

## 1. Algorithm Completion (Personalized):

Student Number: 123456789 (Example)

Personalized Algorithm 1 (Fibonacci):

```
int fibonacci(int n) {  
    if (n <= 1) return n; // Base case (digits 8, 9)  
    return fibonacci(n - 1) + fibonacci(n - 2); // Recursive case  
}
```

Worst-Case Operation Count:

- $O(2^n)$  time complexity (exponential growth).
- $O(n)$  space complexity (due to recursive calls).

Best-Case: 1 operation (when  $n$  is 0 or 1). Average-Case: Similar to worst-case, slightly better due to some early returns.

## Personalized Algorithm 2 (Maze Solving):

```
bool solveMaze(int x, int y) {  
    if (x == N - 1 && y == N - 1) { // Base case (reached goal) (digits 6, 7)  
        solution[x][y] = 0;  
        printSolution();  
        return true; // Found solution  
    }  
  
    if (isSafe(x, y)) {  
        solution[x][y] = 1; // Mark as part of the solution path  
  
        if (solveMaze(x + 1, y) || solveMaze(x, y + 1))  
            return true;  
  
        solution[x][y] = 0; // Backtrack (unmark)  
    }  
    return false; // No solution in this path  
}
```

Worst-Case Operation Count:

- Exponential in the worst case ( $O(4^n)$ ), as it potentially explores every path in a maze with many branching points.

## 2. Recursive Function Analysis:

Factorial:

- Base Case:  $n = 0$  (Factorial of 0 is 1).
- Recursive Case:  $n > 0$ .  $\text{factorial}(n) = n * \text{factorial}(n - 1)$

Fibonacci:

- Base Cases:  $n = 0$  or  $n = 1$  (First two Fibonacci numbers are 0 and 1).
- Recursive Case:  $n > 1$ .  $\text{fibonacci}(n) = \text{fibonacci}(n - 1) + \text{fibonacci}(n - 2)$

Maze Solving:

- Base Case: Reaching the goal coordinates (N-1, N-1).
- Recursive Case: Explore neighboring cells (if safe) until the goal is reached or a dead end is encountered (then backtrack).

## 3. Backtracking Problem (N-Queens):

Refer to the code file attached

## 4. Complexity Analysis:

- Factorial:
  - Recursive:  $O(n)$  time and space.
  - Iterative:  $O(n)$  time,  $O(1)$  space.
- Fibonacci:
  - Recursive:  $O(2^n)$  time,  $O(n)$  space.
  - Iterative:  $O(n)$  time,  $O(1)$  space.
- N-Queens:
  - Recursive:  $O(N!)$  time (worst case),  $O(N)$  space.

## 5. Recursion vs. Iteration:

- Recursion:
  - Elegant for tree traversal and divide-and-conquer algorithms.
  - Can lead to stack overflow if not used carefully.
- Iteration:
  - Generally more efficient for simple loops and tasks with limited stack space.
  - Can be less intuitive for recursive problems.