

What is a marginal distribution?

$$\mu_n(i) = P(X_n = i)$$

↑  
prob.

Meaning:

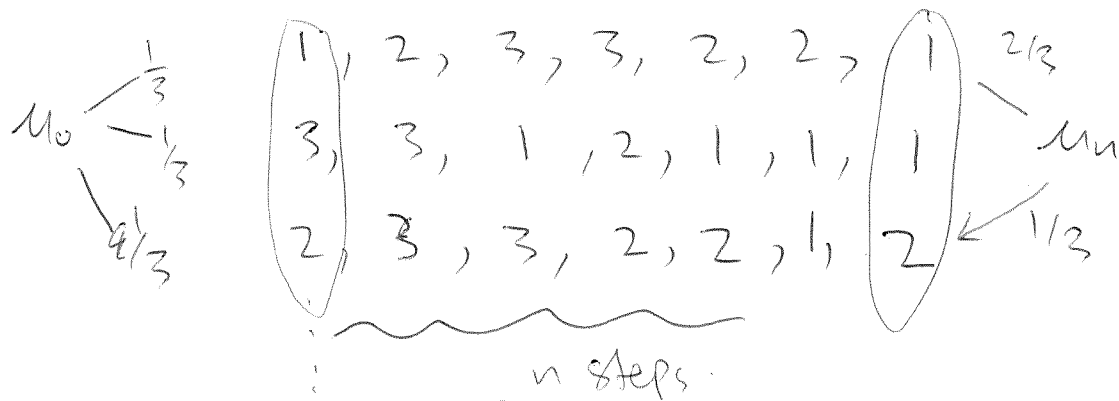
$$\mu_n = \mu_0 P^n$$

matrix

← use this

Interpretation  
(intuition)

Realisations



lots of realisations

$$\mu_0 = (\frac{1}{3} \ \frac{1}{3} \ \frac{1}{3})$$

$$X = 1 \quad 2 \quad 3$$

prob. of starting from each state.

$$\xrightarrow{P^n}$$

$$\mu_n = (\frac{2}{3}, \frac{1}{3}, 0)$$

$$X = (1 \ 2 \ 3)$$

prob. of being in each state after n steps

Expected Value.

$X =$	1	2	3	4	5
$V =$	1	5	3	2	10
$\pi =$	$\frac{1}{10}$	$\frac{2}{10}$	$\frac{3}{10}$	$\frac{3}{10}$	$\frac{1}{10}$

$$E[V] = \pi V^T = 1 \times \frac{1}{10} + 5 \times \frac{2}{10} + 3 \times \frac{3}{10} + \dots$$

$$\begin{bmatrix} \frac{1}{10} & \frac{2}{10} & \frac{3}{10} \\ \frac{1}{10} & \frac{2}{10} & \frac{3}{10} \\ \frac{1}{10} & \frac{2}{10} & \frac{3}{10} \end{bmatrix}$$

$$X = \begin{matrix} 1 & 2 & 3 \\ \hline \mu_0 = (\frac{1}{5} & \frac{2}{5} & \frac{2}{5}) \end{matrix}$$

prob. "array"

$$\mu_0 = (1 \ 0 \ 0)$$