



MAHARASHTRA STATE BOARD OF TECHNICAL EDUCATION
(Autonomous)
(ISO/IEC-27001-2005 Certified)

Winter – 2012 Examinations

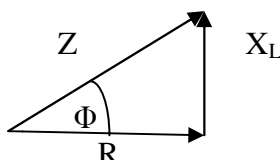
Subject Code : 12055

Model Answer

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- 1 a) Definition :- opposition to the flow of electric current 1 mark
Unit:- Ohm or Ω 1 mark
- 1 b) Definition: no. of cycles / oscillations of alternating qty. completed in 1 sec. 1 mark
Unit: hertz or cycles / second. 1 mark
- 1 c) Active Network:- network that consists one or more energy sources. 1 mark
Example: circuit containing voltage and current source/s. 1 mark
- 1 d) Power factor: cosine of angle between voltage and current or ratios R/Z , (active power)/(apparent power) or kW/kVA of a circuit. 2 marks

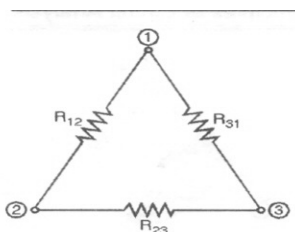
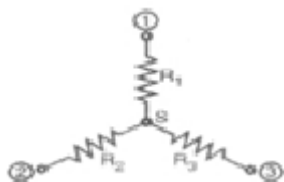
1 e)



1/2 mark
each R, X_L ,
Z & Φ

- 1 f) Admittance:-Reciprocal of Impedance $Y = 1/Z$ 1 mark
Unit:- mho or Siemens or \mathcal{U} 1 mark
- 1 g) For 3 phase delta connection Line voltage = Phase voltage or $V_L = V_{ph}$ 2 marks
- 1 h) Balanced load – The impedances in each of the 3 phases are equal in magnitude and same in nature (phase angle) 1 mark
Unbalanced load – all the three phase impedances are not identical in magnitude and in nature (phase angle) 1 mark
- 1 i) Mesh analysis steps 1) mark loop currents 2) Mark polarity for voltage drops 3) write loop equations 4) solve them by any one method (simultaneous or matrix) 1/2 mark for each point

1 j)



1/2 Mark

$$R_{12} = R_1 + R_2 + (R_1 R_2) / R_3$$

$$R_{23} = R_2 + R_3 + (R_2 R_3) / R_1$$

$$R_{31} = R_3 + R_1 + (R_3 R_1) / R_2$$

1/2 mark
each

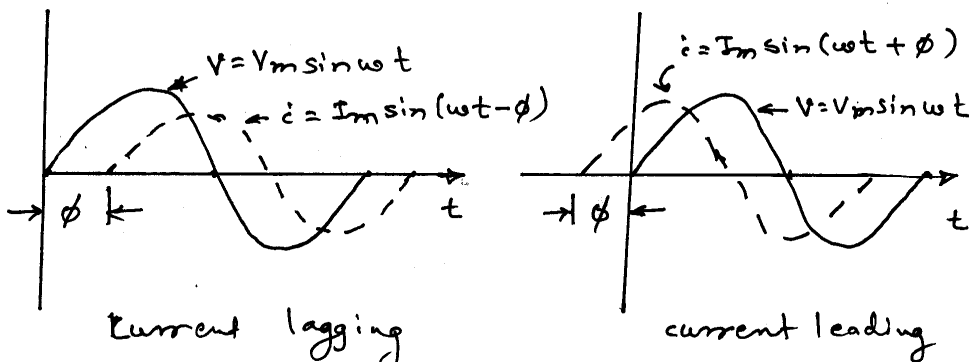


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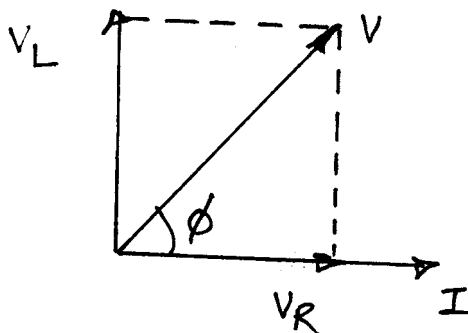
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- 1 k) Thevenin's theorem:- States that current flowing through any load resistance (R_L) of an active, bilateral circuit can be calculated by Thevenin's theorem as $I_L = V_{th} / (R_{th} + R_L)$ where,
 V_{th} = the open circuit voltage measured across load terminals by removing the load resistance
 R_{th} (called as the Thevenin's equivalent source resistance) = resistance measured across load terminals after removing the load resistance and replacing all sources by their internal resistances. 2 marks for correct statement
- 1 l) For maximum power transfer $R_L = R_S$, where R_L = Load resistance connected across the terminals of the source whose internal resistance is R_S . 1 mark
- 1 m) Types of energy sources 1) Current source 2) Voltage source 1 mark each
- 1 n) Q factor for series resonant circuit – it is the voltage magnification in series circuit or ratio: V_C/V or V_L/V 2 marks
- 2 a) In case of purely inductive circuit $v = V_m \sin \omega t$ and $i = I_m (\sin \omega t - \pi/2)$
 $p = v \times i = V_m \sin \omega t \cdot I_m (\sin \omega t - \pi/2)$
 $= V_m I_m \sin \omega t (-\cos \omega t)$
 $= -V_m I_m \cdot (\sin 2\omega t)/2$
 $= -(V_m I_m)/2 \times (\sin 2\omega t)$
Average value over a cycle of the term $\sin 2\omega t = 0$
 \therefore Average power consumed by purely inductive circuit, $P = 0$ 1 mark
- 2 b)  1 mark each for waveform
- Lag :- one waveform (current in this case) reaches its maximum or zero value after other waveform (voltage in this case) by an angle Φ (time phase)
Lead :- one wave form (current in this case) reaches its maximum or zero value before other waveform (voltage in this case) by an angle Φ (time phase) 1 mark each for definition
- 2 c) Definition 1) phase angle (Φ) :- time related angle between voltage and current in degrees or radians. 1 mark each
2) Active power P:- It the power which is responsible for work done in circuit $P = VI \cos \Phi$.



- 3) Reactive power :- It the power which is developed in the reactance of the circuit but does no work over a cycle .OR It is the power stored and released by L and C. given by $Q = V I \sin \Phi$ or $I^2 X$
- 4) Apparent power :- it is the product of r.m.s. values of applied voltage and circuit current or the power that seems to be drawn in terms of V & I.
 $S = VI$ or $I^2 Z$.

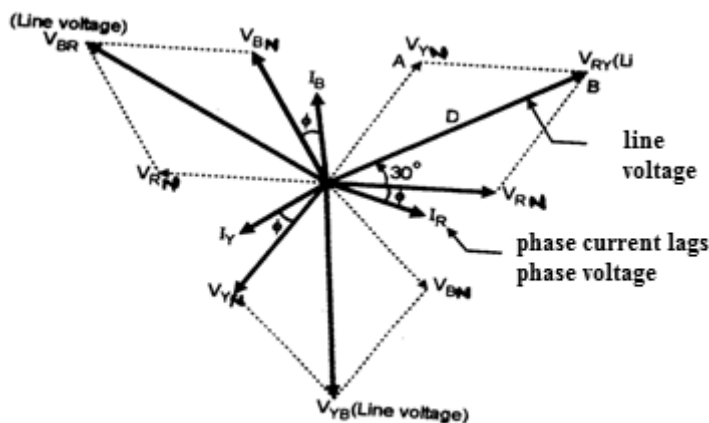
- 2 d) Phasor diagram of R-L- series circuit



Neat
diagram – 2
Marks

Correct
labeling – 2
Marks

- 2 e For balaced star connection the phasor diagram is as shown below:



Phasor
diagram:

unlabeled
or partially
labeled 1
mark,

fully
labeled 2
Marks

$$\begin{aligned} V_{RY} &= 2 \times V_{RN} \times \cos \theta \\ V_{RY} &= \text{line voltage} = V_L \\ V_{RN} &= \text{Phase Voltage} = V_{ph} \\ V_L &= 2 \times V_{ph} \times \cos \theta, \theta = 30^\circ \\ \therefore V_L &= 2 \times V_{ph} \times \cos 30^\circ \\ \therefore V_L &= 2 V_{ph} \times \frac{\sqrt{3}}{2} \\ \therefore V_L &= \sqrt{3} V_{ph} \end{aligned}$$

1 mark

1 mark



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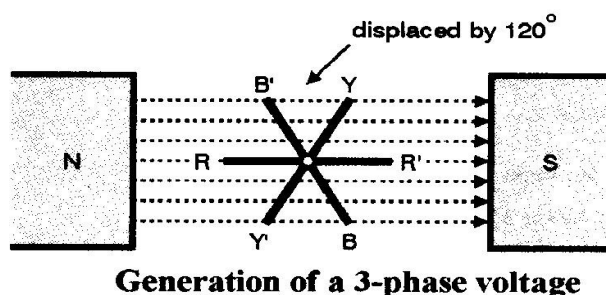
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- 2 f) $Z_{ph} = 8 + j8 \Omega$
 ii) $V_{ph} = V_L = 400 \text{ V}$ 1 mark
 i) $I_{ph} = V_{ph}/Z_{ph} = 400/(8+j8) = 400 \angle 0^\circ / 11.31 \angle 45^\circ = 35.37 \angle -45^\circ \text{ A}$
 $I_L = \sqrt{3} I_{ph} = 61.26 \text{ A}$ 1 mark
 iii) $PF = \cos(-45^\circ) = 0.707 \text{ lag.}$ 1 mark
 iv) $P = \sqrt{3} V_L I_L \cos \Phi = 30006.6 \text{ W} = 30 \text{ kW}$ 1 mark
- 3 a) $R = 5 \Omega$
 $X_L = 2 \pi f L = 62.83 \Omega$ ½ mark
 $X_C = 1 / (2 \pi f C) = 63.66 \Omega$ ½ mark
 i) $Z = \sqrt{R^2 + (X_L - X_C)^2} = 5.068 \Omega$ ½ mark
 ii) $I = V/Z = 230/5.068 = 45.38 \text{ A}$ 1 mark
 iii) $PF = R/Z = 0.986$ lead as $X_C > X_L$ ½ mark
 iv) $P = VI \cos \Phi = 230 \times 45.38 \times 0.986 = 10291.27 \text{ W} = 10.29 \text{ kW}$ 1 mark
- 3 b) The Condition for series resonance is $X_L = X_C$
 $X_L = \text{inductive reactance and } X_C = \text{capacitive reactance}$ 1 mark
 $\therefore 2 \pi f_0 L = 1/2 \pi f_0 C, f_0 = \text{resonant frequency}$ 1 mark
 $\therefore f_0^2 = 1/\{(2 \pi)^2 LC\}$ 1 mark
 $\therefore f_0 = 1/(2 \pi \sqrt{LC}) \text{ Hz}$ 1 mark
- 3 c) $Z = 8 + j6 \Omega = R + jX$
 $R = 8, X = 6$
 $g = \text{conductance and } b = \text{susceptance}$
 $g = R/(R^2 + X^2) \text{ and } b = X/(R^2 + X^2)$ 1 mark
 $g = 0.08 \text{ mho } b = 0.06 \text{ mho or } \angle 33.7^\circ$ each for g and b
 $Y = g - jb = 0.08 - j0.06 \text{ mho (rectangular form)}$ 1 mark
 $Y = 0.1 \angle -36.87^\circ \text{ (polar form)}$ 1 mark
- 3 d) Advantages of polyphase circuit
 1) for same amount of power size of 3 ph machine is smaller
 2) for same amount of power transmission size of conductor is smaller
 3) Maintenance is easier & cheaper
 4) 3 ph motors are self starting
 5) More power can be transmitted
 6) Better Power Factor 1 mark for each point (Any Four)

3 e)



2 marks for figure or equiv. Fig.

Points expected:



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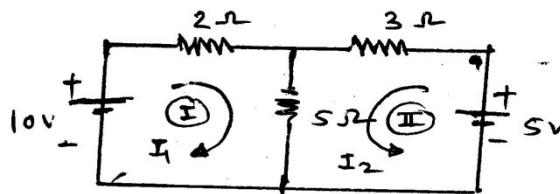
Model Answer

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- 1) 3 coils/ winding (conductor) displaced by 120 degree in space.
- 2) Placed in uniform magnetic field.
- 3) Winding system rotated
- 4) Emf generated in each conductor by faradays laws and lenz's law
- 5) Induced emfs in the windings are sinusoidal, equal in magnitude & displaced by 120 degrees in time phase.

2 mark for explanation

3 f)



For loop I -

$$2I_1 + 5(I_1 + I_2) - 10 = 0$$

$$\therefore 7I_1 + 5I_2 = 10 \quad \text{--- (1)}$$

For loop II -

$$3I_2 + 5(I_2 + I_1) - 5 = 0$$

$$\therefore 5I_1 + 8I_2 = 5 \quad \text{--- (2)}$$

solving simultaneously or by matrix method
on calculator

$$\begin{bmatrix} 7 & 5 \\ 5 & 8 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} 10 \\ 5 \end{bmatrix}$$

$$I_1 = 1.774 \text{ A} \quad \& \quad I_2 = -0.48 \text{ A}$$

Meaning of negative I_2 is its direction is reverse
current flowing through 3Ω resistor is I_2

$$= \underline{\underline{0.48 \text{ A}}}$$

1 mark

1 mark

1 mark

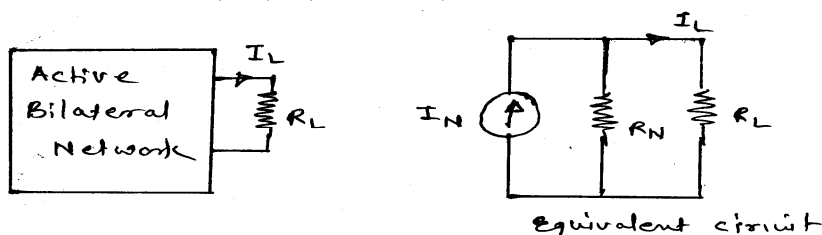
1 mark

4 a)

Norton's theorem statement :- current flowing through a load resistor R_L of an active bilateral circuit can be found with the help of Norton's theorem as

$$I_L = I_N \times (R_N) / (R_N + R_L)$$

2 mark



Where -

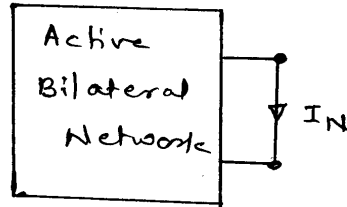
- i) I_N is the short circuit Norton's current flowing through the shorted



load terminals

To Find I_N

1 mark

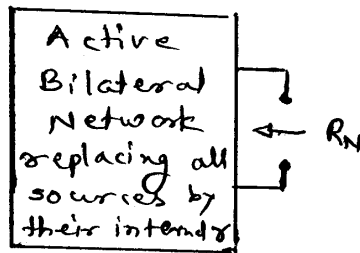


and

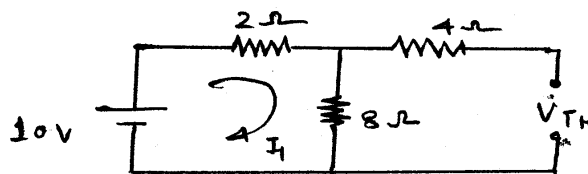
- ii) R_N is the Norton's equivalent resistance measured across load terminals by removing load resistance and replacing all sources by their internal resistances

To Find R_N

1 mark



- 4 b) Current through 8 ohm resistor using Thevenin's theorem is
1) step 1 : find V_{TH}



V_{TH} = voltage across 8 ohm resistor
for this calculate I_1

$$I_1 = \frac{10}{2+8} = 1 \text{ A}$$

1 Mark

$$V_{TH} = 8 I_1 = 8 \times 1 = 8 \text{ V}$$

1 Mark

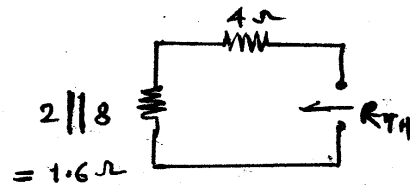
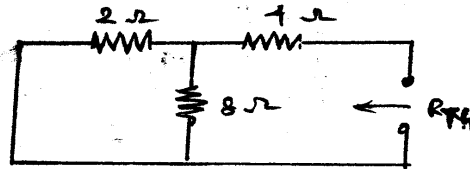


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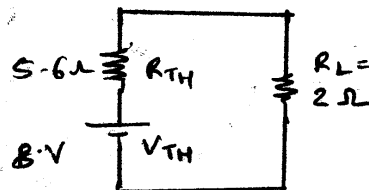
ii) step 2 - To find R_{TH}



1 mark

$$R_{TH} = 4 + 1.6 = 5.6 \Omega$$

iii) Equivalent circuit



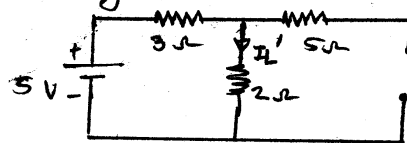
1 mark

$$\therefore I_L = \frac{V_{TH}}{R_{TH} + R_L} = \frac{8}{5.6 + 2} = 1.052 A$$

4 c)

Superposition theorem -

i) using 5V source

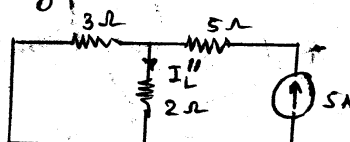


1/2 mark fig

$$I_L' = \frac{5}{3+2} = 1 A$$

1 mark

ii) using 5A source



1/2 mark fig

$$I_L'' = I \times \frac{3}{3+2} = 5 \times \frac{3}{5} = 3 A$$

1 mark

$$I_L = I_L' + I_L'' = 1 + 3 \quad \boxed{I_L = 4 A}$$

1 mark



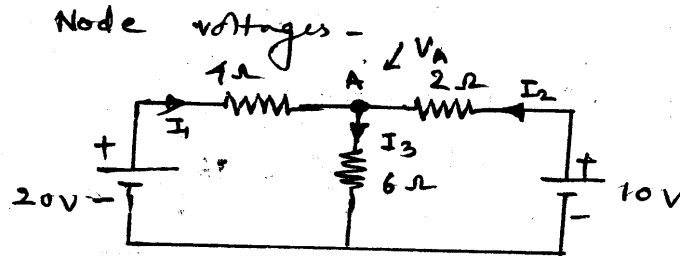
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4 d)



By KCL

$$-I_1 + I_2 = I_3$$

$$\frac{20 - V_A}{4} + \frac{10 - V_A}{2} = \frac{V_A - 0}{6}$$

1 mark

$$60 - 3V_A + 60 - 6V_A = 2V_A$$

$$120 = 11V_A$$

$$\therefore V_A = 10.91 \text{ V}$$

1 mark

Current thn' 6Ω resistor is I_3

$$I_3 = \frac{V_A}{6} = \frac{10.91}{6} = 1.82 \text{ A}$$

2 mark



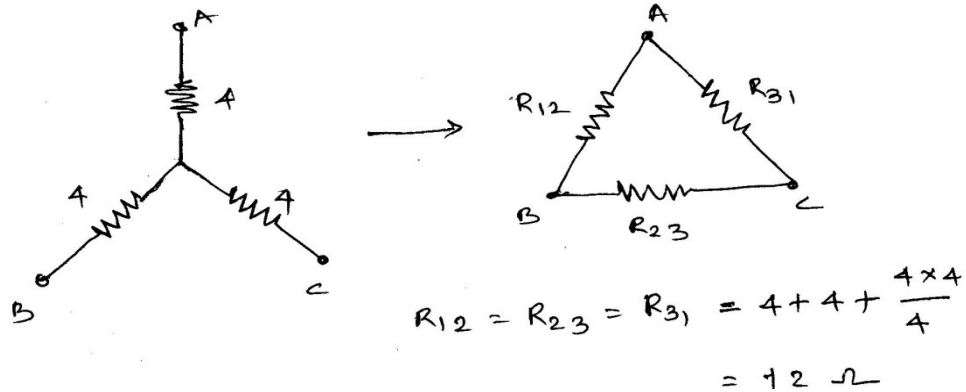
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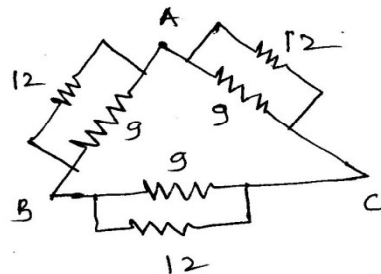
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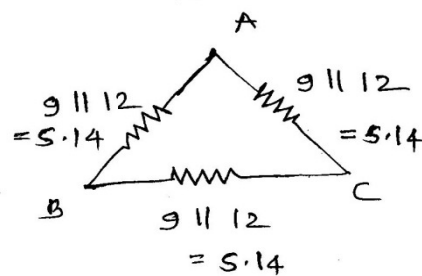
4 e)



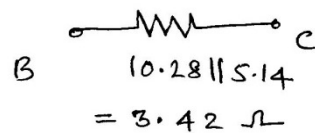
1 mark



1 mark



1 mark



1 mark



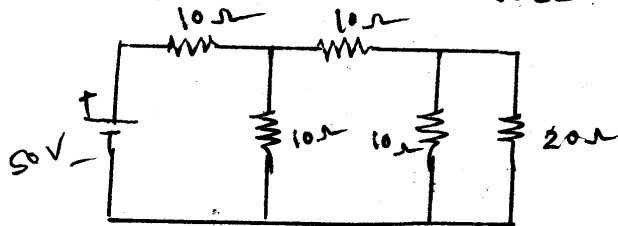
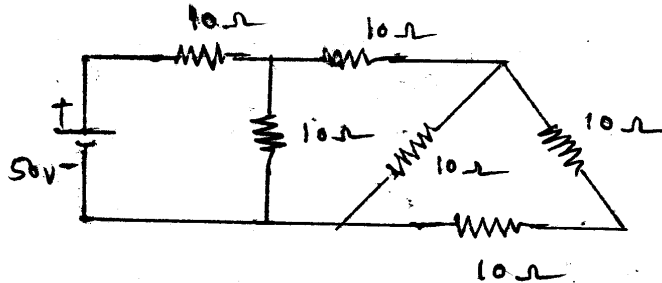
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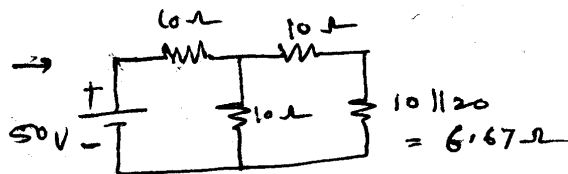
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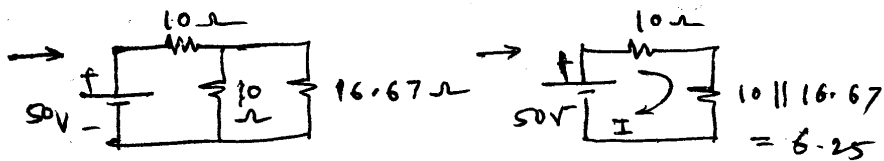
4 f)



1 mark



1 mark

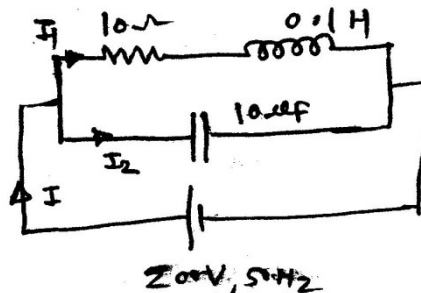


1 mark

$$I = \frac{50}{10 + 6.25} = 3.077 \text{ A}$$

1 mark

5 a)



$$X_L = 2\pi fL = 2\pi \times 50 \times 0.1 = 31.41 \Omega$$

$$X_C = 1/2\pi fC = 1/(2\pi \times 50 \times 10 \times 10^{-6}) = 318.3 \Omega$$

$$Z_1 = 10 + j31.41 \Omega$$

$$Z_2 = 0 - j318.3 \Omega$$

½ mark

$$Y_1 = 1/Z_1 \text{ or } g_1 - jb_1$$

$$Y_2 = 1/Z_2 \text{ or } g_2 + jb_2$$

$$g_1 = R / (R^2 + X^2) = 10/(10^2 + 31.41^2) = 9.2 \times 10^{-3} \text{ mho}$$

$$b_1 = X/(R^2 + X^2) = 31.41/(10^2 + 31.41^2) = 0.029 \text{ mho}$$

½ mark

$$g_2 = 0 \text{ mho}, b_2 = 318.3/318.3^2 = 0.00314 \text{ mho}$$

½ mark

$$Y_1 = 0.0092 - j0.029 \text{ mho} = 0.03 \angle -72.4^\circ \text{ mho}$$

1 mark

1 mark



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$$Y_2 = 0 + j0.00314 \text{ mho} = 0.0031 \angle 90^\circ$$

$$I_1 = V \times Y_1 = 200 \angle 0^\circ \times 0.03 \angle -72.4^\circ = 6 \angle -72.4^\circ = 1.81 - j 5.72 \text{ Amp}$$

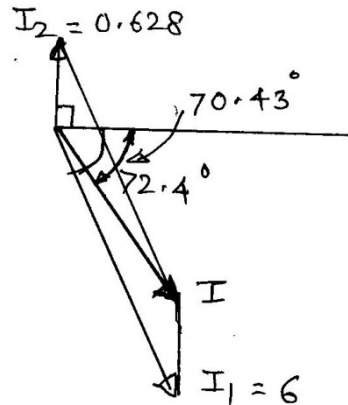
1 mark

$$I_2 = V \times Y_2 = 200 \angle 0^\circ \times 0.0031 \angle 90^\circ = 0.628 \angle 90^\circ = 0 + j0.628 \text{ Amp}$$

1 mark

$$I = I_1 + I_2 = 1.81 - j 5.72 + 0 + j0.628 = 1.81 - j 5.092 = 5.4 \angle -70.43^\circ \text{ Amp}$$

1 mark



1 ½ mark

5 b) $R = 20 \Omega$, $X_L = 2\pi fL = 2\pi \times 50 \times 0.3 = 94.25 \Omega$

1 mark

$$Z_{ph} = \sqrt{R^2 + X_L^2} = 96.35 \Omega$$

1 mark

$$V_{ph} = V_L = 400 \text{ V, delta connection}$$

1 mark

$$I_{ph} = V_{ph}/Z_{ph} = 400/96.35 = 4.15 \text{ A}$$

1 mark

$$I_L = \sqrt{3} I_{ph} = \sqrt{3} \times 4.15 = 7.19 \text{ A}$$

1 mark

$$\cos \phi = R/Z = 20/96.35 = 0.207 \text{ lag}$$

1 mark

$$P = \sqrt{3} V_L I_L \cos \phi = \sqrt{3} \times 400 \times 7.19 \times 0.207 = 1031.14 \text{ W} = 1.031 \text{ kW}$$

2 marks



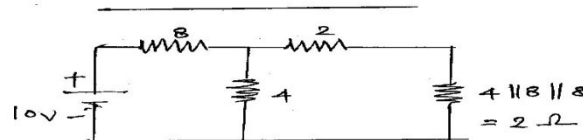
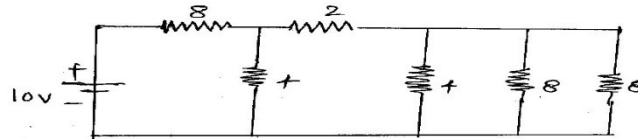
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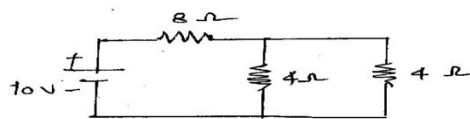
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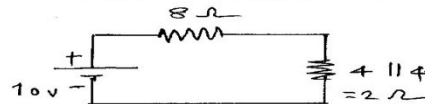
5 c)



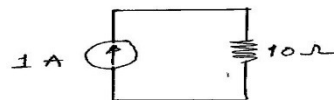
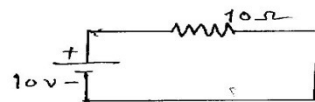
2 Marks



2 Marks

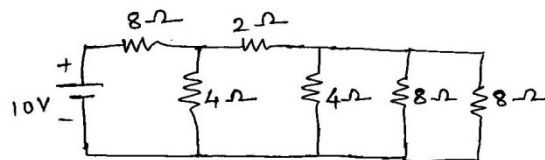


2 Marks

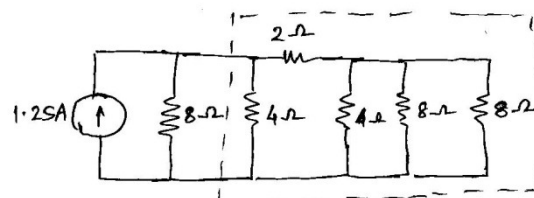


2 Marks

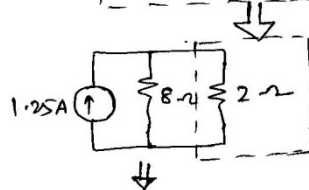
OR



Converting 10V source and 8Ω resistance into current source



3 Marks



3 Marks



2 Marks



6 a) $R = 5\Omega$

i) $X_L = 2\pi fL = 62.83 \Omega$

ii) $X_C = 1/(2\pi fC) = 31.83 \Omega$

iii) $Z = \sqrt{R^2 + (X_L - X_C)^2} = 31.4 \Omega$

iv) $I = V/Z = 230/31.4 = 7.32 \text{ A}$

v) $\text{Pf} = R/Z = 0.16$

vi) $V_L = I X_L = 459.9 \text{ V}$

1 Mark

1 Mark

1 Mark

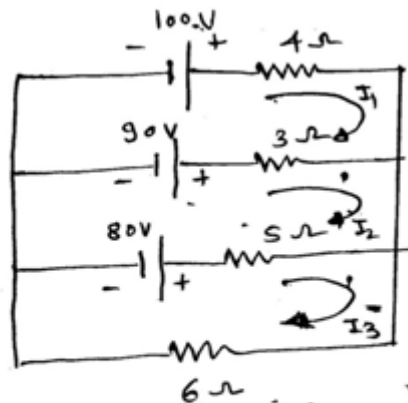
1 Mark

1 ½ Mark

1 ½ Mark

1 Mark

6 b)



1 Mark

write equation for three loops

$$4I_1 + 3(I_1 - I_2) + 90 - 100 = 0$$

$$7I_1 - 3I_2 = 10 \quad \text{--- (1)}$$

1 mark

$$3(I_2 - I_1) + 5(I_2 - I_3) + 80 - 90 = 0$$

$$-3I_1 + 8I_2 - 5I_3 = 10 \quad \text{--- (2)}$$

1 mark

$$5(I_3 - I_2) + 6I_3 - 80 = 0$$

$$-5I_2 + 11I_3 = 80 \quad \text{--- (3)}$$

1 mark

The matrix is

$$\begin{bmatrix} 7 & -3 & 0 \\ -3 & 8 & -5 \\ 0 & -5 & 11 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = \begin{bmatrix} 10 \\ 10 \\ 80 \end{bmatrix}$$

2 Marks

$$I_3 = \left[\begin{array}{ccc|ccc} 7 & -3 & 10 & 7 & -3 & 0 \\ 3 & 8 & 10 & 3 & 8 & -5 \\ 0 & 5 & 80 & 0 & 5 & 11 \end{array} \right]$$

Solving above equations, $I_3 = 12.465 \text{ A}$

2 marks



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Model Answer

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- c) $Z_{ph} = 15 + j20 = 25 \angle 53.13^\circ \Omega$ 1 Mark
 $V_{ph} = V_L / \sqrt{3}$ (Star connection) $= 400 / \sqrt{3} = 231 \text{ V}$
 $I_{ph} = V_{ph} / Z_{ph} = 9.24 \angle -53.13^\circ \text{ A}$
 $I_L = I_{ph} = 9.24 \text{ A}$
i) $PF = \cos \phi = \cos(53.13^\circ) = 0.6$ or $R/Z = 0.6$ 1 Mark
ii) Active power $= P = \sqrt{3} V_L I_L \cos \phi = 3841 \text{ W} = 3.81 \text{ kW}$ 1 Mark
iii) Reactive power $= Q = \sqrt{3} V_L I_L \sin \phi$ (Where $\sin \phi = 0.8$) $= 5121 \text{ VAR}$
 $= 5.12 \text{ kVAR}$ 1 Mark
iv) Apparent power $= S = \sqrt{3} V_L I_L = 6401 \text{ VA} = 6.4 \text{ kVA}$ 1 Mark
v) $V_{ph} = V_L / \sqrt{3}$ (Star connection) $= 400 / \sqrt{3} = 231 \text{ V}$ 1 Mark
vi) $I_L = I_{ph} = 9.24 \text{ A}$ 1 Mark
vii) $I_{ph} = 9.24 \text{ A}$ 1 Mark