## Logic and Language: Exercise (Week 5)

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## 2 Pregroups

## 2.1

(4) Forward direction:

$$\underbrace{\frac{1^l \longrightarrow 1^l 1}{1^l \longrightarrow 1}}_{1^l \longrightarrow 1} \underbrace{\frac{1^l 1 \longrightarrow 1}{1^l \longrightarrow 1}}_{1} \xrightarrow{(1)}$$

Backward direction:

$$\frac{1 \longrightarrow 1^l 1}{1^l} (2)$$

(5) Forward direction:

Backward direction:

$$\frac{\overline{A \to A1} \ (1) \quad \overline{1 \to A^r A^{rl}} \ (2)}{\frac{A \to A(A^r A^{rl})}{A \to (AA^r)A^{rl}} \ (1)} \quad \xrightarrow{\overline{AA^r \to 1}} \ (3)}{\frac{A \to 1A^{rl}}{A \to A^{rl}} \ \to} \quad \underline{1A^{rl} \to A^{rl}} \ (1)$$

(6) Forward direction:

Forward direction: 
$$\frac{\overline{(AB)^l \to (1(AB))^l} \to \overline{1 \to (B^lA^l)^r(B^lA^l)}}{1 \to (B^lA^l)^r(B^lA^l)(AB))^l} \to \overline{(AB)^l \to (((B^lA^l)^r(B^lA^l)(AB)))^l} \to \overline{(AB)^l \to ((B^lA^l)^r(B^l(A^l(AB))))}} \xrightarrow{(1)} \overline{(AB)^l \to ((B^lA^l)^r(B^l(A^l(AB))))}} \xrightarrow{(1)} \overline{(AB)^l \to ((B^lA^l)^r(B^l(AB)))^l}} \xrightarrow{(AB)^l \to ((B^lA^l)^r(B^l(B)))^l} \xrightarrow{(AB)^l \to ((B^lA^l)^r(B^l(B)))^l}} \xrightarrow{(AB)^l \to ((B^lA^l)^r))^l} \xrightarrow{(AB)^l \to ((B^lA^l)^r))^l}} \xrightarrow{(AB)^l \to ((B^lA^l)^r))^l} \xrightarrow{(AB)^l \to ((B^lA^l)^r))^l} \xrightarrow{(AB)^l \to ((B^lA^l)^r)^l}} (5)$$