

Loss functions classification

28 September 2023

07:06

① Binary cross Entropy.

9 yes 1 no 1 yes 9 no

uncertainty.

10 y 0 n 0 y 10 no

certain.

5 y 5 n

5 y 5 n

uncertainty ①

Entropy = 1

$$Loss = -y_{act} \log(\hat{y}) - (1-y_{act}) \log(1-\hat{y})$$

y_{act} = actual

\hat{y} = predicted.

$$-\frac{1}{n} \left[\sum_{i=1}^n y \log(\hat{y}) + (1-y) \log(1-\hat{y}) \right]$$

class 1 class 0

$y_{act} = 0$

$$= 0 \times \log(\hat{y}) + (1-0) \log(1-\hat{y})$$

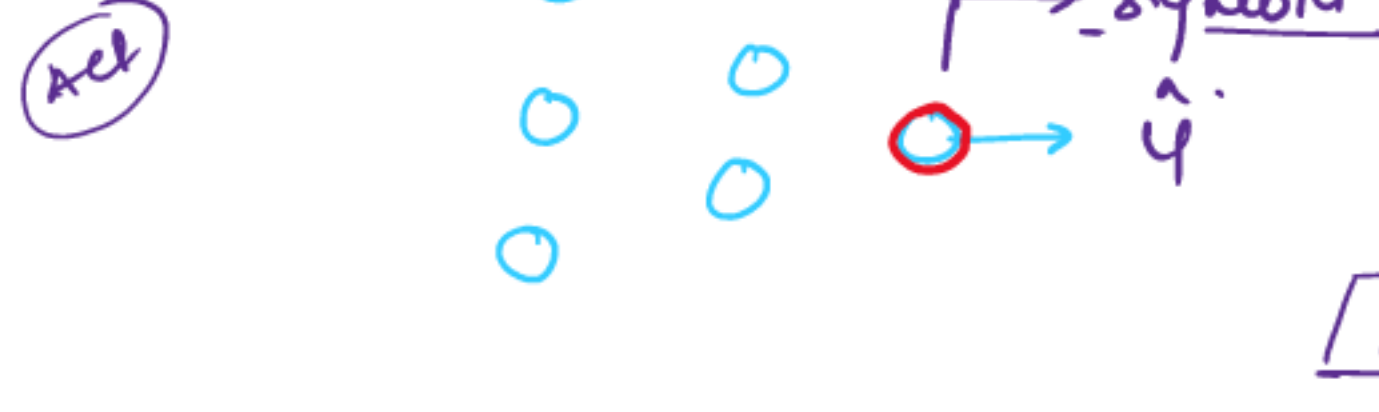
$$= 0 + (1) \log(1-\hat{y})$$

$$= \underline{\log(1-\hat{y})}$$

$y_{act} = 1$

$$= 1 \times \log(\hat{y}) + 0 \times \log(1-\hat{y})$$

$$= \underline{\log(\hat{y})}$$



Categorical cross Entropy.

used in multiclass classification problems.

Approach

receive

pipeline

0 → List

0 → log

0 → non

0 → high

$$Loss = -\sum_{i=1}^K y_{act,i} \log(\hat{y}_i)$$

→ predicted.

$$-y_1 \log \hat{y}_1 - y_2 \log \hat{y}_2 - y_3 \log \hat{y}_3 - y_4 \log \hat{y}_4$$

actual

Age	cat	class	y_1	y_2	y_3	\hat{y}_1	\hat{y}_2	\hat{y}_3
7	red	A	1	0	0	0.3	0.2	0.5
8	red	B	0	1	0	0.3	0.2	0.5
9	red	C	0	0	1	0.3	0.2	0.5

$$-1 \log(0.3) - 0 \times \log(0.2) - 0 \times \log(0.5)$$

$$\underline{-\log(0.3)}$$

all the probabilities summation = 1
Basically we are softmax into the output layer.

target variable must be converted into one hot encoding.

it produces an array of one hot encoding for probable matches of each category.

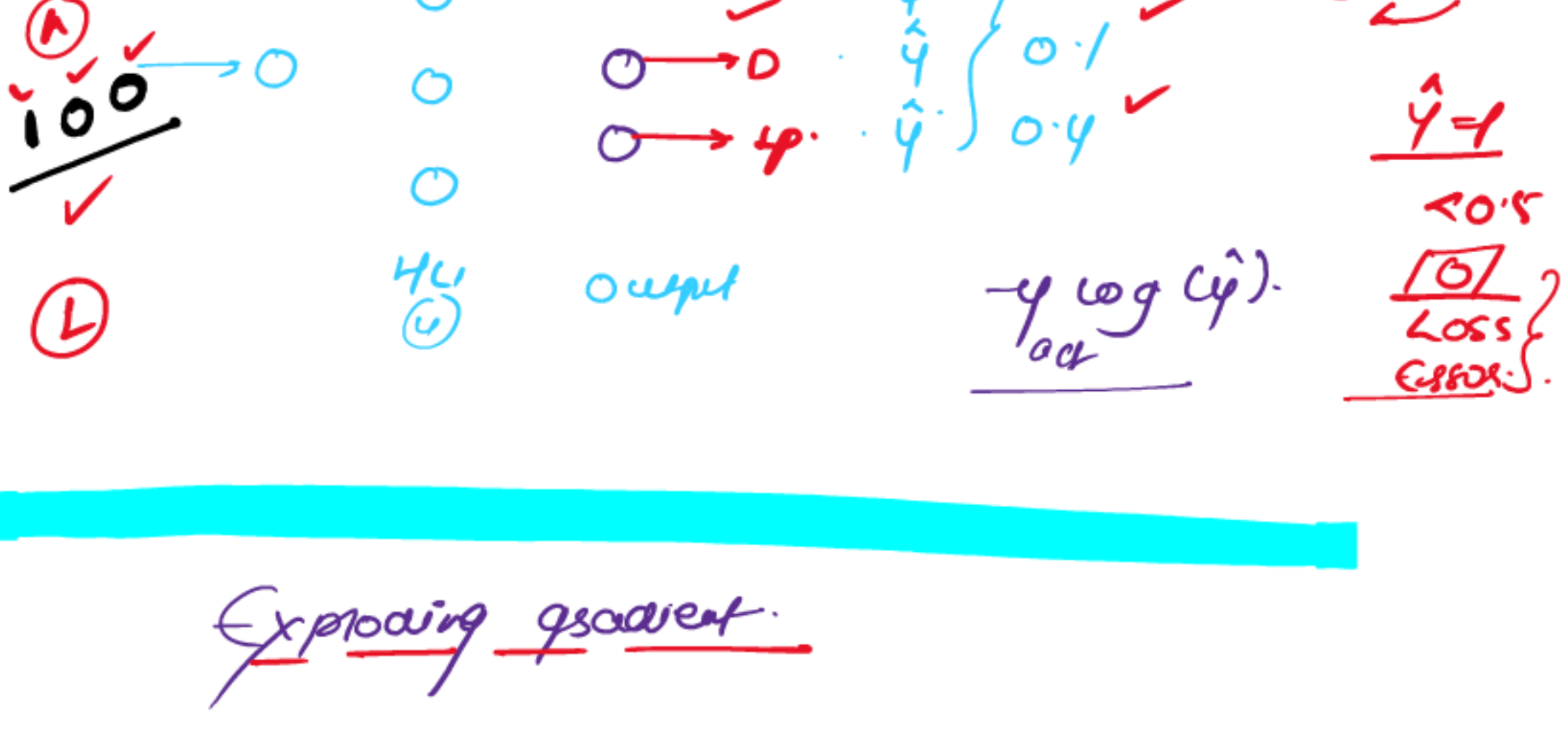
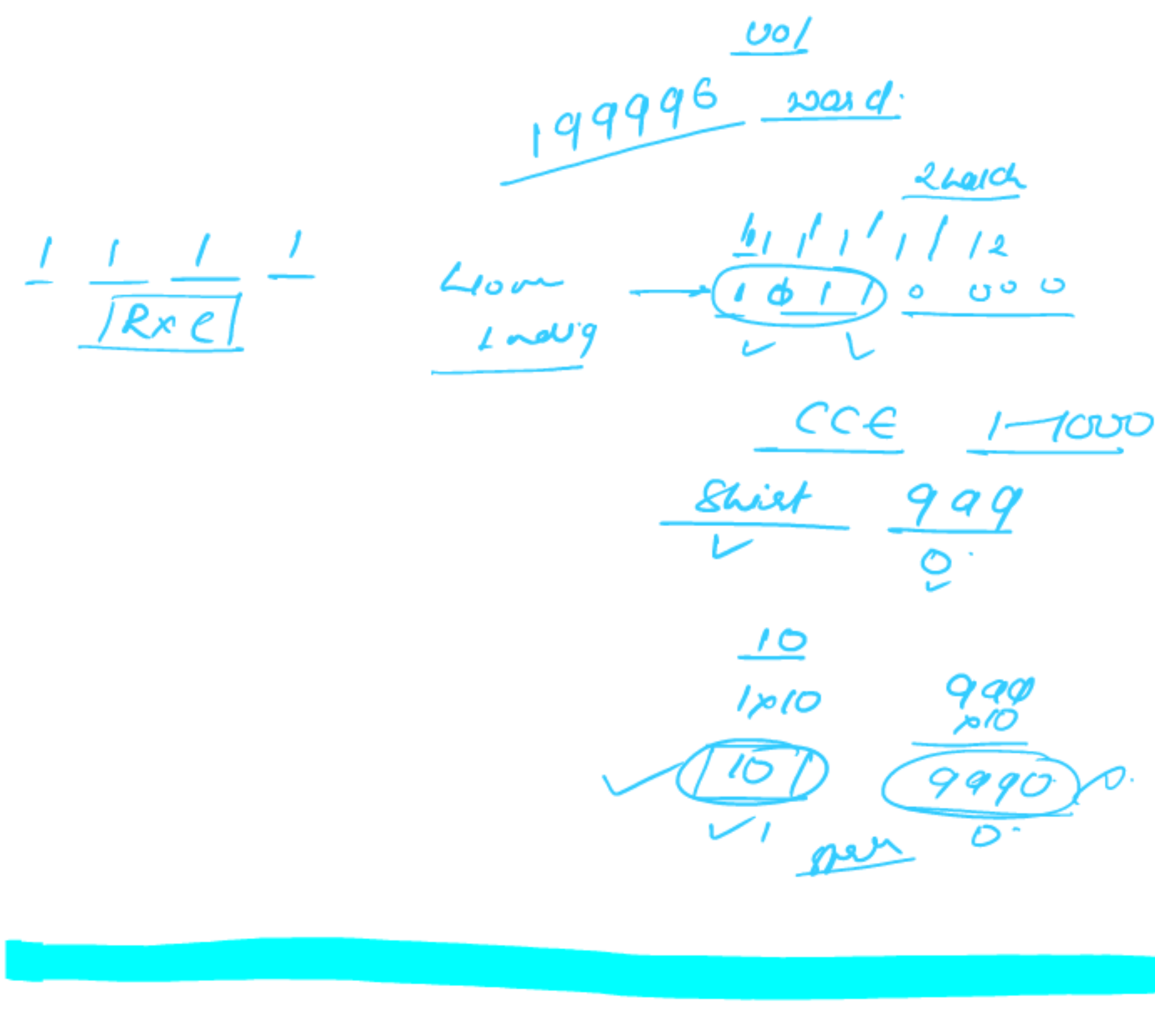
Spote categorical cross Entropy.

it is frustrating when you are dealing with or working with large classification problems.

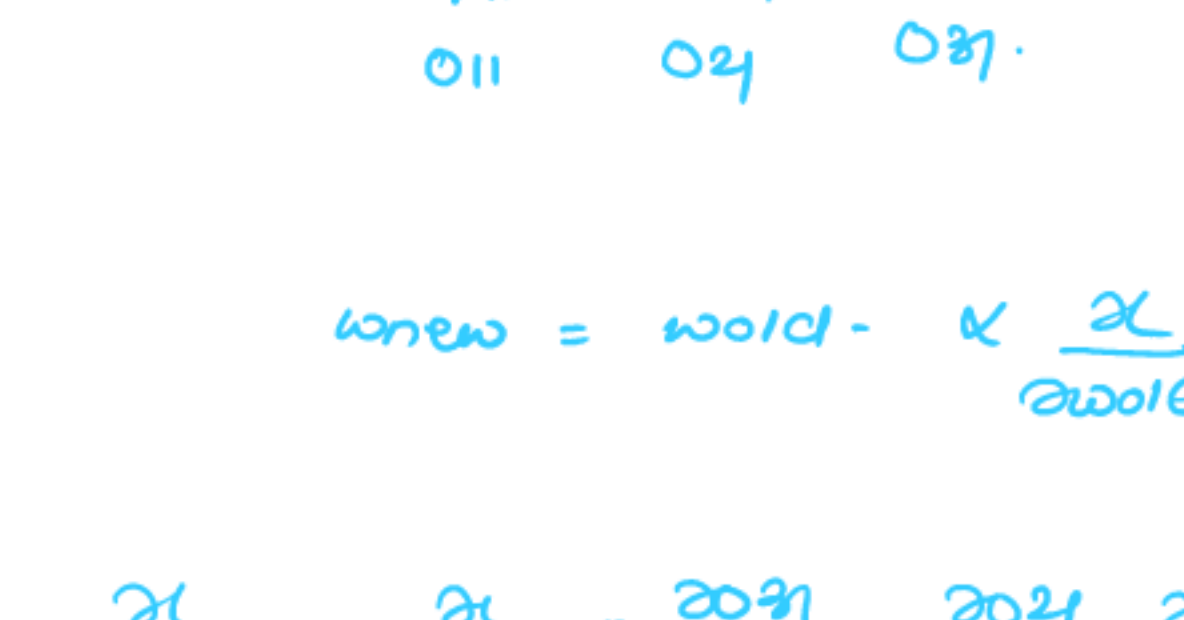
And if suppose you are doing one hot encoding it requires significant amount of memory.

Age	cat	class	CCE	Spote
7	red	A	1 0 0	1 [1 0 0]
8	red	B	0 1 0	0 [0 1 0]
9	red	C	0 0 1	0 [0 0 1]

Spote categorical cross Entropy performs same calculations without requiring one hot encoding of target column.



Exponential gradient.



$$w_{new} = w_{old} - \eta \frac{\partial L}{\partial w_{old}}$$

$$\frac{\partial L}{\partial w_{old}} = \frac{\partial L}{\partial z_1} \times \frac{\partial z_1}{\partial w_{old}} \times \frac{\partial z_1}{\partial z_2} \times \frac{\partial z_2}{\partial w_{old}}$$

$$= 1 \times 10 \times 0.25 \times 0.5$$

$$= \underline{1.25}$$

$$w_{new} = w_{old} - \eta \frac{\partial L}{\partial w_{old}}$$

$$= w_{old}$$

significal



$\alpha \uparrow$

Solution.

① proper weight initialization.

gradient get larger and larger in case of back propagation.

Model experiences high learning.

Exponential growth in model parameters.