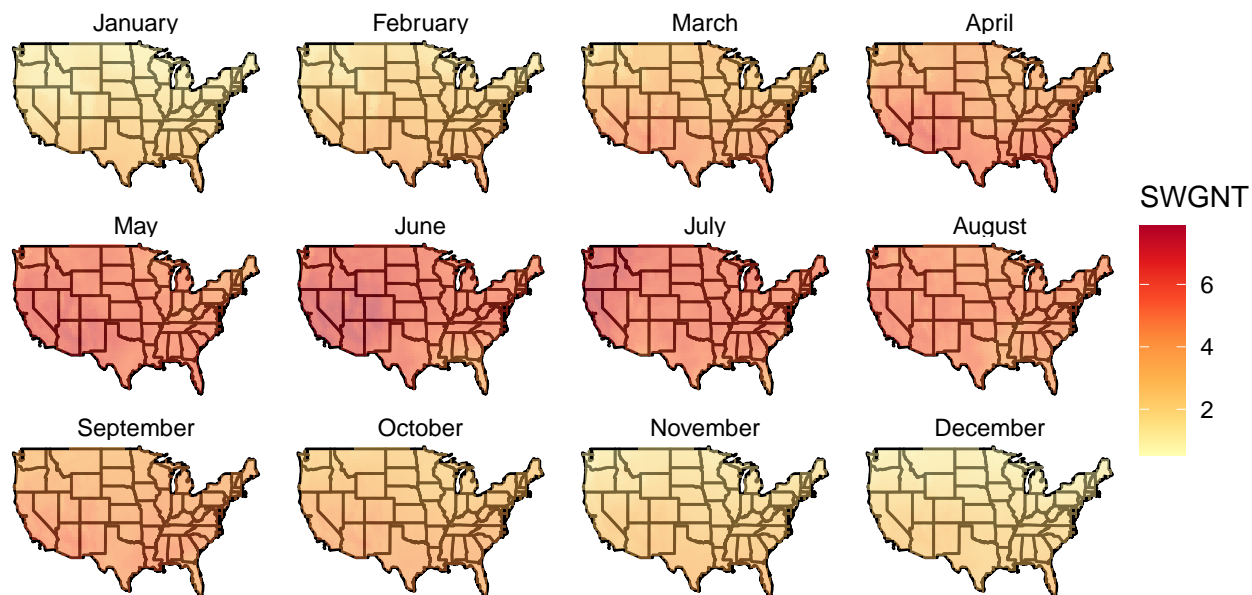
ggplot(usa49r, aes(long, lat, group = group)) +
  geom_polygon(colour = "black", fill = "wheat", alpha = .5) +
  coord_fixed(1.45) +
  theme_void() +
```

```
geom_raster(data = ysol, aes(lon, lat, fill = SWGNT), interpolate = F, inherit.aes = F, alpha = .95) +
scale_fill_distiller(palette = "YlOrRd", direction = 1)
```



```
# By months, kWh/day
msol <- group_by(gsol, loc_id, lat, lon, region, month) %>%
  summarise(SWGNT = sum(SWGNT/mdays)/1e3)

ggplot(usa49r, aes(long, lat, group = group)) +
  geom_polygon(colour = "black", fill = "wheat", alpha = .5) +
  coord_fixed(1.45) +
  theme_void() +
  geom_raster(data = msol, aes(lon, lat, fill = SWGNT), interpolate = F, inherit.aes = F, alpha = .95) +
  scale_fill_distiller(palette = "YlOrRd", direction = 1) +
  facet_wrap(~month)
```



```
# Aggregation regions
dhsol <- group_by(gsol, region, yday, hour) %>% # lat, lon,
  summarise(SWGNT = mean(SWGNT))
summary(dhsol$SWGNT)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##  0.000   0.000   7.611 162.951 291.846 937.517
```

```
# Estimated weather factors
dhsol$WF <- dhsol$SWGNT / 800
dhsol$WF[dhsol$WF > 1] <- 1
dhsol$WF[dhsol$WF < .03] <- 0 # kick-starting irradiance
summary(dhsol$WF)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.0000 0.0000 0.0000 0.2025 0.3648 1.0000
```

```
dhsol
```

```
## # A tibble: 420,480 x 5
## # Groups:   region, yday [17,520]
##   region yday hour SWGNT WF
##   <fct> <dbl> <int> <dbl> <dbl>
## 1 AL      1     0  0     0
## 2 AL      1     1  0     0
## 3 AL      1     2  0     0
## 4 AL      1     3  0     0
## 5 AL      1     4  0     0
```

```
## 6 AL      1      5 0      0
## 7 AL      1      6 0      0
## 8 AL      1      7 0.281 0
## 9 AL      1      8 23.9  0
## 10 AL     1      9 75.4  0.0942
## # ... with 420,470 more rows

# Add slice-names
dhsol$slice <- paste0("d", formatC(dhsol$yday, width = 3, flag = "0"),
                     "_h", formatC(dhsol$hour, width = 2, flag = "0"))
dhsol
```

```
## # A tibble: 420,480 x 6
## # Groups:   region, yday [17,520]
##   region yday hour SWGNT   WF slice
##   <fct> <dbl> <int> <dbl> <dbl> <chr>
## 1 AL      1      0 0      0    d001_h00
## 2 AL      1      1 0      0    d001_h01
## 3 AL      1      2 0      0    d001_h02
## 4 AL      1      3 0      0    d001_h03
## 5 AL      1      4 0      0    d001_h04
## 6 AL      1      5 0      0    d001_h05
## 7 AL      1      6 0      0    d001_h06
## 8 AL      1      7 0.281 0    d001_h07
## 9 AL      1      8 23.9  0    d001_h08
## 10 AL     1      9 75.4  0.0942 d001_h09
## # ... with 420,470 more rows
```

```
dim(dhsol)[1] / 365/24 # 48, i.e. one region is missing - DC
```

```
## [1] 48
```

```
dhsol$region <- as.character(dhsol$region)
reg_names[!(reg_names %in% unique(dhsol$region))]
```

```
## [1] "DC"
```

```
# Use MD weather data for DC
dhsol_DC <- dhsol[dhsol$region == "MD",]
dim(dhsol_DC)
```

```
## [1] 8760      6
```

```
dhsol_DC$region <- "DC"
dhsol_DC
```

```
## # A tibble: 8,760 x 6
## # Groups:   region, yday [365]
##   region yday hour SWGNT   WF slice
##   <chr> <dbl> <int> <dbl> <dbl> <chr>
## 1 DC      1      0 0      0    d001_h00
## 2 DC      1      1 0      0    d001_h01
## 3 DC      1      2 0      0    d001_h02
## 4 DC      1      3 0      0    d001_h03
## 5 DC      1      4 0      0    d001_h04
## 6 DC      1      5 0      0    d001_h05
## 7 DC      1      6 0      0    d001_h06
## 8 DC      1      7 10.8 0    d001_h07
```

```
## 9 DC      1      8 96.1 0.120 d001_h08
## 10 DC     1      9 202. 0.253 d001_h09
## # ... with 8,750 more rows

# Add DC
dhsol <- bind_rows(dhsol, dhsol_DC)
dim(dhsol)[1] / 365/24

## [1] 49

length(unique(dhsol$region)) == nreg # double-check

## [1] TRUE

size(gsol); rm(gsol)

## [1] "1.5 Gb"
```

## Wind availability factors

code

```
# Hourly wind speed data at 50 meters height for US, 2018
# (source: NASA/MERRA2, preprocessed)
load("data/merra2/nasa_wnd_US49.RData")
gwnd

## # A tibble: 26,481,480 x 19
##   datetime      loc_id WS50M   lon   lat US_100km_buffer US_10km_buffer
##   <dtm>          <int> <dbl> <dbl> <dbl> <lgl>          <lgl>
## 1 2017-01-01 00:30:00 132062  7.46 -81.9 24.5 TRUE          FALSE
## 2 2017-01-01 00:30:00 132063  7.67 -81.2 24.5 TRUE          FALSE
## 3 2017-01-01 00:30:00 132064  7.78 -80.6 24.5 TRUE          FALSE
## 4 2017-01-01 00:30:00 132065  7.92 -80   24.5 TRUE          FALSE
## 5 2017-01-01 00:30:00 132638  6.98 -81.9 25   TRUE          FALSE
## 6 2017-01-01 00:30:00 132639  6.93 -81.2 25   TRUE          FALSE
## 7 2017-01-01 00:30:00 132640  7.43 -80.6 25   TRUE          TRUE
## 8 2017-01-01 00:30:00 132641  7.82 -80   25   TRUE          FALSE
## 9 2017-01-01 00:30:00 132642  7.98 -79.4 25   TRUE          FALSE
## 10 2017-01-01 00:30:00 133213  6.70 -82.5 25.5 TRUE          FALSE
## # ... with 26,481,470 more rows, and 12 more variables: non_US <lgl>,
## #   drop <lgl>, US_land <lgl>, offshore <lgl>, nearest_neighbor <chr>,
## #   region <fct>, buff_10km <chr>, offshore_names <chr>, hour <int>,
## #   month <fct>, mdays <int>, yday <int>

if (is.factor(gwnd$region)) gwnd$region <- as.character(gwnd$region)

# Simplified aggregated wind-power curve as a function of wind speed.
# (assumed, should be replaced by read)
WindPowerCurve <- function(x = NULL,
                           xcutin = 4, xpeak = 14, xpeak2 = 20, xcutoff = 28,
                           ycutoff = .9, round = 3) {
  # x - wind speed in m/s
  # xcutin, xcutoff - operational speed of wind (m/s, min and max respectively)
  # xpeak, xpeak2 - the range of speed of with peak (nameplate) power
  # ycutoff - output factor at cut off (max) wind speed
  ff1 <- function(x1) {
```

```

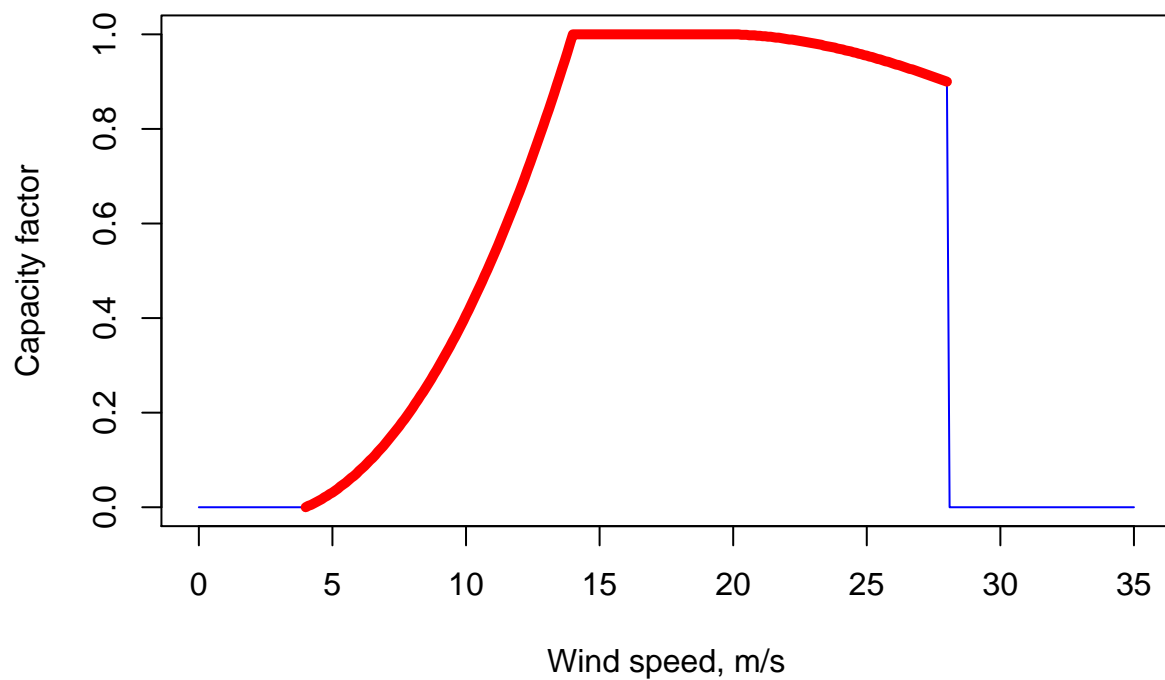
xx <- c(xcutin, 0.5 * (xpeak + xcutin), xpeak)
xx2 <- xx * xx
xx3 <- xx * xx2
yy <- c(0, .3, 1)
ff <- lm(yy ~ 0 + xx + xx + xx2 + xx3)
predict(ff, data.frame(
  xx = x1,
  xx2 = x1 * x1,
  xx3 = x1 * x1 * x1
))
}
ff2 <- function(x2) {
  xx <- c(xpeak2, 0.5 * (xcutoff + xpeak2), xcutoff)
  xx2 <- xx * xx
  xx3 <- xx * xx2
  yy <- c(1, .51 * (ycutoff + 1), ycutoff)
  ff <- lm(yy ~ 0 + xx + xx + xx2 + xx3)
  predict(ff, data.frame(
    xx = x2,
    xx2 = x2 * x2,
    xx3 = x2 * x2 * x2
  ))
}
y <- rep(0., length(x))
ii <- x <= xcutin
y[ii] <- 0
ii <- x > xcutoff
y[ii] <- 0
ii <- x >= xpeak & x <= xpeak2
y[ii] <- 1
ii <- x > xcutin & x < xpeak
y[ii] <- ff1(x[ii])
ii <- x > xpeak2 & x <= xcutoff
y[ii] <- ff2(x[ii])
return(round(y, round))
# splinefun(xx, yy, method = "natural")
}

# Check
WindPowerCurve(0:30)

## [1] 0.000 0.000 0.000 0.000 0.000 0.000 0.031 0.077 0.136 0.210 0.300 0.406 0.528
## [13] 0.667 0.825 1.000 1.000 1.000 1.000 1.000 1.000 1.000 0.997 0.990 0.981
## [25] 0.969 0.955 0.938 0.920 0.900 0.000 0.000

x <- seq(0, 35, by = .1)
plot(x, WindPowerCurve(x), type = "l", col = "blue", lwd = 1,
      xlab = "Wind speed, m/s", ylab = "Capacity factor")
x1 <- seq(4, 28, by = .1)
points(x1, WindPowerCurve(x1), type = "l", col = "red", lwd = 5)

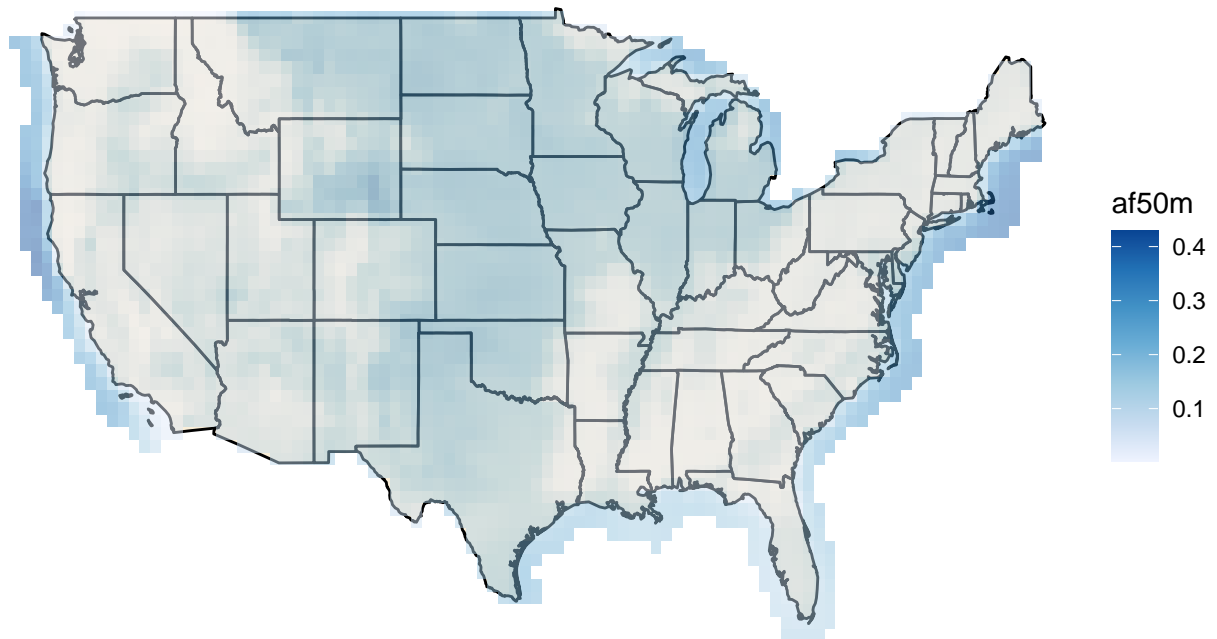
```



```
# Availability factor for wind-energy technologies,
# estimated based on the wind-power curve
gwnd$af50m <- WindPowerCurve(gwnd$WS50M)

# Annual availability factor of wind turbines by location
ywnd <- group_by(gwnd, loc_id, lat, lon, region) %>%
  summarise(af50m = sum(af50m)/365/24)

ggywnd <- function(ii = rep(T, length(ywnd$loc_id))) {
  ggplot(usa49r, aes(long,lat, group = group)) +
    geom_polygon(colour = "black", fill = "wheat", alpha = .5) +
    coord_fixed(1.45) +
    theme_void() +
    geom_raster(data = ywnd[ii,], aes(lon, lat, fill = af50m),
               interpolate = F, inherit.aes = F, alpha = .95) +
    scale_fill_distiller(palette = "Blues", direction = 1)
}
ggywnd()
```



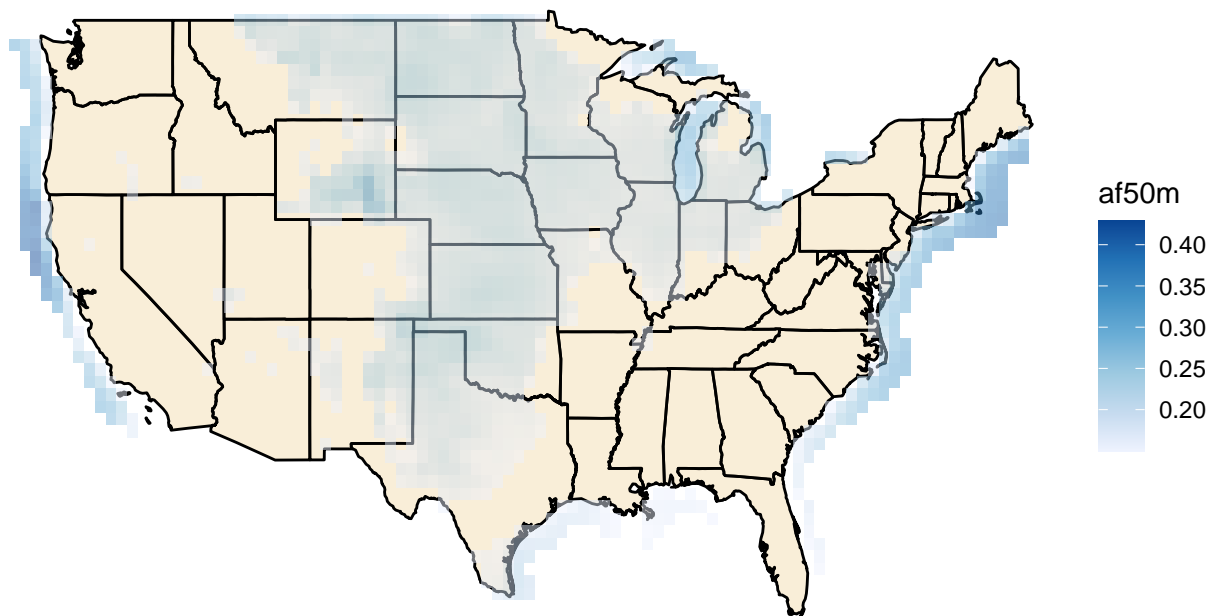
```
# filtered  
ii <- ywnd$af50m >= .15; summary(ii)
```

```
##      Mode   FALSE    TRUE  
## logical   1723    1300
```

```
ggywnd(ii)
```

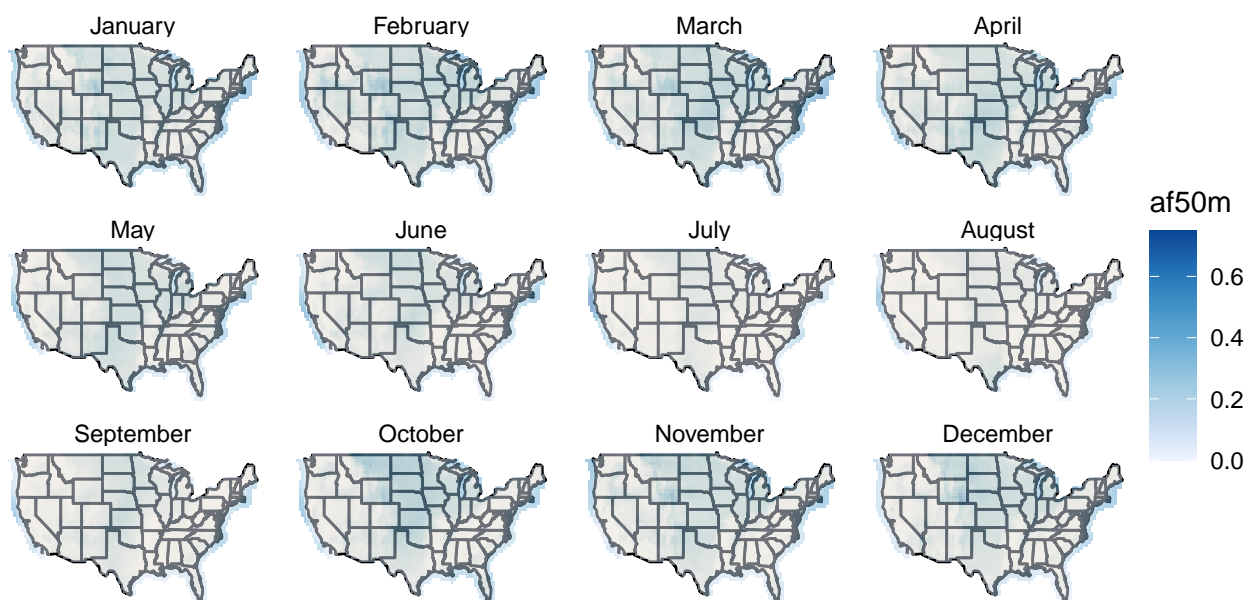
```
## Warning: Raster pixels are placed at uneven horizontal intervals and will be  
## shifted. Consider using geom_tile() instead.
```





```
# Aggregation by months
mwnd <- group_by(gwnd, loc_id, lat, lon, region, month) %>%
  summarise(af50m = sum(af50m/mdays)/24)

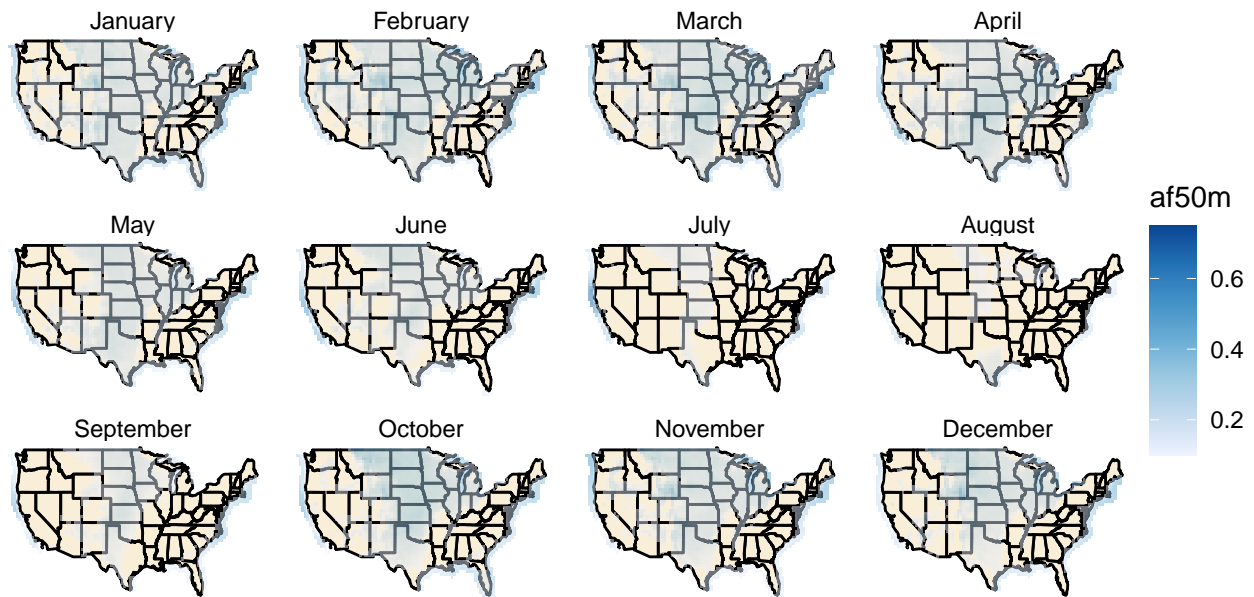
ggmwnd <- function(mm = rep(T, length(mwnd$loc_id))) {
  ggplot(usa49r, aes(long,lat, group = group)) +
    geom_polygon(colour = "black", fill = "wheat", alpha = .5) +
    coord_fixed(1.45) +
    theme_void() +
    geom_raster(data = mwnd[mm,], aes(lon, lat, fill = af50m),
               interpolate = F, inherit.aes = F, alpha = .95) +
    scale_fill_distiller(palette = "Blues", direction = 1) + # , trans = "log10"
    facet_wrap(~month)
}
ggmwnd()
```



```
mm <- mwnd$af50m >= .1; summary(mm)
```

```
##      Mode  FALSE   TRUE
## logical 16570 19706
```

```
ggmwnd(mm)
```



```
# Averaging by annual potential
# `loc_id_??` is locations with the ranged potential
yy_20 <- ywnd$af50m >= .20; summary(yy_20); loc_id_20 <- ywnd$loc_id[yy_20]

##      Mode   FALSE    TRUE
## logical  2303     720

yy_15 <- ywnd$af50m >= .15 & ywnd$af50m < .20; summary(yy_15); loc_id_15 <- ywnd$loc_id[yy_15]

##      Mode   FALSE    TRUE
## logical  2443     580

yy_10 <- ywnd$af50m >= .10 & ywnd$af50m < .15; summary(yy_10); loc_id_10 <- ywnd$loc_id[yy_10]

##      Mode   FALSE    TRUE
## logical  2553     470

# Check for overlay
any(loc_id_20 %in% loc_id_15) | any(loc_id_10 %in% loc_id_20)

## [1] FALSE

# Assuming 4 megawatts per square kilometer (about 10 megawatts per square mile, NREL)
# for offshore: 3-5 megawatts (MW) per square kilometer
# Taking one grid cell is about ~50x60 km, or ~3000 sq.km,
# one grid cell can accomodate up to 12GW (3000 * 4 / 1e3) onshore or 9GW offshore.
# For simplicity let's assume up to 5GW can be used for both
# on- and off-shore wind power capacity per one cell of the grid.
# I.e. up to ~50% of therritory presumably might be used for wind energy
```

```

# from technical perspective. The number can be adjusted in constraints.
# hist(gwnd$af50m)
WINN_GW_max <- 5 # max GW Onshore per cell
WINF_GW_max <- 5 # max GW Offshore per cell
gwnd$max_GWh <- WINN_GW_max * gwnd$af50m # GWh per hour

# Onshore wind resource
# Filter and aggregate by regions locations
# with potential for locations with > 20% availability factor
ii <- (gwnd$loc_id %in% loc_id_20) & gwnd$US_10km_buffer
summary(ii)

##      Mode      FALSE      TRUE
## logical 21707280 4774200

wnd_af20 <- group_by(gwnd[ii,], datetime, region) %>%
  summarise(max_GWh = sum(max_GWh, na.rm = T),
            af50m = mean(af50m))
wnd_af20

## # A tibble: 210,240 x 4
## # Groups:   datetime [8,760]
##   datetime          region max_GWh af50m
##   <dtm>              <chr>    <dbl> <dbl>
## 1 2017-01-01 00:30:00 CA      2.7  0.54
## 2 2017-01-01 00:30:00 CO      9.74 0.244
## 3 2017-01-01 00:30:00 DE       5    1
## 4 2017-01-01 00:30:00 IA     41.6 0.308
## 5 2017-01-01 00:30:00 IL      0.04 0.004
## 6 2017-01-01 00:30:00 KS     24.7 0.0771
## 7 2017-01-01 00:30:00 MA      9.48 0.948
## 8 2017-01-01 00:30:00 MD       3.1  0.62
## 9 2017-01-01 00:30:00 MI     25.1 0.295
## 10 2017-01-01 00:30:00 MN     78.7 0.375
## # ... with 210,230 more rows

sum(wnd_af20$max_GWh)/1e3 # Total estimated onshore potential

## [1] 5288.6

unique(wnd_af20$region) # regions with onshore wind potential

## [1] "CA" "CO" "DE" "IA" "IL" "KS" "MA" "MD" "MI" "MN" "MT" "NC" "ND" "NE" "NJ"
## [16] "NM" "NY" "OH" "OK" "SD" "TX" "VA" "WI" "WY"

wnd_GW_max_reg <- group_by(gwnd[ii,], region, loc_id) %>%
  summarise(max_GWh = WINN_GW_max * sum(af50m),
            af50m = mean(af50m)) %>%
  ungroup() %>% group_by(region) %>%
  summarise(max_GW = WINN_GW_max * n(),
            max_GWh = sum(max_GWh))
sum(wnd_GW_max_reg$max_GWh/1e3); sum(wnd_af20$max_GWh)/1e3 # check

## [1] 5288.6
## [1] 5288.6

```

```

# Offshore wind resource
ii <- (gwnd$loc_id %in% loc_id_20) & gwnd$offshore
summary(ii)

##      Mode      FALSE      TRUE
## logical 24948480 1533000

wndf_af20 <- group_by(gwnd[ii,], datetime, region) %>%
  summarise(max_GWh = sum(max_GWh, na.rm = T),
            af50m = mean(af50m))
wndf_af20

## # A tibble: 166,440 x 4
## # Groups:   datetime [8,760]
##   datetime          region max_GWh af50m
##   <dtm>             <chr>    <dbl> <dbl>
## 1 2017-01-01 00:30:00 CA      76.0  0.460
## 2 2017-01-01 00:30:00 DE       5    1
## 3 2017-01-01 00:30:00 IL     0.265 0.053
## 4 2017-01-01 00:30:00 MA     72.9  0.972
## 5 2017-01-01 00:30:00 MD     10    1
## 6 2017-01-01 00:30:00 ME     47.8  0.956
## 7 2017-01-01 00:30:00 MI     55.6  0.463
## 8 2017-01-01 00:30:00 MN       5    1
## 9 2017-01-01 00:30:00 NC     59.4  0.517
## 10 2017-01-01 00:30:00 NJ     29.1  0.972
## # ... with 166,430 more rows

sum(wndf_af20$max_GWh)/1e3 # Total offshore wind potential

## [1] 2250.915

unique(wndf_af20$region) # regions with offshore wind potential

## [1] "CA" "DE" "IL" "MA" "MD" "ME" "MI" "MN" "NC" "NJ" "NY" "OH" "OR" "RI" "SC"
## [16] "TX" "VA" "WA" "WI"

wndf_GW_max_reg <- group_by(gwnd[ii,], region, loc_id) %>%
  summarise(af50m = mean(af50m),
            max_GWh = sum(af50m)) %>%
  ungroup() %>% group_by(region) %>%
  summarise(max_GW = 5 * n(),
            max_GWh = sum(af50m))
sum(wndf_af20$max_GWh)/1e3; sum(wndf_af20$max_GWh)/1e3 # check

## [1] 2250.915
## [1] 2250.915

```

## Weather classes in the model

Weather classes (in the energyRt package) are used to store/add weather factors to the model data.

code

```

# Solar AF
# dim(dhsol)
# head(dhsol)
ii <- rep(T, dim(dhsol)[1]) # filter if needed

SOLAR_AF <- newWeather("SOLAR_AF",
  description = "Ground level insolation AF",
  # unit = "kWh/kWh_max",
  slice = "HOURLY",
  weather = data.frame(
    region = as.character(dhsol$region[ii]),
    # year = 2018,
    slice = dhsol$slice[ii],
    wval = dhsol$WF[ii]
  ))

head(SOLAR_AF@weather)

##   region year   slice wval
## 1    AL   NA d001_h00    0
## 2    AL   NA d001_h01    0
## 3    AL   NA d001_h02    0
## 4    AL   NA d001_h03    0
## 5    AL   NA d001_h04    0
## 6    AL   NA d001_h05    0

dim(SOLAR_AF@weather)[1] / 49 / 365 / 24 # Check: must be == 1

## [1] 1

# Wind AF (onshore)
wnd_af20$slice <- datetime2tsdh(wnd_af20$datetime)
wnd_af20

## # A tibble: 210,240 x 5
## # Groups:   datetime [8,760]
##   datetime          region max_GWh af50m slice
##   <dtm>          <chr>    <dbl> <dbl> <chr>
## 1 2017-01-01 00:30:00 CA      2.7  0.54 d001_h00
## 2 2017-01-01 00:30:00 CO      9.74 0.244 d001_h00
## 3 2017-01-01 00:30:00 DE       5    1    d001_h00
## 4 2017-01-01 00:30:00 IA     41.6 0.308 d001_h00
## 5 2017-01-01 00:30:00 IL      0.04 0.004 d001_h00
## 6 2017-01-01 00:30:00 KS     24.7 0.0771 d001_h00
## 7 2017-01-01 00:30:00 MA      9.48 0.948 d001_h00
## 8 2017-01-01 00:30:00 MD      3.1  0.62 d001_h00
## 9 2017-01-01 00:30:00 MI     25.1 0.295 d001_h00
## 10 2017-01-01 00:30:00 MN     78.7 0.375 d001_h00
## # ... with 210,230 more rows

dim(wnd_af20)[1] / 365/24 # number of regions with the onshore potential

## [1] 24

ii <- rep(T, dim(wnd_af20)[1]) #
summary(wnd_af20$af50m)

```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.0000 0.0494 0.1493 0.2253 0.3231 1.0000
```

```
# wnd_af20$region <- as.character(wnd_af20$region)
WINON20_AF <- newWeather("WINON20_AF",
  description = "Onshore wind potential af20",
  region = unique(wnd_af20$region[ii]),
  # unit = "kWh/kWh_max",
  slice = "HOURL",
  weather = data.frame(
    region = as.character(wnd_af20$region[ii]),
    # year = 2010,
    slice = wnd_af20$slice[ii],
    wval = wnd_af20$af50m[ii]
  ))
head(WINON20_AF@weather)
```

```
##      region year    slice      wval
## 1      CA   NA d001_h00 0.54000000
## 2      CO   NA d001_h00 0.24350000
## 3      DE   NA d001_h00 1.00000000
## 4      IA   NA d001_h00 0.30848148
## 5      IL   NA d001_h00 0.00400000
## 6      KS   NA d001_h00 0.07714063
```

```
dim(WINON20_AF@weather)[1] / 365 / 24 # Check - number of regions with the data
```

```
## [1] 24
```

```
# Wind AF (offshore)
wndf_af20$slice <- datetime2tsdh(wndf_af20$datetime)
wndf_af20
```

```
## # A tibble: 166,440 x 5
## # Groups:   datetime [8,760]
##      datetime      region max_GWh af50m slice
##      <dtm>      <chr>    <dbl> <dbl> <chr>
## 1 2017-01-01 00:30:00 CA      76.0  0.460 d001_h00
## 2 2017-01-01 00:30:00 DE       5    1    d001_h00
## 3 2017-01-01 00:30:00 IL     0.265 0.053 d001_h00
## 4 2017-01-01 00:30:00 MA     72.9  0.972 d001_h00
## 5 2017-01-01 00:30:00 MD     10    1    d001_h00
## 6 2017-01-01 00:30:00 ME     47.8  0.956 d001_h00
## 7 2017-01-01 00:30:00 MI     55.6  0.463 d001_h00
## 8 2017-01-01 00:30:00 MN      5    1    d001_h00
## 9 2017-01-01 00:30:00 NC     59.4  0.517 d001_h00
## 10 2017-01-01 00:30:00 NJ     29.1  0.972 d001_h00
## # ... with 166,430 more rows
```

```
dim(wndf_af20)[1] / 365/24
```

```
## [1] 19
```

```
ii <- rep(T, dim(wndf_af20)[1]) #
summary(wndf_af20$af50m)
```

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## 0.00000 0.04948 0.18450 0.27774 0.42129 1.00000
```

```
wndf_af20$region <- as.character(wndf_af20$region)
WINOF20_AF <- newWeather("WINOF20_AF",
  description = "Offshore wind potential af20",
  # unit = "kWh/kWh_max",
  region = unique(wndf_af20$region),
  slice = "HOURL",
  weather = data.frame(
    region = as.character(wndf_af20$region[ii]),
    # year = 2010,
    slice = wndf_af20$slice[ii],
    wval = wndf_af20$af50m[ii]
  ))
head(WINOF20_AF@weather)
```

```
##   region year   slice    wval
## 1    CA   NA d001_h00 0.4603636
## 2    DE   NA d001_h00 1.0000000
## 3    IL   NA d001_h00 0.0530000
## 4    MA   NA d001_h00 0.9717333
## 5    MD   NA d001_h00 1.0000000
## 6    ME   NA d001_h00 0.9564000
```

```
dim(WINOF20_AF@weather)[1] / 365 / 24
```

```
## [1] 19
```

## Supply

Declaration of resources (upstream technologies) in the model.  
Here we use only solar and wind energy.

code

```
RES_SOL <- newSupply(
  name = "RES_SOL",
  description = "Terrestrial solar radiation - maximum potential",
  commodity = "SOL",
  unit = "GWh",
  # Weather factors could be used to regulate hourly supply of the resources.
  # Though to reduce the model dimension, it is enough to use
  # weather factors in technologies.
  # weather = data.frame(
  #   weather = c("SOLAR_AF"),
  #   wava.up = c(1)
  # ),
  # availability = list(
  #   # region = dh$region,
  #   # slice = dh$slice365,
  #   ava.up = 1e10 # Max available resource in hour, i.e. no limit by now
  # ),
  slice = "ANNUAL"
)
```



```

RES_WIN <- newSupply(
  name = "RES_WIN",
  description = "Onshore wind - maximum potential",
  commodity = "WIN",
  region = unique(wnd_af20$region),
  unit = "GWh",
  # weather = data.frame(
  #   weather = c("SOLAR_AF"),
  #   wava.up = c(1)
  # ),
  # availability = list(
  #   region = wnd_af20$region,
  #   slice = wnd_af20$slice,
  # # here is an alternative (equivalent) way to use weather factors in supply
  #   ava.up = wnd_af20$max_GWh # Max available resource in hour
  # ),
  slice = "ANNUAL"
)

RES_WFF <- newSupply(
  name = "RES_WFF",
  description = "Offshore wind - maximum potential",
  commodity = "WFF",
  region = unique(wndf_af20$region),
  unit = "GWh",
  # weather = data.frame(
  #   weather = c("SOLAR_AF"),
  #   wava.up = c(1)
  # ),
  # availability = list(
  #   region = wndf_af20$region,
  #   slice = wndf_af20$slice,
  #   ava.up = wndf_af20$max_GWh # Max available resource in hour
  # ),
  slice = "ANNUAL"
)

SUP_BIO <- newSupply(
  name = "SUP_BIO",
  description = "Biomass resource, annual",
  commodity = "BIO",
  unit = "GWh",
  availability = data.frame(
    cost = convert("USD/kWh", "MUSD/GWh", .05) # arbitrary, assuming expensive
  ),
  slice = "ANNUAL"
)

```

## Power generating technologies

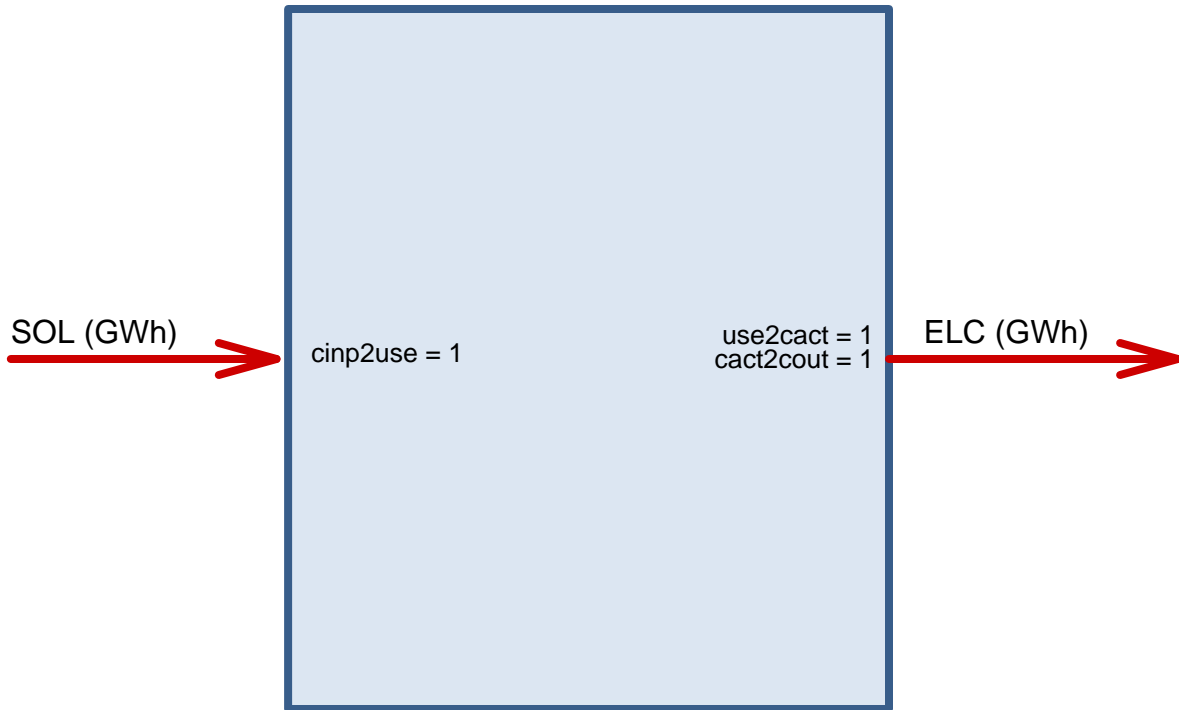
code

```

ESOL <- newTechnology(
  name = "ESOL",
  description = "Utility Scale Solar PV",
  # region = "AZ",
  input = list(
    comm = "SOL",
    unit = "GWh"
  ),
  output = list(
    comm = "ELC",
    unit = "GWh"
  ),
  cap2act = 365*24,
  af = list(
    af.fx = 1 # forcing output when resource is available
  ),
  weather = list(
    weather = c("SOLAR_AF"),
    waf.fx = 1 # weather factor (multiplier) will be applied to af.fx
  ),
  fixom = list(
    fixom = 10 # assumed, 1% of investment costs a year
  ),
  invcost = list(
    # Assuming 1$/Watt
    # https://www.nrel.gov/news/press/2017/nrel-report-utility-scale-solar-pv-system-cost-fell-last-year
    invcost = 1000 # convert("USD/W", "MUSD/GW", 1)
  ),
  start = list(
    start = 2018
  ),
  olife = list(
    olife = 25
  )
)
draw(ESOL)

```

## ESOL Utility Scale Solar PV



```

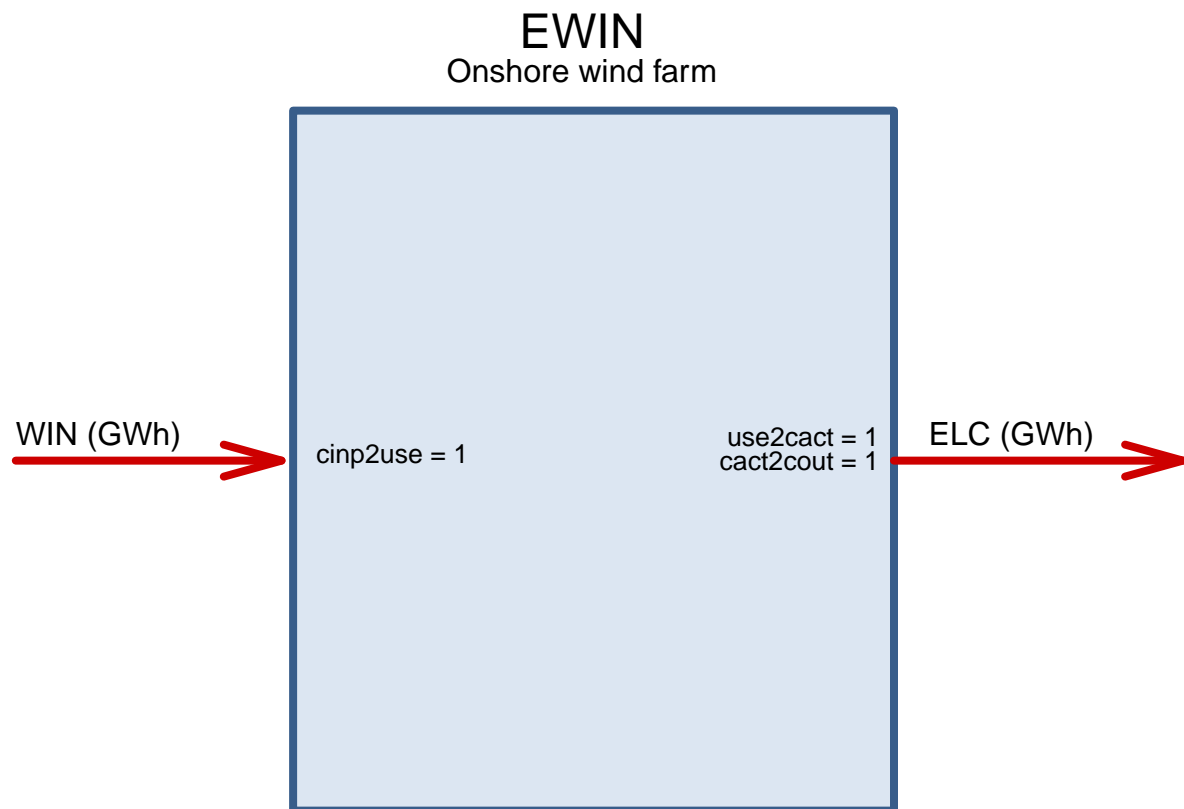
EWIN <- newTechnology(
  name = "EWIN",
  description = "Onshore wind farm",
  WINON20_AF@region, # Limiting to regions with available resource
  input = list(
    comm = "WIN",
    unit = "GWh"
  ),
  output = list(
    comm = "ELC",
    unit = "GWh"
  ),
  cap2act = 365*24,
  af = list(
    af.fx = 1 # forcing output when resource is available
  ),
  weather = list(
    weather = c("WINON20_AF"),
    waf.fx = c(1)
    # waf.up = c(1) #
  ),
  fixom = list(
    fixom = 15 # Assumed, 1% a year
  ),
  invcost = list(
    # Assuming 1.5$/Watt
  )

```

```

# https://www.irena.org/-/media/Files/IRENA/Agency/Publication/2018/Jan/IRENA_2017_Power_Costs_2018
invcost = 1500 #
),
start = list(
  start = 2018
),
olife = list(
  olife = 25
)
)
draw(EWIN)

```



```

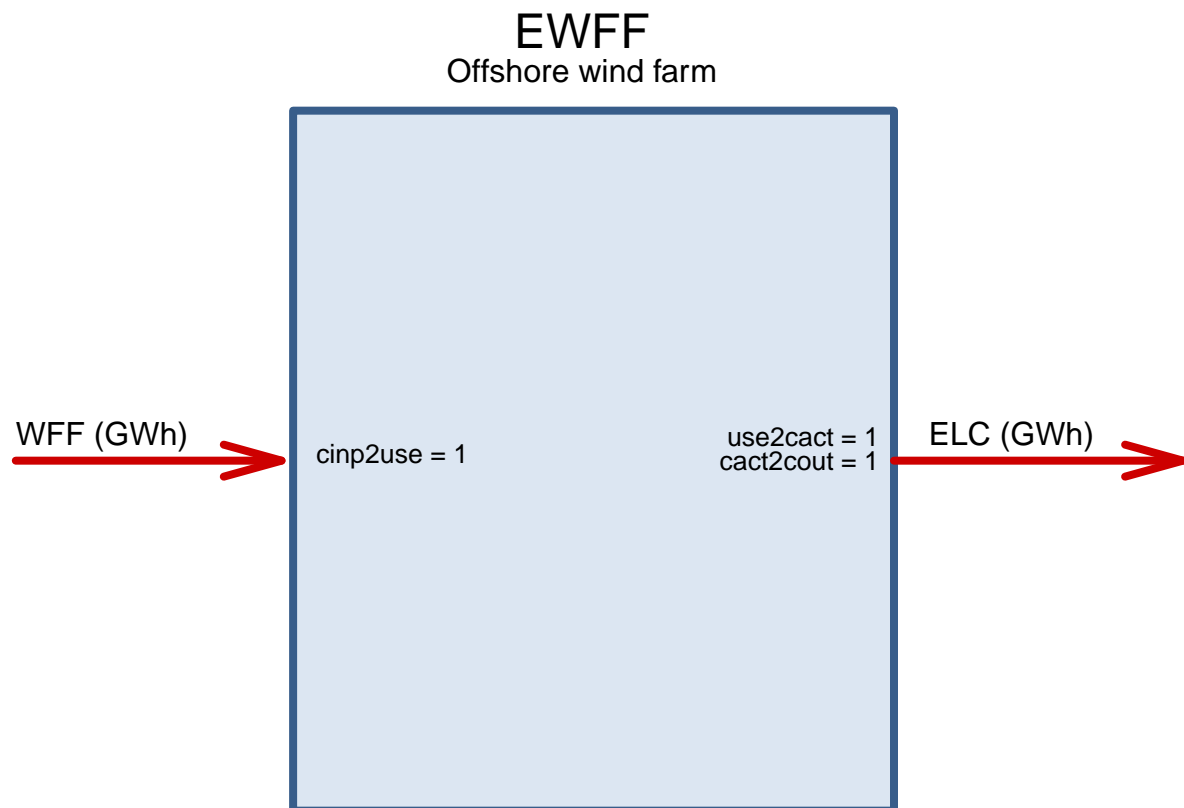
EWFF <- newTechnology(
  name = "EWFF",
  description = "Offshore wind farm",
  region = WINOF20_AF@region, # Limiting to regions with available resource
  input = list(
    comm = "WFF",
    unit = "GWh"
  ),
  output = list(
    comm = "ELC",
    unit = "GWh"
  ),
  cap2act = 365*24,
  af = list(

```

```

    af.fx = 1 # forcing output when resource is available
  ),
  weather = list(
    weather = c("WINOF20_AF"),
    waf.up = c(1) #
  ),
  fixom = list(
    fixom = 45 # Assumed, 1% a year
  ),
  invcost = list(
    # Assuming 3-4.5$/Watt
    # https://www.irena.org/-/media/Files/IRENA/Agency/Publication/2018/Jan/IRENA_2017_Power_Costs_2018
    # https://www.energy.gov/sites/prod/files/2019/08/f65/2018%20Offshore%20Wind%20Market%20Report.pdf
    invcost = 3500 # convert("USD/W", "MUSD/GW", 1)
  ),
  start = list(
    start = 2018
  ),
  olife = list(
    olife = 25
  )
)
draw(EWFF)

```



```

CSOL_UP <- newConstraints(
  name = "CSOL_UP",

```

```

eq = "<=",
type = "capacity",
for.each = data.frame(
  year = USENSYS$modelYear,
  tech = "ESOL",
  region = as.character(PV_GW_max_reg$region)),
rhs = data.frame(
  # year = USENSYS$modelYear,
  # tech = "ESOL",
  region = as.character(PV_GW_max_reg$region),
  rhs = PV_GW_max_reg$GW_up
)) # limit on solar capacity (resource)

CWIN_UP <- newConstraintS(
  name = "CWIN_UP",
  eq = "<=",
  type = "capacity",
  for.each = data.frame(
    year = USENSYS$modelYear,
    tech = "EWIN",
    region = wnd_GW_max_reg$region),
  rhs = data.frame(
    region = wnd_GW_max_reg$region,
    rhs = wnd_GW_max_reg$max_GW)) # limit on onshore wind capacity (resource)

CWFF_UP <- newConstraintS(
  name = "CWFF_UP",
  eq = "<=",
  type = "capacity",
  for.each = list(
    year = USENSYS$modelYear,
    tech = "EWFF",
    region = wndf_GW_max_reg$region),
  rhs = data.frame(
    region = wndf_GW_max_reg$region,
    rhs = wndf_GW_max_reg$max_GW)) # limit on onshore wind capacity (resource)

```

## Thermal backup

Generic thermal technology as a back-up capacity to cover gaps between renewables generation and consumption, for example, biomass-, biogas-to-power or conventional natural gas turbines. The idea of adding the technology to the optimization, is to identify potential substitution between storage, grid, and back-up capacity. To avoid use of the technology for base load generation, we assume high costs and upper bounds on the availability factor.

code

```

BIO <- newCommodity('BIO', slice = "ANNUAL")

EBIO <- newTechnology(
  name = "EBIO",
  description = "Thermal backup",
  input = list(

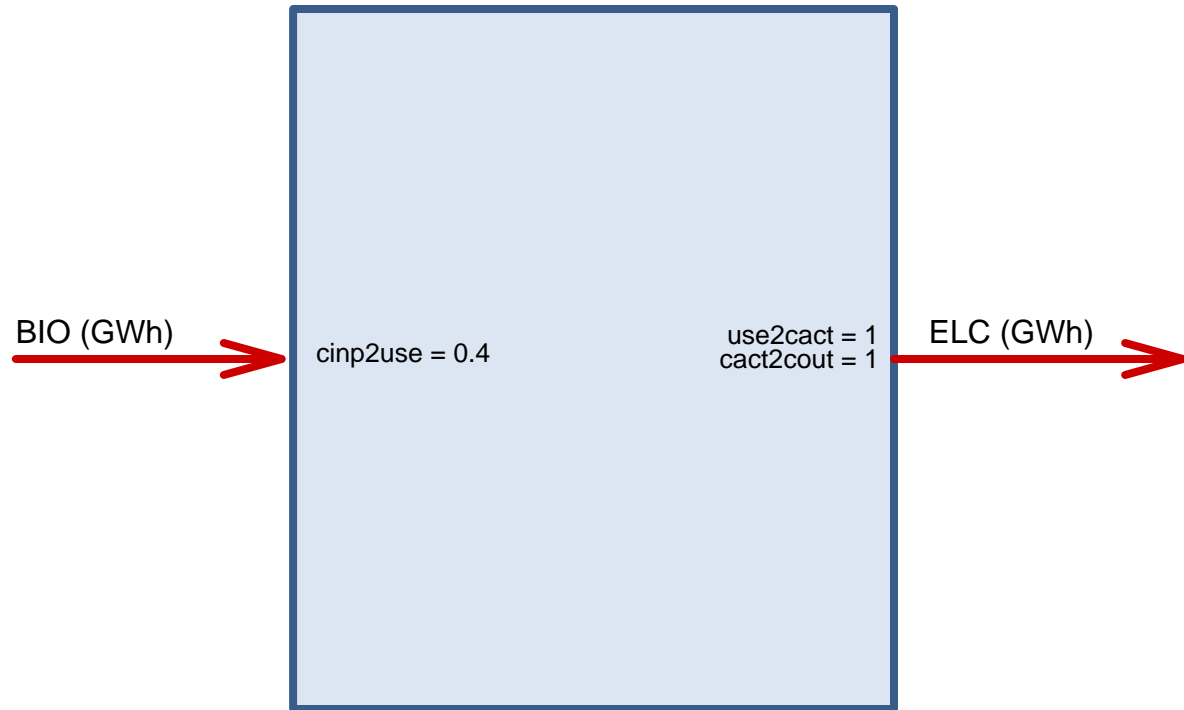
```

```

    comm = "BIO",
    unit = "GWh"
),
output = list(
    comm = "ELC",
    unit = "GWh"
),
cap2act = 365*24,
afs = list(
    slice = "ANNUAL",
    # afs.up = .1 # up tp 10% capacity usitilization through the year
    afs.up = .4 # up to 40% capacity usitilization through the year
),
ceff = list(
    comm = "BIO",
    cinp2use = .4
),
invcost = list(
    invcost = 2400 #
),
# fixom = list(
#   fixom = 20 # Assumed, 2% a year
# ),
# see the fuel cost
# varom = list(
#   varom = convert("cents/kWh", "MUSD/GWh", 5) # assuming expensive operation
# ),
olife = list(
    olife = 20
),
slice = "HOURL"
)
draw(EBIO)

```

## EBIO Thermal backup



```
# (1200/20 + 20/20 + 0.1*365*24*.05/.4) / (365*24*.1)
```

## Storage technologies

code

```
# STGBTR Hourly ####
# See IRENA 2030 (from 77 to 574, p.77)
# NREL, 4-hours battery storage, grid-connected
STGBTR <- newStorage(
  name = 'STGBTR',
  commodity = 'ELC',
  description = "Generic grid-integrated storage, 1 hour plus",
  cap2stg = 1, # in kWh or 1-hour storage
  olife = list(olife = 20),
  invcost = list(
    invcost = convert("USD/kWh", "MUSD/GWh", 300)
  ),
  seff = data.frame(
    inpeff = 0.8, # assumed efficiency of charging
    stgeff = 0.9 # assumed efficiency of storing energy (annual)
    # outeff = 1 # discharge efficiency
  )
)
```



```

# STGBTR1 <- newStorage(
#   name = 'STGBTR',
#   commodity = 'ELC',
#   description = "Generic grid-integrated intraday storage (battery)",
#   cap2stg = 4, # 4-hours battery
#   olife = list(olife = 20),
#   invcost = list(
#     # See IRENA 2030 (from 77 to 574, p.77)
#     # invcost = convert("USD/kWh", "MUSD/GWh", 200)
#     invcost = convert("USD/kW", "MUSD/GW", 300 * 4) # 1200 USD/kW for 4-hours battery
#   ),
#   seff = data.frame(
#     inpeff = 0.8, # assumed efficiency of charging
#     stgeff = 0.9, # assumed efficiency of storing energy (annual)
#     cinp.up = 24*365 / 4, # 4-hours charging
#     cout.up = 24*365 / 4 # 4-hours storage (discharging, i.e. GW capacity)
#     # outeff = 1 # discharge efficiency
#   )
# )
#
#
# # STGP2P Daily - within 365 days ####
STGP2P <- newStorage(
  name = 'STGP2P',
  commodity = 'ELC',
  description = "Power-to-power type of technology",
  cap2stg = 100, # if in PJ, convert("GWh", "PJ"),
  olife = list(
    olife = 25),
  invcost = 100, # USD/kWh, assumption
  seff = data.frame(
    inpeff = 0.8, # power to H2 efficiency
    cinp.up = 24*365, # speed of P2X conversion for 1GW of storage
    cout.up = 24*365, # speed of X2P conversion for 1GW of storage
    outeff = 0.625 # H2 to power efficiency
    # # stgeff = .9
    # # cinp.up = 24*365,
    # # cout.up = 24*365
  ),
  varom = list(
    # Assuming high operational costs, adding ~ 5 cents/kWh
    inpcost = convert("USD/kWh", "MUSD/GWh", .05)
  )
)

```

## Interregional UHV electrical grid

code

```

# Propose trade matrix between regions
{
  if (F) {

```

```

# Load trade matrix from your file
trd_xl <- readxl::read_excel("data/trade_matrix01.xlsx",
                             range = "A1:AX50")

trd_nbr <- as.matrix(trd_xl[,-1])
trd_nbr[lower.tri(trd_nbr)] <- NA
rownames(trd_nbr) <- trd_xl$region
} else {
  # Or create trade matrix for all neighbour regions
  trd_nbr <- matrix(rep(NA, nreg_in_gis*nreg_in_gis),
                    nrow = nreg_in_gis,
                    dimnames = list(reg_names_in_gis, reg_names_in_gis))

  head(trd_nbr)

  for (i in 1:length(reg_names)) {
    trd_nbr[i, nbr[[i]]] <- 1
    trd_nbr[nbr[[i]], i] <- 1
  }
  dim(trd_nbr)
  summary(!is.na(c(trd_nbr)))
  ii <- reg_names_in_gis %in% reg_names
  trd_nbr <- trd_nbr[ii, ii]
  dim(trd_nbr)
  # For bidirectional trade, keep only one direction
  trd_nbr[lower.tri(trd_nbr)] <- NA
  summary(!is.na(c(trd_nbr)))
}
head(trd_nbr)
# write.csv(trd_nbr, file = "data/trade_matrix.csv")
trd_nbr[trd_nbr == 0] <- NA

# Convert the matrix to data.frame (table) format
trd_dt <- as.data.frame.table(trd_nbr, stringsAsFactors = F)
trd_dt <- trd_dt[!is.na(trd_dt$Freq),]
head(trd_dt)
dim(trd_dt)
trd_dt <- dplyr::distinct(trd_dt)
dim(trd_dt)
names(trd_dt) <- c("src", "dst", "trade")
trd_dt$trade <- with(trd_dt, paste0("TRBD_UHV_", src, "_", dst))
head(trd_dt)

# Map region flows
trd_map <- left_join(trd_dt, reg_centers[,1:3], by = c("src" = "region"))
trd_map <- left_join(trd_map, reg_centers[,1:3], by = c("dst" = "region"))
trd_map <- trd_map %>%
  rename(xsrc = x.x, ysrc = y.x,
         xdst = x.y, ydst = y.y)
trd_map <- as_tibble(trd_map)

# Filter excessive connections
dim(trd_dt); dim(trd_map)
drop_route <- function(reg1, reg2) {

```

```

(trd_dt$src == reg1 & trd_dt$dst == reg2) | (trd_dt$src == reg2 & trd_dt$dst == reg1)
}
# trd_dt[ii & grepl("TJ", trd_dt$trade),]
ii <- rep(TRUE, length(trd_dt$src))
ii <- ii & !drop_route("AL", "FL")
ii <- ii & !drop_route("GA", "NC")
ii <- ii & !drop_route("CT", "RI")
ii <- ii & !drop_route("VT", "MA")
ii <- ii & !drop_route("NY", "MA")
ii <- ii & !drop_route("PA", "DE")
ii <- ii & !drop_route("UT", "NM")
ii <- ii & !drop_route("VA", "DC")
ii <- ii & !drop_route("AL", "TN")
if (F) {
  # Drop unused routes (scen_REN5)
  # names(TRBD_UHV_NEI@data)[!(names(TRBD_UHV_NEI@data) %in% vTradeCap$trade[!is.na(vTradeCap$GW)])]
  # [1] "TRBD_UHV_SD_MN" "TRBD_UHV_WI_IA" "TRBD_UHV_NY_NJ"
  # [4] "TRBD_UHV_OR_NV" "TRBD_UHV_ID_UT" "TRBD_UHV_WV_MD"
  # [7] "TRBD_UHV_KY_VA" "TRBD_UHV_NE_MO" "TRBD_UHV_CO_AZ"
  # [10] "TRBD_UHV_OK_NM" "TRBD_UHV_TX_AR"
  ii <- ii & !drop_route("SD", "MN")
  ii <- ii & !drop_route("WI", "IA")
  ii <- ii & !drop_route("NY", "NJ")
  ii <- ii & !drop_route("OR", "NV")
  ii <- ii & !drop_route("ID", "UT")
  ii <- ii & !drop_route("WV", "MD")
  ii <- ii & !drop_route("KY", "VA")
  # ii <- ii & !drop_route("NE", "MO")
  ii <- ii & !drop_route("CO", "AZ")
  ii <- ii & !drop_route("OK", "NM")
  ii <- ii & !drop_route("TX", "AR")
  # Drop more (after optimization check)
  ii <- ii & !drop_route("VA", "TN")
  # ii <- ii & !drop_route("MO", "TN")
  ii <- ii & !drop_route("NC", "TN")
  ii <- ii & !drop_route("KY", "MO")
  ii <- ii & !drop_route("KY", "WV")
  ii <- ii & !drop_route("NV", "AZ")
}
length(trd_dt$src[ii])

library(ggplot2)
trd_flows_map <-
ggplot(data = usa49r) +
  geom_polygon(aes(x = long, y = lat, group = group), fill = "wheat",
    colour = "white", alpha = 1, size = .5) + # aes fill = id,
  coord_fixed(1.3) +
  guides(fill=FALSE) + # do this to leave off the color legend
  theme_void() + labs(title = "Interregional electricity trade routes (long distance grid), open for in
  theme(plot.title = element_text(hjust = 0.5),
    plot.subtitle = element_text(hjust = 0.5)) +
  geom_segment(aes(x=xsrc, y=ysrc, xend=xdst, yend=ydst),
    data = trd_map[ii,], inherit.aes = FALSE, size = 3,

```

```

      alpha = 1, colour = "grey", lineend = "round", show.legend = T) +
    geom_point(data = reg_centers, aes(x, y), colour = "white") +
    geom_segment(aes(x=xsrc, y=ysrc, xend=xdst, yend=ydst),
      data = trd_map[ii,], inherit.aes = FALSE, size = .1,
      # arrow = arrow(type = "closed", angle = 15,
      #               length = unit(0.15, "inches")),
      colour = "white", alpha = 1,
      lineend = "butt", linejoin = "mitre", show.legend = T) + # , name = "Trade, PJ"
    geom_text_repel(aes(x, y, label = region), data = reg_centers)
trd_flows_map
trd_map <- trd_map[ii,]; rownames(trd_map) <- NULL
trd_dt <- trd_dt[ii,]; rownames(trd_dt) <- NULL
# ggsave("fig/trd_flows_map.pdf", trd_flows_map, device = "pdf")
}

# Calculate distance between regions centers:
labpt <- getCenters(usa49reg)
# rownames(labpt) <- labpt[, "region"]

# Estimate grid length, losses, costs
trd_dt$distance_km <- 0.
for (i in 1:dim(trd_dt)[1]) {
  rg_dst <- trd_dt$dst[i]
  rg_src <- trd_dt$src[i]
  ii <- labpt$region == rg_dst
  lab_dst <- c(labpt$x[ii], labpt$y[ii])
  ii <- labpt$region == rg_src
  lab_src <- c(labpt$x[ii], labpt$y[ii])
  trd_dt$distance_km[i] <- raster::pointDistance(
    lab_src, lab_dst, T)/1e3
}

# Assume 15% longer distance due to a landscape
trd_dt$distance_km <- 1.15 * trd_dt$distance_km
# Assume losses 2% per 1000 km
# trd_dt$losses <- round(trd_dt$distance_km / 1e3 * 0.02, 4)
# Assume losses 1% per 1000 km (UHVDC)
trd_dt$losses <- round(trd_dt$distance_km / 1e3 * 0.01, 4)
trd_dt$teff <- 1 - trd_dt$losses
# The assumption is based on ABB's 4000-8000 MUSD per 12GW UHVDC, 2000km, 1-5% system losses
# i.e. ~$160-333 MUSD/1000km per 1GW of the total system
# assuming ~$200 MUSD/1000km per 1GW of power line,
# and $50 MUSD/GW for 1GW converter stations on each end
trd_dt$invcost <- round(trd_dt$distance_km / 1e3 * 200) # MUSD/GW of 1000km UHVDC
trd_dt$invcost <- round(trd_dt$invcost * 1.5) # Adding land costs (50%, an assumption)
trd_dt <- as_tibble(trd_dt)

# Define trade object for every route,
# store in a repository object
TRBD_UHV_NEI <- newRepository(name = "TRBD_UHV_NEI")
for (i in 1:dim(trd_dt)[1]) {
  src <- trd_dt$src[i]
  dst <- trd_dt$dst[i]
  trd_nm <- paste0("TRBD_UHV_", src, "_", dst) # Trade object name

```

```

cmd_nm <- "UHV"
# Trade class for every route
trd <- newTrade(trd_nm,
  commodity = cmd_nm,
  # source = c(src, dst),
  # destination = c(src, dst),
  routes = list(
    src = c(src, dst),
    dst = c(dst, src)
  ),
  trade = data.frame(
    src = c(src, dst),
    dst = c(dst, src),
    # Maximum capacity per route in GW
    # ava.up = convert("GWh", "GWh", 60), (!!! bug)
    teff = trd_dt$teff[i] # trade losses
    # cost = trd_dt$cost[i] # trade costs
    # markup = trd_dt$cost[i] # and/or markup
  ),
  #!!! New stuff - testing
  capacityVariable = TRUE, # The trade route has capacity (not just flow) and can be en
  # bidirectional = TRUE, #
  invcost = data.frame(
    # src = src,
    # dst = dst,
    # year = 2010,
    region = c(dst, src),
    # invcost = trd_dt$distance_km[i] / 1e3 * 250 / 2 #
    invcost = trd_dt$invcost[i] / 2
  ),
  # olife = data.frame(
  olife = 80,
  # ),
  cap2act = convert("GWh", "GWh", 24*365)
)

TRBD_UHV_NEI <- add(TRBD_UHV_NEI, trd)
}
rm(trd)
length(TRBD_UHV_NEI@data)

```

```
## [1] 100
```

```
names(TRBD_UHV_NEI@data)
```

```

## [1] "TRBD_UHV_MT_ND" "TRBD_UHV_MT_SD" "TRBD_UHV_ND_SD" "TRBD_UHV_MT_WY"
## [5] "TRBD_UHV_SD_WY" "TRBD_UHV_WA_ID" "TRBD_UHV_MT_ID" "TRBD_UHV_WY_ID"
## [9] "TRBD_UHV_ND_MN" "TRBD_UHV_SD_MN" "TRBD_UHV_WI_MN" "TRBD_UHV_WA_OR"
## [13] "TRBD_UHV_ID_OR" "TRBD_UHV_ME_NH" "TRBD_UHV_VT_NH" "TRBD_UHV_SD_IA"
## [17] "TRBD_UHV_WI_IA" "TRBD_UHV_MN_IA" "TRBD_UHV_NH_MA" "TRBD_UHV_SD_NE"
## [21] "TRBD_UHV_WY_NE" "TRBD_UHV_IA_NE" "TRBD_UHV_VT_NY" "TRBD_UHV_NY_PA"
## [25] "TRBD_UHV_MA_CT" "TRBD_UHV_NY_CT" "TRBD_UHV_MA_RI" "TRBD_UHV_NY_NJ"
## [29] "TRBD_UHV_PA_NJ" "TRBD_UHV_ID_NV" "TRBD_UHV_OR_NV" "TRBD_UHV_WY_UT"
## [33] "TRBD_UHV_ID_UT" "TRBD_UHV_NV_UT" "TRBD_UHV_OR_CA" "TRBD_UHV_NV_CA"

```

```
## [37] "TRBD_UHV_PA_OH" "TRBD_UHV_IN_OH" "TRBD_UHV_WI_IL" "TRBD_UHV_IA_IL"
## [41] "TRBD_UHV_IN_IL" "TRBD_UHV_NJ_DE" "TRBD_UHV_PA_WV" "TRBD_UHV_OH_WV"
## [45] "TRBD_UHV_PA_MD" "TRBD_UHV_DC_MD" "TRBD_UHV_DE_MD" "TRBD_UHV_WV_MD"
## [49] "TRBD_UHV_WY_CO" "TRBD_UHV_NE_CO" "TRBD_UHV_UT_CO" "TRBD_UHV_IN_KY"
## [53] "TRBD_UHV_OH_KY" "TRBD_UHV_IL_KY" "TRBD_UHV_WV_KY" "TRBD_UHV_NE_KS"
## [57] "TRBD_UHV_CO_KS" "TRBD_UHV_WV_VA" "TRBD_UHV_MD_VA" "TRBD_UHV_KY_VA"
## [61] "TRBD_UHV_IA_MO" "TRBD_UHV_NE_MO" "TRBD_UHV_IL_MO" "TRBD_UHV_KY_MO"
## [65] "TRBD_UHV_KS_MO" "TRBD_UHV_NV_AZ" "TRBD_UHV_UT_AZ" "TRBD_UHV_CA_AZ"
## [69] "TRBD_UHV_CO_AZ" "TRBD_UHV_CO_OK" "TRBD_UHV_KS_OK" "TRBD_UHV_MO_OK"
## [73] "TRBD_UHV_VA_NC" "TRBD_UHV_KY_TN" "TRBD_UHV_VA_TN" "TRBD_UHV_MO_TN"
## [77] "TRBD_UHV_NC_TN" "TRBD_UHV_OK_TX" "TRBD_UHV_CO_NM" "TRBD_UHV_AZ_NM"
## [81] "TRBD_UHV_OK_NM" "TRBD_UHV_TX_NM" "TRBD_UHV_TN_MS" "TRBD_UHV_AL_MS"
## [85] "TRBD_UHV_TN_GA" "TRBD_UHV_AL_GA" "TRBD_UHV_NC_SC" "TRBD_UHV_GA_SC"
## [89] "TRBD_UHV_MO_AR" "TRBD_UHV_OK_AR" "TRBD_UHV_TN_AR" "TRBD_UHV_TX_AR"
## [93] "TRBD_UHV_MS_AR" "TRBD_UHV_TX_LA" "TRBD_UHV_MS_LA" "TRBD_UHV_AR_LA"
## [97] "TRBD_UHV_GA_FL" "TRBD_UHV_WI_MI" "TRBD_UHV_IN_MI" "TRBD_UHV_OH_MI"
```

```
TRBD_UHV_NEI@data[[1]]@invcost
```

```
##   region year invcost
## 1     ND   NA     120
## 2     MT   NA     120
```

```
mobj <- c(mobj, "trd_dt", "trd_map")
```

## Exogenous trade routes

code

```
TRFX_UHV_NEI <- newRepository("TRFX_UHV_NEI")
# emptrd <- newTrade("EmptyClassTrade")
for (i in 1:length(TRBD_UHV_NEI@data)) {
  route <- TRBD_UHV_NEI@data[[i]]
  # route@capacityVariable <- FALSE
  # route@invcost <- emptrd@invcost
  # route@olife <- emptrd@olife
  # route@cap2act <- emptrd@cap2act
  # route@trade$ava.up <- 60 # Assumption
  route@stock <- data.frame(year = 2018, stock = 60) # Assumption
  route@start <- 2100
  route@name <- sub("^TRBD", "TRFX", route@name)
  TRFX_UHV_NEI <- add(TRFX_UHV_NEI, route)
}
```

```
names(TRFX_UHV_NEI@data)
```

```
## [1] "TRFX_UHV_MT_ND" "TRFX_UHV_MT_SD" "TRFX_UHV_ND_SD" "TRFX_UHV_MT_WY"
## [5] "TRFX_UHV_SD_WY" "TRFX_UHV_WA_ID" "TRFX_UHV_MT_ID" "TRFX_UHV_WY_ID"
## [9] "TRFX_UHV_ND_MN" "TRFX_UHV_SD_MN" "TRFX_UHV_WI_MN" "TRFX_UHV_WA_OR"
## [13] "TRFX_UHV_ID_OR" "TRFX_UHV_ME_NH" "TRFX_UHV_VT_NH" "TRFX_UHV_SD_IA"
## [17] "TRFX_UHV_WI_IA" "TRFX_UHV_MN_IA" "TRFX_UHV_NH_MA" "TRFX_UHV_SD_NE"
## [21] "TRFX_UHV_WY_NE" "TRFX_UHV_IA_NE" "TRFX_UHV_VT_NY" "TRFX_UHV_NY_PA"
## [25] "TRFX_UHV_MA_CT" "TRFX_UHV_NY_CT" "TRFX_UHV_MA_RI" "TRFX_UHV_NY_NJ"
## [29] "TRFX_UHV_PA_NJ" "TRFX_UHV_ID_NV" "TRFX_UHV_OR_NV" "TRFX_UHV_WY_UT"
```

```
## [33] "TRFX_UHV_ID_UT" "TRFX_UHV_NV_UT" "TRFX_UHV_OR_CA" "TRFX_UHV_NV_CA"
## [37] "TRFX_UHV_PA_OH" "TRFX_UHV_IN_OH" "TRFX_UHV_WI_IL" "TRFX_UHV_IA_IL"
## [41] "TRFX_UHV_IN_IL" "TRFX_UHV_NJ_DE" "TRFX_UHV_PA_WV" "TRFX_UHV_OH_WV"
## [45] "TRFX_UHV_PA_MD" "TRFX_UHV_DC_MD" "TRFX_UHV_DE_MD" "TRFX_UHV_WV_MD"
## [49] "TRFX_UHV_WY_CO" "TRFX_UHV_NE_CO" "TRFX_UHV_UT_CO" "TRFX_UHV_IN_KY"
## [53] "TRFX_UHV_OH_KY" "TRFX_UHV_IL_KY" "TRFX_UHV_WV_KY" "TRFX_UHV_NE_KS"
## [57] "TRFX_UHV_CO_KS" "TRFX_UHV_WV_VA" "TRFX_UHV_MD_VA" "TRFX_UHV_KY_VA"
## [61] "TRFX_UHV_IA_MO" "TRFX_UHV_NE_MO" "TRFX_UHV_IL_MO" "TRFX_UHV_KY_MO"
## [65] "TRFX_UHV_KS_MO" "TRFX_UHV_NV_AZ" "TRFX_UHV_UT_AZ" "TRFX_UHV_CA_AZ"
## [69] "TRFX_UHV_CO_AZ" "TRFX_UHV_CO_OK" "TRFX_UHV_KS_OK" "TRFX_UHV_MO_OK"
## [73] "TRFX_UHV_VA_NC" "TRFX_UHV_KY_TN" "TRFX_UHV_VA_TN" "TRFX_UHV_MO_TN"
## [77] "TRFX_UHV_NC_TN" "TRFX_UHV_OK_TX" "TRFX_UHV_CO_NM" "TRFX_UHV_AZ_NM"
## [81] "TRFX_UHV_OK_NM" "TRFX_UHV_TX_NM" "TRFX_UHV_TN_MS" "TRFX_UHV_AL_MS"
## [85] "TRFX_UHV_TN_GA" "TRFX_UHV_AL_GA" "TRFX_UHV_NC_SC" "TRFX_UHV_GA_SC"
## [89] "TRFX_UHV_MO_AR" "TRFX_UHV_OK_AR" "TRFX_UHV_TN_AR" "TRFX_UHV_TX_AR"
## [93] "TRFX_UHV_MS_AR" "TRFX_UHV_TX_LA" "TRFX_UHV_MS_LA" "TRFX_UHV_AR_LA"
## [97] "TRFX_UHV_GA_FL" "TRFX_UHV_WI_MI" "TRFX_UHV_IN_MI" "TRFX_UHV_OH_MI"
```

```
TRFX_UHV_NEI@data[[1]]
```

```
## An object of class "trade"
## Slot "name":
## [1] "TRFX_UHV_MT_ND"
##
## Slot "description":
## [1] ""
##
## Slot "commodity":
## [1] "UHV"
##
## Slot "routes":
##   src dst
## 1  MT  ND
## 2  ND  MT
##
## Slot "trade":
##   src dst year slice ava.up ava.fx ava.lo cost markup teff
## 1  MT  ND   NA  <NA>    NA     NA     NA   NA     NA 0.992
## 2  ND  MT   NA  <NA>    NA     NA     NA   NA     NA 0.992
##
## Slot "aux":
## [1] acomm unit
## <0 rows> (or 0-length row.names)
##
## Slot "aeff":
## [1] acomm      src      dst      year      slice      csrc2aout csrc2ainp
## [8] cdst2aout cdst2ainp
## <0 rows> (or 0-length row.names)
##
## Slot "invcost":
##   region year invcost
## 1     ND   NA     120
## 2     MT   NA     120
##
## Slot "olife":
```

```

## [1] 80
##
## Slot "start":
## [1] 2100
##
## Slot "end":
## [1] Inf
##
## Slot "stock":
##   year stock
## 1 2018    60
##
## Slot "capacityVariable":
## [1] TRUE
##
## Slot "GIS":
## NULL
##
## Slot "cap2act":
## [1] 8760
##
## Slot "misc":
## list()
##
## Slot ".S3Class":
## [1] "trade"

# Dropping converter stations
TRFX_ELC_NEI <- newRepository("TRFX_ELC_NEI")
# emptrd <- newTrade("EmptyClassTrade")
for (i in 1:length(TRFX_UHV_NEI@data)) {
  route <- TRFX_UHV_NEI@data[[i]]
  route@commodity <- "ELC"
  # route@trade$ava.up <- 60 # Assumption
  route@name <- sub("_UHV_", "_ELC_", route@name)
  TRFX_ELC_NEI <- add(TRFX_ELC_NEI, route)
}

names(TRFX_ELC_NEI@data)

## [1] "TRFX_ELC_MT_ND" "TRFX_ELC_MT_SD" "TRFX_ELC_ND_SD" "TRFX_ELC_MT_WY"
## [5] "TRFX_ELC_SD_WY" "TRFX_ELC_WA_ID" "TRFX_ELC_MT_ID" "TRFX_ELC_WY_ID"
## [9] "TRFX_ELC_ND_MN" "TRFX_ELC_SD_MN" "TRFX_ELC_WI_MN" "TRFX_ELC_WA_OR"
## [13] "TRFX_ELC_ID_OR" "TRFX_ELC_ME_NH" "TRFX_ELC_VT_NH" "TRFX_ELC_SD_IA"
## [17] "TRFX_ELC_WI_IA" "TRFX_ELC_MN_IA" "TRFX_ELC_NH_MA" "TRFX_ELC_SD_NE"
## [21] "TRFX_ELC_WY_NE" "TRFX_ELC_IA_NE" "TRFX_ELC_VT_NY" "TRFX_ELC_NY_PA"
## [25] "TRFX_ELC_MA_CT" "TRFX_ELC_NY_CT" "TRFX_ELC_MA_RI" "TRFX_ELC_NY_NJ"
## [29] "TRFX_ELC_PA_NJ" "TRFX_ELC_ID_NV" "TRFX_ELC_OR_NV" "TRFX_ELC_WY_UT"
## [33] "TRFX_ELC_ID_UT" "TRFX_ELC_NV_UT" "TRFX_ELC_OR_CA" "TRFX_ELC_NV_CA"
## [37] "TRFX_ELC_PA_OH" "TRFX_ELC_IN_OH" "TRFX_ELC_WI_IL" "TRFX_ELC_IA_IL"
## [41] "TRFX_ELC_IN_IL" "TRFX_ELC_NJ_DE" "TRFX_ELC_PA_WV" "TRFX_ELC_OH_WV"
## [45] "TRFX_ELC_PA_MD" "TRFX_ELC_DC_MD" "TRFX_ELC_DE_MD" "TRFX_ELC_WV_MD"
## [49] "TRFX_ELC_WY_CO" "TRFX_ELC_NE_CO" "TRFX_ELC_UT_CO" "TRFX_ELC_IN_KY"
## [53] "TRFX_ELC_OH_KY" "TRFX_ELC_IL_KY" "TRFX_ELC_WV_KY" "TRFX_ELC_NE_KS"
## [57] "TRFX_ELC_CO_KS" "TRFX_ELC_WV_VA" "TRFX_ELC_MD_VA" "TRFX_ELC_KY_VA"

```



```
## [61] "TRFX_ELC_IA_MO" "TRFX_ELC_NE_MO" "TRFX_ELC_IL_MO" "TRFX_ELC_KY_MO"
## [65] "TRFX_ELC_KS_MO" "TRFX_ELC_NV_AZ" "TRFX_ELC_UT_AZ" "TRFX_ELC_CA_AZ"
## [69] "TRFX_ELC_CO_AZ" "TRFX_ELC_CO_OK" "TRFX_ELC_KS_OK" "TRFX_ELC_MO_OK"
## [73] "TRFX_ELC_VA_NC" "TRFX_ELC_KY_TN" "TRFX_ELC_VA_TN" "TRFX_ELC_MO_TN"
## [77] "TRFX_ELC_NC_TN" "TRFX_ELC_OK_TX" "TRFX_ELC_CO_NM" "TRFX_ELC_AZ_NM"
## [81] "TRFX_ELC_OK_NM" "TRFX_ELC_TX_NM" "TRFX_ELC_TN_MS" "TRFX_ELC_AL_MS"
## [85] "TRFX_ELC_TN_GA" "TRFX_ELC_AL_GA" "TRFX_ELC_NC_SC" "TRFX_ELC_GA_SC"
## [89] "TRFX_ELC_MO_AR" "TRFX_ELC_OK_AR" "TRFX_ELC_TN_AR" "TRFX_ELC_TX_AR"
## [93] "TRFX_ELC_MS_AR" "TRFX_ELC_TX_LA" "TRFX_ELC_MS_LA" "TRFX_ELC_AR_LA"
## [97] "TRFX_ELC_GA_FL" "TRFX_ELC_WI_MI" "TRFX_ELC_IN_MI" "TRFX_ELC_OH_MI"
```

```
TRFX_ELC_NEI@data[[1]]
```

```
## An object of class "trade"
## Slot "name":
## [1] "TRFX_ELC_MT_ND"
##
## Slot "description":
## [1] ""
##
## Slot "commodity":
## [1] "ELC"
##
## Slot "routes":
##   src dst
## 1  MT  ND
## 2  ND  MT
##
## Slot "trade":
##   src dst year slice ava.up ava.fx ava.lo cost markup teff
## 1  MT  ND   NA <NA>    NA     NA     NA   NA     NA 0.992
## 2  ND  MT   NA <NA>    NA     NA     NA   NA     NA 0.992
##
## Slot "aux":
## [1] acomm unit
## <0 rows> (or 0-length row.names)
##
## Slot "aeff":
## [1] acomm      src      dst      year      slice      csrc2aout csrc2ainp
## [8] cdst2aout cdst2ainp
## <0 rows> (or 0-length row.names)
##
## Slot "invcost":
##   region year invcost
## 1     ND   NA     120
## 2     MT   NA     120
##
## Slot "olife":
## [1] 80
##
## Slot "start":
## [1] 2100
##
## Slot "end":
## [1] Inf
```

```
##
## Slot "stock":
##   year stock
## 1 2018     60
##
## Slot "capacityVariable":
## [1] TRUE
##
## Slot "GIS":
## NULL
##
## Slot "cap2act":
## [1] 8760
##
## Slot "misc":
## list()
##
## Slot ".S3Class":
## [1] "trade"
TRFX_ELC_NEI@data[[1]]@olife
## [1] 80
```

## Inverter and rectifier stations

code

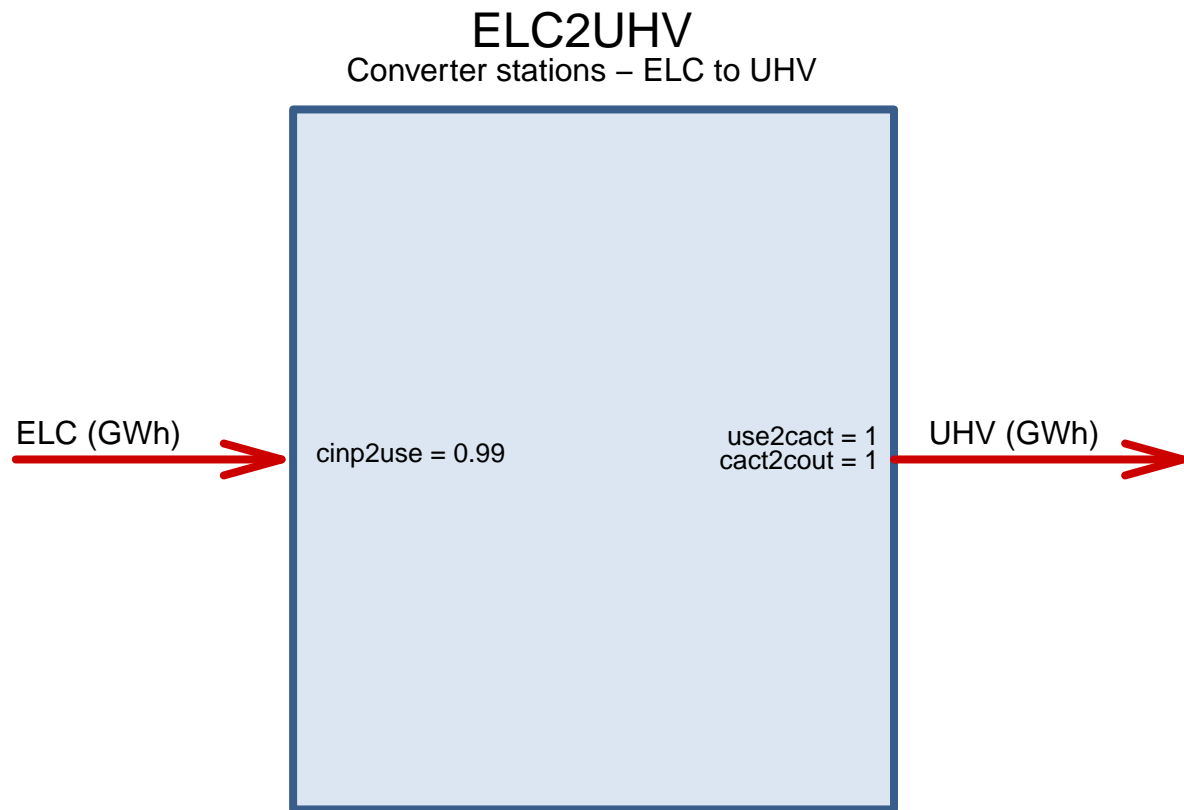
```
# Parameters assumed or calibrated based on
# ABB's 4000-8000 MUSD per 12GW, 2000km, 1-5%
# and other sources

ELC2UHV <- newTechnology(
  name = "ELC2UHV",
  description = "Converter stations - ELC to UHV",
  input = list(
    comm = "ELC",
    unit = "GWh"
    # unit = "PJ"
  ),
  output = list(
    comm = "UHV",
    unit = "GWh"
    # unit = "PJ"
  ),
  # cap2act = 31.536,
  cap2act = 24*365,
  ceff = list(
    comm = "ELC",
    cinp2use = .99 # see also Siemens -- 3% total losses for HVDC/1000km
  ),
  slice = "HOURL",
  invcost = list(
    invcost = 50 #
```

```

),
  olife = 20 # assumed
)
draw(ELC2UHV)

```



```

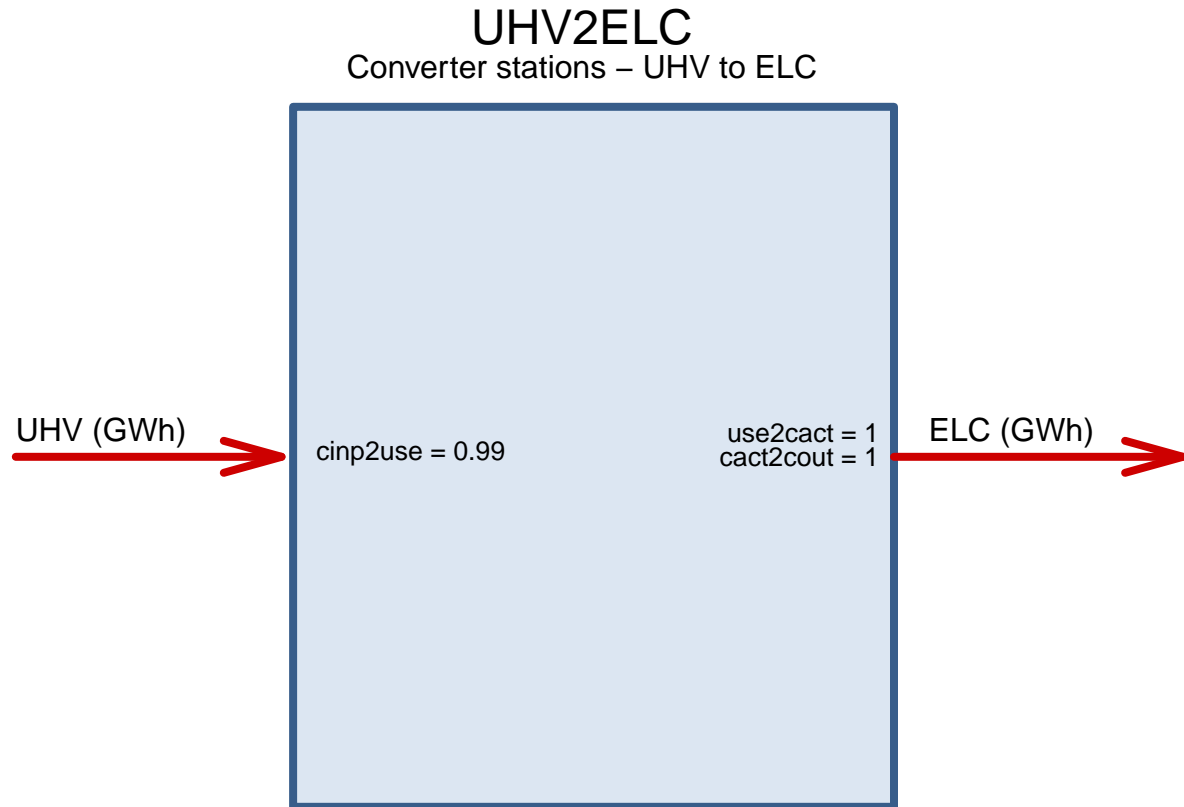
UHV2ELC <- newTechnology(
  name = "UHV2ELC",
  description = "Converter stations - UHV to ELC",
  input = list(
    comm = "UHV",
    unit = "GWh"
    # unit = "PJ"
  ),
  output = list(
    comm = "ELC",
    unit = "GWh"
    # unit = "PJ"
  ),
  # cap2act = 31.536,
  cap2act = 24*365,
  ceff = list(
    comm = "UHV",
    cinp2use = .99
  ),
  slice = "HOURL",
  invcost = list(

```

```

    invcost = 50 # Assumed, based on ABB data
  ),
  olife = 20 # assumed
)
draw(UHV2ELC)

```



## Trade with the rest of the world (ROW)

Currently used to estimate curtailments and the system failure to meet the demand.

code

```

EEXP <- newExport(
  name = "EEXP",
  description = "Supply curtailments (artificial export to capture excessive ELC production by renewable)",
  commodity = "ELC",
  exp = list(
    price = convert("USD/kWh", "MUSD/GWh", .01/100) # 1/100 cents per kWh
  )
)

EIMP <- newImport(
  name = "EIMP",
  description = "Demand curtailments, electricity import at high price (to identify shortages)",

```

```

commodity = "ELC",
imp = list(
  price = convert("USD/kWh", "MUSD/GWh", 10) # USD per kWh, marginal price
)
)

DEMCURT <- newCommodity(
  name = "DEMCURT",
  agg = list(
    comm = "ELC",
    agg = 1
  )
)
# DEMCURT@agg

DIMP <- newImport(
  name = "EIMP",
  description = "Demand curtailments, electricity import at high price (to identify shortages)",
  commodity = "ELC",
  imp = list(
    price = convert("USD/kWh", "MUSD/GWh", 10) # USD per kWh, marginal price
  )
)

# Curtailed demand technology
# i.e. generating technology with high costs

```

code

```

# memory managements in GAMS: https://support.gams.com/solver:error\_1001\_out\_of\_memory
{gams_options <- "
*$exit
energyRt.holdfixed = 0;
energyRt.dictfile = 0;
option solvelink = 0;
option iterlim = 1e9;
option reslim = 1e7;
option threads = 12;
option LP = CPLEX;
energyRt.OptFile = 1;
*option savepoint = 1;
*option bRatio = 0;
*execute_loadpoint 'energyRt_p';
$onecho > cplex.opt
interactive 1
advind 0
*tuningtilim 2400
aggcutlim 3
aggfill 10
aggind 25
bardisplay 2
parallelmode -1
lpmethod 6
*printoptions 1

```

```

names no
freegamsmodel 1
*memoryemphasis 1
threads -1
$offecho
*$exit
"} # GAMS options ####

{cplex_options <- "
interactive 1
CPXPARAM_Advance 0
*tuningtilim 2400
aggcutlim 3
aggfill 10
aggind 25
bardisplay 2
parallelmode -1
lpmethod 6
*prntoptions 1
names no
*freegamsmodel 1
*memoryemphasis 1
threads -1
"} # CPLEX parameters ####

{inc4 <-
"parameter zModelStat;
zModelStat = energyRt.ModelStat;
execute_unload 'USENSYS_scenario.gdx';"} # inc4.gms

# if (F) { # Save the workspace (manual)
# save.image(file = USENSYS$file)
# load(USENSYS$file)
# }

GAMS <- list(
  lang = "GAMS",
  inc3 = gams_options
)

PYOMO <- list(
  lang = "PYOMO",
  files = list(
    cplex.opt = cplex_options
  )
)

JuMP = list(
  lang = "JuMP",
  files = list(
    cplex.opt = cplex_options
  )
)

```

```

mobj <- c(mobj, "USENSYS", "GAMS", "PYOMO", "JuMP")

pkgObj <- function(pkg = "energyRt", envir = .GlobalEnv) {
  # returns list of the package objects
  ii <- sapply(ls(envir = envir), function(x) {
    i <- attr(class(get(x, envir = envir)), "package") == pkg
    if(length(i) == 0) i <- F
    i
  })
  names(ii)[ii] # names of objects
}
pkgObj()

## [1] "BIO" "CELC2DEM100CAPFX" "CELC2DEM100CAPUP" "CSOL_UP"
## [5] "CWFF_UP" "CWIN_UP" "DEM_ELC_DH" "DEM_ELC_FX"
## [9] "DEM100" "DEM100DEXP" "DEM35" "DEM35EXP"
## [13] "DEMCURT" "DEMY" "DEMYEXP" "DIMP"
## [17] "DSMD" "EBIO" "EEXP" "EIMP"
## [21] "ELC" "ELC2DEM100" "ELC2DEM35" "ELC2DEM35CAP"
## [25] "ELC2DSMD" "ELC2UHV" "ESOL" "EWFF"
## [29] "EWIN" "RES_SOL" "RES_WFF" "RES_WIN"
## [33] "route" "SOL" "SOLAR_AF" "STGBTR"
## [37] "STGP2P" "SUP_BIO" "TRBD_UHV_NEI" "TRFX_ELC_NEI"
## [41] "TRFX_UHV_NEI" "UHV" "UHV2ELC" "WFF"
## [45] "WIN" "WINOF20_AF" "WINON20_AF"

save(list = unique(c(pkgObj(), mobj)), file = USENSYS$file)

```

## The Model

The base model and scenario:

- generic electricity (ELC);
- three types of renewables; - two types of energy storage;
- no inter-regional trade/dispatch.

```

# Repository with all the data-objects
reps <- add(newRepository('main_repository'),
  # Commodities
  ELC, SOL, WIN, WFF, UHV,
  # Resources (supply)
  RES_SOL, RES_WIN, RES_WFF,
  # Weather factors
  SOLAR_AF, WINOF20_AF, WINON20_AF,
  # Generating technologies
  ESOL, EWIN, EWFF,
  # Storage
  STGBTR
  # STGBTR1, #STGP2P1,
  # UHV grid
  # UHV,
  # TRBD_UHV_NEI,
  # ELC2UHV, UHV2ELC
  # Export/Import,

```

```

# EEXP, EIMP,
# ELC demand with load curve (24 hours x 365 days)
# DEM_ELC_DH
# DEM_ELC_FX, # flat
# Optimized location
# DEM100,
# ELC2DEM100,
# CELC2DEM100CAPFX,
# CELC2DEM100CAPUP, # optional limit on capacity per region
# Fixed location, 24h intraday flexibility (DSM)
# DSMD,
# ELC2DSMD,
# >= 35% capacity utilization, optimized location
# DEM35,
# ELC2DEM35,
# DEM35EXP,
# ELC2DEM35CAP
)
length(reps@data)
names(reps@data)

# model-class object
mdl <- newModel(
  name = 'RENBAL',
  description = "Renewables balancing model",
  ## in case of infeasibility, `dummy` variables can be added
  # debug = data.frame(#comm = "ELC",
  #                     dummyImport = 1e6,
  #                     dummyExport = 1e6),
  region = reg_names,
  discount = 0.05,
  slice = list(ANNUAL = "ANNUAL",
               # MONTH = timeslices$MONTH,
               # HOUR = timeslices$HOUR
               YDAY = timeslices365$YDAY,
               HOUR = timeslices365$HOUR
               ),
  repository = reps,
  GIS = usa49reg,
  early.retirement = F)

# Check the model time-slices
head(mdl@sysInfo@slice@levels)

# Set milestone-years
# mdl <- setMilestoneYears(mdl, start = 2015, interval = c(1, 2, 5, 6, 7, rep(10, 3)))
mdl <- setMilestoneYears(mdl, start = 2018, interval = c(1))
mdl@sysInfo@milestone # check

# (optional) the model info
{mdl@description <- "
USENSYS, power sector, renewables balancing version,
49 regions, 1 hour resolution,

```



```
3 types of renewables,  
1 types of storages,  
Endogenous UHVDC grid,  
4 types of demand,  
no initial stock."}  
  
# (optional) GAMS and CPLEX options  
mdl@misc$includeBeforeSolve <- cplex_options  
# (optional) save GDX file with the solution  
mdl@misc$includeAfterSolve <- inc_after_solve
```