AIN SHAMS UNIVERSITY
FACULTY OF ENGINEERING
CREDIT HOURS ENGINEERING PROGRAMS
SOPHOMORE (All Programs)

Fall 2022 | **Major Task (Part 1)** | **Total: 15 marks**

PHM111: Probability and Statistics

1/18

Name: **ID:** **Deadline: Week 7**

Please, Solve each problem in its assigned place ONLY (the empty space below it)

Statistics

Part I

1. Name and define the two areas of statistics.

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2. Why are samples used in statistics?

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3. In each of these statements, tell whether descriptive or inferential statistics have been used:

a. In the year 2030, 148 million Americans will be enrolled in an HMO. (……..)

b. Nine out of ten on-the-job fatalities are men. (……..)

c. The median household income for people aged 25–34 is $35,888. (……..)

4. Classify each variable as qualitative or quantitative:

a) Number of bicycles sold in 1 year by a large sporting goods store. (……..)
b) Classification of children in a day care center (infant, toddler, preschool) (……)
c) Weights of fish caught in Lake George. (……..)
d) Marital status of faculty members in a large university. (……..)

5. Classify each variable as discrete or continuous:

a) Water temperatures of six swimming pools in Pittsburgh on a given day. (……..)
b) Weights of cats in a pet shelter. (……..)
c) Number of cheeseburgers sold each day by a hamburger stand on a college campus. (……..)
d) Number of DVDs rented each day by a video store. (……..)

6. Name the four basic sampling methods.

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7. Classify each sample as random, systematic, stratified, or cluster:

a) In a large school area, all teachers from two buildings are interviewed to determine whether they believe the students have less homework to do now than in previous years. (……)

b) Every seventh customer entering a shopping mall is asked to select her or his favorite store. (……)

Part II

1. Name the three types of frequency distributions and explain when each should be used.

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2. The following two frequency distributions are incorrectly constructed. State the reason why.

a.

Class	Frequency
27–32	1
33–38	0
39–44	6
45–49	4
50–55	2

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b.

Class	Frequency
123–127	3
128–132	7
138–142	2
143–147	19

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3. Shown here are the number of inches of rain received in 1 year in 25 selected cities in the United States. Construct a grouped frequency distribution and a cumulative frequency distribution with 6 classes.

6	37	14	45	22	32	33	49	55
94	38	83	85	40	67	36	67	
71	52	52	55	63	49	44	58	

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Class	Class limits	Class boundaries	Frequency	Cumulative Frequency
1				
2				
3				
4				
5				
6				

4. Do Students Need Summer Development? For 108 randomly selected college applicants, the following frequency distribution for entrance exam scores was obtained. Construct a histogram, frequency polygon, and ogive for the data.

Class	Class limits	Class boundaries	Frequency	Cumulative Frequency
1	90–98		6	
2	99–107		22	
3	108–116		43	
4	117–125		28	
5	126–134		9	

Applicants who score above 107 need not enroll in a summer developmental program. In this group, how many students do not have to enroll in the developmental program?

Histogram:

Frequency Polygon:

Ogive:

5. The math and reading achievement scores from the National Assessment of Educational Progress for selected states are listed below. Construct a back-to back stem and leaf plot with the data.

Math					Reading				
52	66	69	62	61	65	76	76	66	67
63	57	59	59	55	71	70	70	66	61
55	59	74	72	73	61	69	78	76	77
68	76	73			77	77	80		

Stem	Leaf

6. The state gas tax in cents per gallon for 25 states is given below. Construct a grouped frequency distribution and a cumulative frequency distribution with 5 classes.

7.5	16	23.5	17	22
21.5	19	20	27.1	20
22	20.7	17	28	20
23	18.5	25.3	24	31
14.5	25.9	18	30	31.5

Class	Class limits	Class boundaries	Frequency	Cumulative Frequency
1				
2				
3				
4				
5				

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Part III

1. The average undergraduate grade point average (GPA) for the 25 top-ranked medical schools is listed below.

3.80	3.77	3.70	3.74	3.70
3.86	3.76	3.68	3.67	3.57
3.83	3.70	3.80	3.74	3.67
3.78	3.74	3.73	3.65	3.66
3.75	3.64	3.78	3.73	3.64.

Find the mean, the median, the mode, and the midrange.

Data in ascending order

Mean =			
Median =			
Mode =		**Midrange =**	

2. For the following data, construct a grouped frequency distribution with six classes then find the mean and modal class.

1013 1867 1268 1666 2309 1231 3005 2895 2166 1136
1532 1461 1750 1069 1723 1827 1155 1714 2391 2155
1412 1688 2471 1759 3008 2511 2577 1082 1067 1062
1319 1037 2400.

Class	Class limits	Class boundaries	Frequency	Cumulative Frequency
1				
2				
3				
4				
5				
6				

The mean =……..

The modal class =……..

3. Find the weighted mean price of three models of automobiles sold. The number and price of each model sold are shown in this list.

Model	Number	Price
A	8	$10,000
B	10	12,000
C	12	8,000.

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4. An instructor grades exam, 20%; term paper, 30%; final exam, 50%. A student had grades of 83, 72, and 90, respectively, for exams, term paper, and final exam. Find the student's final average. Use the weighted mean.

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5. Calculate the median from the following data:

Group	**Frequency**			
60 – 64	**1**			
65 – 69	**5**			
70 – 74	**9**			
75 – 79	**12**			
80 – 84	**7**			
85 – 89	**2**			

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6. Calculate the mode from the following data:

Group	**Frequency**			
150 - 154	5			
155 - 159	2			
160 - 164	6			
165 - 169	8			
170 - 174	9			
175 - 179	11			
180 - 184	6			
185 - 189	3			

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7. For these situations, state which measure of central tendency (mean, median, or mode) should be used.

a) The most typical case is desired. (……..)
b) The data are categorical. (……..)
c) The values are to be divided into two approximately equal groups, one group containing the larger values and one containing the smaller values. (……..)

8. Describe which measure of central tendency—mean, median, or mode—was probably used in each situation.

a) The average number of children per family in the Plaza Heights Complex is 1.8. (……..)
b) Most people prefer red convertibles over any other color. (……..)
c) The average age of college professors is 42.3 years. (……..)

Part IV

1. Find the range, variance, and standard deviation. Assume the data represent samples, and use the shortcut formula for the unbiased estimator to compute the variance and standard deviation:

The normal daily high temperatures (in degrees Fahrenheit) in January for 10 selected cities are as follows:

50, 37, 29, 54, 30, 61, 47, 38, 34, 61

The normal monthly precipitation (in inches) for these same 10 cities is listed here:

4.8, 2.6, 1.5, 1.8, 1.8, 3.3, 5.1, 1.1, 1.8, 2.5

Which set is more variable?

For normal daily high temperatures:

n	***X***			
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

……

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For normal monthly precipitation:

n	***X***			
1				
2				
3				
4				
5				
6				
7				
8				
9				
10				

……

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The more variable set is……

Because……..

2. Team batting averages for major league baseball in 2005 are represented below. Find the variance and standard deviation for each league.

NL		**AL**	
0.252–0.256	4	0.256–0.261	2
0.257–0.261	6	0.262–0.267	5
0.262–0.266	1	0.268–0.273	4
0.267–0.271	4	0.274–0.279	2
0.272–0.276	1	0.280–0.285	1

For NL:

Class limits	*Class boundaries*				

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For AL:

Class limits	*Class boundaries*				

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3. The average age of senators in the 108th Congress was 59.5 years. If the standard deviation was 11.5 years, find the *z* scores corresponding to the oldest and youngest senators: Robert C. Byrd (D, WV), 86, and John Sununu (R, NH), 40.

For Robert C. Byrd:

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For John Sununu:

……

……

4. The average teacher's salary in a particular state is $54,166. If the standard deviation is $10,200, find the salaries corresponding to the following *z* scores.

a. 2 *b.* -1 *c.* 0

a- .....

b- .....

c- .....

5. Find the percentile rank for each value in the data set. The data represent the values in billions of dollars of the damage of 10 hurricanes.

1.1, 1.7, 1.9, 2.1, 2.2, 2.5, 3.3, 6.2, 6.8, 20.3.

1.1 is .....

1.7 is .....

1.9 is .....

2.1 is .....

2.2 is .....

2.5 is .....

3.3 is .....

6.2 is .....

6.8 is .....

20.3 is .....

6. check each data set for outliers.

a. 24, 32, 54, 31, 16, 18, 19, 14, 17, 20

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b. 321, 343, 350, 327, 200

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7. identify the five-number summary and find the interquartile range.

19, 16, 48, 22, 7

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8. Construct a boxplot for the following data representing the number of games pitched by major league baseball's earned run average (ERA) leaders for the past few years.

30, 34, 29, 30, 34, 29, 31, 33, 34, 27, 30, 27, 34, 32.

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The Box Plot:

9. Starting teacher salaries (in equivalent U.S. dollars) for upper secondary education in selected countries are listed below. Which set of data is more variable? (The U.S. average starting salary at this time was $29,641.)

Europe		**Asia**	
Sweden	$48,704	Korea	$26,852
Germany	41,441	Japan	23,493
Spain	32,679	India	18,247
Finland	32,136	Malaysia	13,647
Denmark	30,384	Philippines	9,857
Netherlands	29,326	Thailand	5,862
Scotland	27,789		

For Europe:

n	***X***			
1				
2				
3				
4				
5				
6				
7				

……

……

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For Asia:

n	***X***			
1				
2				
3				
4				
5				
6				

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The more variable set is……

Because……

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Name: **ID:** **14/18**

Classical Probability, Counting Techniques, Conditional Probability

Part I

1. An experiment involves tossing a pair of dice, one green and one red, and recording the numbers that come up. If x equals the outcome on the green die and y the outcome on the red die, describe the sample space S

(a) by listing the elements (x, y);

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(b) by using the rule method.

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2. For the sample space of Exercise 1,

(a) list the elements corresponding to the event A that the sum is greater than 8;

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……

(b) list the elements corresponding to the event B that a 2 occurs on either die;

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(c) list the elements corresponding to the event C that a number greater than 4 comes up on the green die;

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(d) list the elements corresponding to the event $A \cap C$;

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(e) list the elements corresponding to the event $A \cap B$;

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……

(f) list the elements corresponding to the event $B \cap C$;

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……

(g) construct a Venn diagram to illustrate the intersections and unions of the events A, B and C.

3. An experiment consists of tossing a die and then flipping a coin once if the number on the die is even. If the number on the die is odd, the coin is flipped twice. Construct a tree diagram to show the 18 elements of the sample space *S*. then:

(a) list the elements corresponding to the event *A* that a number less than 3 occurs on the die;

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(b) list the elements corresponding to the event *B* that two tails occur;

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(c) list the elements corresponding to the event A';

……

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(d) list the elements corresponding to the event $A' \cap B$;

……

……

(e) list the elements corresponding to the event $A \cup B$.

……

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4. If $S = \{x \mid 0 < x < 12\}$, $M = \{x \mid 1 < x < 9\}$, and $N = \{x \mid 0 < x < 5\}$, find

(a) $M \cup N$;

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(b) $M \cap N$;

……

……

(c) $M' \cap N'$

……

……

5. (a) How many three-digit numbers can be formed from the digits 0, 1, 2, 3, 4, 5, and 6 if each digit can be used only once?

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(b) How many of these are odd numbers?

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(c) How many are greater than 330?

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6. Three lottery tickets for first, second, and third prizes are drawn from a group of 40 tickets. Find the number of sample points in *S* for awarding the 3 prizes if each contestant holds only 1 ticket.

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7. How many ways are there to select 3 candidates from 8 equally qualified recent graduates for openings in an accounting firm?

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Part II

1. A box contains 500 envelopes, of which 75 contain $100 in cash, 150 contain $25, and 275 contain $10. An envelope may be purchased for $25. What is the sample space for the different amounts of money? Assign probabilities to the sample points and then find the probability that the first envelope purchased contains less than $100.

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2. A pair of fair dice is tossed. Find the probability of getting

(a) a total of 8;

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(b) at most a total of 5.

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3. In a high school graduating class of 100 students, 54 studied mathematics, 69 studied history, and 35 studied both mathematics and history. If one of these students is selected at random, find the probability that:

(a) the student took mathematics or history;

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(b) the student did not take either of these subjects;

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(c) the student took history but not mathematics.

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4. In an experiment to study the relationship of hypertension and smoking habits, the following data are collected for 180 individuals:

	Nonsmokers	Moderate Smokers	Heavy Smokers
H	21	36	30
NH	48	26	19

where *H* and *NH* in the table stand for *Hypertension* and *Non-hypertension*, respectively. If one of these individuals is selected at random, find the probability that the person is

(a) experiencing hypertension, given that the person is a heavy smoker;

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……

(b) a nonsmoker, given that the person is experiencing no hypertension.

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5. Pollution of the rivers in the United States has been a problem for many years. Consider the following events:

A: the river is polluted,

B: a sample of water tested detects pollution,

C: fishing is permitted.

Assume

$P(A) = 0.3,\ P(B \mid A) = 0.75,\ P(B \mid A') = 0.20,\ P(C \mid A \cap B) = 0.20,$

$P(C \mid A' \cap B) = 0.15,\ P(C \mid A \cap B') = 0.80,\ P(C \mid A' \cap B') = 0.90.$

(a) Find $P(A \cap B \cap C)$.

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……

(b) Find $P(B' \cap C)$.

……

……

(c) Find $P(C)$.

……

……

(d) Find the probability that the river is polluted, given that fishing is permitted, and the sample tested did not detect pollution.

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6. Police plan to enforce speed limits by using radar traps at four different locations within the city limits. The radar traps at each of the locations L_1, L_2, L_3, and L_4 will be operated 40%, 30%, 20%, and 30% of the time. If a person who is speeding on her way to work has probabilities of 0.2, 0.1, 0.5, and 0.2, respectively, of passing through these locations, what is the probability that she will receive a speeding ticket?

If the person received a speeding ticket on her way to work, what is the probability that she passed through the radar trap located at L_2?

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7. A regional telephone company operates three identical relay stations at different locations. During a one-year period, the number of malfunctions reported by each station and the causes are shown below.

Station	***A***	***B***	***C***
Problems with electricity supplied (ES)	2	1	1
Computer malfunction (CM)	4	3	2
Malfunctioning electrical equipment (ME)	5	4	2
Caused by other human errors (H)	7	7	5

Suppose that a malfunction was reported, and it was found to be caused by other human errors. What is the probability that it came from station *C*?

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