



Subject Code: 17304

SUMMER – 15 EXAMINATIONS  
Model Answer- Strength of Materials

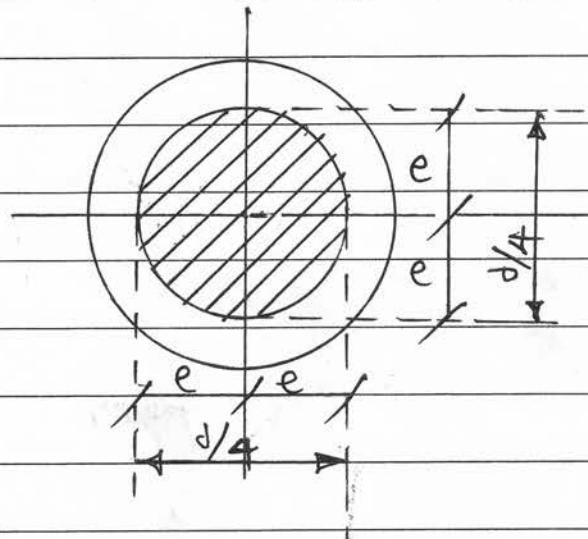
Total Pages: 01 / 40

**Important Instruction to Examiners:-**

- 1) The answers should be examined by key words & not as word to word as given in the model answers scheme.
- 2) The model answers & answers written by the candidate may vary but the examiner may try to access the understanding level of the candidate.
- 3) The language errors such as grammatical, spelling errors should not be given more importance.
- 4) While assessing figures, examiners, may give credit for principle components indicated in the figure.
- 5) The figures drawn by candidate & model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 6) Credit may be given step wise for numerical problems. In some cases, the assumed contact values may vary and there may be some difference in the candidate's answers and model answer.
- 7) In case of some questions credit may be given by judgment on part of examiner of relevant answer based on candidates understanding.
- 8) For programming language papers, credit may be given to any other programme based on equivalent concept.

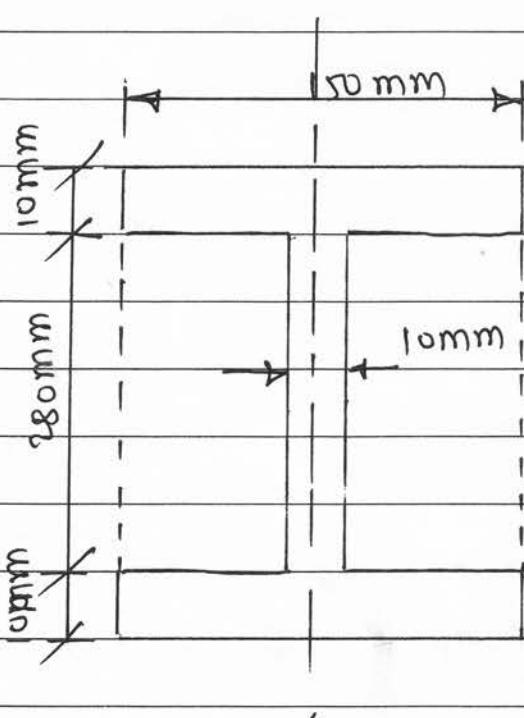
**Important notes to examiner**

Q.NO	SOLUTION	MARKS
Q-1 A		
a)	<p>i) Fatigue : it is property of material by virtue of it resists the failure of material under fluctuating or repeated loading</p>	01 M
	<p>ii) creep : the continuous deformation of material which undergoes with time due to application of external steady load is called creep.</p>	01 M
b)	<p>i) principal plane : are the two planes where the normal stress (<math>\sigma</math>) is the maximum or minimum and no shear stresses.</p>	01 M
	<p>ii) principal stress : The normal stresses (<math>\sigma</math>) acting on the principal planes</p>	01 M
c)	$-F = \frac{\delta M}{\delta x}$	01 M
	<p>the rate of change of bending moment is equal to shear force</p>	01 M
	<p>if <math>\frac{\delta F}{\delta x} = 0</math>, bending moment is maximum which shows the point of max. B.M and point of zero shear or the point of changing the sign of S.F</p>	

Q.NO	SOLUTION	MARKS
(d)	Assumption in theory of bending	
i>	The value of young's modulus of Elasticity $\frac{1}{2}M$ is same in tension and compression	1/2 M
ii>	The material of beam is homogenous and Isotropic.	for any four
iii>	The Transverse sections which were plane before bending remain plane after Bending also.	
iv)	the Beam initially straight and all longitudinal filament bend into circular arcs with common centre of curvature.	
v>	The radius of curvatures large as compare to the dimensions of the cross-section	
vi>	Each layer of the Beam is free to expand to or contract independently of the layers, above or below it.	
e)	Core of section for circular column.	
		02 M

Q.NO	SOLUTION	MARKS
f)	$E = 3K(1-2\mu)$ where as $E = 2G(1+\mu)$ $E$ = Young's modulus $K$ = Bulk modulus $G$ = Shear modulus $\mu$ = Poisson's ratio	01 M 01 M
g)	i) $\theta = 45^\circ$ $\theta = 135^\circ$ are angle where tangential stress is maximum	01 M 01 M
h)	Bending stress distribution diagram for rectangular section for simply supported & cantilever Beam.	
		01 M
a)	Beam Section	
b)	Bending stress variation diagram for simply supported Beam	01 M
c)	Bending stress variation for cantilever beam	01 M

Q NO	SOLUTION	MARKS
(Q-1-B)		
a) given :		
i) $P = 40 \text{ kN}$ ii) $\sigma_{\text{permissible}} = 150 \text{ MPa}$		
we have		
$\sigma = \frac{P}{A} = \frac{P}{\frac{\pi}{4} \times d^2}$	01 M	
∴ put the value of 'P' & 'σ'		
$150 = \frac{40 \times 10^3}{\frac{\pi}{4} \times d^2}$	01 M	
$\therefore d^2 = \frac{40 \times 10^3}{\frac{\pi}{4} \times 150}$	01 M	
$d^2 = \frac{40 \times 10^3}{117.81}$		
$d^2 = 339.52$		
$d = 18.43 \text{ mm}$	01 M	
b) given data :		
i) $d = 1 \text{ m}$ ii) fluid pressure = $1.5 \text{ N/mm}^2$		
$\sigma_{\text{tensile}} = 450 \text{ N/mm}^2$ factor of safety = 4.5		
since hoop stress is twice the longitudinal stress, pipe will fail if the hoop stress exceeds the working stress.		

Q. NO	SOLUTION	MARKS
	$\therefore \text{Hoop stress } (\sigma_c) = \frac{\text{Ultimate stress}}{\text{Factor of safety}}$ $= \frac{450}{4.5} = 100 \text{ N/mm}^2$	1/2 M
	$\sigma_c = \frac{Pd}{2t}$	01 M
	$100 = \frac{1.5 \times 1000}{2 \times t}$	01 M
	$\therefore \text{Thickness of pipe } [t = 7.5 \text{ mm}]$	01 M
c)	 <p>given data:</p> $B = 150 \text{ mm}$ $H = 300 \text{ mm}$ $b = \text{width of shaded portion } (150 - 10) = 140 \text{ mm}$ $h = \text{height of shaded portion } (300 - 2 \times 10) = 280 \text{ mm}$	1/2 M for fig 1/2 M for given data
i)	$I_{xx} = \frac{B^3}{12} - \frac{bh^3}{12} = \frac{1}{12} [B^3 - bh^3]$	01 M
	$I_{xx} = \frac{1}{12} [150 \times 300^3 - 140 \times 280^3]$	01 M
	$I_{xx} = 81.39 \times 10^6 \text{ mm}^4$	01 M

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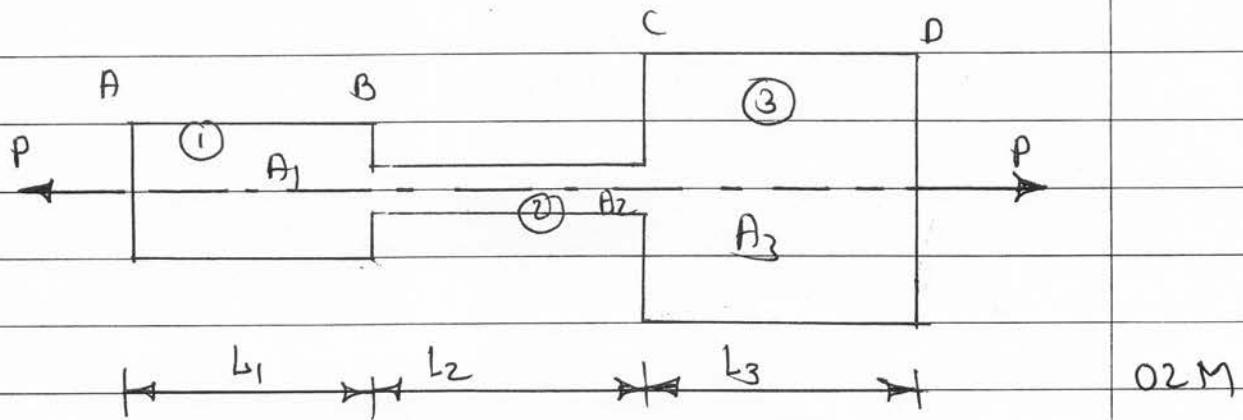
Q.NO

SOLUTION

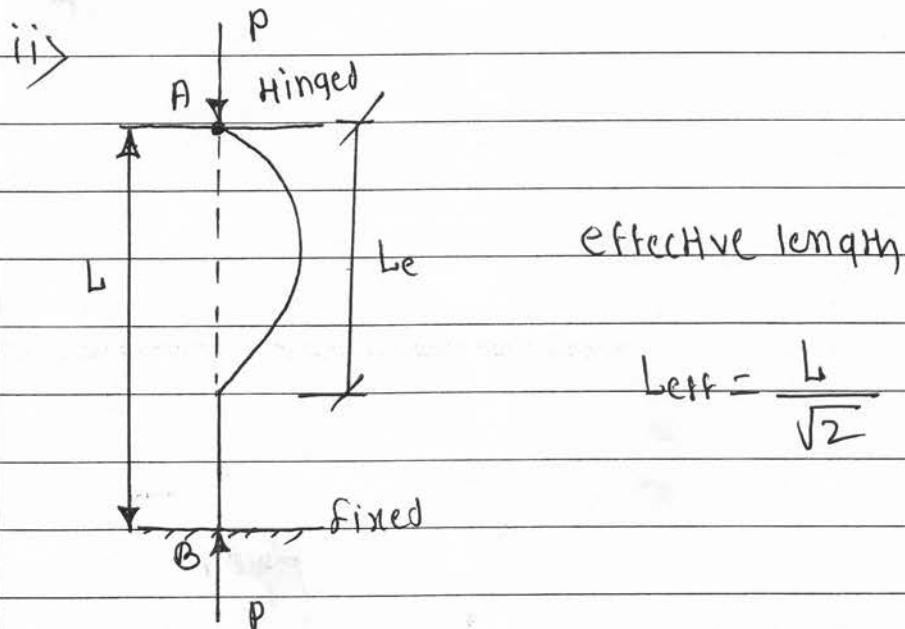
MARKS

Q-2(a)

i) uniformly varying section showing axial load

where as  $P$  = axial load

$A_1, A_2, A_3$  &  $L_1, L_2, L_3$  are the c/s-area & length  
of section (1) (2) (3)



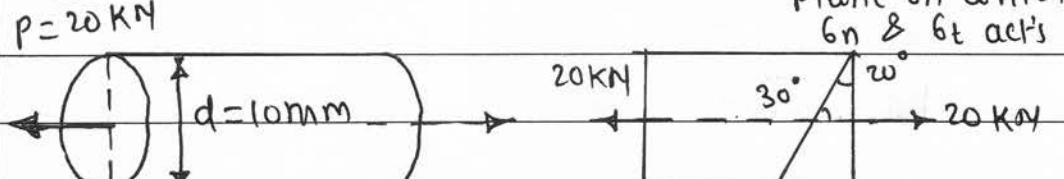
$$L_{eff} = \frac{L}{\sqrt{2}}$$

01 M  
for  
formula

01 M  
for  
fig

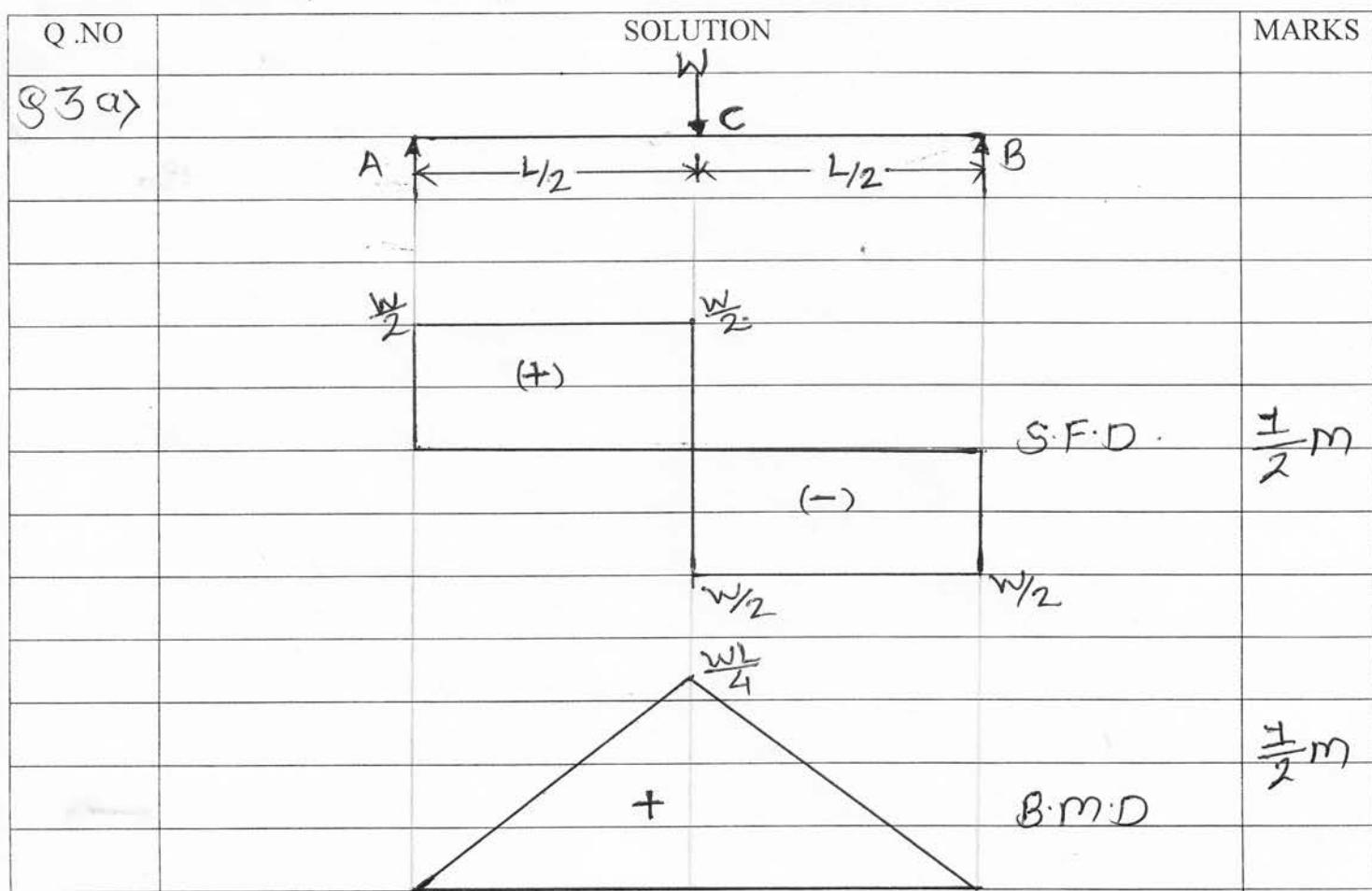
Q.NO	SOLUTION	MARKS
b)	Assumptions in Euler's column Theory i) The material of the column is perfectly homogeneous and isotropic ii) The column is initially straight and of uniform lateral dimensions iii) The load on the column is exactly axial. iv) The column is long and fails due to buckling or bending only v) The self weight of the column is neglected. vi) The column is stressed upto the limit of proportionality	(for each any four)
c)	given data $L = 300 \text{ mm}$ $d = 20 \text{ mm}$ $t = 100^\circ\text{C}$ Total extension = $0.4 \text{ mm}$ $E = 2 \times 10^5 \text{ N/mm}^2$ $\alpha = 12 \times 10^{-6} / {}^\circ\text{C}$	$\frac{1}{2} \text{ M}$
	Total extension of the rod = free expansion + Extension $\delta L$ due to force 'P'	
	$0.4 = (L \alpha t) + \delta L$ due to force 'P' $0.4 = (300 \times 12 \times 10^{-6} \times 100) + \delta L$ $0.4 = 0.36 + \delta L$ $\therefore \boxed{\delta L = 0.04 \text{ mm}}$	$\frac{1}{2} \text{ M}$

Q.NO	SOLUTION	MARKS
Q-2 (c) (continued)	But	
	$\delta L = \frac{P \cdot L}{AE}$	1/2 M
	$0.04 = \frac{P \times 300}{\left(\frac{\pi \times 20^2}{4}\right) \times 2 \times 10^5}$	1/2 M
	$\therefore P = 0.04 \times \frac{\left(\frac{\pi \times 20^2}{4}\right) \times 2 \times 10^5}{300}$	1/2 M
	$P = 8.377 \times 10^3 \text{ N}$ or $P = 8.377 \text{ kN}$	01 M
d)		
i)	$A_1 = 40 \times 40 = 1600 \text{ mm}^2$ $A_2 = 20 \times 20 = 400 \text{ mm}^2$ $A_3 = 30 \times 30 = 900 \text{ mm}^2$ $L_1 = 1 \text{ m} = 1000 \text{ mm}$ $L_2 = 1 \text{ m} = 1000 \text{ mm}$ $L_3 = 1.5 \text{ m} = 1500 \text{ mm}$	
ii)	To find unknown value of 'P'	
	$\Sigma F_x = -120 + 220 - P + 160$ $P = 260 \text{ kN}$ (←)	01 M
iii)	$\delta L = \delta L_1 + \delta L_2 + \delta L_3$ $\delta L = \frac{P_1 L_1}{A_1 E} + \frac{P_2 L_2}{A_2 E} + \frac{P_3 L_3}{A_3 E}$	01 M 2

Q. NO	SOLUTION	MARKS
	$\delta_L = \frac{1}{E} \left[ \frac{P_1 L_1}{A_1} + \frac{P_2 L_2}{A_2} + \frac{P_3 L_3}{A_3} \right]$	1/2 M
	$= \frac{1}{2 \times 10^5} \left[ \frac{(120 \times 10^3) \times 1000}{1600} + \frac{(-100 \times 10^3) \times 1000}{400} + \frac{(160 \times 10^3) \times 1500}{900} \right]$	0.1 M
	$= \frac{1}{2 \times 10^5} [ 75 \times 10^3 - 250 \times 10^3 + 266.67 \times 10^3 ]$	
	$\boxed{\delta_L = 0.458 \text{ mm}}$	0.1 M
e)	given data $d = 10 \text{ mm}$ $P_x = \text{axial pull} = 20 \text{ kN} = 20 \times 10^3 \text{ N}, \sigma_u = 0, q = 0$	
	$p = 20 \text{ kN}$ 	1/2 M
	i) $A = \frac{\pi}{4} \times d^2 = \frac{\pi}{4} \times 10^2 = 78.539 \text{ mm}^2$	1/2 M
	ii) $\sigma_x = \frac{P_x}{A} = \frac{20 \times 10^3}{78.539} = 254.65 \text{ N/mm}^2$	1/2 M
	$\theta = 90^\circ - 30^\circ = 60^\circ$	

Q.NO	SOLUTION	MARKS
iii>	To find normal stress ( $\sigma_n$ ) and tangential stress ( $\sigma_t$ )	
	$\sigma_n = \left( \frac{6x+6y}{2} \right) + \left( \frac{6x-6y}{2} \right) \cos 2\theta + q \cdot \sin 2\theta$ $= \left( \frac{254.65+0}{2} \right) + \left( \frac{254.65-0}{2} \right) \cos(2 \times 60^\circ) + 0$	1/2 M
	$\sigma_n = \frac{254.65}{2} + \frac{254.65-0}{2} \cos 120^\circ$	
	$\boxed{\sigma_n = 63.66 \text{ N/mm}^2 \text{ (tensile)}}$	1/2 M
	$\sigma_t = \left( \frac{6x-6y}{2} \right) \sin 2\theta - q \cdot \cos 2\theta$ $= \left( \frac{254.65-0}{2} \right) \sin(2 \times 60^\circ) - 0$	1/2 M
	$\sigma_t = \frac{254.65}{2} \sin 120^\circ$	
	$\boxed{\sigma_t = 110.266 \text{ N/mm}^2}$	1/2 M
f)	given data : $L = 3m = 3000mm$ $d = 1m = 100mm$ $t = 15mm$ , $\rho = 1.5 \text{ N/mm}^2$ $E = 2 \times 10^5 \text{ N/mm}^2$ $\mu = 0.25$	
i>	To find circumferential strain ( $e_c$ )	1/2 M
	$e_c = \frac{Pd}{4tE} (2-\mu)$	

Q.NO	SOLUTION	MARKS
	$= \frac{1.5 \times 1000}{4 \times 15 \times 2 \times 10^5} (2 - 0.25)$	1/2 M
	$e_c = 2.1875 \times 10^{-4}$	1/2 M
ii>	To find longitudinal strain ( $e_L$ )	
	$e_L = \frac{Pd}{4tE} (1 - 2\mu)$	1/2 M
	$e_L = \frac{1.5 \times 1000}{4 \times 15 \times 2 \times 10^5} (1 - 2 \times 0.25)$	1/2 M
	$e_L = 6.25 \times 10^{-5}$	01 M



i) Support reactions

$$a) \sum F_y = 0.$$

$$R_A + R_B = w \quad \text{--- (i)}$$

$$b) \sum m @ A = 0$$

$$w \times \frac{L}{2} - R_B \times L = 0.$$

$$\therefore R_B = \frac{wL}{2 \cdot L} = \frac{w}{2}.$$

$$\frac{1}{2}m$$

$$\therefore R_A = w - R_B = w - \frac{w}{2} = \frac{w}{2}.$$

$$\frac{1}{2}m$$

ii) S.F. Calculation

$$S.F. \text{ at just left of } A = 0 \quad KN$$

$$S.F. \text{ at just right of } A = R_A = \frac{w}{2} \quad KN$$

$$S.F. \text{ at just left of } C = \frac{w}{2} \quad KN$$

Q.NO	SOLUTION	MARKS
Q3a)	$S.F \text{ at just right of } C = \frac{W}{2} - W = -\frac{W}{2} \text{ KN}$	
Contd...	$S.F \text{ at just left of } B = -\frac{W}{2} \text{ KN}$	1m
	$S.F \text{ at just right of } B = -\frac{W}{2} + RB = 0 \text{ KN}$	
iii) B.M calculation	$B.M \text{ at } A = B.M \text{ at } B = 0 \text{ KN.m} \dots \text{simple support}$	
	* As the point of Concentric load is under the point load the maximum B.M will be developed under the point load i.e. at C	
	$\therefore \text{Max. B.M}_C = R_A \times \frac{L}{2} = \frac{W}{2} \times \frac{L}{2} = \frac{WL}{4} \quad \frac{1}{2} \text{ m}$	
	* The maximum shear force will be developed at the supports, due to Symmetry maximum S.F at support A & B is equal	
	Maximum S.F = $R_A \text{ or } R_B = \frac{W}{2} \quad \frac{1}{2} \text{ m}$	
Q3b)	<p>The diagram shows a horizontal beam A-B-C-D-E. At support A, there is an upward reaction of 35 KN. A downward concentrated load of 30 KN acts at point C. A downward uniformly distributed load of 15 KN/m acts over a 6m span from A to D. A downward concentrated load of 30 KN acts at point E. A horizontal dimension line between B and C is labeled 2m. A dimension line between D and E is labeled 1/2 m.</p> <p>A Shear Force Diagram (SFD) is drawn below the beam. At point A, there is a vertical jump from zero to +35 KN. From A to D, the SFD is a straight line starting at +35 KN and ending at -55 KN, with a slope of -10 KN/m. A horizontal dimension line between A and D is labeled x = 2.33m. The area under this line is marked with a plus sign (+) above the axis and a minus sign (-) below the axis. At point D, there is a vertical jump to +55 KN. From D to E, the SFD is a constant line at +55 KN. A horizontal dimension line between D and E is labeled 1/2 m. The area under this line is marked with a plus sign (+) above the axis.</p>	

Q.NO	SOLUTION	MARKS
Q3b>		
Cont...	<p>B.M.D (KN·m)</p>	$\frac{1}{2} \text{ m}$
	i) Support reaction	
a)	$\sum F_y = 0$ $R_A + R_B = (15 \times 6) + 30 = 120 \text{ KN} \quad \text{--- (i)}$	
b)	$\sum M @ A = 0$ $(15 \times 6 \times 3) + (30 \times 8) - R_B \times 6 = 0$ $510 = 6 R_B$ $\therefore R_B = 85 \text{ KN}$	1m
	$\therefore R_A = 35 \text{ KN}$	
ii) S.F. Calculation		
	S.F. at just left of A = 0 KN	
	S.F. at just right of A = $R_A = 35 \text{ KN}$	
	S.F. at just left of B = $35 - (15 \times 6) = -55 \text{ KN}$	1m
	S.F. at just right of B = $-55 + 85 = 30 \text{ KN}$	
	S.F. at just left of C = $30 \text{ KN}$	
	S.F. at just right of C = $30 - 30 = 0 \text{ KN}$	
	Let D be the point of Contact Shear.	
	from similar triangles	
	$\frac{35}{x} = \frac{55}{6-x}$	

Q.NO	SOLUTION	MARKS
Q3b		
Cont...	$\therefore x = \frac{35 \times 6}{35+55} = 2.33 \text{ m from A.}$	
	iii) B.M. Calculation	
	B.M at A = 0 simple support	
	B.M at C = 0 free end of overhang. 1M	
	B.M at D = $R_A \times 2.33 - (15 \times 2.33 \times \frac{2.33}{2})$	
	B.M at D = $40.83 \text{ KN.m}$	
	B.M at B = $R_A \times 6 - (15 \times 6 \times 3) = -60 \text{ KN.m}$	
Q3c)		1 M for S.F.D & B.M.D
	<p>i) Support reactions  <math>\therefore \sum F_y = 0; R_A = 4 + (2 \times 2) = 8 \text{ KN}</math> 1M</p>	
	<p>ii) S.F. calculation</p> <p>4 KN S.F. at just left of A = 0 KN</p> <p>S.F. at just right of A = <math>R_A = 8 \text{ KN}</math></p> <p>S.F. at just C = <math>8 \text{ KN}</math> 1M</p> <p>S.F. at just left of B = <math>8 - (2 \times 2) = 4 \text{ KN}</math></p> <p>S.F. at just right of B = <math>4 - 4 = 0 \text{ KN}</math>.</p>	
	<p>(-)   2nd degree parabola. iii) B.M. calculation.</p> <p>B.M at B = 0 --- free end.</p> <p>B.M at C = <math>-4 \times 2 - 2 \times 2 \times 1 = -12 \text{ KN.m}</math> 1M</p> <p>B.M at A = <math>-4 \times 4 - 2 \times 2 \times 3 = -28 \text{ KN.m}</math></p>	

Q.NO	SOLUTION	MARKS
Q3d)	<p>Diagram of a beam A-B. At point A, there is a vertical reaction <math>R_A = 4 \text{ kN}</math> and a horizontal reaction <math>R_A = 2 \text{ kN}</math>. There is a downward concentrated load of <math>2 \text{ kN}</math> at point C (1m from A). There is a downward distributed load of <math>1 \text{ kN/m}</math> over the last 2m of the beam (from D to B).</p>	
	<p>FBD showing the beam with applied loads. It includes a vertical reaction <math>R_A = 4 \text{ kN}</math> at A, a horizontal reaction <math>R_A = 2 \text{ kN}</math> at A, a downward concentrated load of <math>2 \text{ kN}</math> at C, and a downward distributed load of <math>1 \text{ kN/m}</math> from D to B.</p>	
	<p>S.F.D (kN)</p> <p>Diagram of the Shear Force Diagram (SFD) showing the variation of shear force along the beam. It starts at 0 at A, drops to <math>-2 \text{ kN}</math> at C, and then decreases linearly to <math>-4 \text{ kN}</math> at B. The area under the SFD is labeled <math>\text{SF.D (kN)}</math>.</p>	
	<p>B.M.D (kN.m)</p> <p>Diagram of the Bending Moment Diagram (BMD) showing the variation of bending moment along the beam. It starts at 0 at A, increases to <math>8 \text{ kN.m}</math> at C, and then follows a parabolic curve to 0 at B. The area under the BMD is labeled <math>\text{B.M.D (kN.m)}</math>.</p>	
i>	Support reaction	
ii>	$\sum F_y = 0 ; R_A = 2 + (1 \times 2) = 4 \text{ kN}$	1M
iii>	S.F. calculation	
	S.F. at left of A = 0 kN	
	S.F. at right of A = $R_A = 4 \text{ kN}$	
	S.F. at left of C = $4 \text{ kN}$	
	S.F. at right of C = $4 - 2 = 2 \text{ kN}$	1M
	S.F. at D = $2 \text{ kN}$	
	S.F. at B = $2 - (1 \times 2) = 0 \text{ kN}$	
iv>	BM calculation	
	BM at B = 0 free end	
	$BM at D = -(1 \times 2 \times 1) = -2 \text{ kN.m}$	
	$BM at C = -(1 \times 2 \times 2) = -4 \text{ kN.m}$	1M
	$BM at A = -(1 \times 2 \times 3) - (2 \times 1) = -8 \text{ kN.m}$	

Q.NO	SOLUTION	MARKS
Q3e>	 	

i> Support reactions

a>  $\sum F_y = 0$

$R_A + R_B = 5 + 7 = 12 \text{ kN}$ .

b>  $\sum M @ A = 0$

$(5 \times 1.5) + (7 \times 3.5) - 4R_B = 0$

$32 = 4R_B$

$\therefore R_B = 8 \text{ kN}$

$\therefore R_A = 12 - 8 = 4 \text{ kN}$ .

ii> S.F. Calculation

S.F at just left of A = 0

S.F at just right of A =  $R_A = 4 \text{ kN}$

S.F at just left of C = 4 kN

S.F at just right of C =  $4 - 5 = -1 \text{ kN}$ .

Q.NO	SOLUTION	MARKS
Q3e)		
Contd...	<p>S.F. at just left of D = <math>-1 \text{ kN}\cdot\text{m}</math></p> <p>S.F. at just right of D = <math>-1 - 7 = -8 \text{ kN}</math></p> <p>S.F. at just left of B = <math>-8 \text{ kN}</math></p> <p>S.F. at just right of B = <math>-8 + R_B = 0 \text{ kN}</math>.</p>	1M
	i) B.M. Calculation.	
	B.M. at A = B.M. at B = 0 ---- Simple Support	
	B.M. at C = $R_A \times 1.5 = 4 \times 1.5 = 6 \text{ kN}\cdot\text{m}$	1M
	B.M. at D = $R_A \times 3.5 - (5 \times 2) = 4 \times 3.5 - 10 = 4 \text{ kN}\cdot\text{m}$ .	
Q3f)		1M
	Given - $M.I_{AB} = 6.283 \times 10^5 \text{ mm}^4$ — (i)	
	Using parallel axis theorem $M.I_{AB}$ is given by	
	$M.I_{AB} = I_G + Ah^2 = \left[ \frac{\pi}{64} D^4 + \frac{\pi}{4} D^2 \times \left(\frac{D}{2}\right)^2 \right]$ — (ii)	1M
	$M.I_{AB} = \frac{\pi}{64} D^4 + \frac{\pi}{16} D^4 = 0.2454 D^4$ — (iii) 1M	
	Equating eqn (i) & (iii)	
	$6.283 \times 10^5 = 0.2454 D^4$	
	$D^4 = 2.56 \times 10^6$	
	$D = (2.56 \times 10^6)^{1/4}$	
	$D = 40 \text{ mm}$ 1M	
	Diameter of disc is 40mm.	

Q.NO	SOLUTION	MARKS
Q4a)	<p>Let, <math>b = 40\text{mm}</math>  <math>d = 60\text{mm}</math></p> $\frac{d}{2} = \frac{60}{2} = 30\text{mm}$	1M

M.I. about AB

By parallel axis theorem.

$$I_{AB} = I_G + A h^2$$

$$= \frac{bd^3}{12} + bd \cdot \left(\frac{d}{2}\right)^2$$

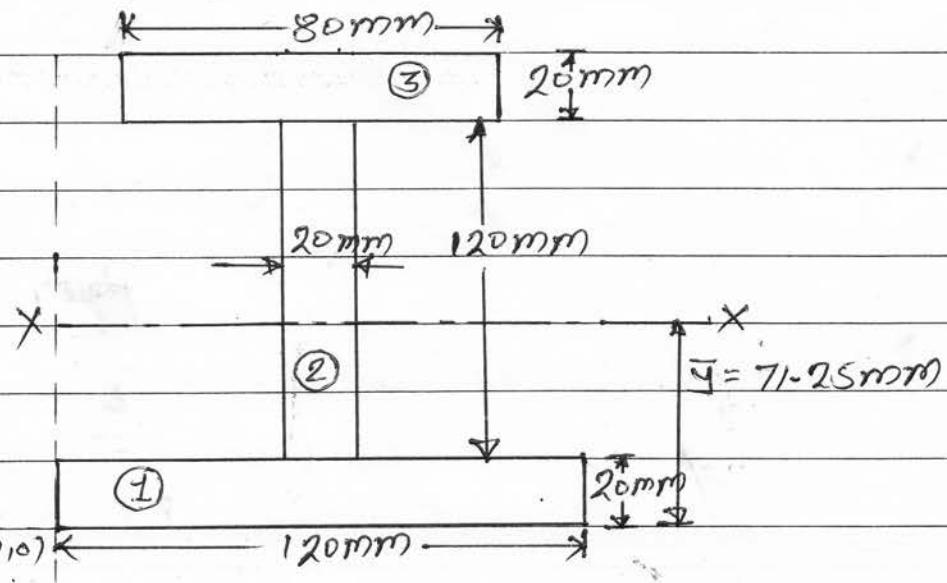
$$= \frac{40 \times 60^3}{12} + 40 \times 60 \times \left(\frac{60}{2}\right)^2$$

$$= 720 \times 10^3 + 2.16 \times 10^6$$

$$I_{AB} = 2.88 \times 10^6 \text{ mm}^4$$

M.I. of solid rectangular section about its smaller side is  $2.88 \times 10^6 \text{ mm}^4$

Q4b)



Q.NO	SOLUTION			MARKS
Q4b>	i) Position of x-x axis ( $\bar{Y}$ )			
Cont...	$a_1 = 120 \times 20$ $= 2400 \text{ mm}^2$ $x_1 = 60 \text{ mm}$ $y_1 = \frac{20}{2} = 10 \text{ mm}$	$a_2 = 120 \times 20$ $= 2400 \text{ mm}^2$ $x_2 = 60 \text{ mm}$ $y_2 = 20 + \frac{120}{2} = 80 \text{ mm}$	$a_3 = 80 \times 20$ $= 1600 \text{ mm}^2$ $x_3 = 60 \text{ mm}$ $y_3 = 20 + 120 + \frac{20}{2} = 150 \text{ mm}$	
	$\therefore \bar{Y} = \frac{a_1 y_1 + a_2 y_2 + a_3 y_3}{a_1 + a_2 + a_3}$ $= \frac{(2400 \times 10) + (2400 \times 80) + (1600 \times 150)}{2400 + 2400 + 1600}$			
	$\bar{Y} = 71.25 \text{ mm from bottom.}$			1M
	ii) M.I. about x-x by parallel axis theorem			
	$I_{xx} = I_{xx_1} + I_{xx_2} + I_{xx_3}$ $I_{xx_1} = [I_{G_1} + A_1 h_1^2] + [I_{G_2} + A_2 h_2^2] + [I_{G_3} + A_3 h_3^2]$			1M
	$I_{xx_1} = \frac{120 \times 20^3}{12} + 2400(71.25 - 10)^2 = 9.08 \times 10^6 \text{ mm}^4 \frac{1}{2} \text{ m}$			
	$I_{xx_2} = \frac{20 \times 20^3}{12} + 2400(71.25 - 80)^2 = 3.06 \times 10^6 \text{ mm}^4 \frac{1}{2} \text{ m}$			
	$I_{xx_3} = \frac{80 \times 20^3}{12} + 1600(71.25 - 150)^2 = 9.97 \times 10^6 \text{ mm}^4 \frac{1}{2} \text{ m}$			
	$\therefore I_{xx} = 9.08 \times 10^6 + 3.06 \times 10^6 + 9.97 \times 10^6$ $I_{xx} = 22.11 \times 10^6 \text{ mm}^4$			
	$\therefore \text{M.I. about x-x axis is } 22.11 \times 10^6 \text{ mm}^4 \frac{1}{2} \text{ m}$			

Q.NO	SOLUTION	MARKS
Q4C>	<p>i) Position of <math>\bar{y}</math>-<math>\bar{y}</math> axis (<math>\bar{x}\bar{e}</math>)</p> $a_1 = 115 \times 10 = 1150 \text{ mm}^2 \quad a_2 = 75 \times 10 = 750 \text{ mm}^2$ $x_1 = \frac{10}{2} = 5 \text{ mm} \quad x_2 = \frac{75}{2} = 37.5 \text{ mm}$ $\bar{x}\bar{e} = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2} = \frac{(1150 \times 5) + (750 \times 37.5)}{1150 + 750}$ $\bar{x}\bar{e} = 17.828 \text{ mm}$ <p>ii) M.I. about <math>\bar{y}</math>-<math>\bar{y}</math> is given by parallel axis theorem</p> $I_{\bar{y}\bar{y}} = I_{\bar{y}\bar{y}_1} + I_{\bar{y}\bar{y}_2}$ $I_{\bar{y}\bar{y}_1} = I_{G_1} + A_1 h_1^2 = \left[ \frac{bd^3}{12} + bcd (\bar{x}\bar{e} - x_1)^2 \right] \quad (1)$ $I_{\bar{y}\bar{y}_1} = \frac{115 \times 10^3}{12} + 1150 (17.828 - 5)^2 = 198.82 \times 10^3 \text{ mm}^4 \quad \frac{1}{2}M$ $I_{\bar{y}\bar{y}_2} = I_{G_2} + A_2 h_2^2 = \frac{10 \times 75^3}{12} + 750 (17.828 - 37.5)^2$ $I_{\bar{y}\bar{y}_2} = 641.80 \times 10^3 \text{ mm}^4 \quad \frac{1}{2}M$ $\therefore I_{\bar{y}\bar{y}} = 840.62 \times 10^3 \text{ mm}^4 \quad 1M$	

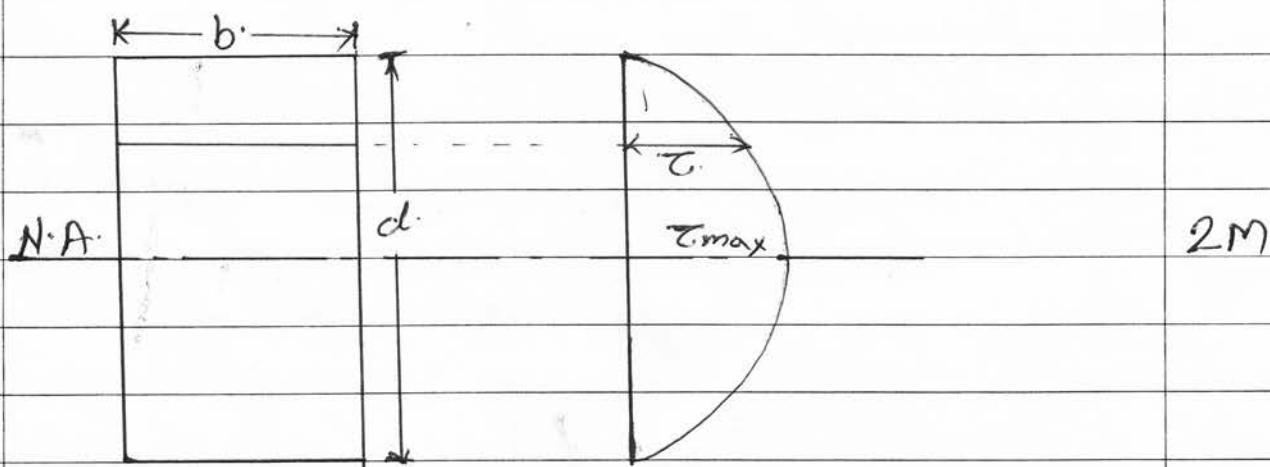
Q.NO	SOLUTION	MARKS
Q4d)	<p>Diagram of an inverted triangle section with base AB = 80mm and height BC = 60mm. A horizontal dashed line at distance <math>\frac{h}{3}</math> from the base is labeled X-X. The vertical axis is labeled Y-Y. The centroid G is at <math>\frac{h}{3}</math> from the base. The distance from the base to the line X-X is labeled 20mm.</p>	
i) M.I. about the G.G of section	$I_{xx} = \frac{bh^3}{36}$	$\frac{1}{2}m$
	$I_{xx} = \frac{80 \times 60^3}{36} = 480 \times 10^3 \text{ mm}^4$	$\frac{1}{2}m$
	$I_{yy} = \frac{hb^3}{12} \times 2 = \frac{2 \times 60 \times 40^3}{12} = 640 \times 10^3 \text{ mm}^4$	$\frac{1}{2}m$
ii) M.I. about the base of triangle.		
	$I_{AB} = \text{By parallel axis theorem}$ $= I_{G1} + Ah^2 = \frac{bh^3}{36} + \frac{1}{2} \times b \times h \times \left(\frac{h}{3}\right)^2$	
	$I_{AB} = \frac{bh^3}{36} + \frac{bh^3}{18} = \frac{bh^3}{12}$	$\frac{1}{2}m$
	$\therefore I_{AB} = \frac{80 \times 60^3}{12} = 1.44 \times 10^6 \text{ mm}^4$	$\frac{1}{2}m$
	<u>OR</u> <u>alternate solution</u>	
iii) $I_{AB} = \frac{bh^3}{12} = \frac{80 \times 60^3}{12} = 1.44 \times 10^6 \text{ mm}^4$		<u>2M</u>

Q.NO	SOLUTION	MARKS
Q4 e)	i) Bending eqn. $\frac{M}{I} = \frac{\sigma}{y} = \frac{E}{R}$	2M

ii) Moment of resistance (M.R)

The resistance offered by the moment of couple due to two equal & opposite forces to the bending moment M due to external loads is called as moment of resistance. moment of resistance is the internal moment setup in the material of the beam.

Q4 f)



Rectangular Section

Shear Stress  
distribution diagram.

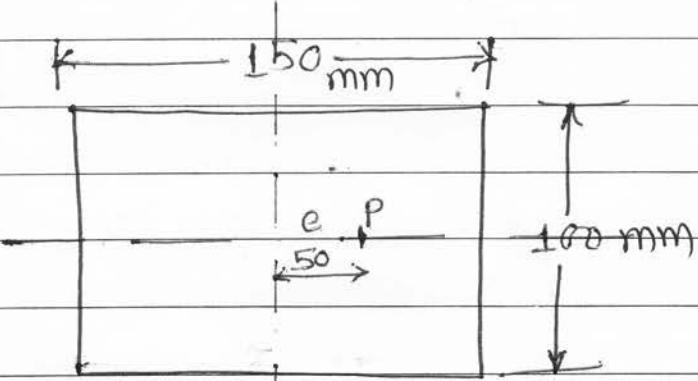
i) Relationship between maximum of avg. shear stress

$$T_{max} = \frac{3}{2} T_{avg}$$

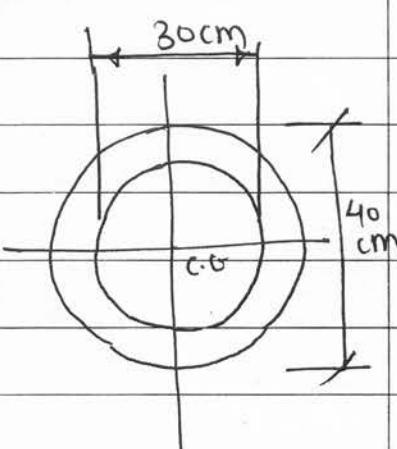
$$T_{max} = 1.5 T_{avg}$$

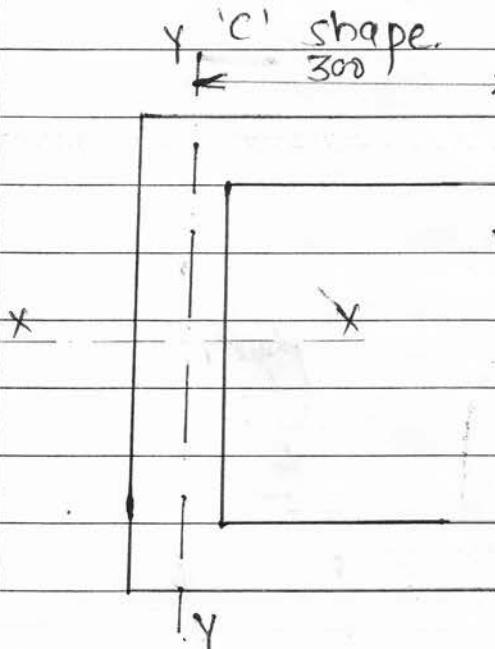
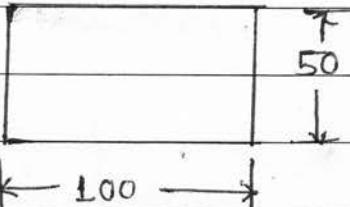
Q.NO	SOLUTION	MARKS
5-d)	<p>Given:- for rectangular beam</p> <p><math>b = 100\text{mm}</math>, <math>d = 150\text{mm}</math></p> <p><math>L = 2\text{m}</math>, <math>\sigma_b = \text{Maximum bending stress} = 28\text{N/mm}^2</math></p> <p><math>\tau_{max} = \text{shear stress} = 2\text{N/mm}^2</math></p> <p>To find:- Intensity of 'udl' i.e. Maximum load supported by beam in <math>\text{N/m}</math>.</p> <p>soln:- <math>\frac{M}{I} = \frac{\sigma_b}{Y}</math> <span style="float: right;"><math>\frac{1}{2}M</math></span></p> <p><math>M = \text{Maximum bending moment}</math>  <math>= \frac{wL^2}{8}</math> → Assuming beam as simply supported beam</p> <p><math>M = \frac{w \times (2)^2}{8} = 0.5w\text{Nm}</math></p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>M = 0.5w \times 10^3 \text{ N-mm}</math> </div> <span style="float: right;"><math>\frac{1}{2}M</math></span> <p><math>I = \frac{bd^3}{12} = \frac{100 \times (150)^3}{12} = 28.125 \times 10^6 \text{ mm}^4</math> <span style="float: right;"><math>\frac{1}{2}M</math></span></p> <p><math>Y = d/2 = \frac{150}{2} = 75\text{mm}</math> <span style="float: right;"><math>\frac{1}{2}M</math></span></p> <p><math>\therefore \frac{M}{I} = \frac{\sigma_b}{Y}</math></p> <p><math>\frac{0.5w \times 10^3}{28.125 \times 10^6} = \frac{28}{75}</math> <span style="float: right;">01M</span></p> <p><math>w = \frac{28 \times 28.125 \times 10^6}{0.5 \times 10^3 \times 75}</math></p> <p><math>w = 21000 \text{ N/m}</math></p> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>w = 21\text{kN/m}</math> </div> <span style="float: right;">→ Ans. (udl)</span> <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>w = 21 \times 2 = 42\text{kN}</math> </div> <span style="float: right;">→ (load)</span> <span style="float: right;">01M</span>	

Q.NO	SOLUTION	MARKS
5-b	Given:- $d = \text{diameter of shaft}$ i.e. circular section $d = 80\text{mm}$ .	
	To find:- limit of eccentricity 'e'	
	<u>Solution:-</u> We know that	
	$G_o = G_b$	1/2 M
	$\frac{P}{A} = \frac{M}{Z}$	1/2 M
	$\frac{P}{A} = \frac{Pe}{Z}$	
	$\frac{1}{A} = \frac{e}{Z}$	
	$e = \frac{Z}{A}$	1/2 M
	$e = \frac{\pi d^3}{32 \times \frac{\pi}{4} d^2}$	1/2 M
	$= \frac{\pi}{328} \times \frac{d^3}{1} \times \frac{4}{\pi} \times \frac{1}{d^2}$	
	$e = \frac{d}{8}$	01 M
	$e = \frac{80}{8}$	
	$e = 10\text{mm}$ <span style="border: 1px solid black; padding: 2px;">→ Ans.</span>	01 M

Q.NO	SOLUTION	MARKS
5-C	<u>Given:-</u> for a rectangular column	
	 <p>b = width of plate = 150mm      d = thickness of column = 100mm      P = <math>150 \times 10^3</math> N, load      e = eccentricity = 50mm</p>	
	<u>To find</u> : (i) Maximum stress intensity ( $\sigma_{max}$ ) (ii) Minimum stress intensity ( $\sigma_{min}$ )	
	<u>Sol<sup>n</sup></u> :- We know that,	
	$\sigma_{max} = \sigma_o + \sigma_b$	1/2 M
	$\sigma_{min} = \sigma_o - \sigma_b$	1/2 M
	$\sigma_o = \frac{P}{A} = \frac{150 \times 10^3}{100 \times 150}$ $= \frac{150 \times 10^3}{150 \times 100}$	
	$\sigma_o = 100 \text{ N/mm}^2$	1/2 M

Q.NO	SOLUTION	MARKS
	$M = M_{yy} = Pe$ $= 150 \times 10^3 \times 50$ $[M = 7.5 \times 10^6 \text{ N-mm}]$	1/2 M
	$I = I_{yy}$ $= \frac{\pi b^4}{6}$ $= \frac{100 \times (150)^4}{6}$ $[I = 375 \times 10^3 \text{ mm}^3]$	1/2 M
	$\sigma_b = \frac{M}{I} = \frac{M_{yy}}{I_{yy}}$ $= \frac{7.5 \times 10^6}{375 \times 10^3}$ $[\sigma_b = 20 \text{ N/mm}^2]$	1/2 M
	$\therefore \sigma_{max} = \sigma_o + \sigma_b$ $= 10 + 20$ $[\sigma_{max} = 30 \text{ N/mm}^2] \rightarrow \text{compressive nature.}$	1/2 M
	$\sigma_{min} = \sigma_o - \sigma_b$ $= 10 - 20$ $[\sigma_{min} = -10 \text{ N/mm}^2] \text{ i.e. tensile nature}$	1/2 M

Q.NO	SOLUTION	MARKS
5-d)	Given:- for circular column $D = \text{External diameter} = 40\text{ cm} = 400\text{ mm}$ $d = \text{Internal diameter.} = 30\text{ cm} = 300\text{ mm}$ $P = 150 \times 10^3 \text{ N} = \text{load}$	
	To find:- ① $\sigma_{max}$ ② $\sigma_{min}$	
	sol:- We know that	
		
	$\sigma_{max} = \sigma_o + \sigma_b$	
	$\sigma_{min} = \sigma_o - \sigma_b$	
	$\sigma_o = \frac{P}{A} = \frac{150 \times 10^3}{\pi \times \frac{(400^2 - 300^2)}{4}} \quad \frac{1}{2}\text{M}$	
	$\sigma_o = 2.7283 \text{ N/mm}^2 \quad \frac{1}{2}\text{M}$	
	$\sigma_b = \frac{M}{Z} = \frac{M}{I/Y} \quad \frac{1}{2}\text{M}$	
	$= \frac{My}{I}$	
	$= \frac{P \times e \times D/2}{\frac{\pi}{64} \times (D^4 - d^4)} \quad \frac{1}{2}\text{M}$	
	$= \frac{150 \times 10^3 \times 200 \times (400/2)}{\frac{\pi}{64} \times (D^4 - d^4)} \quad \frac{1}{2}\text{M}$	

Q.NO	SOLUTION	MARKS
	$\sigma_b = \frac{150 \times 10^3 \times 200 \times 200}{859.029 \times 10^6}$ $\sigma_b = 6.9846 \text{ N/mm}^2$	
		1/2 M
	$\sigma_{max} = \sigma_c + \sigma_b$ $= 2.728 + 6.984$ $\sigma_{max} = 9.7126 \text{ N/mm}^2$	$\rightarrow$ compressive in Nature 1/2 M
	$\sigma_{min} = \sigma_c - \sigma_b$ $= 2.728 - 6.984$ $\sigma_{min} = -4.256 \text{ N/mm}^2$	$\rightarrow$ Tensile in Nature. 1/2 M
5-e)	Given: - for a rectangular rod bent into 'c' shape. 	
		

Q.NO	SOLUTION	MARKS
5-e	$b = 100 \text{ mm}$	
Continues	$d = 50 \text{ mm}$	
	$P = 40 \text{ kN} = 40 \times 10^3 \text{ N}$	
	$e = 300 \text{ mm}$	
	To find:- Resultant along X-X.	
	Solution:- $\sigma_{\max} = \sigma_a + \sigma_b$	
	$\sigma_{\min} = \sigma_a - \sigma_b$	
	$\sigma_a = \frac{P}{A} = \frac{40 \times 10^3}{(100 \times 50)}$	
	$\boxed{\sigma_a = 8 \text{ N/mm}^2}$	1/2 M
	$M = Pe$ $= 40 \times 10^3 \times 300$	
	$\boxed{M = 12 \times 10^6 \text{ mm}^3}$	1/2 M
	$y = \frac{100}{2} = 50 \text{ mm}$	
	$I = \frac{db^3}{12} = \frac{50 \times (100)^3}{12}$	1/2 M
	$\boxed{I = 4.166 \times 10^6 \text{ mm}^4}$	1/2 M
	$\sigma_b = \frac{My}{I} = \frac{12 \times 10^6 \times 50}{4.166 \times 10^6}$	1/2 M
	$\boxed{\sigma_b = 144 \text{ N/mm}^2}$	1/2 M

Q.NO	SOLUTION	MARKS
	$\sigma_{max} = \sigma_0 + \sigma_b$ $= 8 + 144$ $= 152 \text{ MPa}$	
	$\sigma_{max} = 152 \text{ MPa}$ <span style="border: 1px solid black; padding: 2px;"> </span> $\rightarrow \text{'Tension'}$	$\frac{1}{2} M$
	$\sigma_{min} = \sigma_0 - \sigma_b$ $= 8 - 144$ $\sigma_{min} = -136$	
	$\sigma_{min} = -136 \text{ MPa}$ <span style="border: 1px solid black; padding: 2px;"> </span> $\rightarrow \text{compression}$	$\frac{1}{2} M$
	<p>As rod is bent into 'c' shape, it is tension member so tension is considered as +ve and compression is taken as -ve.</p>	
	<p>Resultant stresses developed at section XX.</p>	
	$\sigma_{max} = 152 \text{ MPa}$ $\sigma_{min} = 136 \text{ MPa}$	
5+>	Given:- for rectangular cross section	
		01 M

Q.NO	SOLUTION	MARKS
	To find:- Limit of eccentricity solution:- Case-I : load along x-axis	
	$6_0 = 6_b$	
	$\frac{P}{bd} = \frac{Pe}{db^2/6}$	1/2 M
	$\frac{P}{bd} = \frac{6Pe}{db^2}$	
	$\frac{P}{bd} = \frac{6Pe}{db^2}$	
	$I = \frac{6e}{b}$	
	$e = b/6$	1/2 M
	$= 1000/6$	
	$e = 166.66 \text{ mm}$	1/2 M
	Case-II : - load along Y-axis	along X-axis
	$6_0 = 6_b$	
	$\frac{P}{bd} = \frac{Pe}{bd^2/6}$	1/2 M
	$\frac{P}{bd} = \frac{6Pe}{bd^2}$	
	$\frac{P}{bd} = \frac{6Pe}{bd^2}$	
	$I = \frac{6e}{d}$	
	$e = d/6$	1/2 M
	$e = 2000/6 = 333.33 \text{ mm}$	1/2 M
	along Y axis	

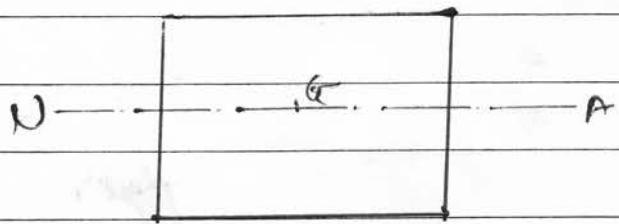
Q.NO	SOLUTION	MARKS
6-a)	Assumptions of Pure torsion are, 1) The shaft material is homogeneous & isotropic (1 M for each any four) 2) The shaft is straight having uniform cross-section 3) The shaft is acted upon by pure torsion 4) shear stress is directly proportional to shear strain. 5) section plane before twisting moment will remain plane even after application of twisting moment.	(01x4)
6-b)	<u>Given</u> :- for a shaft, used to transmit power $P = 20kW = 20 \times 10^3 W$ $N = 150 \text{ rpm}$ $T_{max} = \text{Maximum torque} = 40\% \text{ of } T_{ave}$ $= 0.4 + T_{ave}$ $\boxed{T_{max} = 1.4 T_{ave}}$	1/2 M
	$\tau = 50 \text{ MPa} = 50 \text{ N/mm}^2$	
	<u>To find</u> :- diameter of shaft	
	<u>Solution</u> :- $P = \frac{2\pi P T_{ave}}{60}$	1/2 M
	$20 \times 10^3 = 2\pi \times 150 \times T_{ave}$	
	$T_{ave} = \frac{1.273 \times 10^3}{60} \text{ N-mm}$ $\boxed{T_{ave} = 1.273 \times 10^6 \text{ N-mm}}$	1/2 M

Q.NO	SOLUTION	MARKS
	$T_{max} = 1.4 \text{ Tare}$	
	$T_{max} = 1.4 \times 1.273 \times 10^6$	
	$T_{max} = 1.782 \times 10^6 \text{ Nm}$	01 M
	$1.782 \times 10^3 = \frac{\pi}{16} \times I \times D^3$	1/2 M
	$= \frac{\pi}{16} \times 50 \times D^3$	
	$D = 56.63 \text{ mm}$	→ Ans 01 M
Q-6C)	Given:- for a shaft	
	$d = 40 \text{ mm} = \text{diameter of shaft}$	
	$N = 2000 \text{ rpm}$	
	$T = \text{shear stress} = 85 \text{ MPa}$ $= 85 \text{ N/mm}^2$	
	To find :- Power transmitted by shaft	
	<u>Solution:-</u> $P = \frac{2\pi N T}{60}$	1/2 M
	$T = \frac{\pi}{16} \times I \times (D)^3$ $= \frac{\pi}{16} \times 85 \times (40)^3$ $= 1.068 \times 10^6 \text{ N-mm}$	1/2 M
	$T = 1.068 \times 10^3 \text{ Nm}$	01 M
	$P = \frac{2\pi \times 200 \times 1.068 \times 10^3}{60}$	01 M
	$P = 22.37 \times 10^3 \text{ W}$ $P = 22.37 \text{ kW}$	→ Ans 01 M

Q.NO	SOLUTION	MARKS
6-d)	<p><u>Given:-</u> for a shaft</p> <p><math>P = \text{Power transmitted} = 150 \text{ kW}</math></p> <p><math>P = 150 \times 10^3 \text{ W}</math></p> <p><math>N = 200 \text{ rpm}</math></p> <p><math>T = \text{shear stress} = 80 \text{ N/mm}^2</math></p> <p><math>\theta = \text{Angle of twist} = 1.5^\circ</math></p> <p><math>= \frac{1.5 \times \pi}{180} = 0.02167 \text{ radians.}</math></p> <p><math>L = \text{Length of shaft} = 4 \text{ m}</math>  <math>= 4000 \text{ mm}</math></p> <p><u>G = Modulus of rigidity</u>  <math>= 0.8 \times 10^5 \text{ N/mm}^2</math></p>	
	<p><u>To find :-</u> Diameter of shaft</p> <p><u>solution :-</u> ① On the basis of strength</p>	
	$T = \frac{\pi}{16} \times G \times D^3$ $P = \frac{2\pi N T}{60}$ $150 \times 10^3 = \frac{2\pi \times 200 \times T}{60}$ $T = 7.16 \times 10^3 \text{ Nm}$ $\boxed{T = 7.16 \times 10^6 \text{ Nmm}}$	$\frac{1}{2} M$ $\frac{1}{2} M$ $\frac{1}{2} M$ $\frac{1}{2} M$
	$7.16 \times 10^6 = \frac{\pi}{16} \times 80 \times D^3$ $D = \frac{(7.16 \times 10^6)}{(C\pi/16 \times 80)} = 76.9669$ $\boxed{D = 76.97 \text{ mm}}$	$\frac{1}{2} M$ $\frac{1}{2} M$

Q.NO	SOLUTION	MARKS
	② On the basis of angle of twist i.e. stiffness	
	$\frac{T}{J} = \frac{G\theta}{L}$	1/2 M
	$\frac{T}{\frac{\pi/32 \times D^4}{L}} = \frac{G\theta}{L}$	
	$\frac{7.16 \times 10^6}{\frac{\pi \times D^4}{32}} = \frac{0.8 \times 10^3 \times 0.0261}{4000}$	
	$D^4 = \frac{7.16 \times 10^6 \times 32 \times 4000}{0.8 \times 10^3 \times 0.0261 \times \pi}$	1/2 M
	$= \frac{9.1648 \times 10^{11}}{6.5596 \times 10^3}$	
	$D^4 = 139.71 \times 10^6$	
	$D = 108.72 \text{ mm}$	1/2 M
	larger of above two values, for diameter is taken as suitable diameter	
	$\therefore D = 108.72 \text{ mm}$	→ Ans.

Q.NO	SOLUTION	MARKS
6-e)	<p><u>Given</u> - <math>D = \text{External diameter} = 400\text{mm}</math></p> <p><math>d = \text{Internal diameter} = 200\text{mm}</math></p> <p><math>T = \text{Twisting moment} = 4650\text{Nm}</math>  <math>= 4650 \times 10^3 \text{D-mm}</math></p> <p><math>G = \text{Modulus of rigidity} = 82 \times 10^3 \text{N/mm}^2</math></p> <p><math>L = 20D</math>  <math>= 20 \times 400 = 8000\text{mm}</math></p>	
	<p><u>To find</u></p> <ol style="list-style-type: none"> <li>Maximum intensity of stress</li> <li>Angle of twist</li> </ol>	
	<p><u>Solution</u>:-</p> <ol style="list-style-type: none"> <li>Maximum intensity of stress</li> </ol> $\frac{T}{J} = \frac{T_{max}}{R}$ $J = \frac{\pi}{32} \times (D^4 - d^4)$ $= \frac{\pi}{32} \times (400^4 - 200^4)$ $J = 2,3561 \times 10^9 \text{ mm}^4$ <p style="border: 1px solid black; padding: 5px;">→ Polar M.I.</p>	1/2 M
	$R = D/2 = \frac{400}{2} = 200\text{mm}$	1/2 M
	$\frac{4650 \times 10^3}{2,3561 \times 10^9} = \frac{T_{max}}{200}$ $T_{max} = \frac{4650 \times 10^3 \times 200}{2,3561 \times 10^9}$ $T_{max} = 0.3947 \text{ N/mm}^2$	1/2 M

Q.NO	SOLUTION	MARKS
	(ii) Angle of twist	
	$\frac{T}{J} = \frac{G\alpha}{L}$	1 M
	$\frac{4650 \times 10^3}{2.3561 \times 10^9} = \frac{82.72 \times 10^3 \times \alpha}{8000}$	
	$\alpha = \frac{4650 \times 10^3 \times 8000}{2.3561 \times 10^9}$	1 M
	$= 1.9254 \times 10^{-4}$	
	$\boxed{\alpha = 1.9254 \times 10^{-4} \text{ radians}}$	
	$= 1.9254 \times \frac{180}{\pi}$	
	$\boxed{\alpha = 0.011^\circ}$	0.1 M
6-f-i)	Neutral Axis	
	- When beam is subjected to pure bending there is a layer which will neither be subjected to tension nor compression, such a layer is called neutral layer or neutral axis (N-A)	
		
	- Neutral Axis always passes through centroid or C.G.	0.2 M

Q.NO	SOLUTION		MARKS
6f-ii)	Comparison between solid shaft & hollow shaft		
	for Parameter	Solid shaft	Hollow shaft
1	Polar MI	$J = \frac{\pi}{32} \times (D)^4$	$\frac{\pi}{32} \times (D^4 - d^4)$ (01M) for any two)
2	Polar modulus	$Z = \frac{\pi}{16} \times D^3$	$\frac{\pi}{16} \times (D^4 - d^4)$
3	Toque Toadsmitted	$T = \frac{\pi}{16} \times T \times D^3$	$T = \frac{\pi}{16} \times T \times \left(\frac{D^4 - d^4}{D}\right)$ (01x02)
4	stiffness	Solid shaft has less strength & stiffness than a hollow shaft	Hollow shaft has greater strength & stiffness than a solid shaft