

A9. 1-dim. CA, $k=4, r=1$

$$Z = k^L = k^{k^n} = k^{k^{(2+r+1)}} = 4^3 = 2^{128}$$

• print 100 rules per second.

$$\Rightarrow \frac{2^{128}}{100} \text{ s.} = 107,902,830,708,060,141,889,705,291,549 \text{ years of 365 days.}$$

A10. Not all totalistic rules are legal, for example, if the state $(0,0,0)$ has an output 1, definitely it is not having a silent state, so it is not legal either, but still could be a totalistic rule.

e.g. $k=2, r=1, 1\text{-dim}$

$(t) \rightarrow (t+1)$	
000	1
001	a
010	a
011	b
100	a
101	b
110	b
111	c

totalistic,
no silent state

(a, b, c can be 0 or 1)

A.11. For Android "1-D Cell Automaton" is a simple and nice app and can be found in the next website: play.google.com, looking the name of the app.

A.12. 1-dim. CA: $d=1, k=2, r=1$, totalistic rule 150₀ = 10010110

SUM(t)	3	2	1	0
$a_i(t+1)$	1	0	1	0

• repetitive formula

e.g. cell C2 has a formula = IF(SUM(B7:D7)=3, 1, IF(SUM(B7:D7)=2, 0, IF(SUM(B7:D7)=1, 1, 0)))

We sent the spreadsheet file to Ms. Rybalka.

A.13. formulas Z of possible rules, for 1-Dim. C.A. w.r.t. r, k .

a) all possible rules $Z = k^{k^{(2 \cdot r + 1)}} = k^{(k^{(2 \cdot r + 1)})}$

b) rules that are peripheral $Z_p = k^{(k^{(2 \cdot r)})}$
(ignores the state of the cell itself)

c) rules that are totalistic $Z_t = k^{((2 \cdot r + 1) \cdot (k - 1) + 1)}$

(when, the states are consist of integers and include '0')

the number of the possible sums of cells are

$$= (2 \cdot r + 1) \cdot (k - 1) + 1$$

d) rules that are totalistic and peripheral $Z_{tp} = k^{(2 \cdot r \cdot (k - 1) + 1)}$

A.14. $d=1, r=1, k=2$. C.A

			$a_i(t+1)$								
$a_{i-1}(t)$	$a_i(t)$	$a_{i+1}(t)$		0 ₀	17 ₀	42 ₀	57 ₀	170 ₀	165 ₀	204 ₀	243 ₀
			0								
			1								
			1								
			2								
			1								
			2								
			2								
			3								
- legal				○	×	×	×	×	×	○	×
symmetric				○	×	×	○	×	○	○	×
totalistic				○	×	×	×	×	×	×	×
peripheral				○	×	×	×	×	○	×	×

A.15. 4 behaviours of CAs.

• with CA, we can observe the change of the states of cells based on a rule as time passes. Different rules make different result. (showing different behaviour)

- Class I. monotonous

states of the cells are monotonous.

- Class II. predictable

pattern of states ~~a~~ is predictable.

- Class III. unpredictable

pattern of states is unpredictable.

- Class IV. Half-predictable.

repetitive or stable ~~pattern~~ states, but cells interact ^{with} each other in complex way.