

# Nonparametric Bayes

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Mostly based on **A Tutorial on Bayesian Nonparametric Models** by Samuel J. Gershman.

# Outline

# Introduction

- ▶ What we do in ML is fitting a model to the data
- ▶ That is, we adjust the values of certain parameters

# Linear Regression

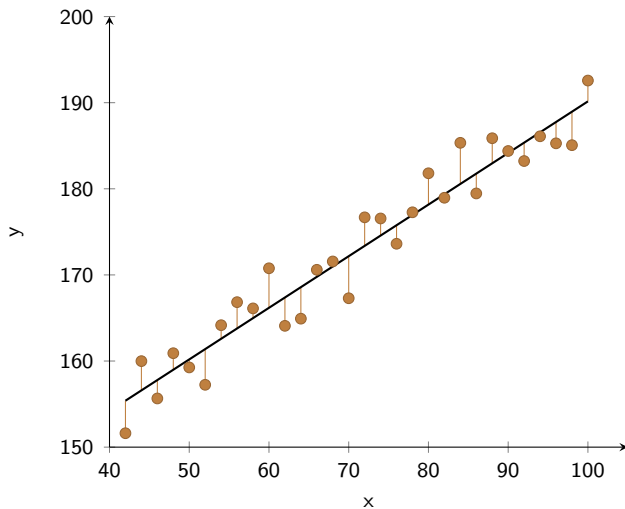


Figure 1: Linear Regression

# Neural Networks

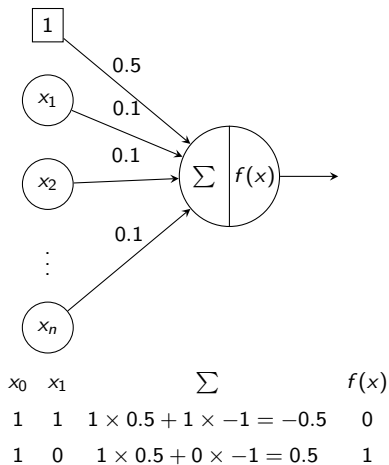


Figure 2: Perceptron

# Hidden Markov Models

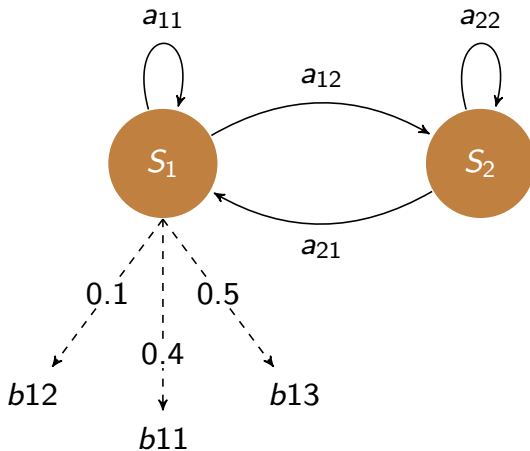
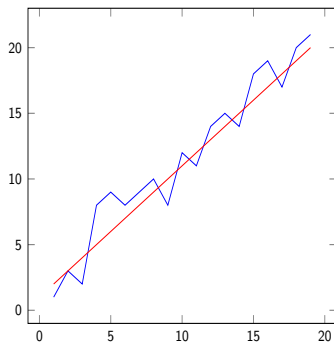
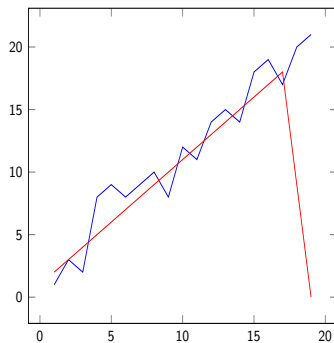


Figure 3: Hidden Markov Models

# Bertrand Russell's Inductivist Turkey



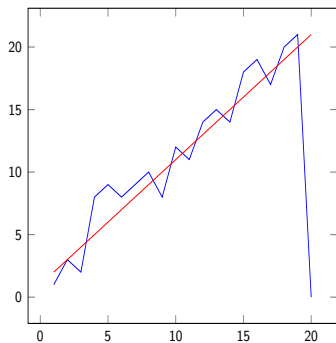
(a) One Model



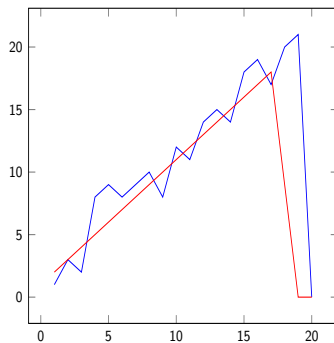
(b) Another Model

Figure 4: A comparison of models

# Bertrand Russell's Inductivist Turkey



(a) One Model



(b) Another Model

Figure 5: A comparison of models



## Bayesian Learning

$$P(h|D) = \frac{P(D|h)P(h)}{P(D)} \quad (1)$$

## Maximum Likelihood Estimation

$$\begin{aligned}h_{MAP} &\equiv \arg \max_{h \in H} P(h|D) \\&= \arg \max_{h \in H} \frac{P(D|h)P(h)}{P(D)} \\&= \arg \max_{h \in H} P(D|h)P(h) \\h_{MLE} &= \arg \max_{h \in H} P(D|h)\end{aligned}\tag{2}$$

# Data is a mess

- ▶ The articles in Wikipedia
- ▶ The species in the planet
- ▶ The hashtags on Twitter

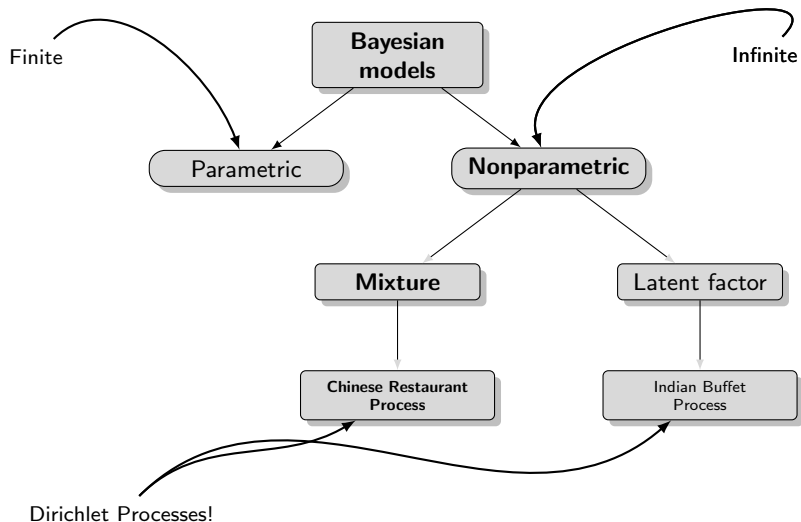
## How the problem is *sometimes* addressed

- ▶ Let's start with the classic approach
- ▶ Let's do clustering
- ▶ Let's use Gaussian Mixture Models (GMM)
- ▶ We can fit several models and then compare them with some metric.

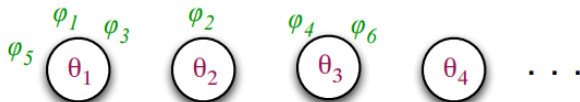
## How we can *alternatively* approach the problem

- ▶ Another interesting approach is to use Bayesian Nonparametric (BNP) models
- ▶ BNP models will build a model than can adapt its complexity to the data

# Bayesian nonparametric models



# Chinese Restaurant Process



- ▶ Infinite number of tables
- ▶ A sequence of customers entering the restaurant and sitting down
- ▶ The first customer enters and sits at the first table
- ▶ The second customer enters and sits...
  - ▶ at the first table with probability  $\frac{1}{1+\alpha}$
  - ▶ at the second table with probability  $\frac{\alpha}{1+\alpha}$

What else can be done?

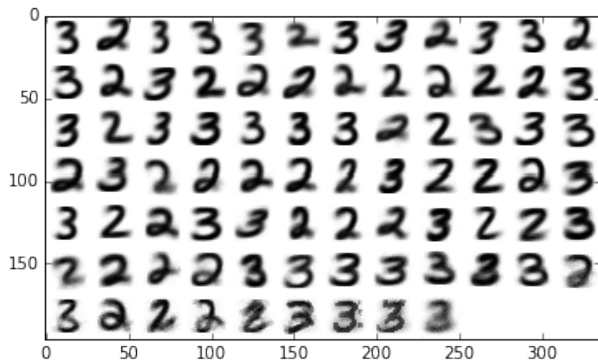


Figure 6: Digit recognition (datamicroscopes)



## What else can be done?

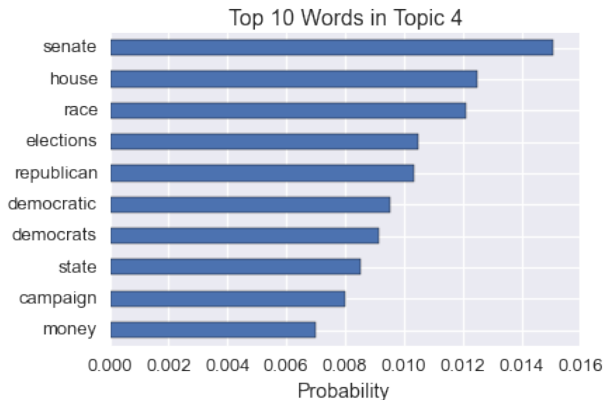


Figure 7: Topic Modeling (datamicroscopes)

## Recap: Bayesian parametric vs nonparametric models

- ▶ Traditional approach (finite)
  - ▶ The number of parameters  $\theta$  (e.g. clusters) is prespecified
  - ▶ We have a prior distribution over parameters  $P(\theta)$
  - ▶ For example, in the Gaussian mixture model, each cluster will be modelled using a parametric model (e. g. Gaussian)
- ▶ Bayesian nonparametric models
  - ▶ We assume that there is an **infinite** number of latent clusters
  - ▶ A finite number of clusters is *inferred* from data
  - ▶ The number of clusters grow as new data points are observed

# Libraries in Python

- ▶ Sklearn
- ▶ Datamicroscopes

## What else to learn?

- ▶ What is the  $\beta$  distribution?
- ▶ What is the Dirichlet distribution?
- ▶ Dirichlet process

# References

- ▶ **Machine Learning** by Tom Mitchell
- ▶ **A Tutorial on Bayesian Nonparametric Models** by Samuel J. Gershman
- ▶ **datamicroscopes** library

Thank you  
Questions?