

Applied Statistical Analysis I/
Quantitative Methods I
POP77003/77051

Fall 2024

Week 10

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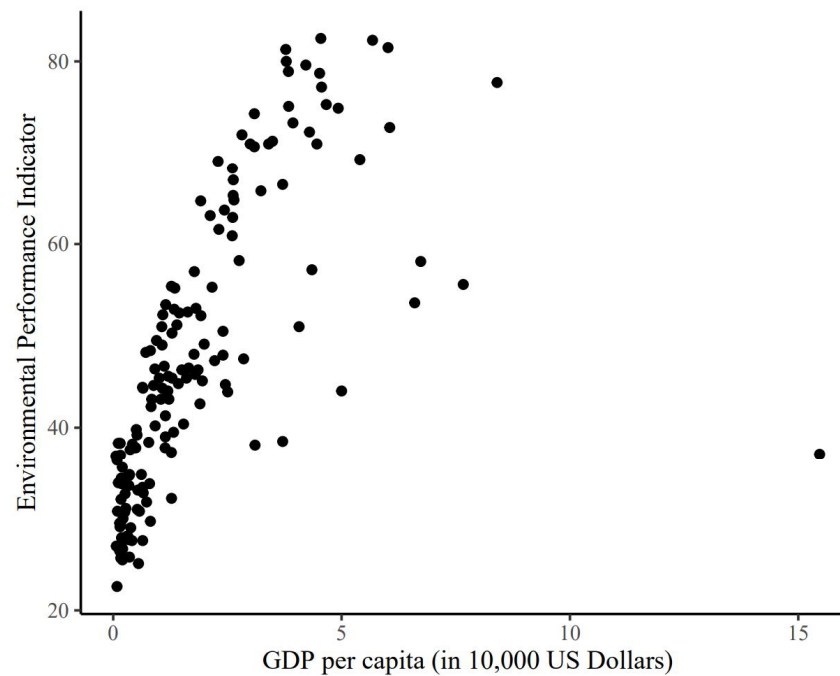
13 November, 2024

Today's Agenda

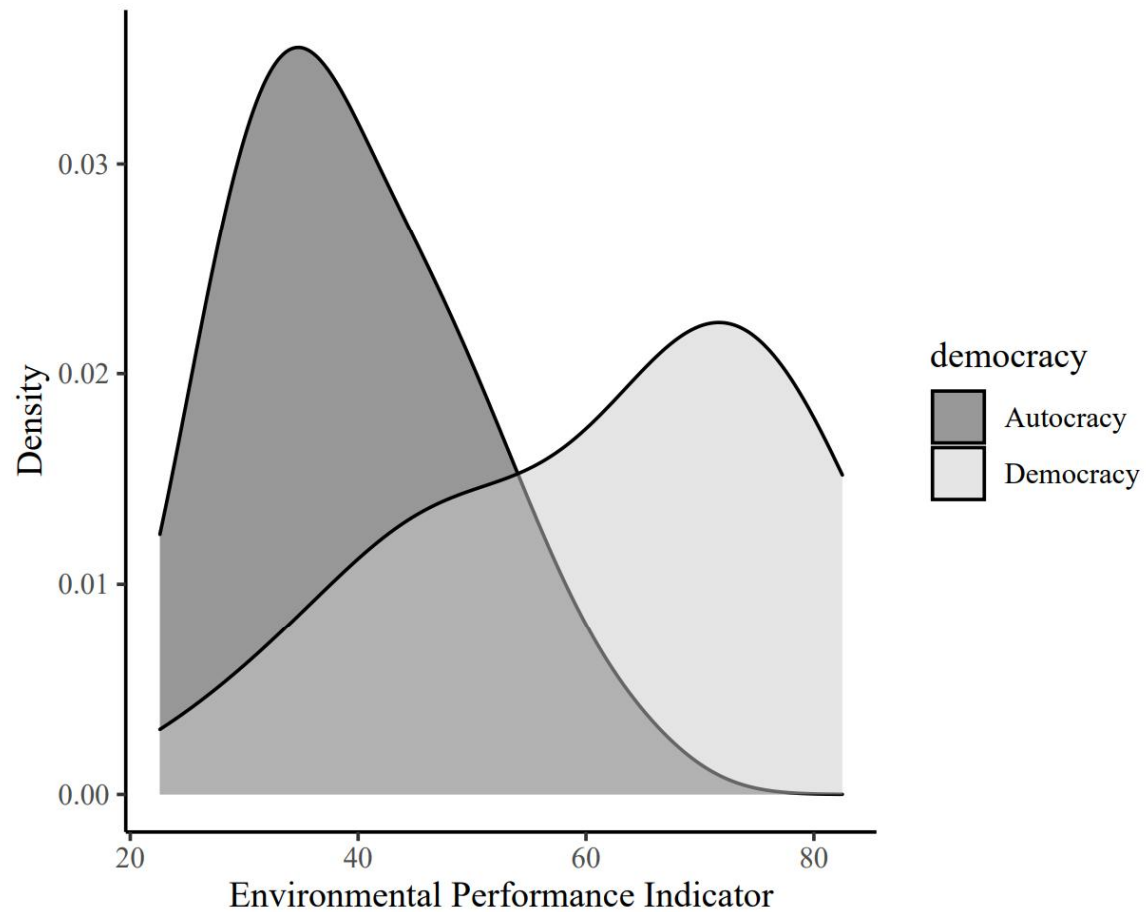
- (1) Lecture recap
- (2) Tutorial exercises

Categorical Explanatory Variables

Income and environmental protection



Regime type and environmental protection



$$\text{Environmental Performance}_i = \alpha + \beta_1 * \text{Regime Type}_i + \beta_2 * \text{Income}_i$$

```
## Call:
## lm(eps_emi ~ democracy + income, data = qog_data)

## Residuals:
##      Min       1Q   Median       3Q      Max
## -53.563  -6.502   0.498   6.773  20.198

## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    35.3027     1.1269  31.327 < 2e-16 ***
## democracy      16.5270     1.8409   8.978 9.08e-16 ***
## income         3.5793     0.4266   8.390 2.92e-14 ***
## ---
## Signif. codes:
## 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

## Residual standard error: 9.982 on 154 degrees of freedom
## (37 observations deleted due to missingness)
## Multiple R-squared:  0.6175, Adjusted R-squared:  0.6126
## F-statistic: 124.3 on 2 and 154 DF, p-value: < 2.2e-16
```

In comparison to autocracies (= reference category), democracies have a 16.5270 scale point higher score on the Environmental Performance Index, under control of income.

$$\hat{Y}_i = \alpha + \beta_1 * \textit{Regime Type}_i + \beta_2 * \textit{Income}_i$$

Model for Autocracies:

$$\hat{Y}_i = 35.303 + (16.527 * \textit{Regime Type}_i) + (3.579 * \textit{Income}_i)$$

$$\hat{Y}_i = 35.303 + (16.527 * 0) + (3.579 * \textit{Income}_i)$$

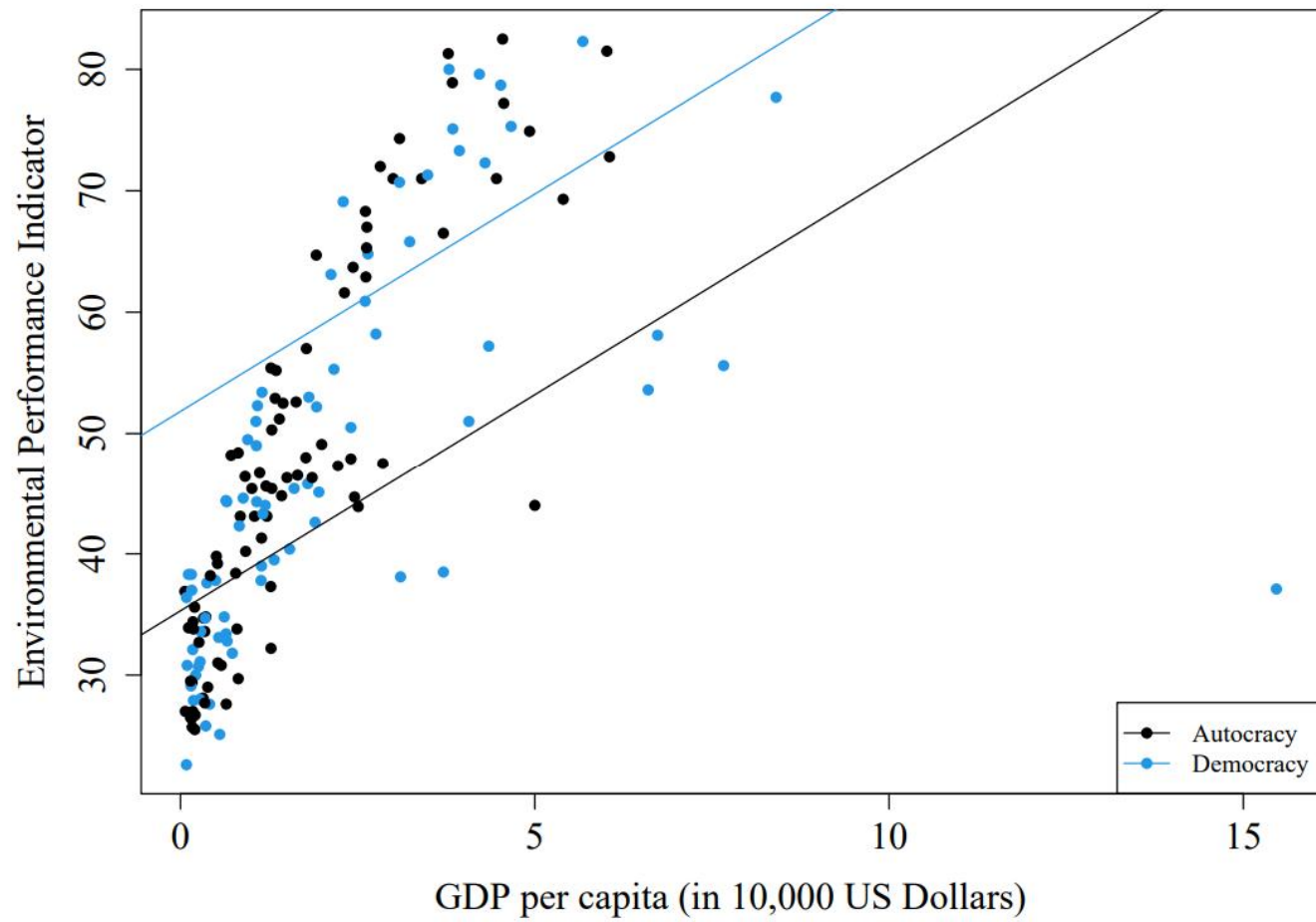
$$\hat{Y}_i = 35.303 + (3.579 * \textit{Income}_i)$$

Model for Democracies:

$$\hat{Y}_i = 35.303 + (16.527 * \textit{Regime Type}_i) + (3.579 * \textit{Income}_i)$$

$$\hat{Y}_i = 35.303 + (16.527 * 1) + (3.579 * \textit{Income}_i)$$

$$\hat{Y}_i = 51.83 + (3.579 * \textit{Income}_i)$$



Categorical Explanatory Variables

How to include categorical explanatory variables with more than two levels?

Categorical Explanatory Variables

$$\text{Environmental performance}_i = \alpha + \beta_1 * \text{Income}_i + \beta_2 * \text{Region}_i + \epsilon_i$$

```
## table(qog_data$ht_region)
##
##           Eastern Europe (1)           Latin America(2)
##                28                20
##   North Africa & the Middle East (3)   Sub-Saharan Africa (4)
##                20                49
## Western Europe and North America (5)           East Asia (6)
##                27                6
##           South-East Asia (7)           South Asia (8)
##                11                8
##           The Pacific (9)           The Caribbean (10)
##                12                13
```

Categorical Explanatory Variables

```
1 # Load package
2 library(fastDummies)
3
4 # Create dummy variables for categorical variable
5 qog_data <- dummy_cols(qog_data,
6                       select_columns = c("ht_region"))
7
8 # Print first 5 rows in dataset
9 head(qog_data[c("ht_region_1",
10                "ht_region_2",
11                "ht_region_3",
12                "ht_region_4",
13                "ht_region_5",
14                "ht_region_6",
15                "ht_region_7",
16                "ht_region_8",
17                "ht_region_9",
18                "ht_region_10")], 5)
```

```
## ht_region_1 ht_region_2 ht_region_3 ht_region_4 ht_region_5
## 1          0          0          0          0          0
## 2          1          0          0          0          0
## 3          0          0          1          0          0
## 4          0          0          0          0          1
## 5          0          0          0          1          0
## ht_region_6 ht_region_7 ht_region_8 ht_region_9 ht_region_10
## 1          0          0          1          0          0
## 2          0          0          0          0          0
## 3          0          0          0          0          0
## 4          0          0          0          0          0
## 5          0          0          0          0          0
```

Categorical Explanatory Variables

```
1 # Run regression model
2 m2 <- lm(epi_epi ~ income +
3         ht_region_1 + ht_region_2 + ht_region_3 +
4         # no region 4 (Sub-Saharan Africa) = reference category.
5         ht_region_5 + ht_region_6 + ht_region_7 + ht_region_8 + ht_region_9 +
6         ht_region_10, data = qog_data)
7
8 # Print results
9 summary(m2)
```

Coefficients: (1 not defined because of singularities)

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	32.3992	1.1296	28.683	< 2e-16 ***
income	1.7410	0.4061	4.287	3.23e-05 ***
ht_region_1	18.4245	1.8769	9.817	< 2e-16 ***
ht_region_2	11.6208	2.0362	5.707	6.01e-08 ***
ht_region_3	9.4434	2.4665	3.829	0.000189 ***
ht_region_5	35.2532	2.4854	14.184	< 2e-16 ***
ht_region_6	16.2287	3.6737	4.418	1.91e-05 ***
ht_region_7	4.1247	2.7820	1.483	0.140281
ht_region_8	-2.1694	3.2676	-0.664	0.507774
ht_region_9	NA	NA	NA	NA
ht_region_10	11.0665	3.5607	3.108	0.002257 **

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.528 on 149 degrees of freedom

(35 observations deleted due to missingness)

Multiple R-squared: 0.7897, Adjusted R-squared: 0.777

F-statistic: 62.16 on 9 and 149 DF, p-value: < 2.2e-16

```

1 # Use relevel to code dummy variables on the fly
2 # specify region 4 (Sub-Saharan Africa) = reference category
3 m3 <- lm(epi_epi ~ income + relevel(as.factor(ht_region), ref = "4"),
4         data = qog_data)
5
6 # Print results
7 summary(m3)

```

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	32.3992	1.1296	28.683	< 2e-16	***
income	1.7410	0.4061	4.287	3.23e-05	***
relevel(as.factor(ht_region), ref = "4")1	18.4245	1.8769	9.817	< 2e-16	***
relevel(as.factor(ht_region), ref = "4")2	11.6208	2.0362	5.707	6.01e-08	***
relevel(as.factor(ht_region), ref = "4")3	9.4434	2.4665	3.829	0.000189	***
relevel(as.factor(ht_region), ref = "4")5	35.2532	2.4854	14.184	< 2e-16	***
relevel(as.factor(ht_region), ref = "4")6	16.2287	3.6737	4.418	1.91e-05	***
relevel(as.factor(ht_region), ref = "4")7	4.1247	2.7820	1.483	0.140281	
relevel(as.factor(ht_region), ref = "4")8	-2.1694	3.2676	-0.664	0.507774	
relevel(as.factor(ht_region), ref = "4")10	11.0665	3.5607	3.108	0.002257	**

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.528 on 149 degrees of freedom

(35 observations deleted due to missingness)

Multiple R-squared: 0.7897, Adjusted R-squared: 0.777

F-statistic: 62.16 on 9 and 149 DF, p-value: < 2.2e-16

Under control of income, Eastern Europe has an Environmental Performance Index score of 18.4245 scale points higher than Sub-Saharan Africa.

Interactions

What are interactions?

Interactions

The association between X on Y might vary depending on the value of a third variable M (=Moderator):

$$\hat{Y}_i = \alpha + \beta_1 X_i + \beta_2 M_i + \beta_3 (X_i M_i) + \epsilon_i$$

The interpretation of the regression coefficients changes:

- α is the expected value of Y when $X = 0$ and $M = 0$
- β_1 is the change in Y when X increases by one unit, when $M = 0$
- β_2 is the change in Y when M increases by one unit, when $X = 0$
- β_3 is the *interaction term* of X and M

Rearrange terms:

$$\hat{Y}_i = \alpha + \beta_2 M_i + (\beta_1 + \beta_3 M_i) X_i + \epsilon_i$$

β_3 is the *added* increase in β_1 , if M increases by one unit.

Categorical by continuous interaction

$$\text{Environmental Performance}_i = \alpha + \beta_1 \text{Income}_i + \beta_2 \text{Regime Type}_i + \beta_3 \text{Income}_i * \text{Regime Type}_i + \epsilon_i$$

```
1 # Run regression model with interaction term
2 int_m2 <- lm(eps_eps ~ income + democracy + income*democracy, data = qog_data)
3
4 # Print results
5 summary(int_m2)
```

```
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    37.1474     1.0684  34.768 < 2e-16 ***
## income         2.1902     0.4532   4.833 3.24e-06 ***
## democracy      3.4490     2.7819   1.240  0.217
## income:democracy 5.1029     0.8686   5.875 2.55e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.046 on 153 degrees of freedom
## (37 observations deleted due to missingness)
## Multiple R-squared:  0.6879, Adjusted R-squared:  0.6818
## F-statistic: 112.4 on 3 and 153 DF, p-value: < 2.2e-16
```

Categorical by continuous interaction

```
## Coefficients:
##               Estimate Std. Error t value Pr(>|t|)
## (Intercept)      37.1474      1.0684  34.768 < 2e-16 ***
## income            2.1902      0.4532   4.833 3.24e-06 ***
## democracyDemocracy 3.4490      2.7819   1.240  0.217
## income:democracyDemocracy 5.1029      0.8686   5.875 2.55e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.046 on 153 degrees of freedom
## (37 observations deleted due to missingness)
## Multiple R-squared:  0.6879, Adjusted R-squared:  0.6818
## F-statistic: 112.4 on 3 and 153 DF, p-value: < 2.2e-16
```

- The average Environmental Protection Index (EPI) for poor (Income=0) autocracies is 37.1474 scale points (α).
- For autocracies, with every additional 10,000 USD of income, the EPI increases by 2.1902 scale points (β_1). → Income effect for autocracies
- For poor democracies, the EPI is 3.4490 scale points higher, in comparison to poor autocracies (β_2).
- For democracies, with every additional 10,000 USD of income, the EPI increases by 7.2931 scale points ($\beta_1 + \beta_3 = 2.1902 + 5.1029 = 7.2931$). → Income effect for democracies

Categorical by continuous interaction

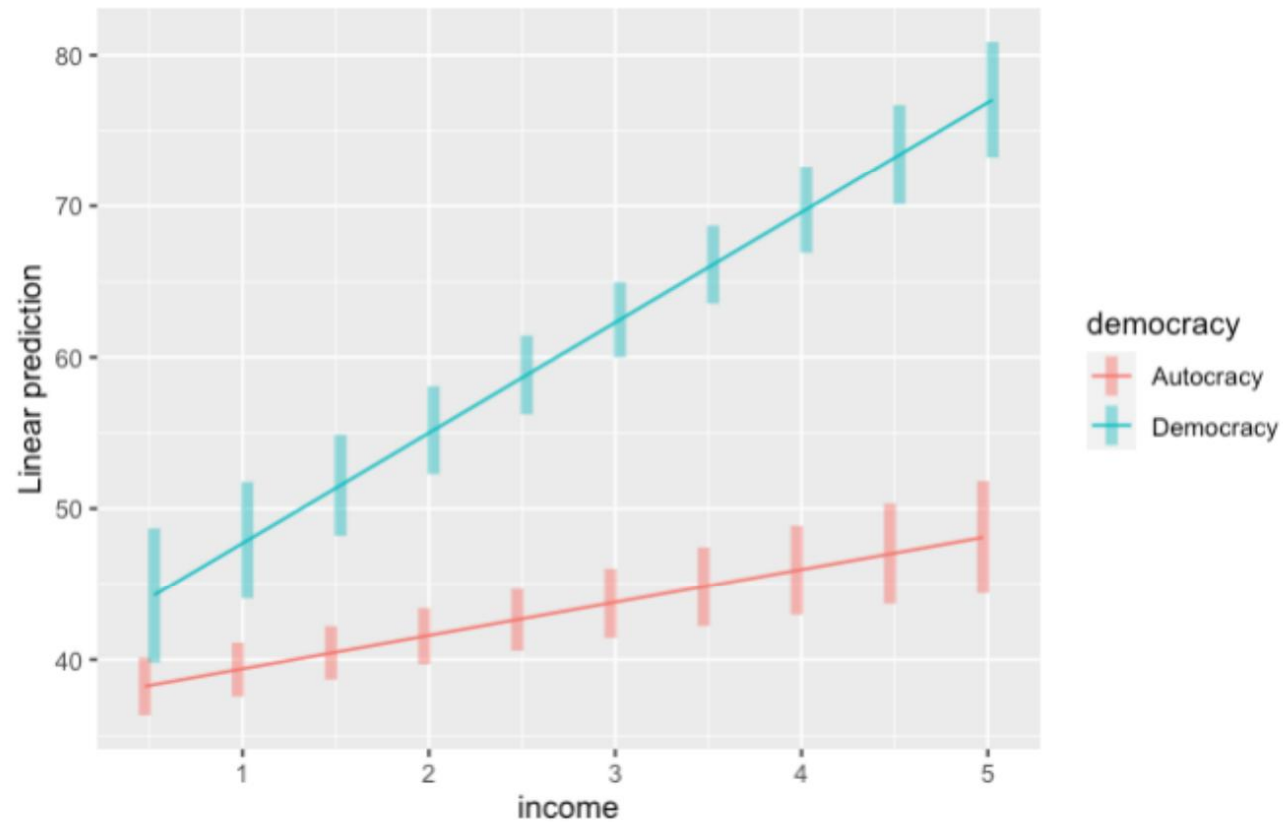
Model for Autocracies (democracy = 0)

$$\begin{aligned}\hat{Y}_i &= 37.1474 + (2.1902 * Income_i) + (3.4490 * Regime Type_i) + \\ &(5.1029 * Income_i * Regime Type_i) \\ \hat{Y}_i &= 37.1474 + (2.1902 * Income_i) + (3.4490 * 0) + (5.1029 * Income_i * 0) \\ \hat{Y}_i &= 37.1474 + (2.1902 * Income_i)\end{aligned}$$

Model for Democracies (democracy = 1)

$$\begin{aligned}\hat{Y}_i &= 37.1474 + (2.1902 * Income_i) + (3.4490 * Regime Type_i) + \\ &(5.1029 * Income_i * Regime Type_i) \\ \hat{Y}_i &= 37.1474 + (2.1902 * Income_i) + (3.4490 * 1) + (5.1029 * Income_i * 1) \\ \hat{Y}_i &= 40.5964 + (7.2931 * Income_i)\end{aligned}$$

Categorical by continuous interaction



Non-linear effects

Model a curvilinear (=curved lines) relationship between an independent variable and the dependent variable.

Include X and the square of X :

$$\hat{Y}_i = \alpha + \beta_1 X_i + \beta_2 X_i^2 + \epsilon_i$$

Non-linear effects

“U-shaped” relationship between democracy and environment protection?

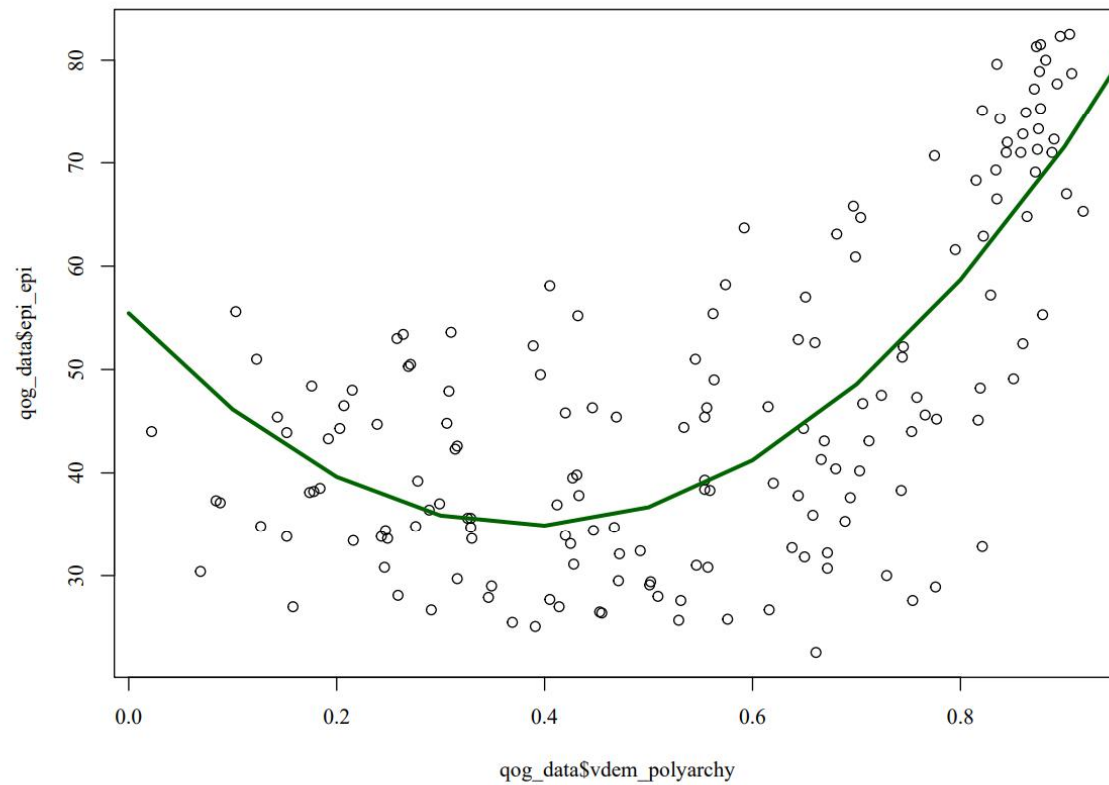
```
1 # Generate quadratic term
2 qog_data$sqr_vdem_polyarchy <- qog_data$vdem_polyarchy^2
3
4 # Run ols regression with quadratic term
5 q_m1 <- lm(emi ~ income + vdem_polyarchy
6           + sqr_vdem_polyarchy,
7           data = qog_data)
8
9 # Print results
10 summary(q_m1)
```

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	39.4244	4.2944	9.180	2.82e-16	***
income	3.0094	0.4576	6.576	7.19e-10	***
vdem_polyarchy	-44.3531	17.7037	-2.505	0.0133	*
sqr_vdem_polyarchy	74.1559	17.0553	4.348	2.50e-05	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 9.133 on 153 degrees of freedom
(37 observations deleted due to missingness)
Multiple R-squared: 0.6819, Adjusted R-squared: 0.6757
F-statistic: 109.3 on 3 and 153 DF, p-value: < 2.2e-16

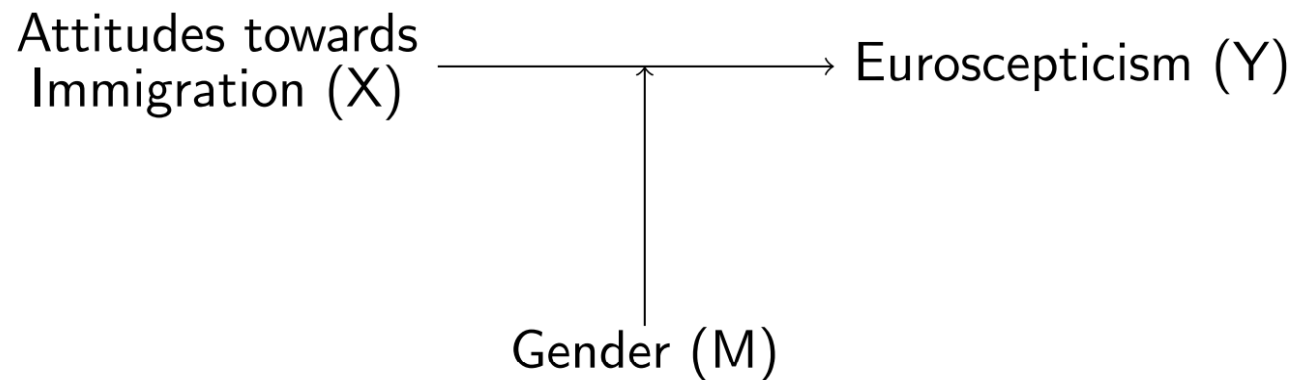
Non-linear effects



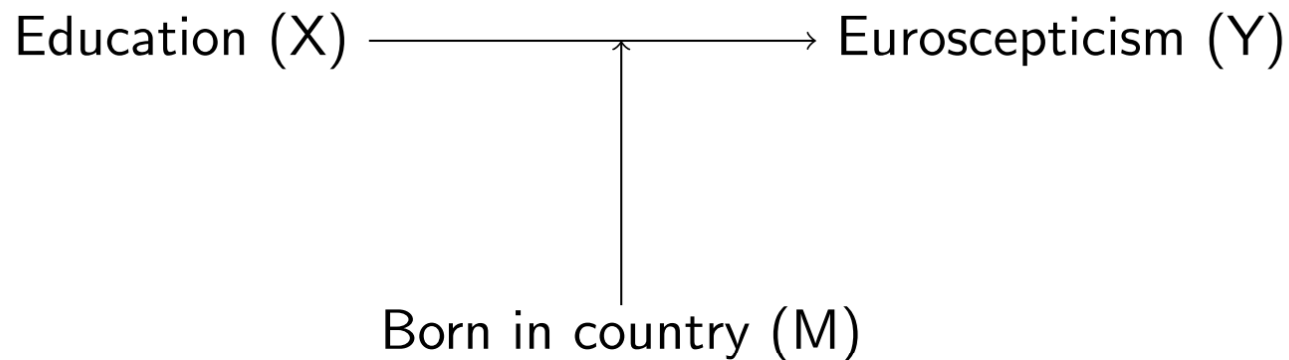
What is the relationship between education and Euroscepticism?

- H_1 : The higher the years of education, the lower the level of Euroscepticism.
- H_2 : The higher the income, the lower the level of Euroscepticism.
- H_3 : The higher the trust in politics, the lower the level of Euroscepticism.
- H_4 : The more positive attitudes towards immigration, the lower the level of Euroscepticism.

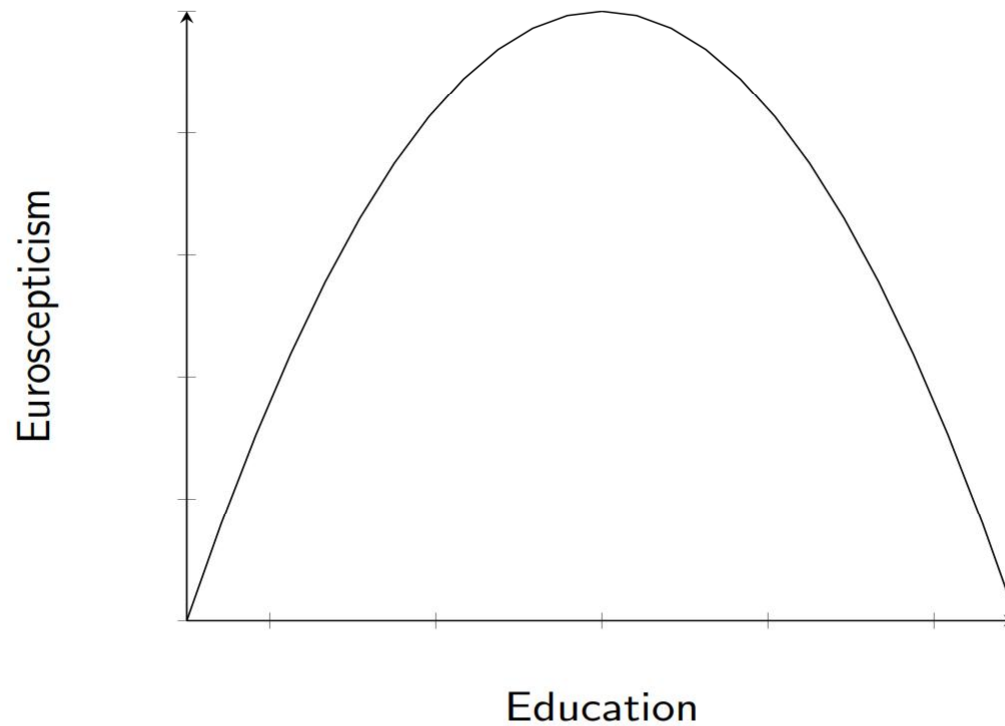
Does gender influence the effect of attitudes towards immigration on Euroscepticism?



Does whether the person was born in the country influence the effect of education on Euroscepticism?



Is the effect of education on Euroscepticism inverted U-shaped?



Is the effect of income on Euroscepticism U-shaped?

