

# Contracts as Automata

## From Specification to Implementation

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*IOG*



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TacticalGrace



justtesting.org



# Ledger Models

## Coins versus accounts

What is the biggest conceptual difference between Ethereum contracts (account model) and Cardano contracts (eUTXO)?

What is the biggest conceptual difference between Ethereum contracts (account model) and Cardano contracts (eUTXO)?

Ethereum contracts compute.  
Cardano contracts verify.

$\sigma$

eUTXO

Account

state

$\sigma$

eUTXO

Account

eUTXO

state

$\sigma$



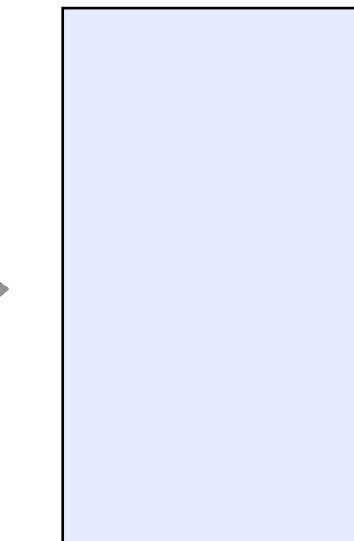
transaction

Account

eUTXO

state

$\sigma$

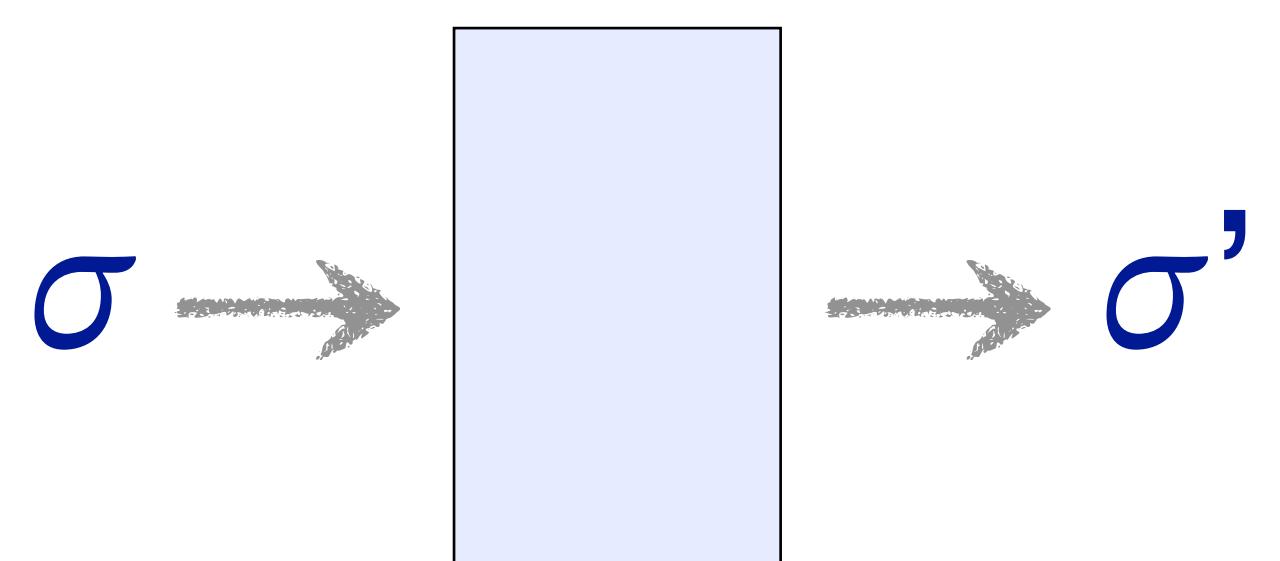


transaction

$\sigma'$

Account

eUTXO



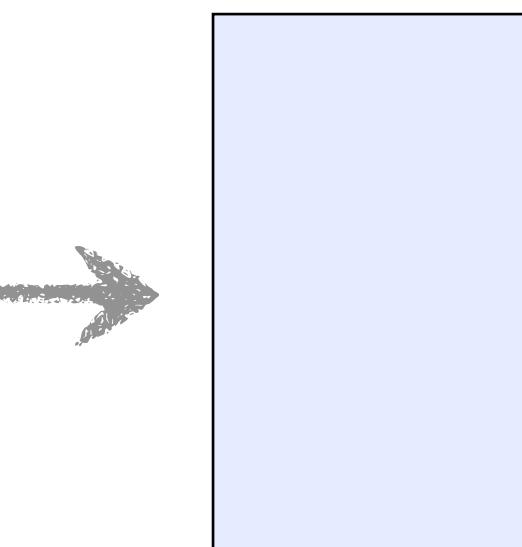
Account

eUTXO

Account

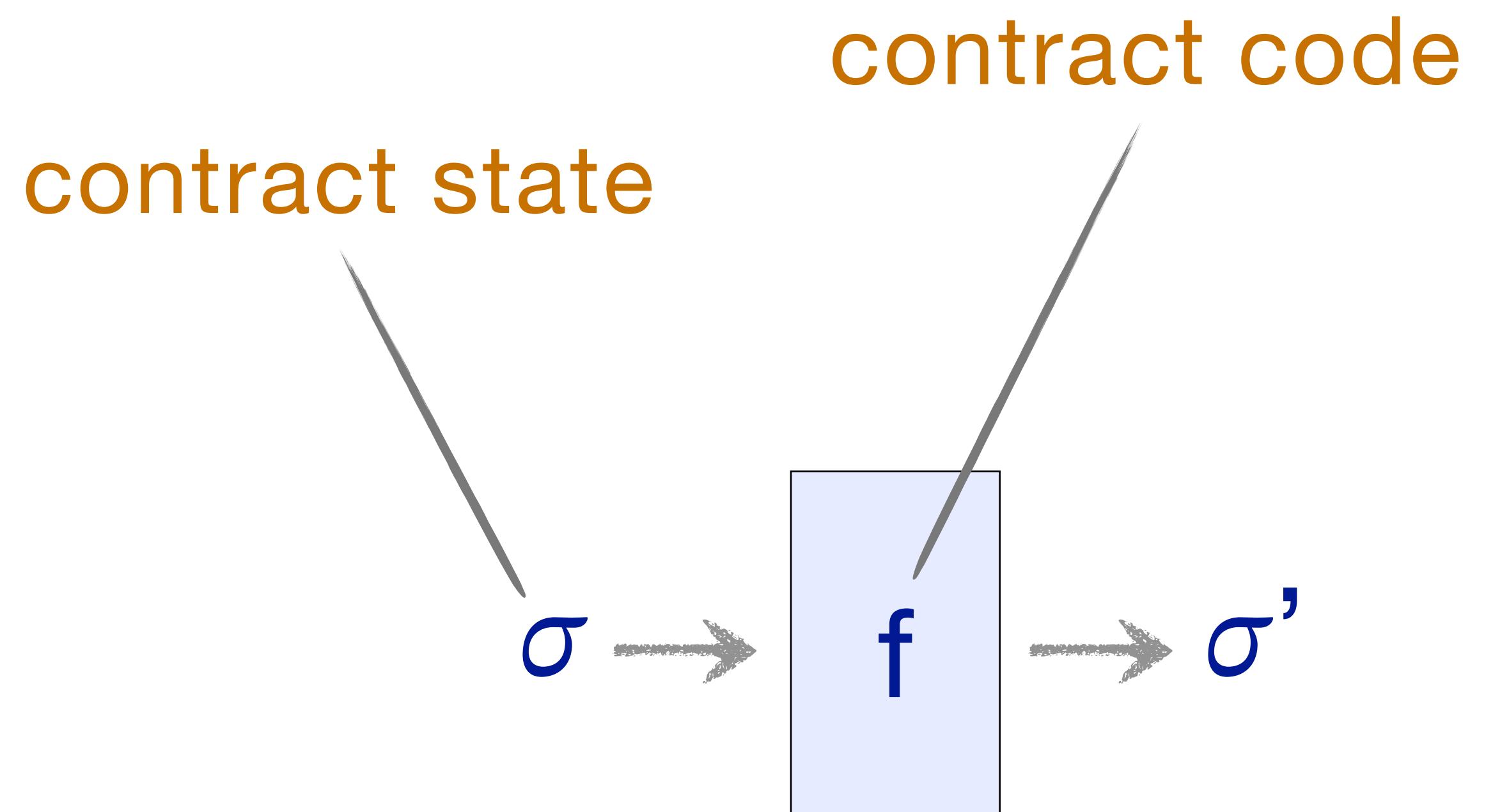
contract state

$\sigma$



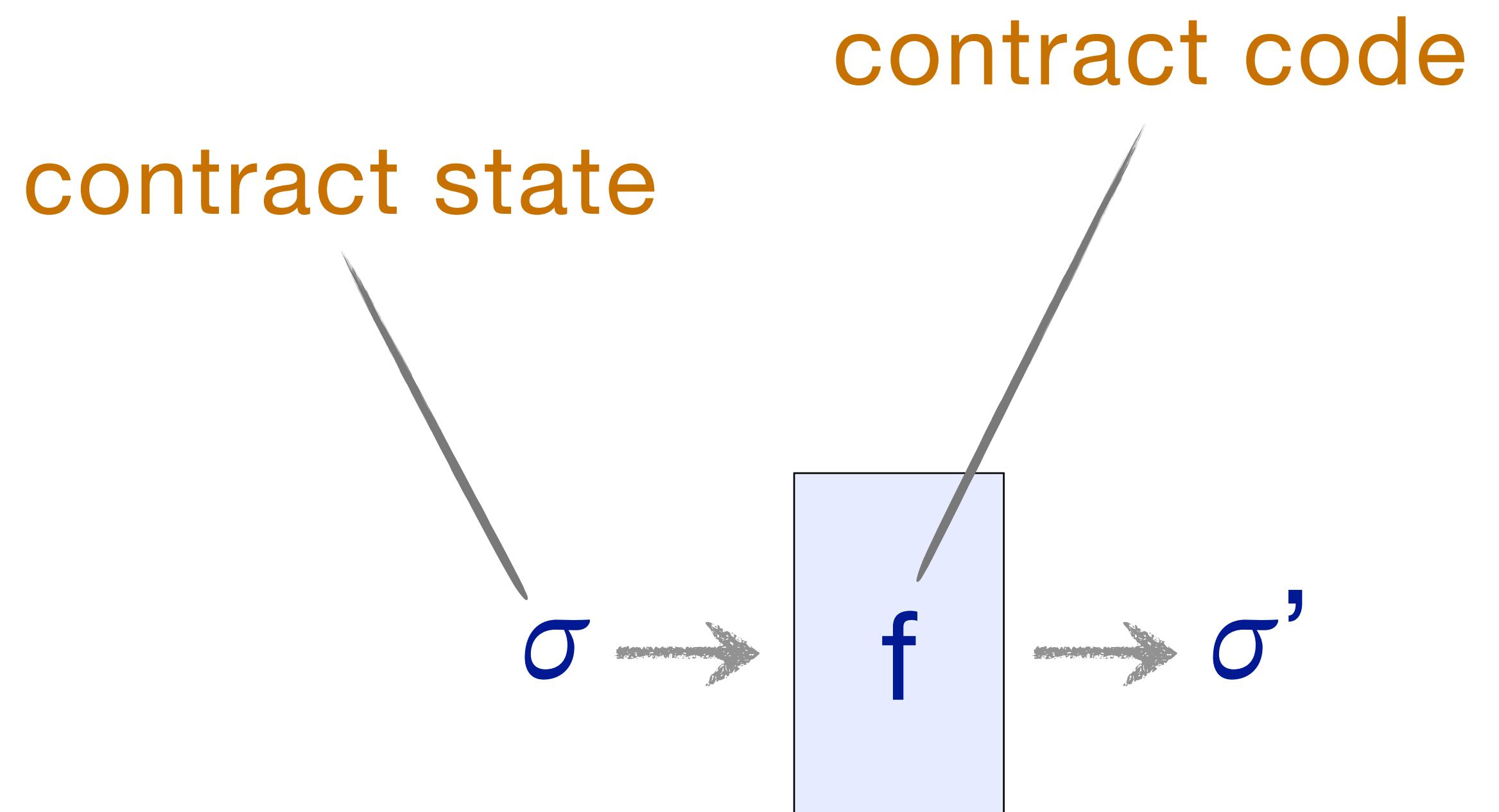
$\rightarrow \sigma'$

eUTXO



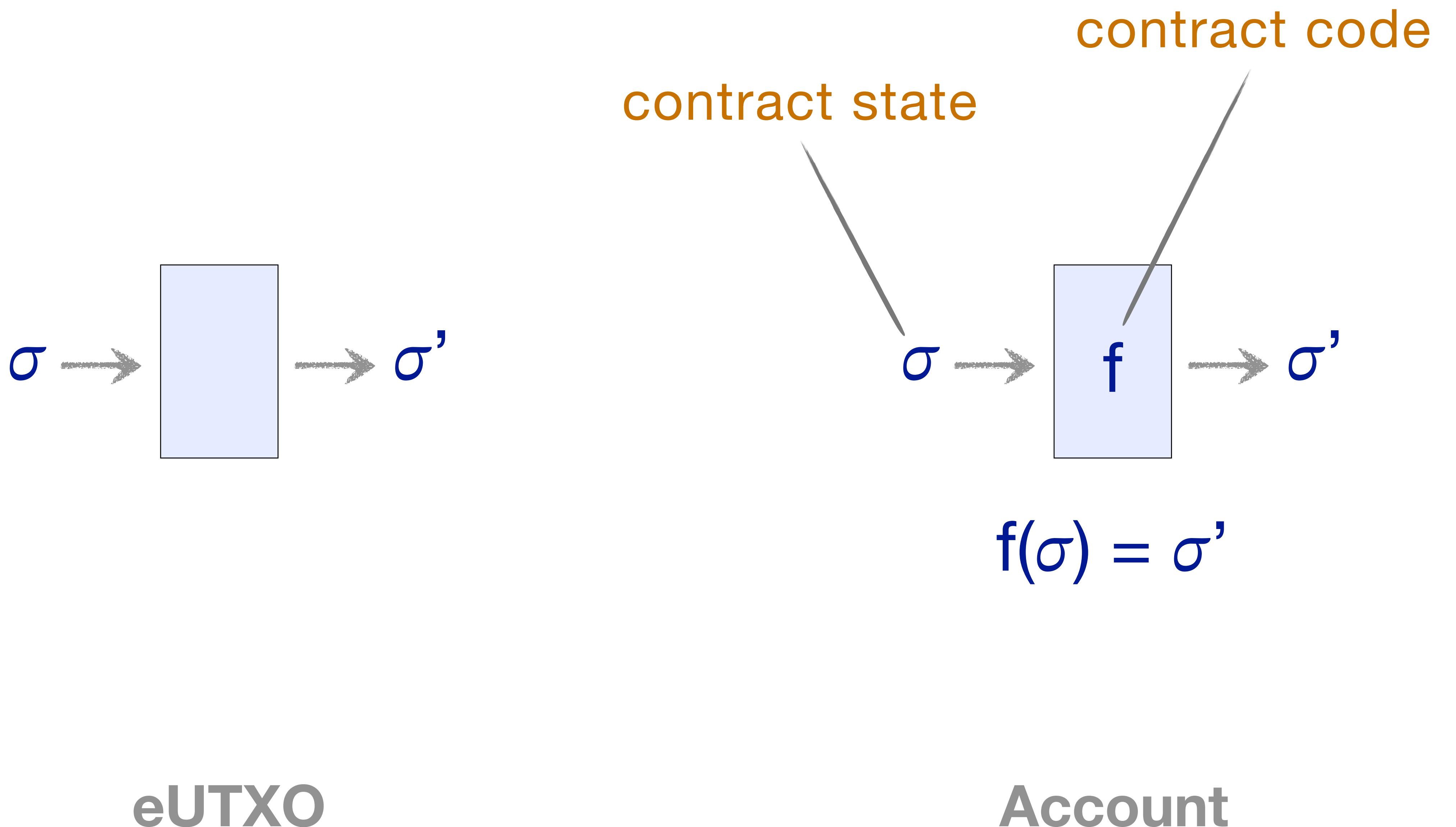
Account

eUTXO

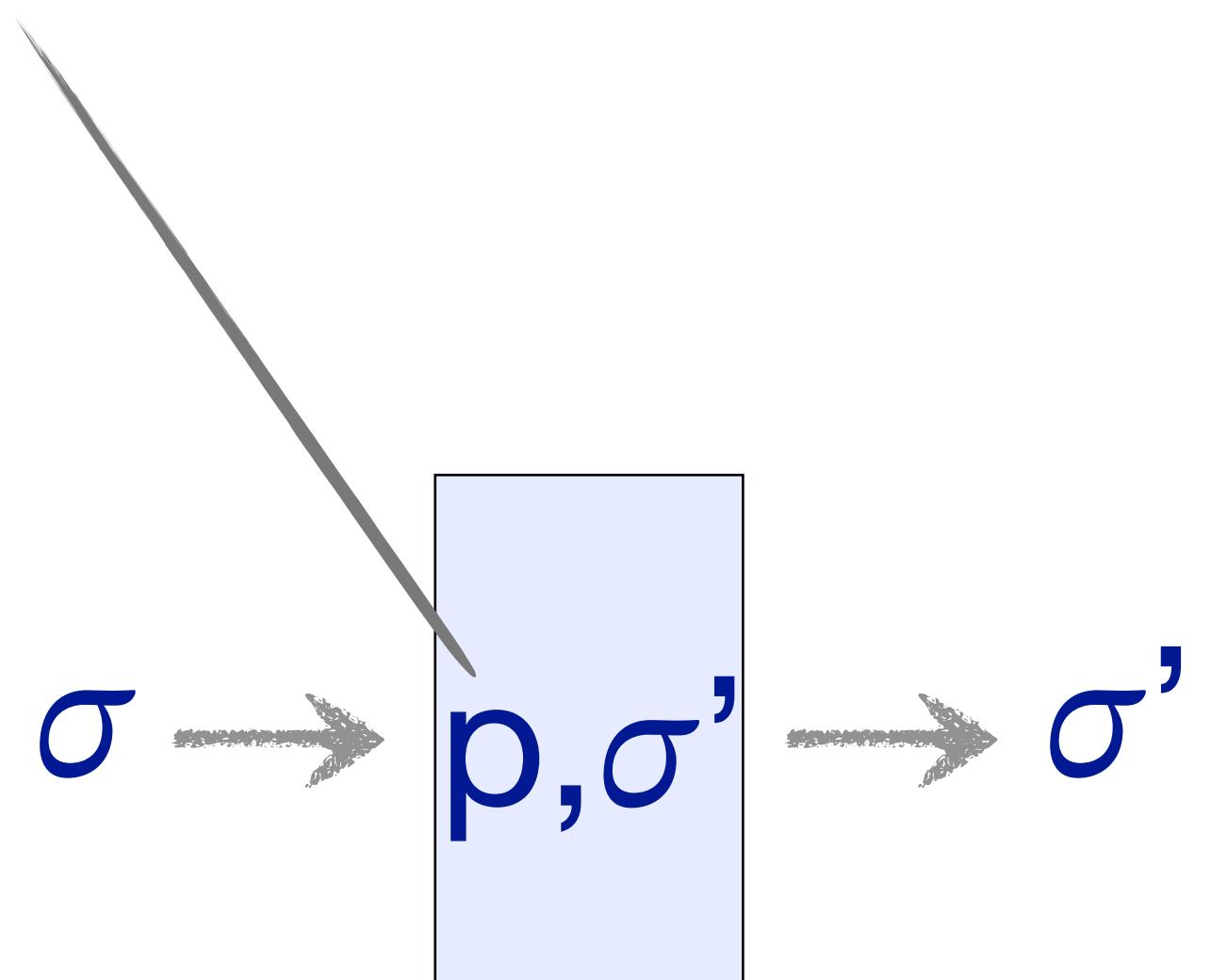


$$f(\sigma) = \sigma'$$

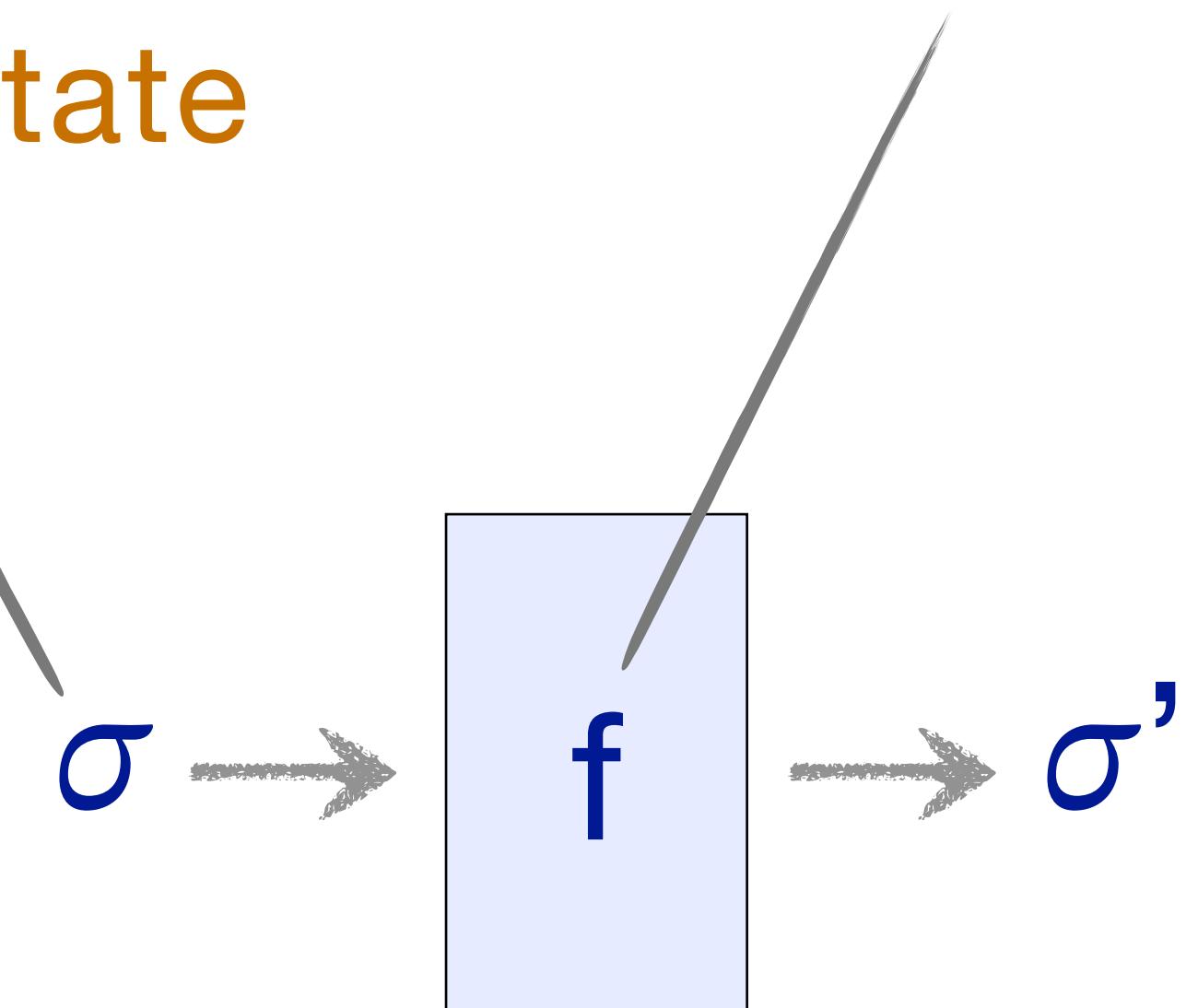
Account



contract code



contract state

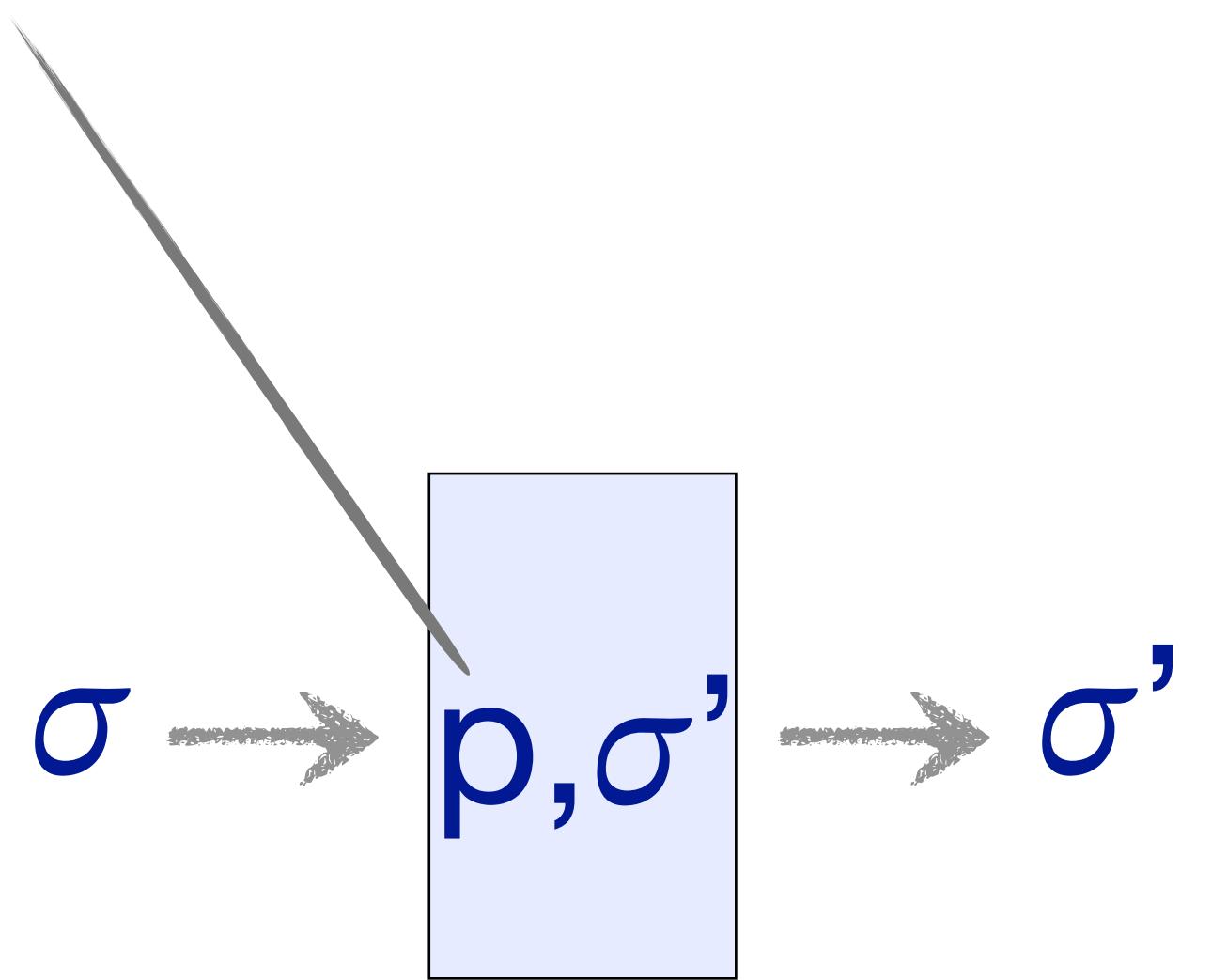


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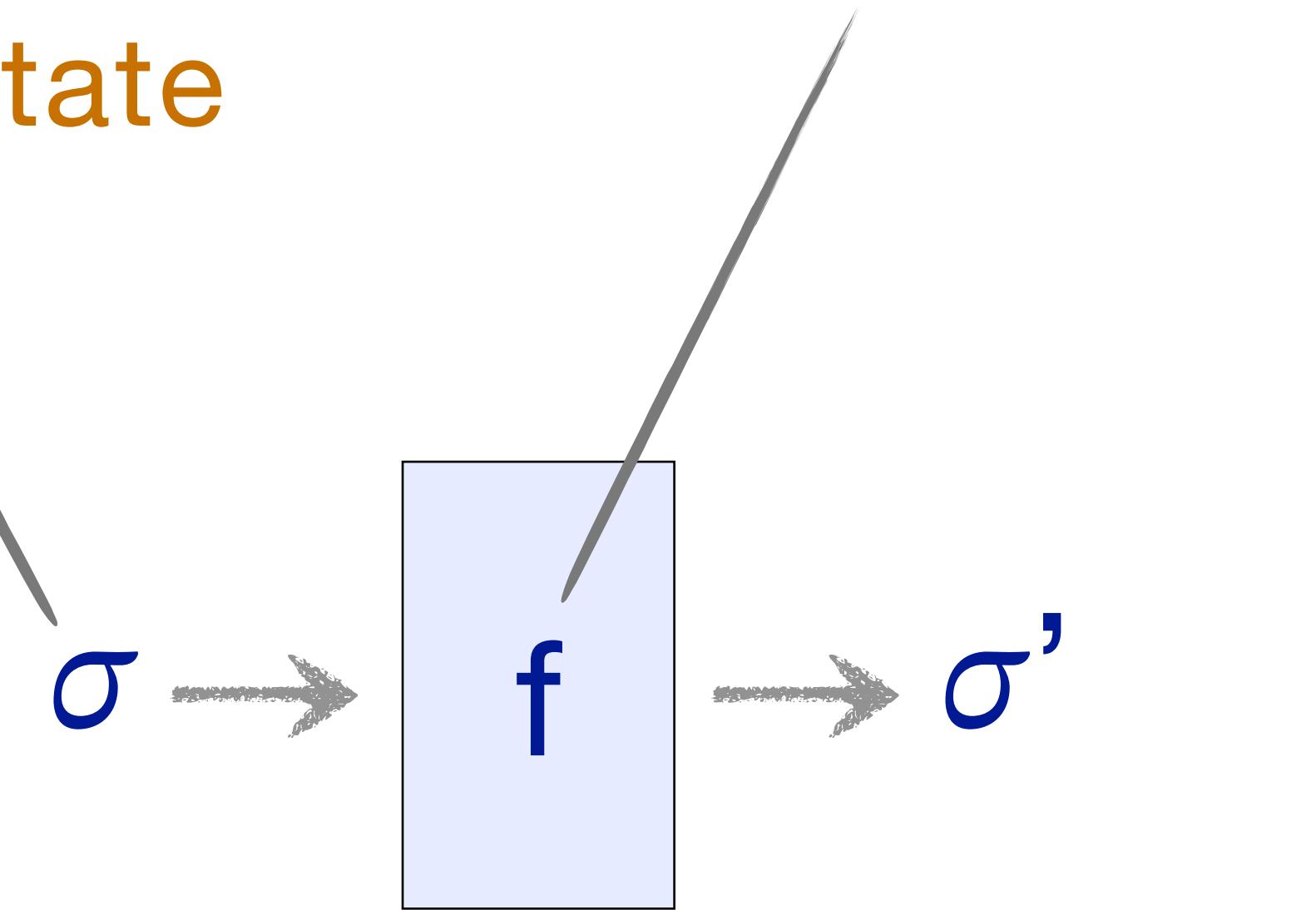
contract code



$$p(\sigma, \sigma') = \text{true}$$

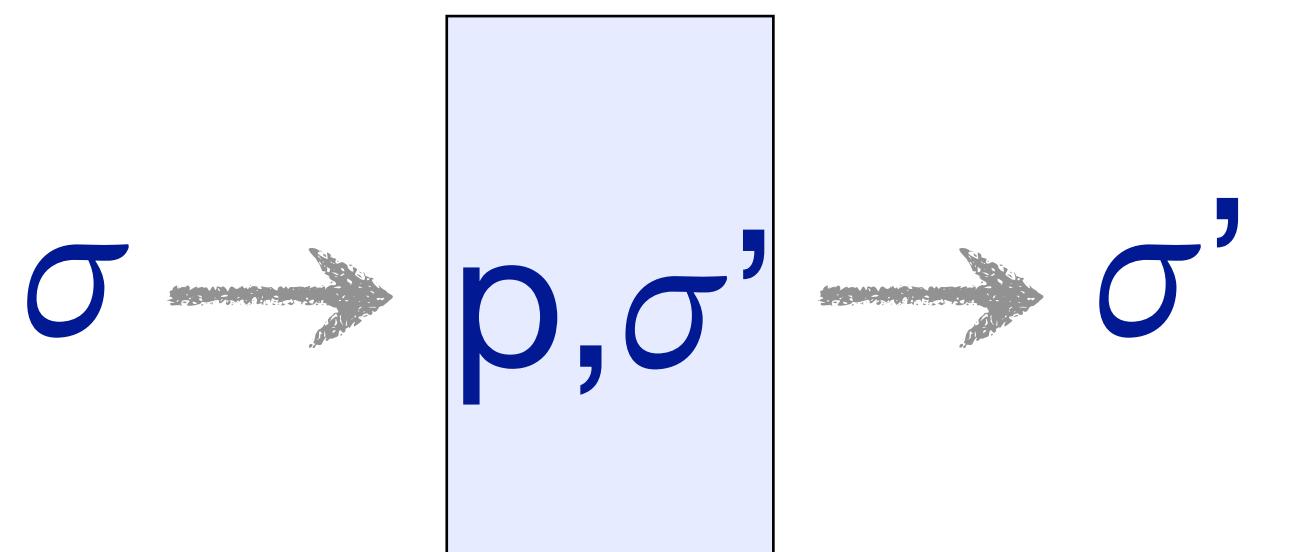
eUTXO

contract state

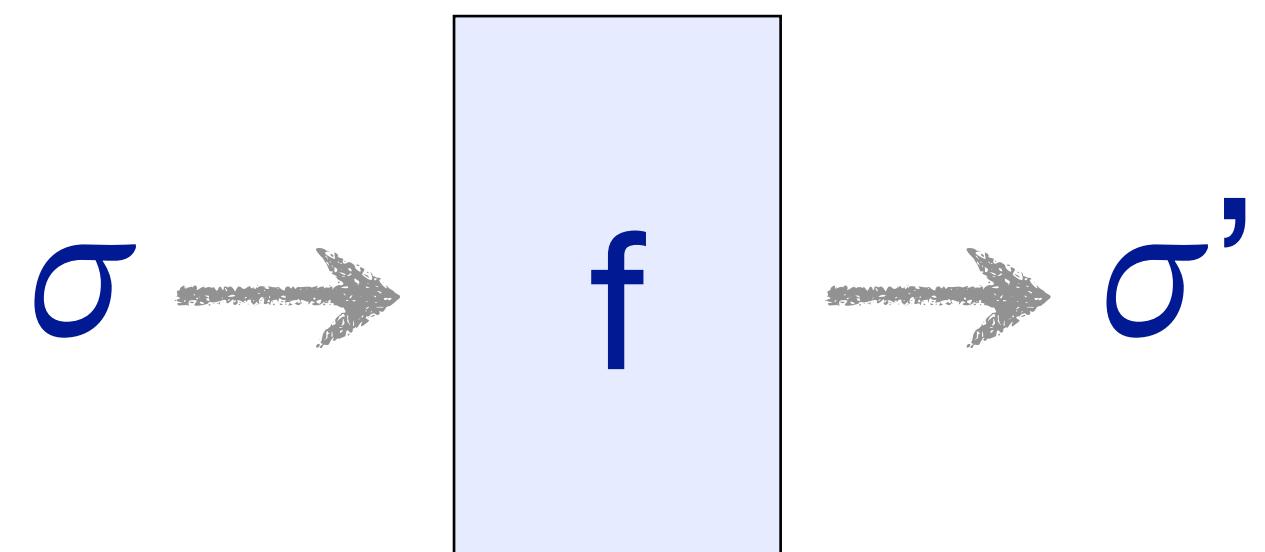


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Account



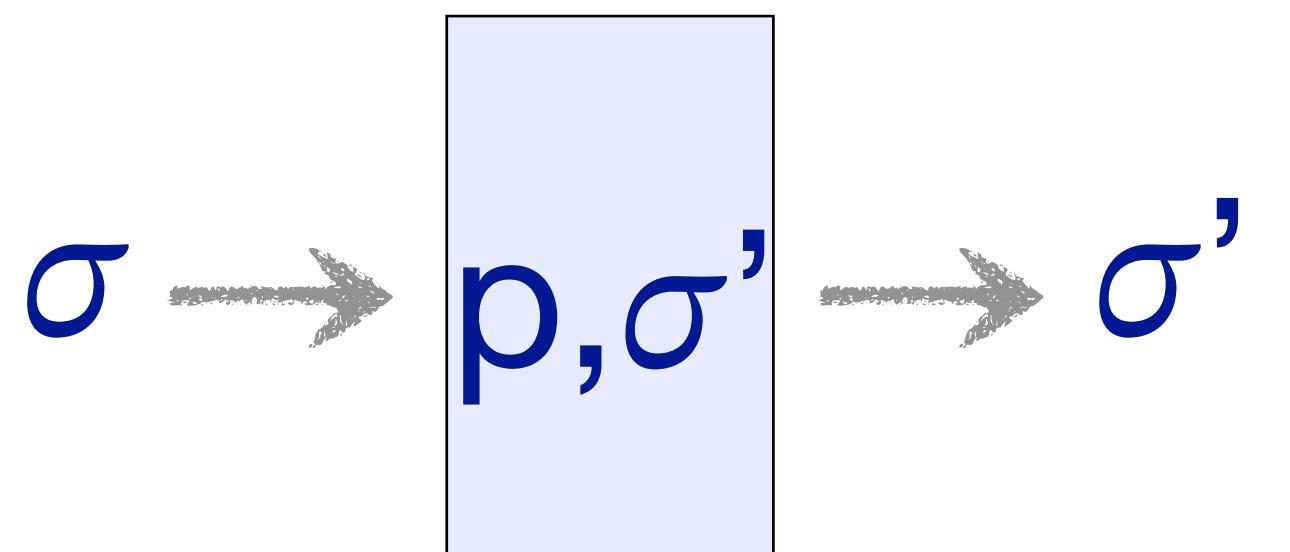
$p(\sigma, \sigma') = \text{true}$



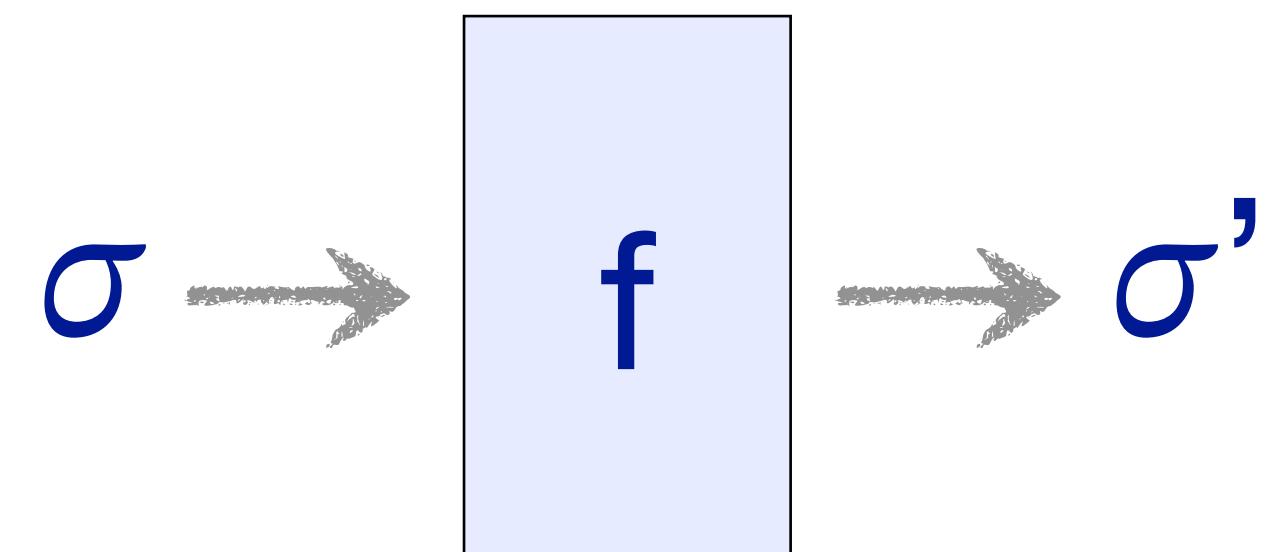
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Account



$p(\sigma, \sigma') = \text{true}$



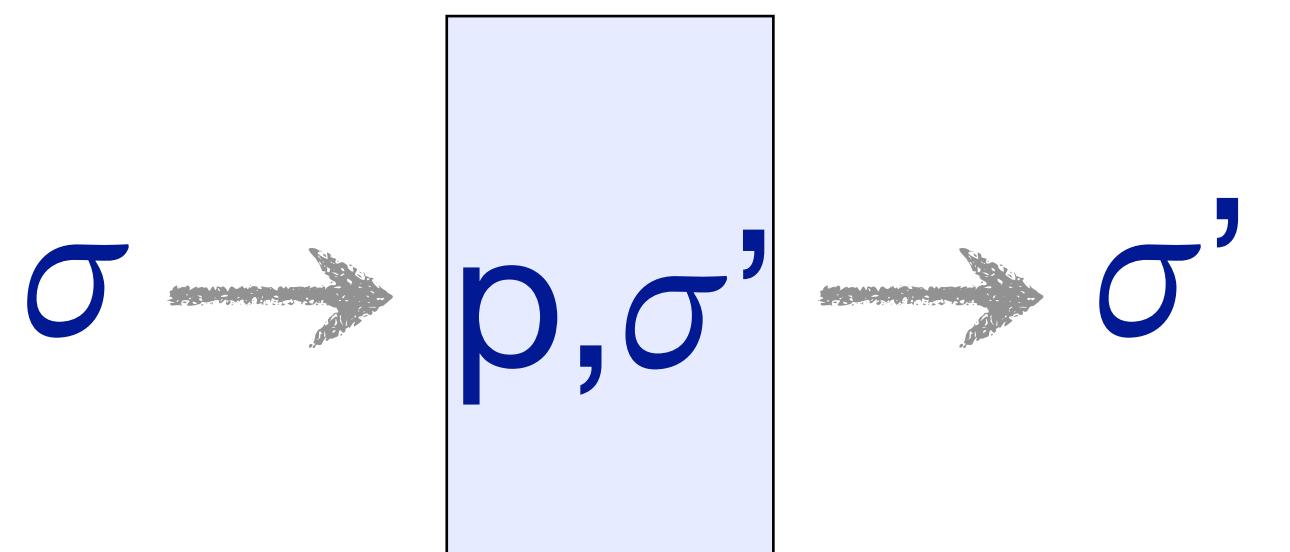
$f(\sigma) = \sigma'$

verification

computation

eUTXO

Account

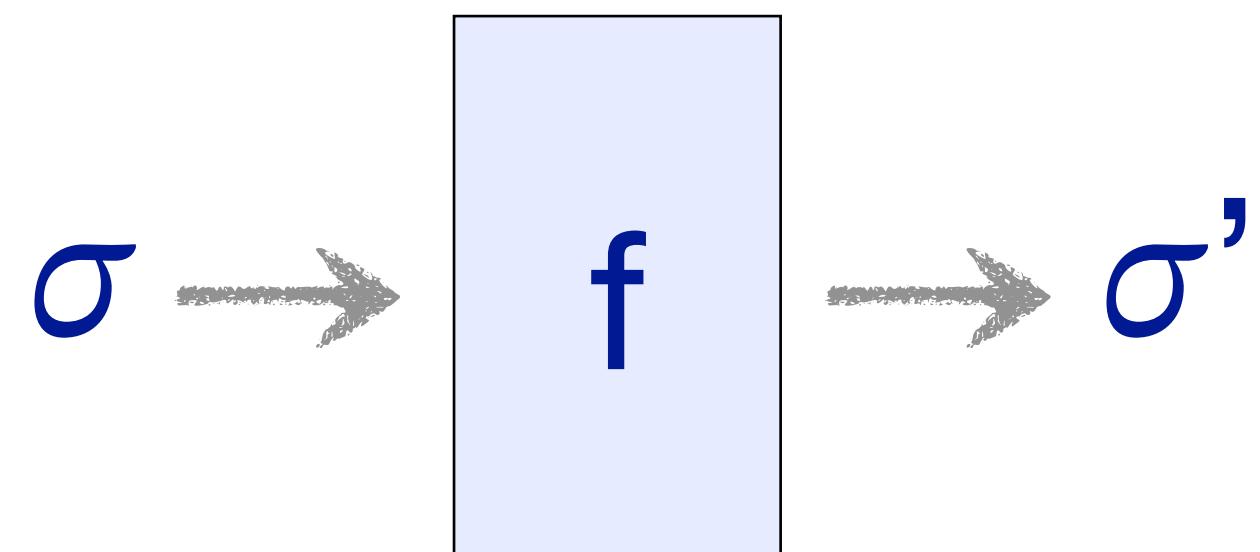


$$p(\sigma, \sigma') = \text{true}$$

verification

determinism

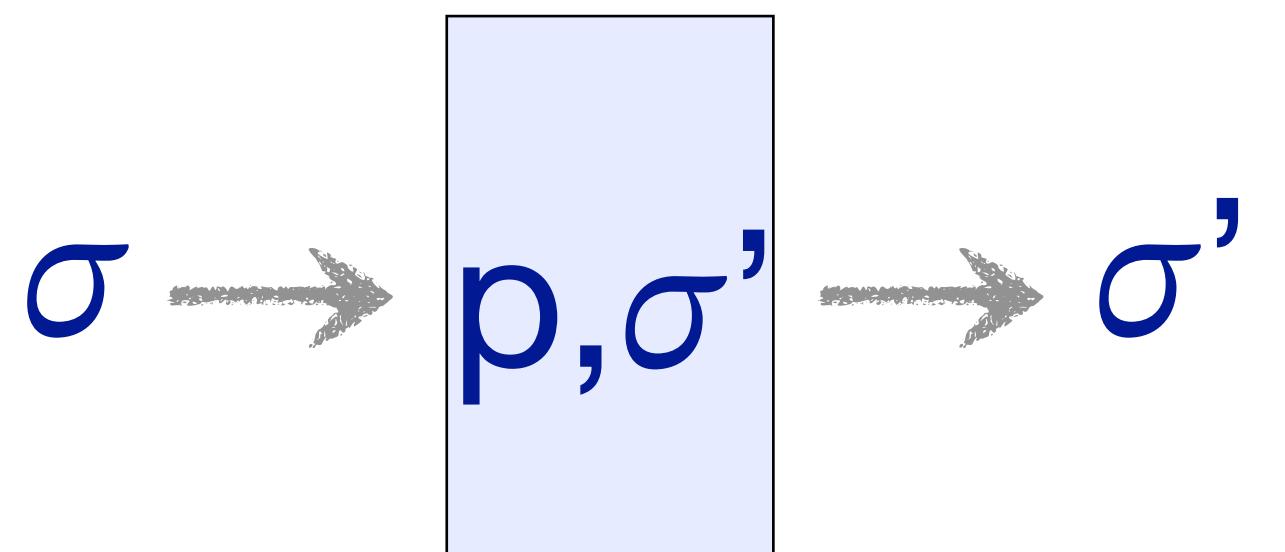
eUTXO



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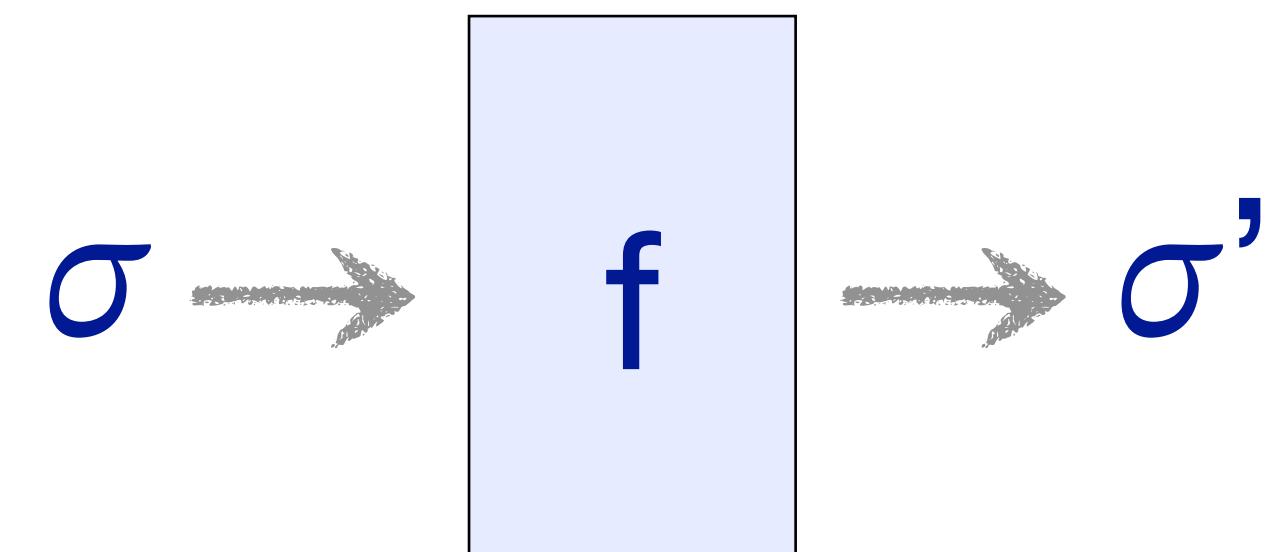
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Account



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verification



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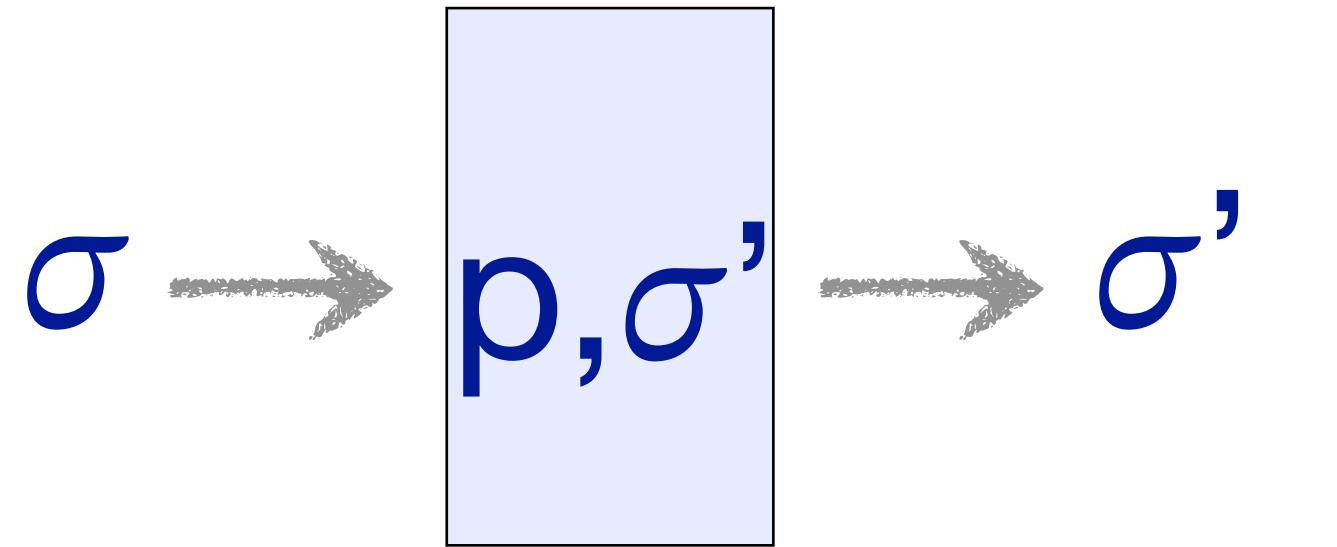
computation

determinism

computation happens off-chain

eUTXO

Account



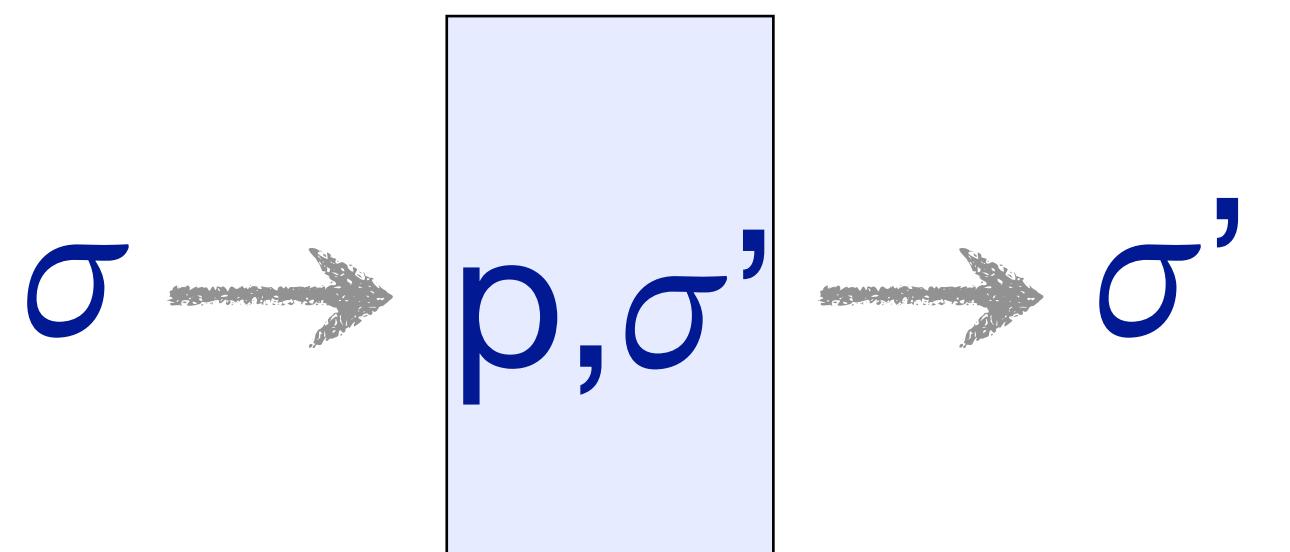
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Needs a programming model

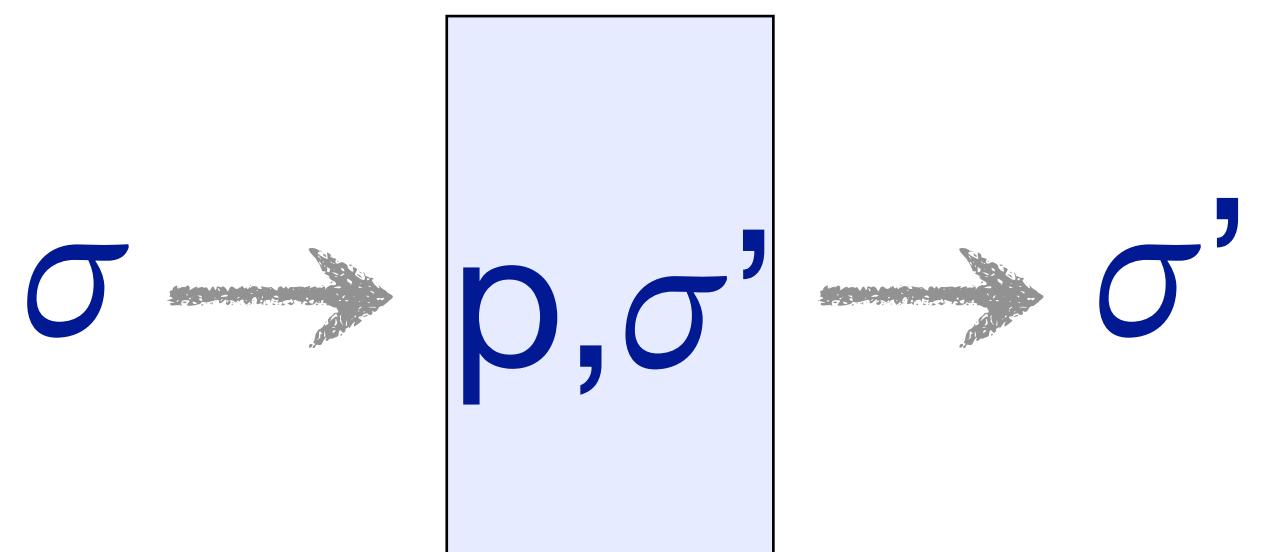
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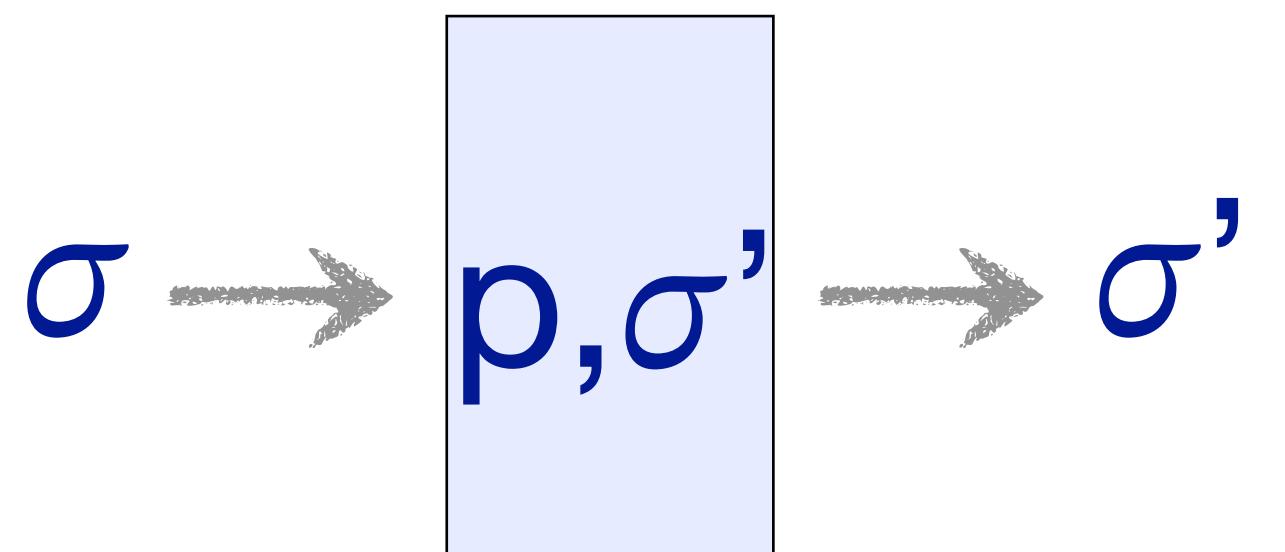
Needs a programming model  
integrate on-chain and off-chain

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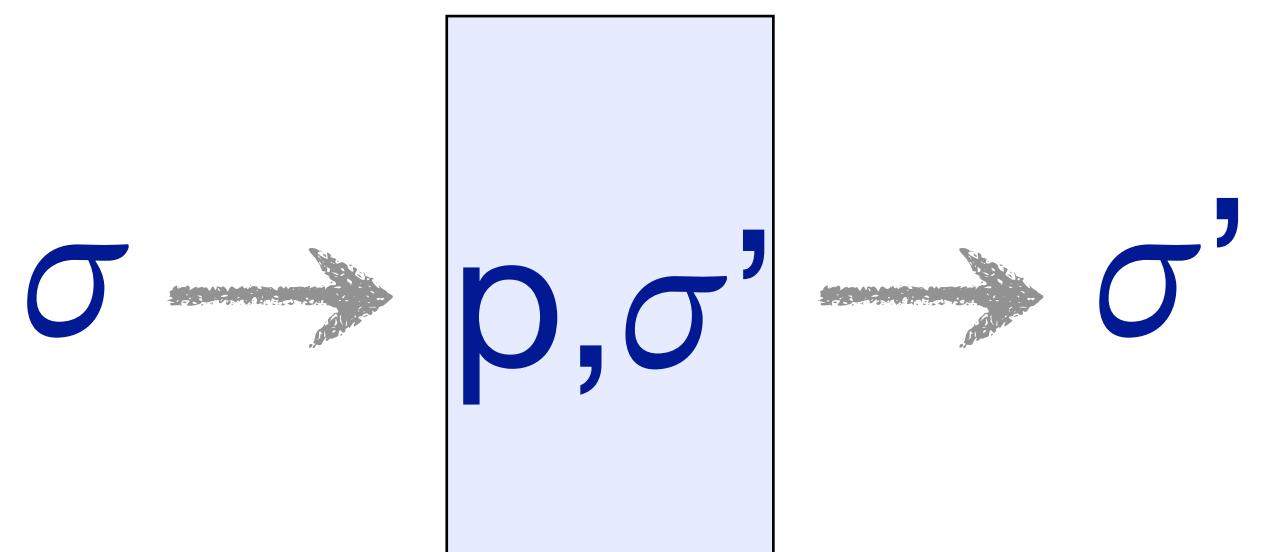
hide implementation details

verification

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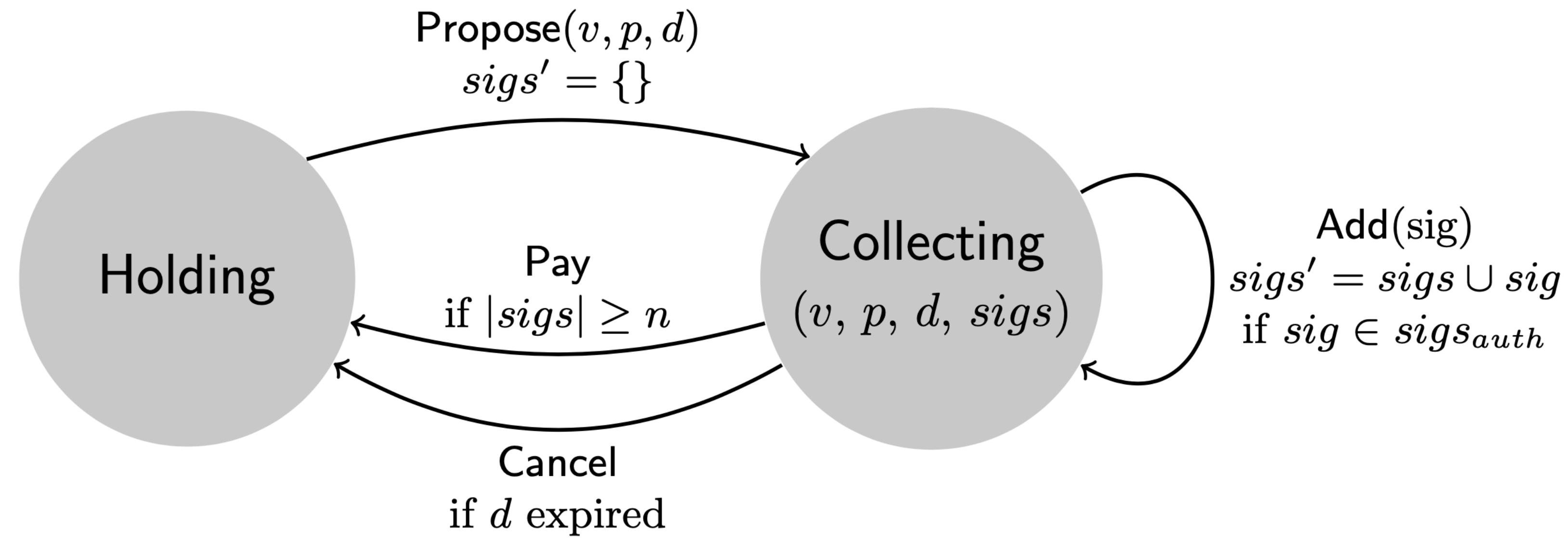
formal reasoning



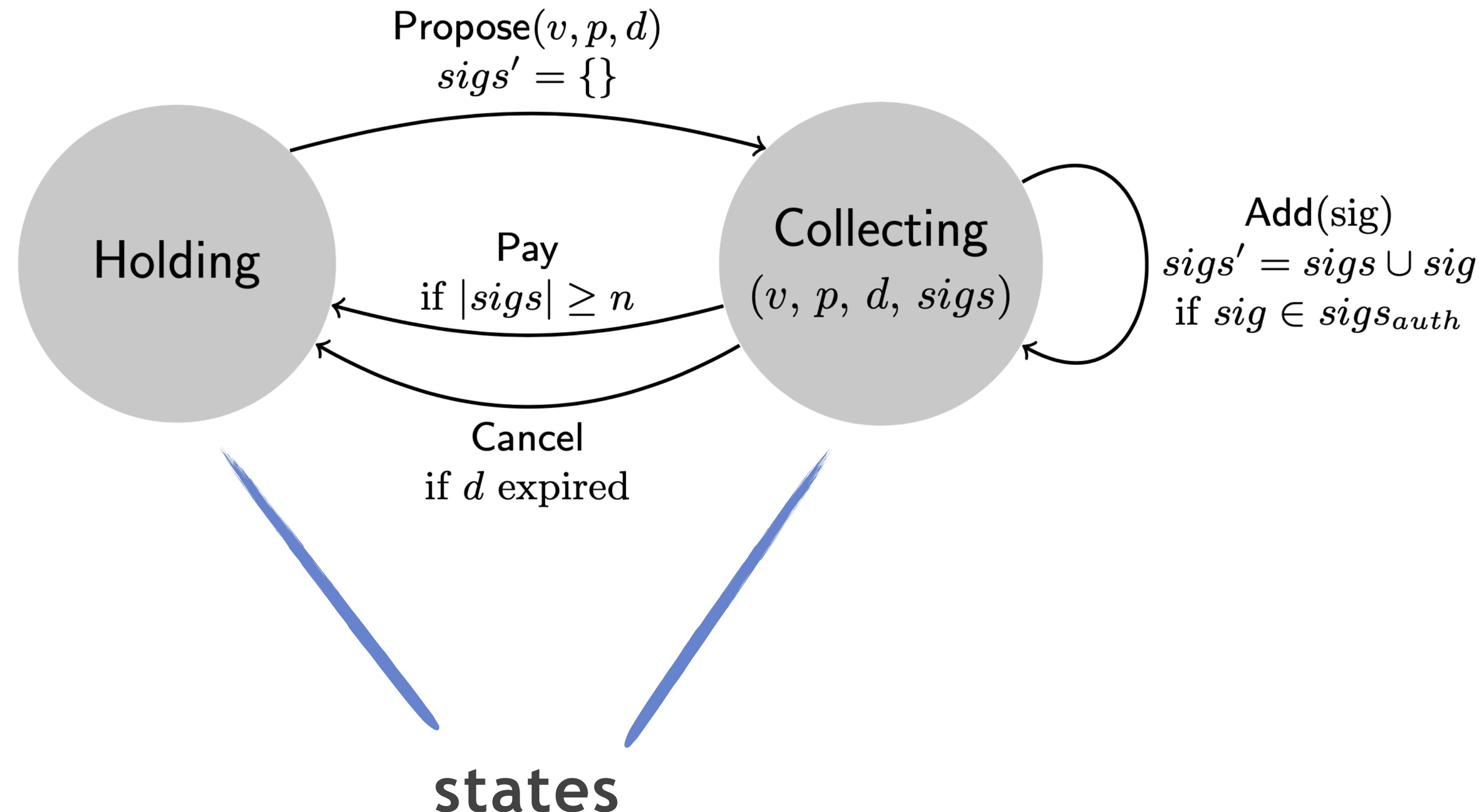
# State Machines

## Logical model for contracts

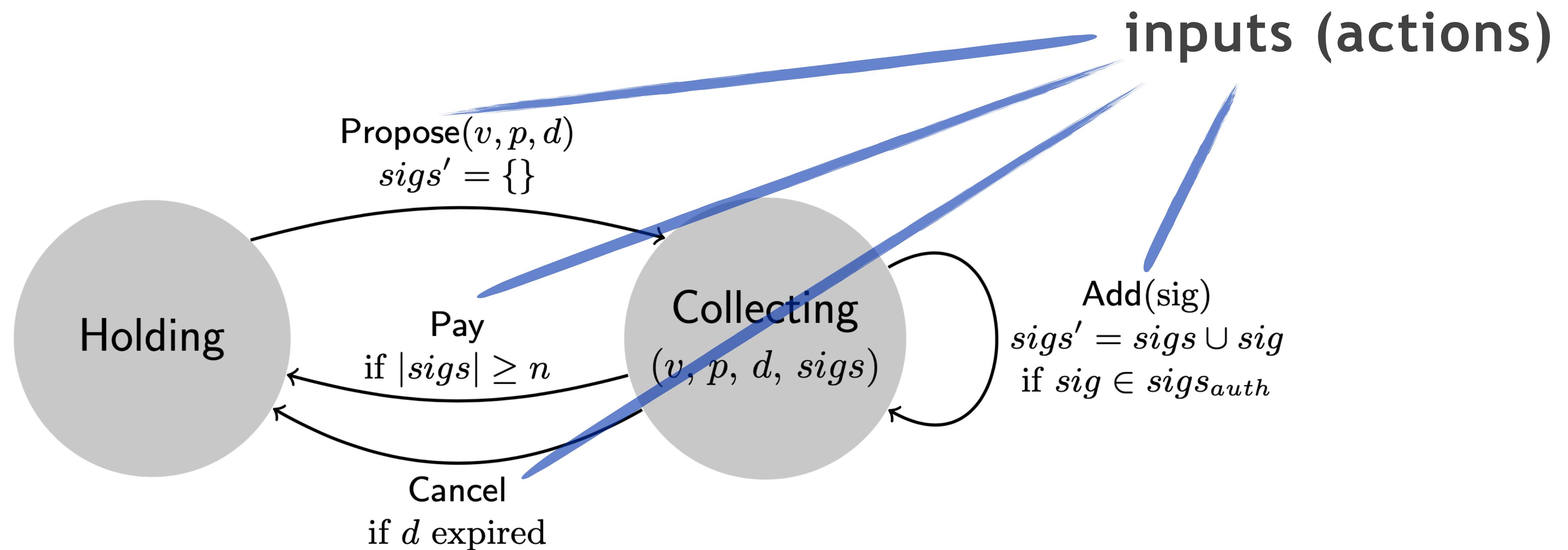
# Constraint Emitting Machines (CEMs)



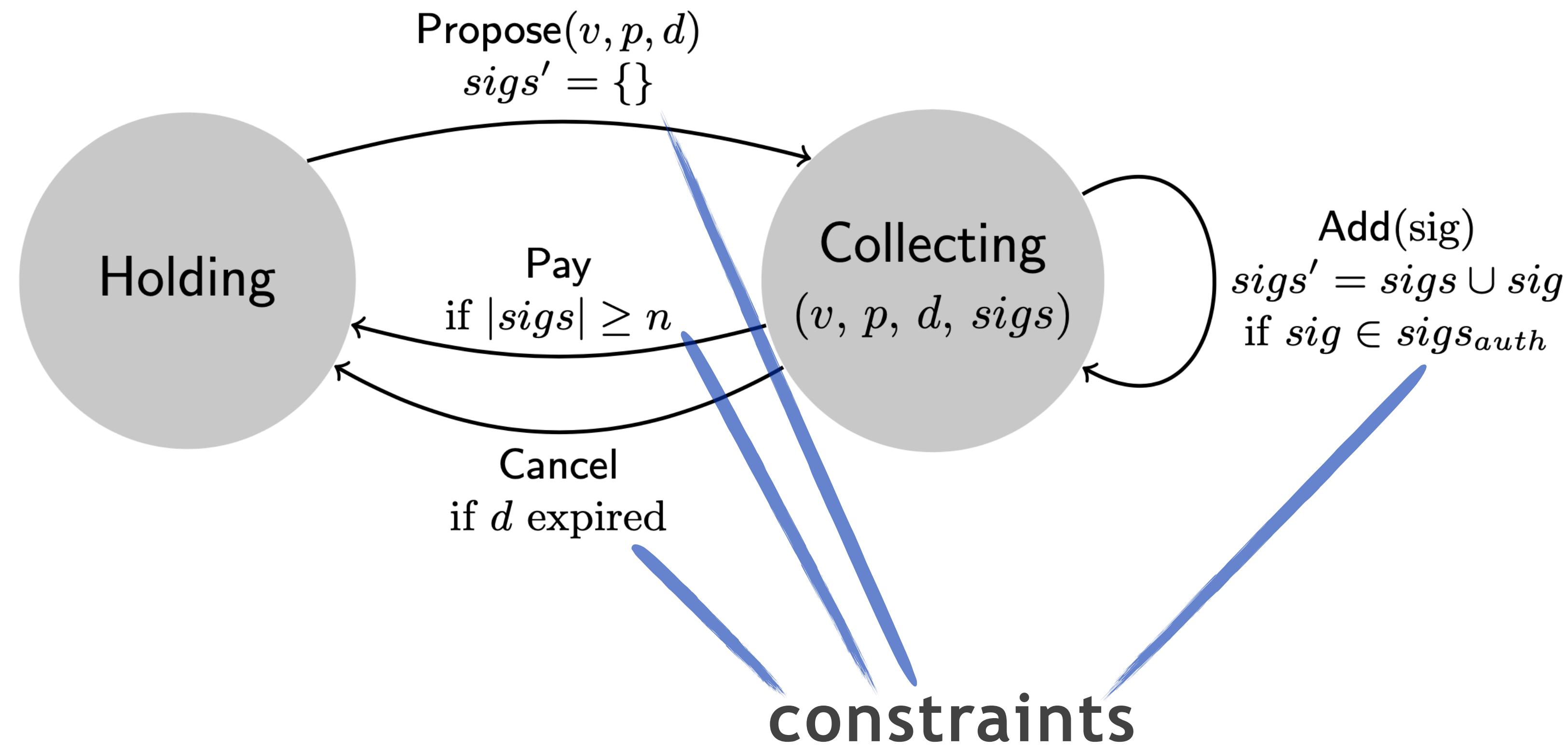
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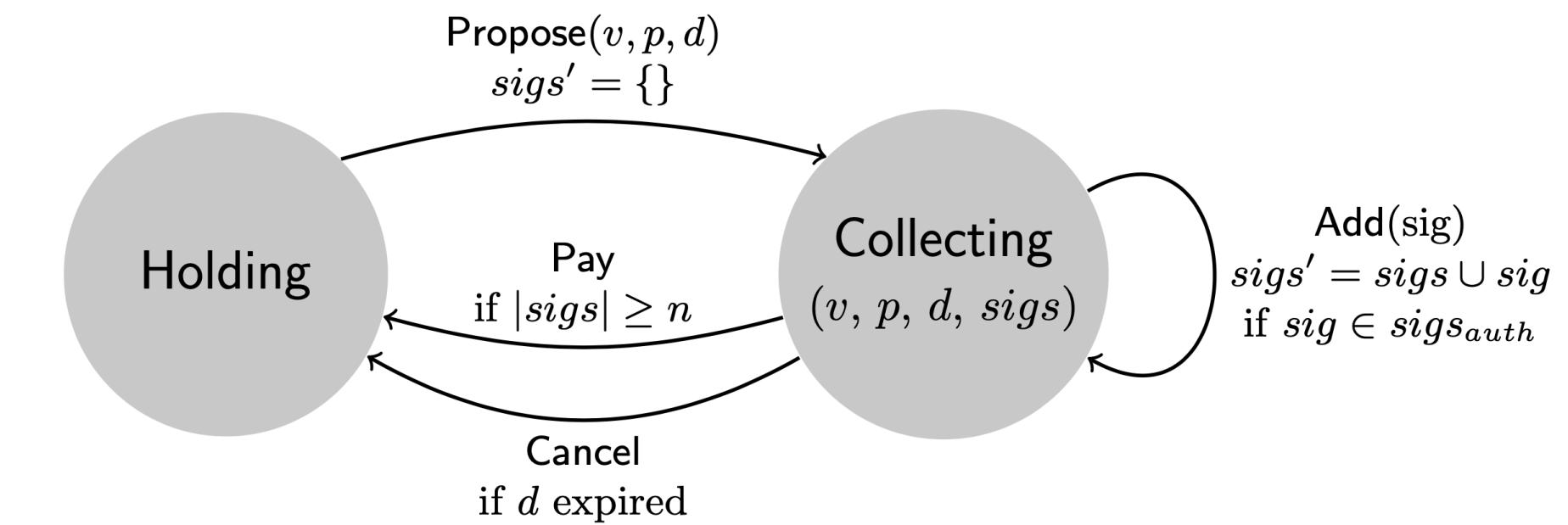


# Constraint Emitting Machines

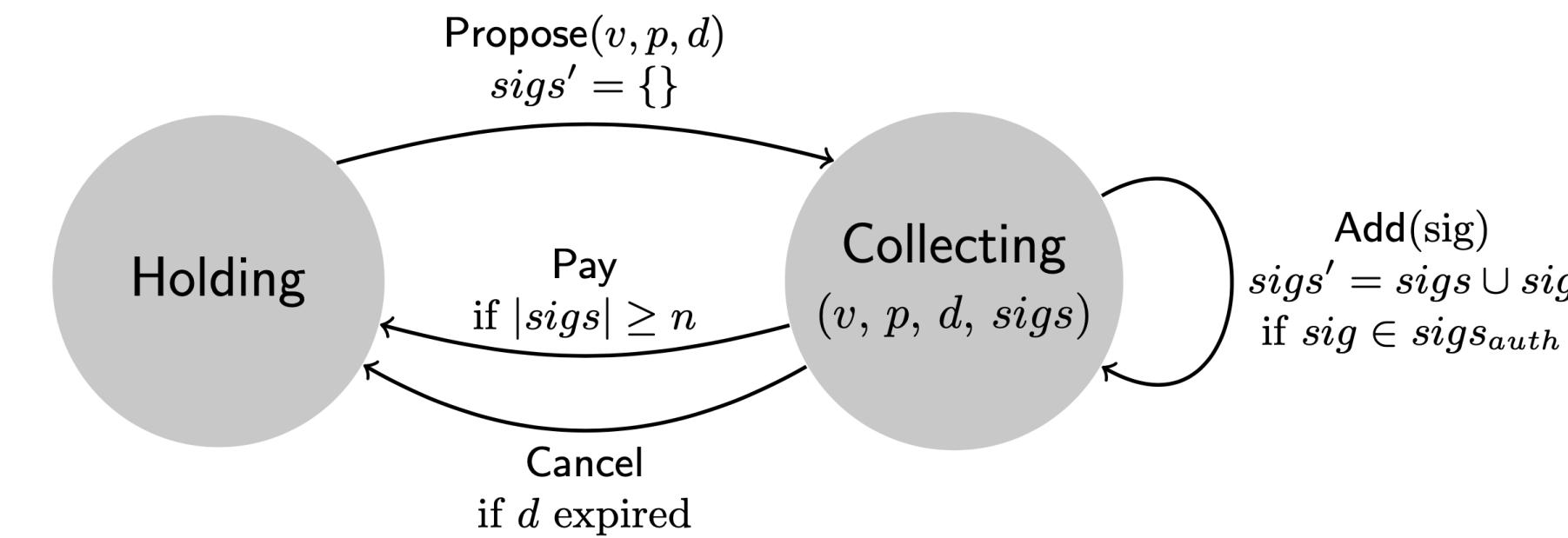


# Constraint Emitting Machines



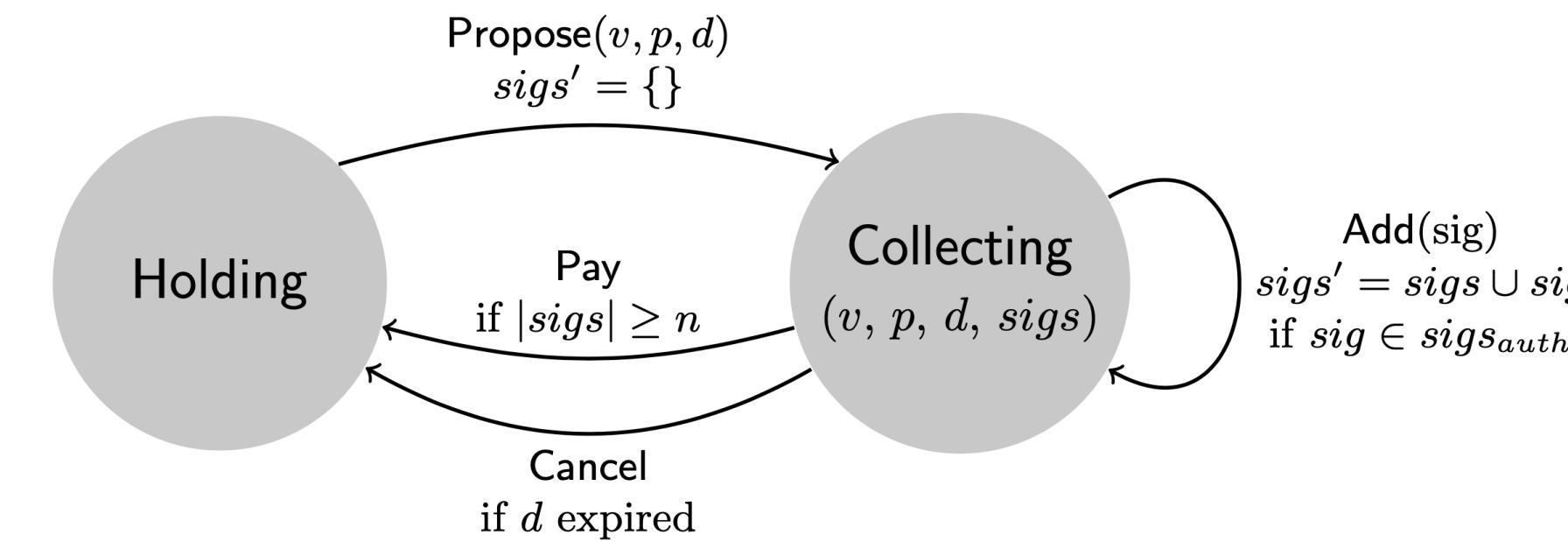


# Plutus state machine library is too inefficient



Plutus state machine library is too inefficient

CEMs not captured by standard automata theory



Plutus state machine library is too inefficient

CEMs not captured by standard automata theory

Constraints serve as guards, but treated like outputs

# Automata Contracts

# Specification & implementation



# Deterministic Finite Automata

base states and transition labels

# Deterministic Finite Automata

Deterministic Finite Automata

contract state and actions

base states and transition labels

augmenting DFA states and labels

base states and transition labels

Deterministic Finite Automata

contract state and actions

augmenting DFA states and labels

specification

base states and transition labels

Deterministic Finite Automata

contract state and actions

augmenting DFA states and labels

specification

relational

base states and transition labels

Deterministic Finite Automata

contract state and actions

augmenting DFA states and labels

specification

relational

whole system view

Deterministic Finite Automata

contract state and actions

specification

relational

whole system view

base states and transition labels

augmenting DFA states and labels



implementation

Deterministic Finite Automata

contract state and actions

specification

relational

whole system view



implementation

functional

base states and transition labels

augmenting DFA states and labels

Deterministic Finite Automata

contract state and actions

specification

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whole system view



implementation

functional

on-chain versus off-chain

base states and transition labels

augmenting DFA states and labels

Do we need a new specification language and framework?

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Maybe we can get started with Agda

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reasoning about the specification

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correctness of refinement

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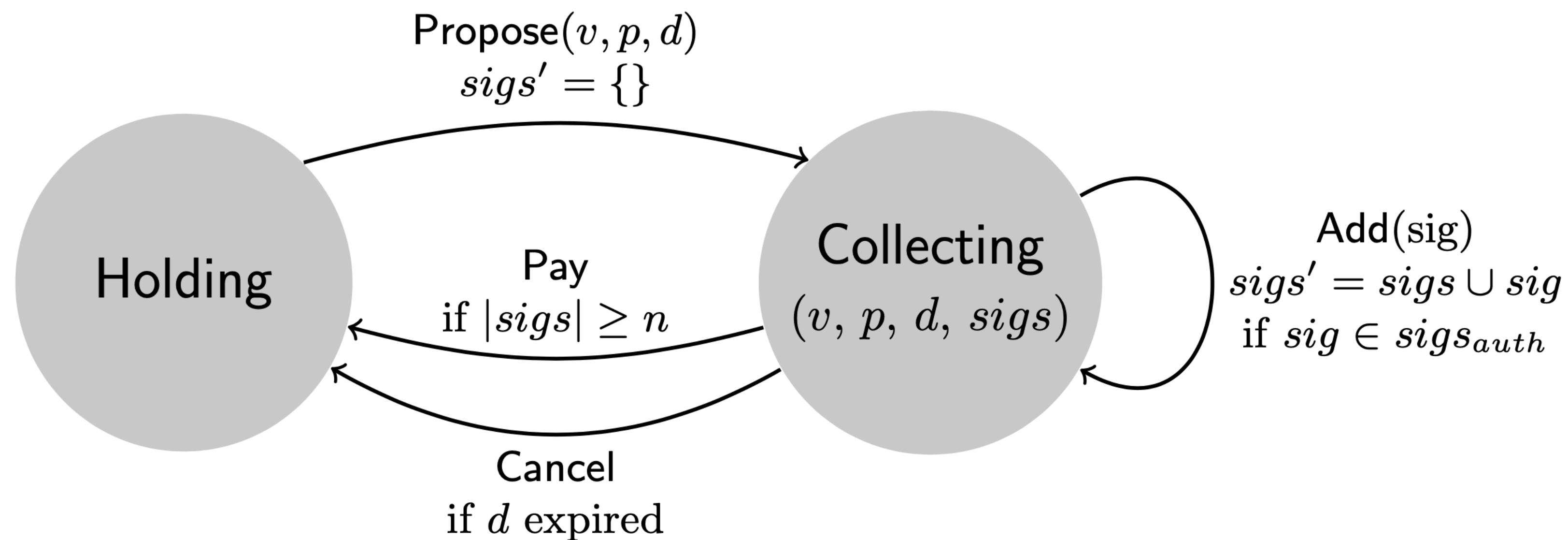
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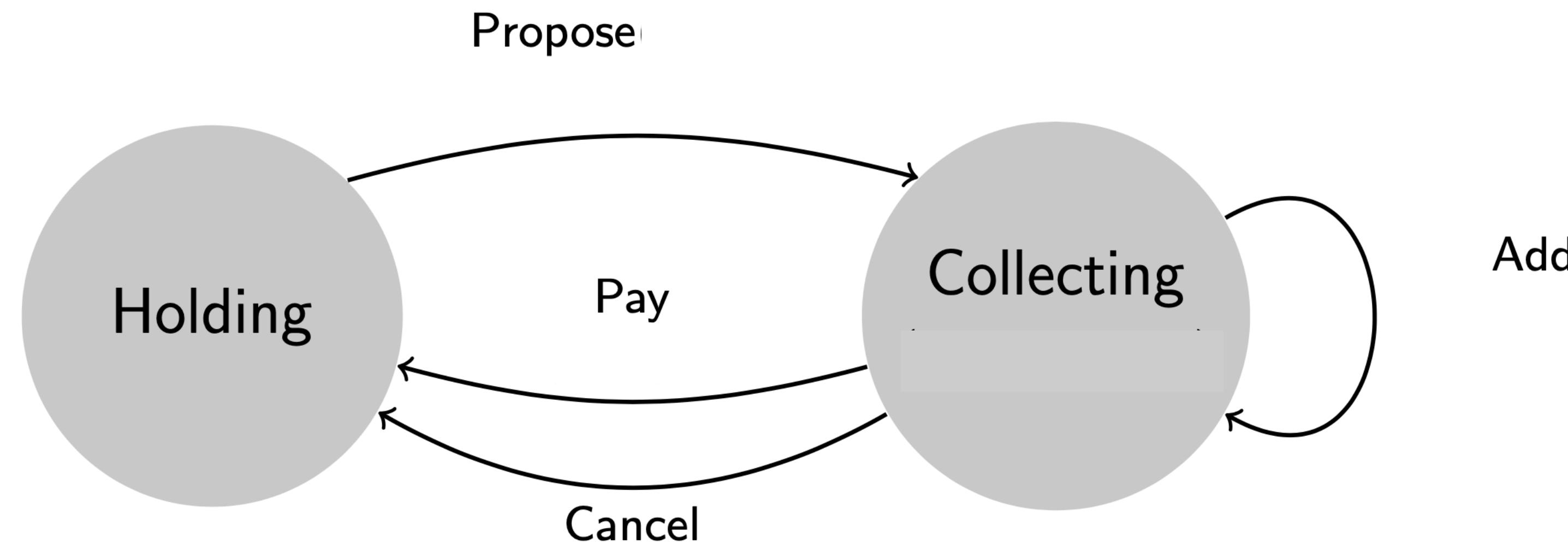
correctness of refinement

code extraction to Haskell

# Our Trusted Example

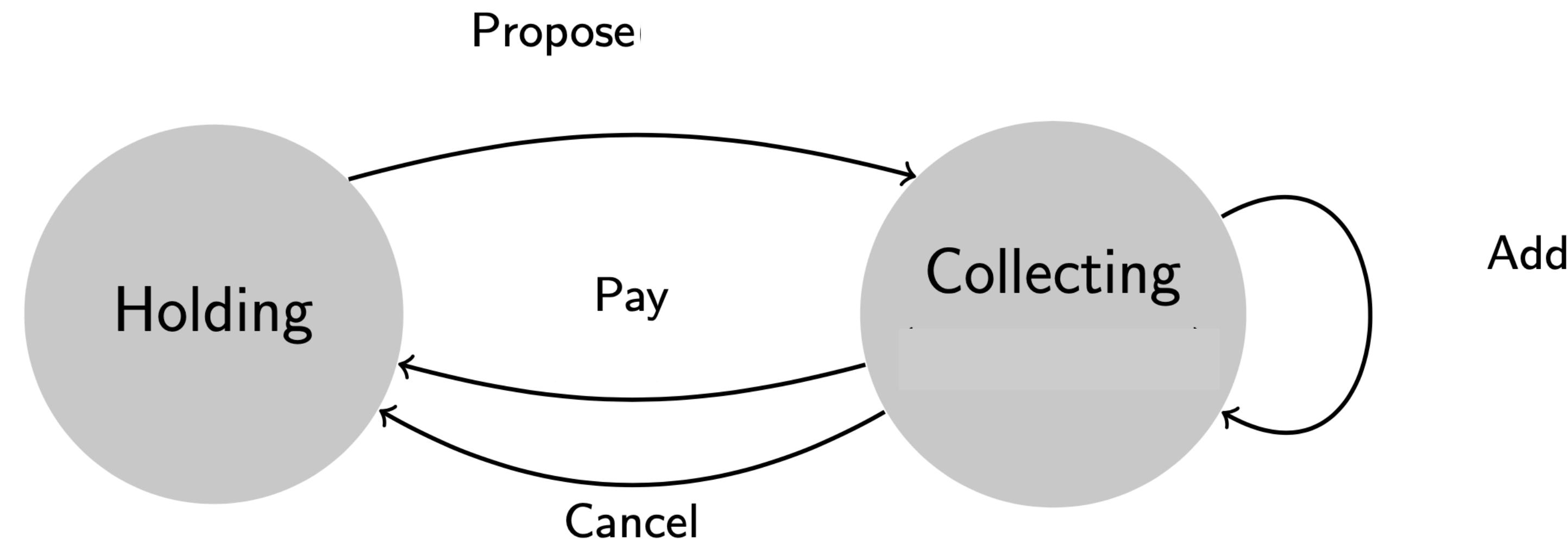


# Automata Specification



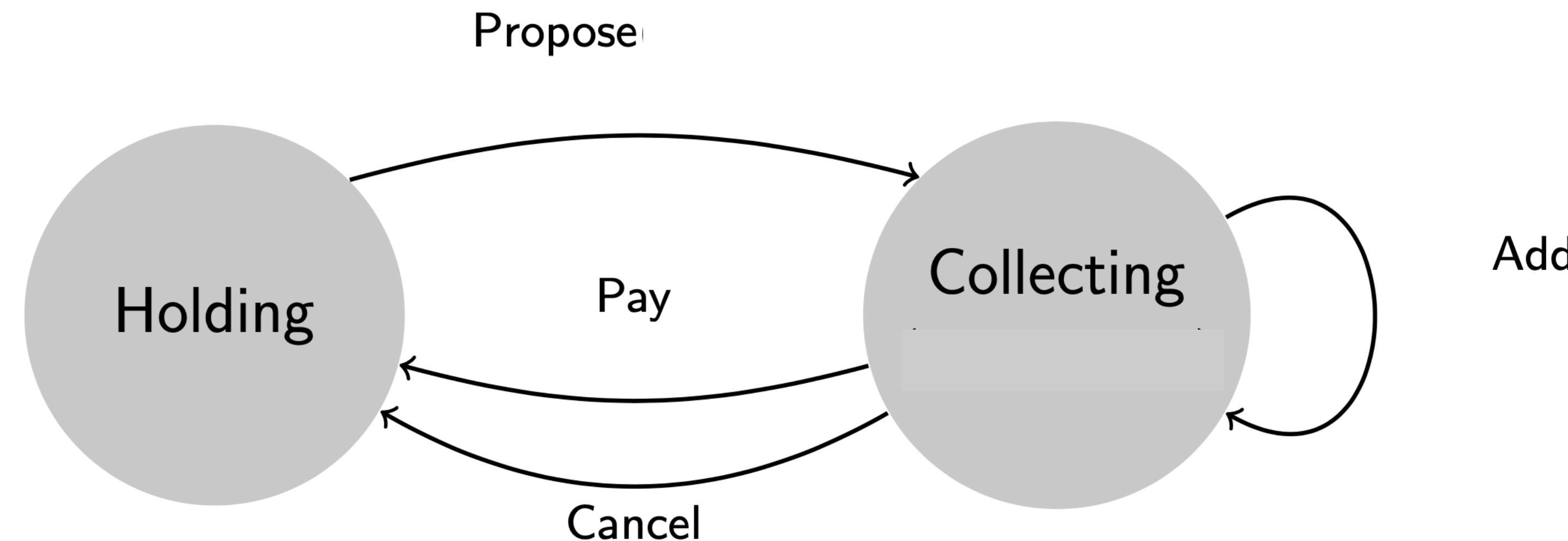
# Automata Specification

## The Base DFA



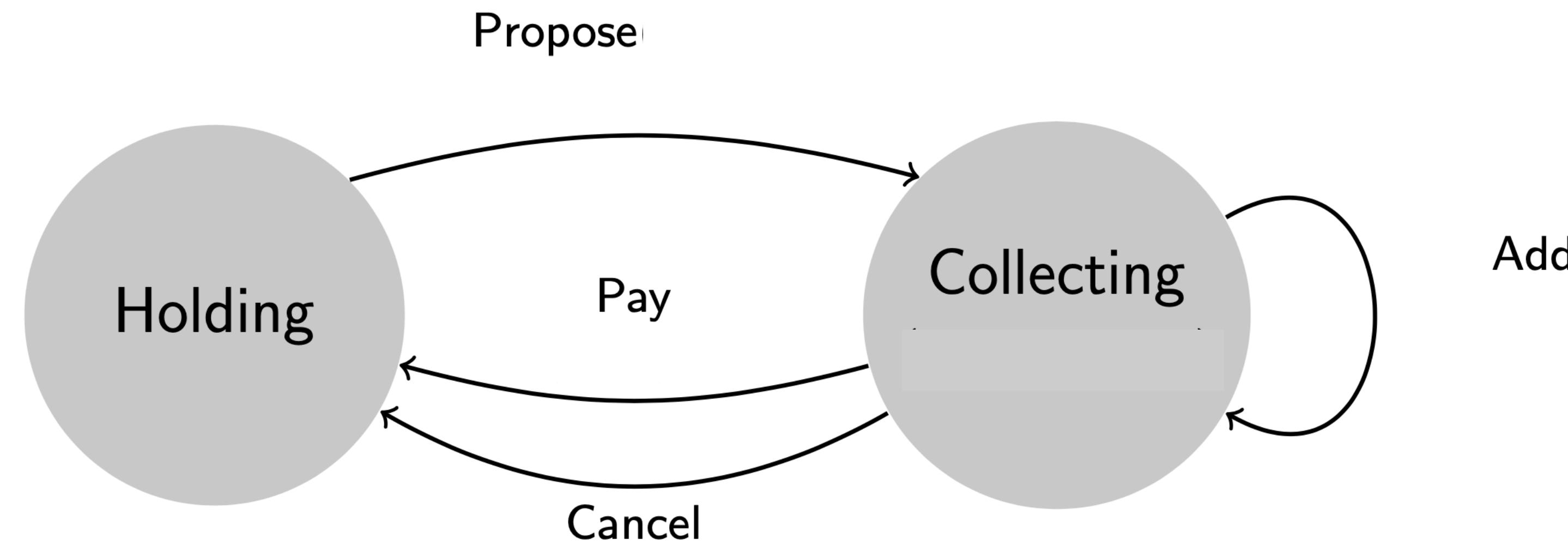
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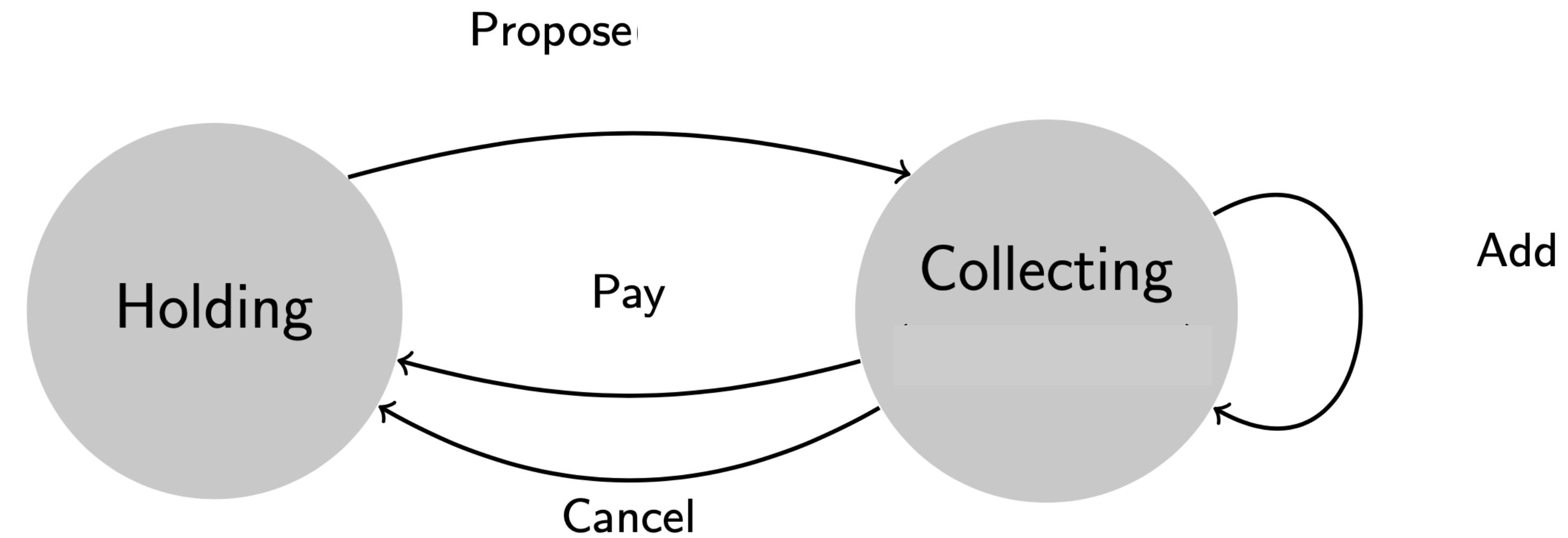


```
data State = Holding | Collecting  
data Label = Propose | Add | Pay | Cancel
```

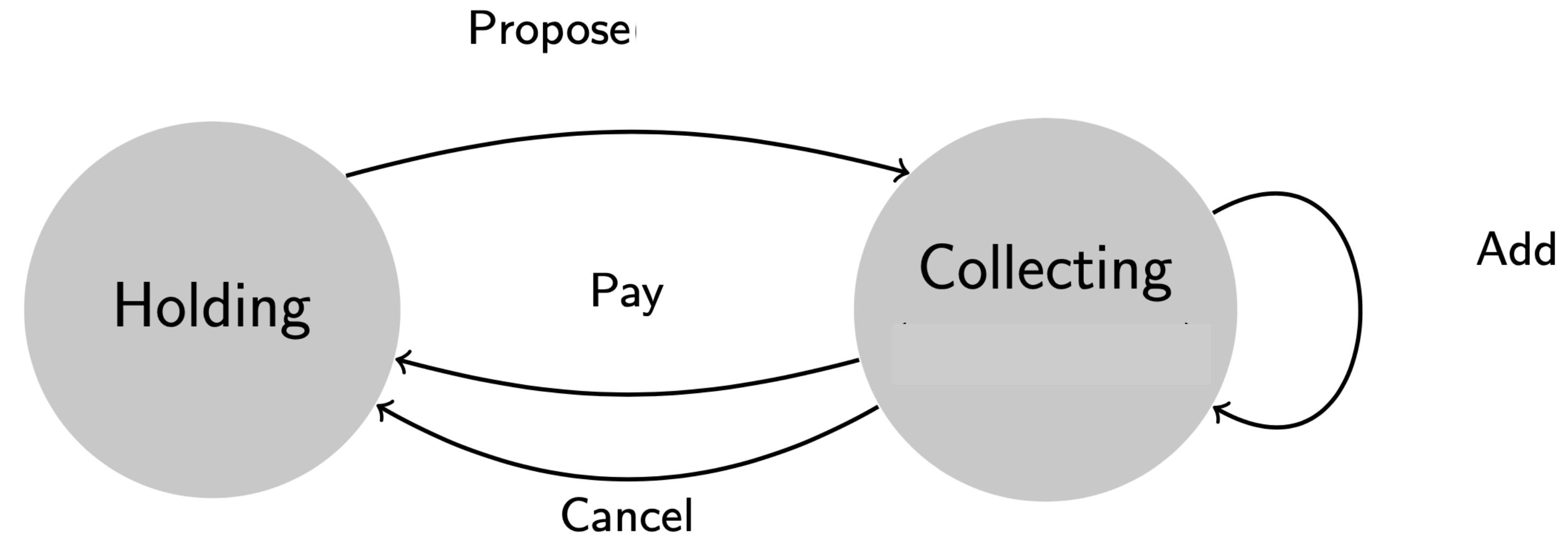
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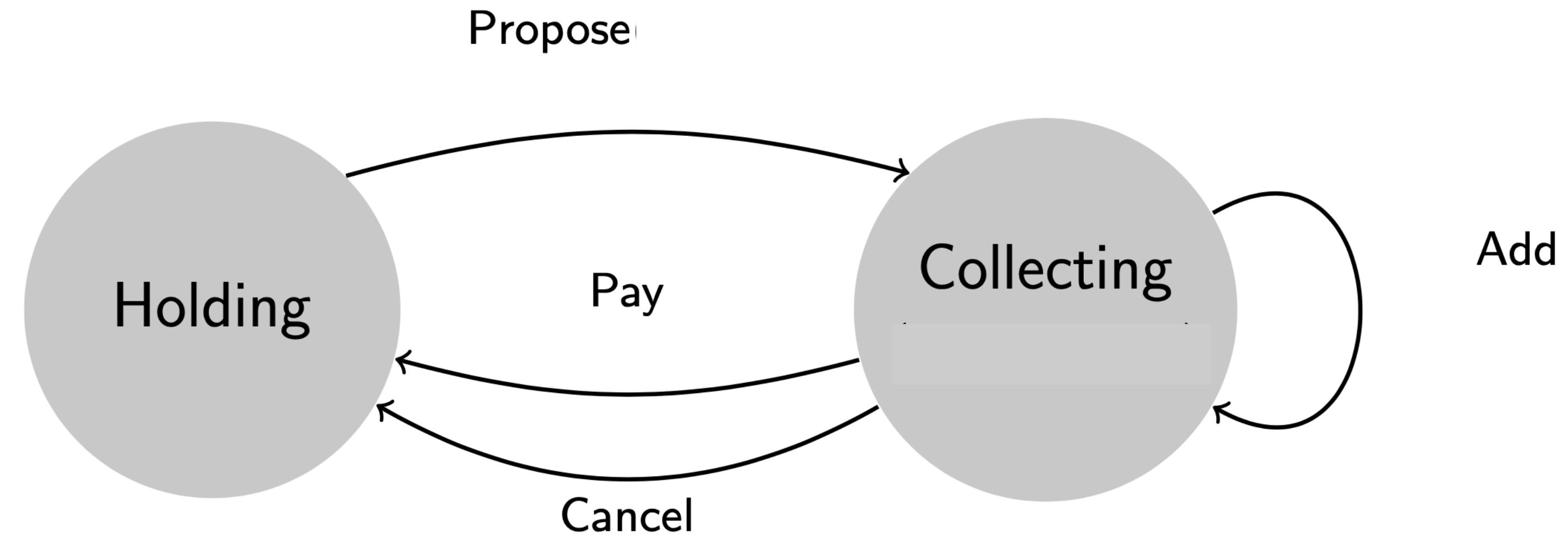


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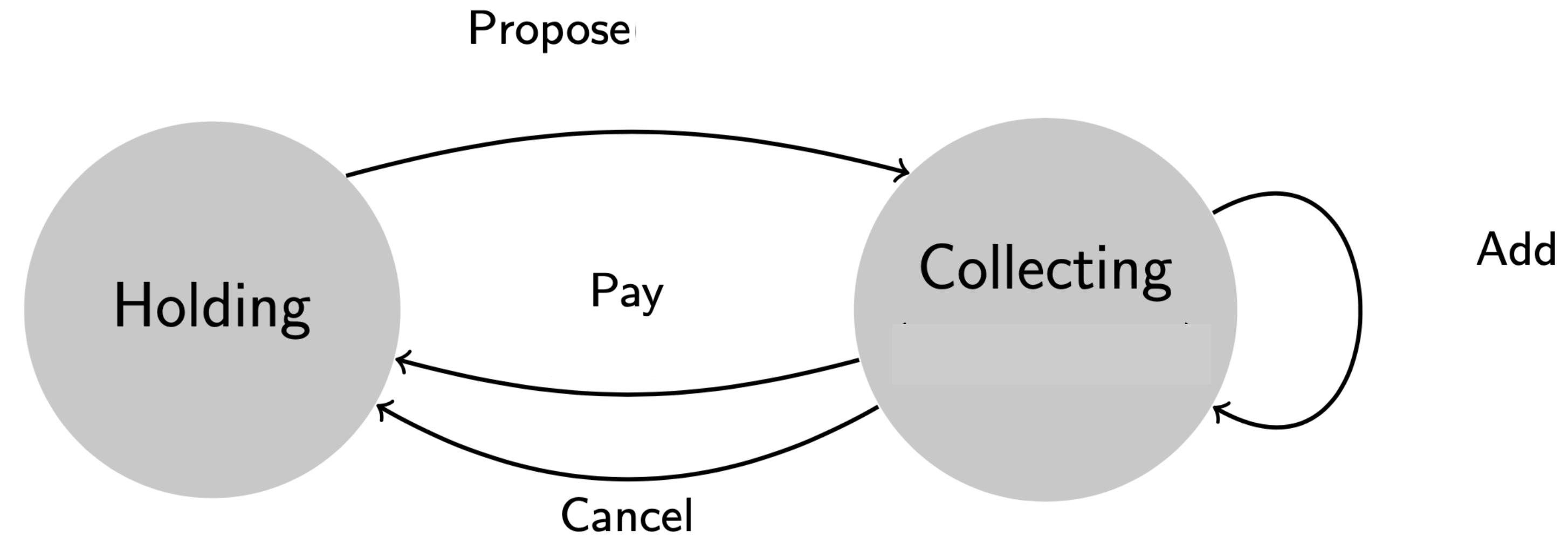


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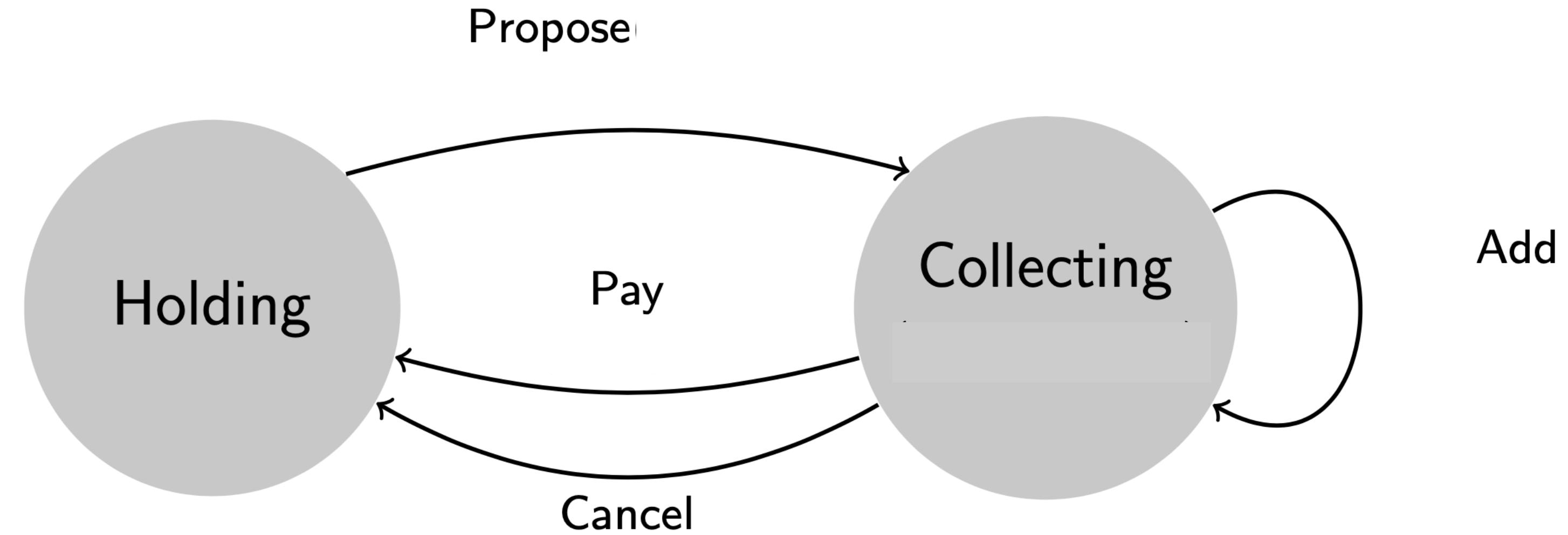


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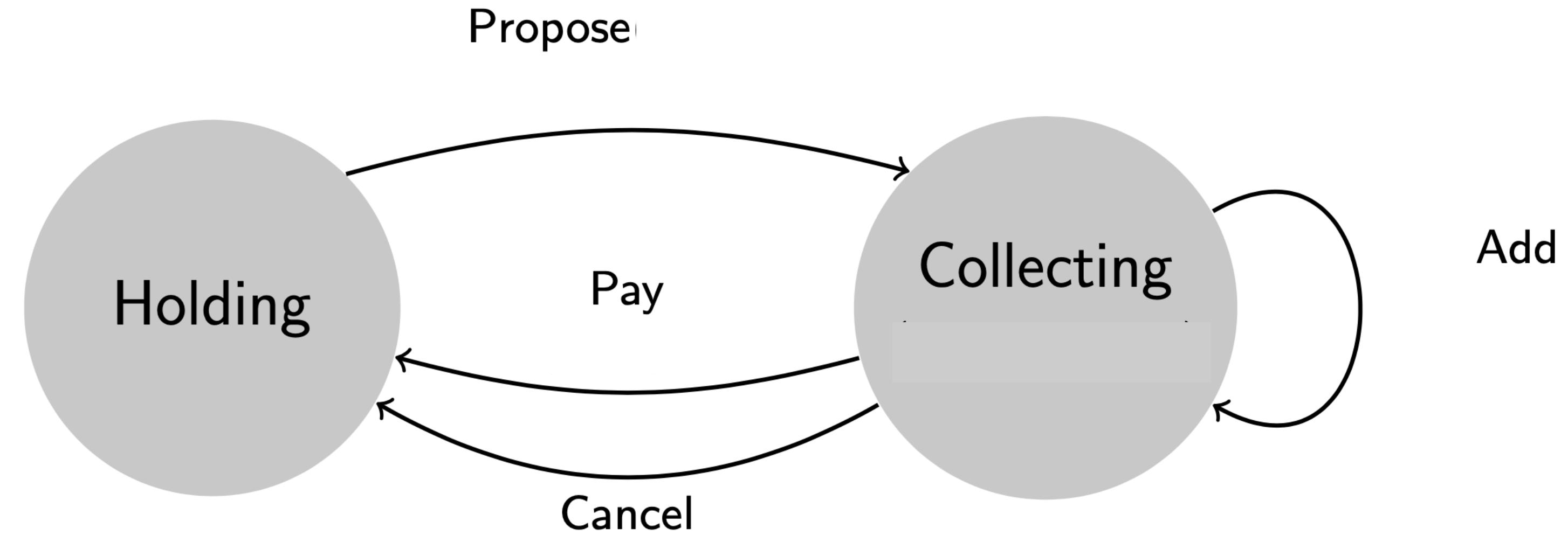


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```



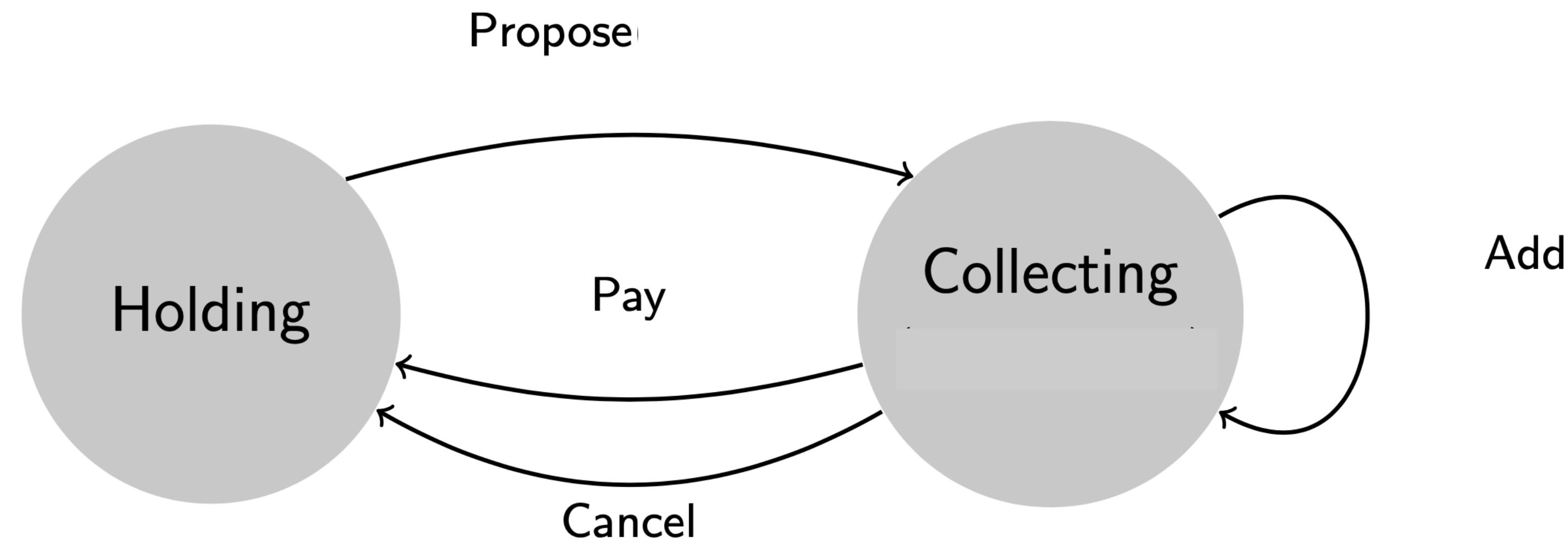
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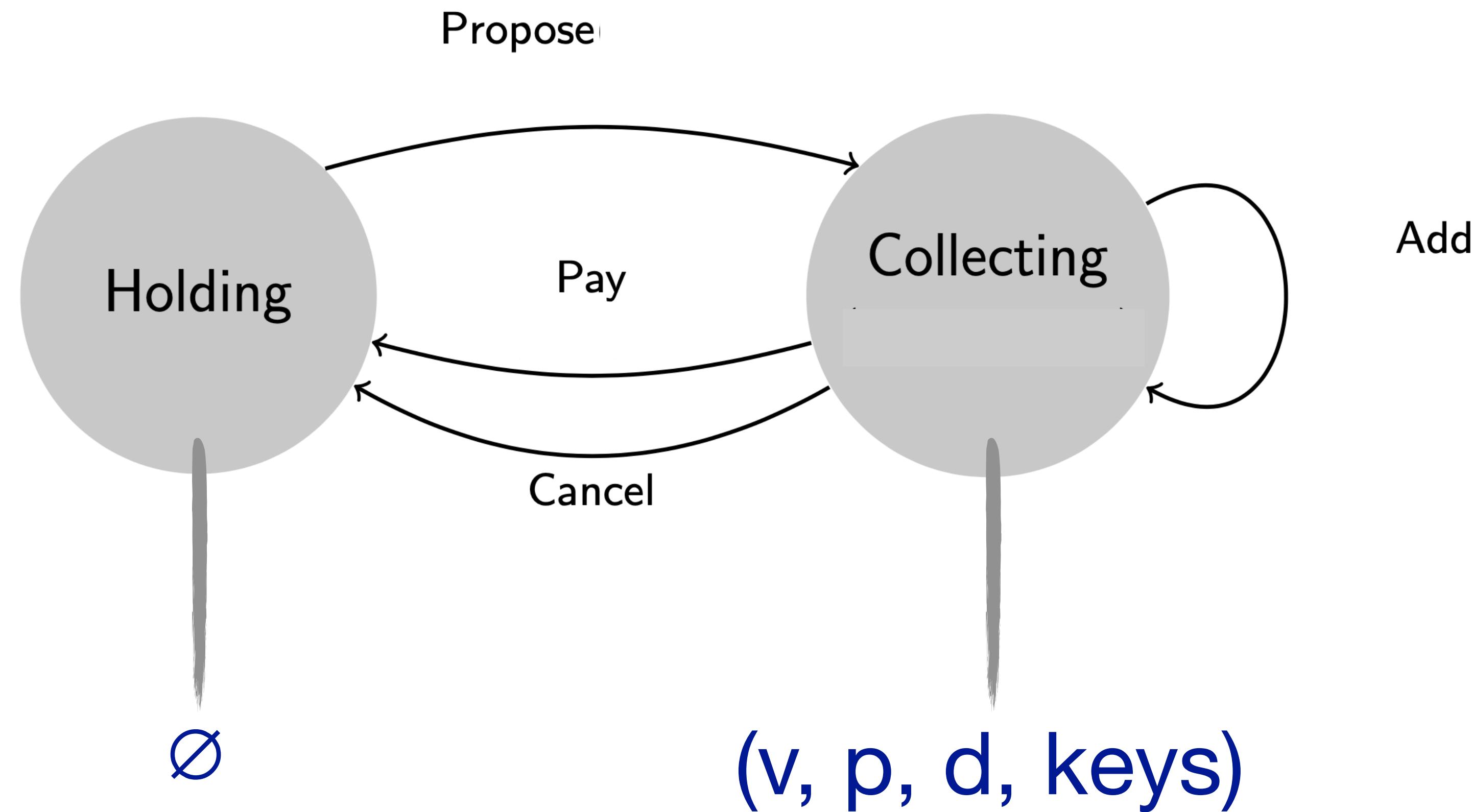
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# Augmentation



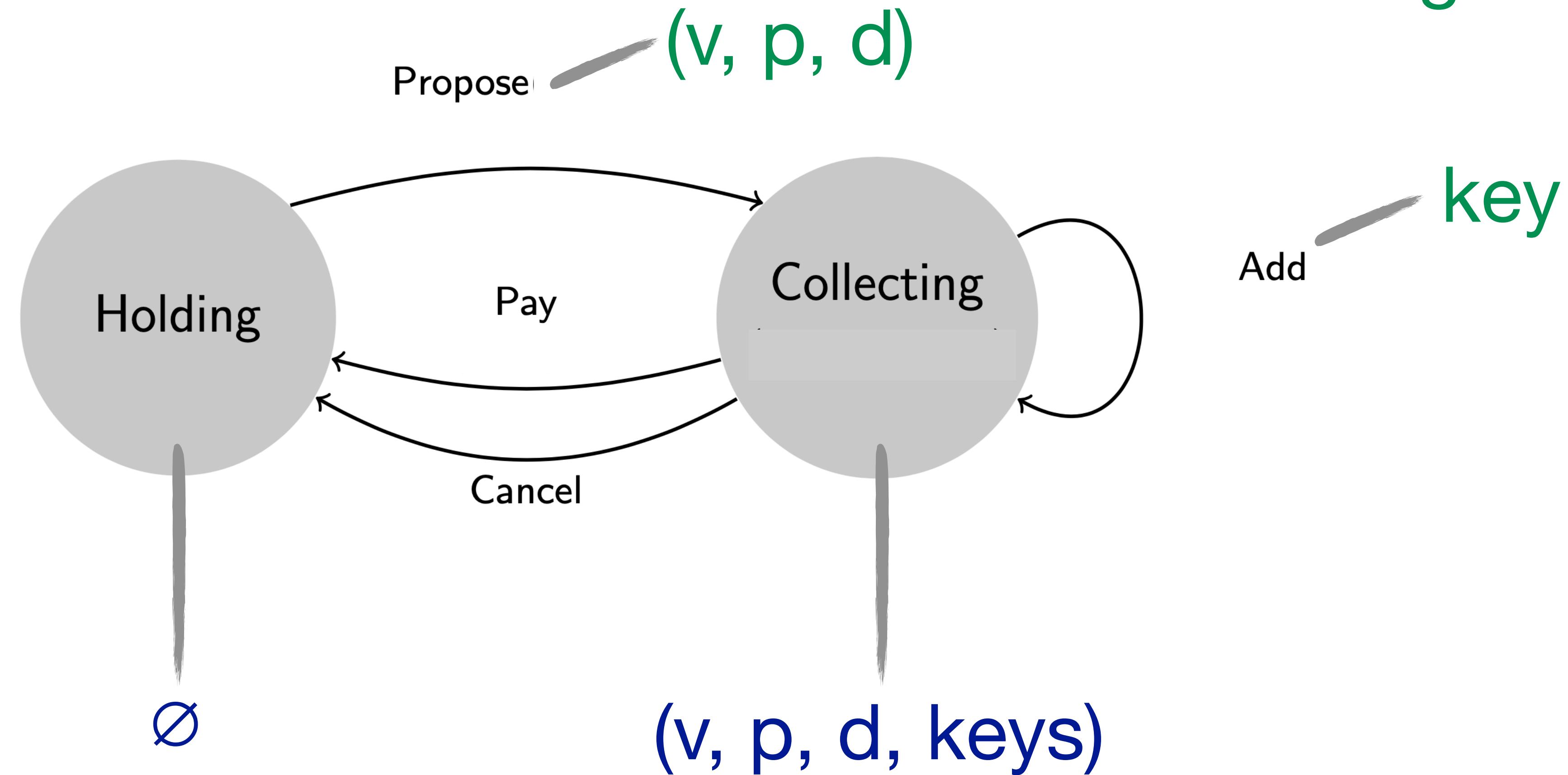
# Augmentation



contract state

# Augmentation

action arguments



contract state

# Configurations – Contract State & Actions

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```
data family ConfState (state : State) where
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                         , inputs: [ReceiveFrom]
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                          , inputs:     [ReceiveFrom]
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```

```
initial : Value -> Conf Holding
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                          , value: Value
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                          , outputs: [PayTo]
                          , duration: (Int, Int)
                          , signers: Set KeyHash
                        }
```

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initial : Value -> Conf Holding
initial val = { state = Holding
```

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type Conf (s: State) = ( state: ConfState s
                          , value: Value
                          , inputs: [ReceiveFrom]
                          , outputs: [PayTo]
                          , duration: (Int, Int)
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```

```
initial : Value -> Conf Holding
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                , value      = val
```

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                          , value: Value
                          , inputs: [ReceiveFrom]
                          , outputs: [PayTo]
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```

```
initial : Value -> Conf Holding
initial val = ( state      = Holding
                , value      = val
                , inputs     = [ReceiveFrom val owner]
```

```
type Conf (s: State) = ( state: ConfState s
                          , value: Value
                          , inputs: [ReceiveFrom]
                          , outputs: [PayTo]
                          , duration: (Int, Int)
                          , signers: Set KeyHash
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```

```
initial : Value -> Conf Holding
initial val = ( state      = Holding
                , value      = val
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                , outputs    = []
```

```
type Conf (s: State) = ( state: ConfState s
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                        )
```

```
initial : Value -> Conf Holding
initial val = ( state      = Holding
                , value      = val
                , inputs     = [ReceiveFrom val owner]
                , outputs    = []
                , duration   = (startTime, startTime)
```

```
type Conf (s: State) = ( state:      ConfState s
                          , value:       Value
                          , inputs:      [ReceiveFrom]
                          , outputs:     [PayTo]
                          , duration:   (Int, Int)
                          , signers:    Set KeyHash
                        )
```

```
initial : Value -> Conf Holding
initial val = ( state      = Holding
                , value       = val
                , inputs      = [ReceiveFrom val owner]
                , outputs     = []
                , duration   = (startTime, startTime)
                , signers    = { owner }
              )
```

# Configuration Relation

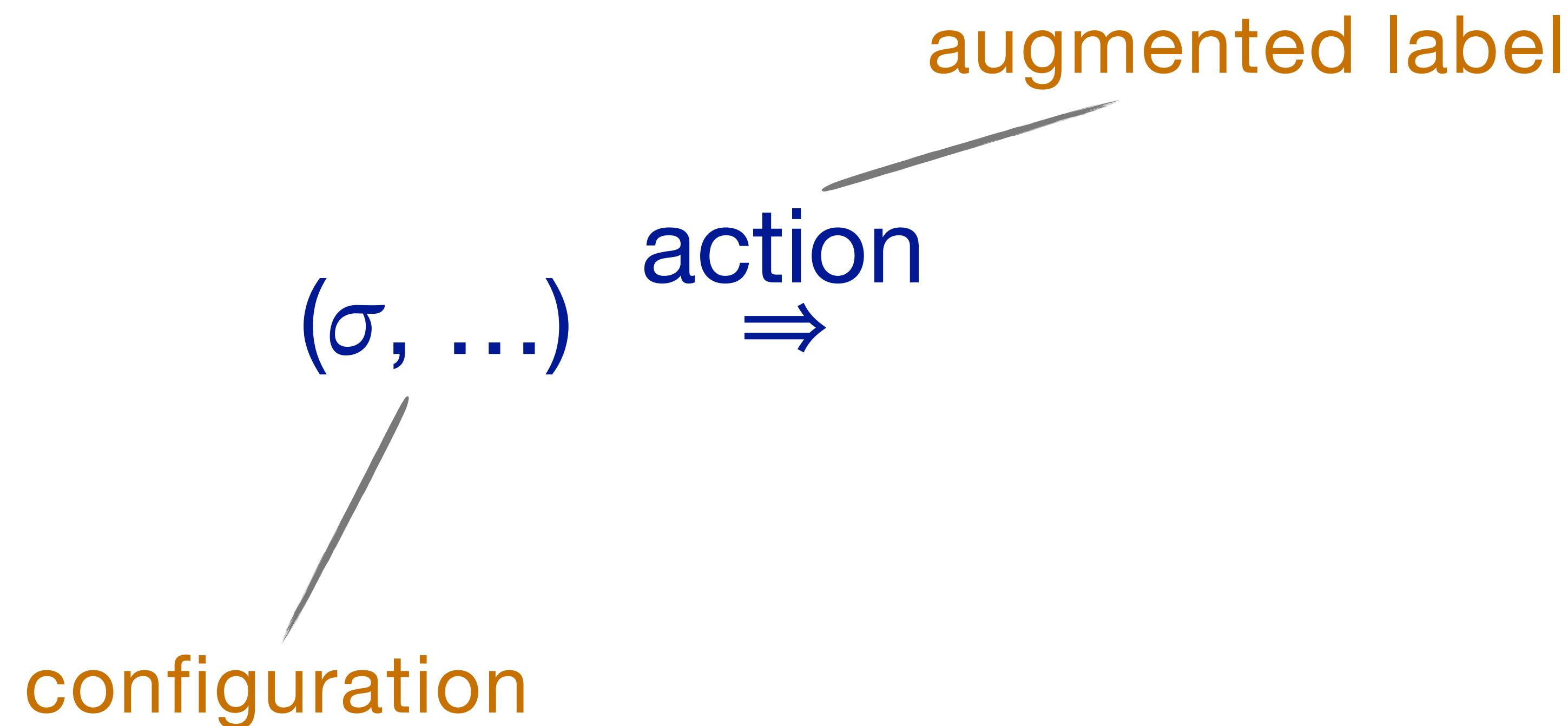
# Configuration Relation

( $\sigma$ , ...)

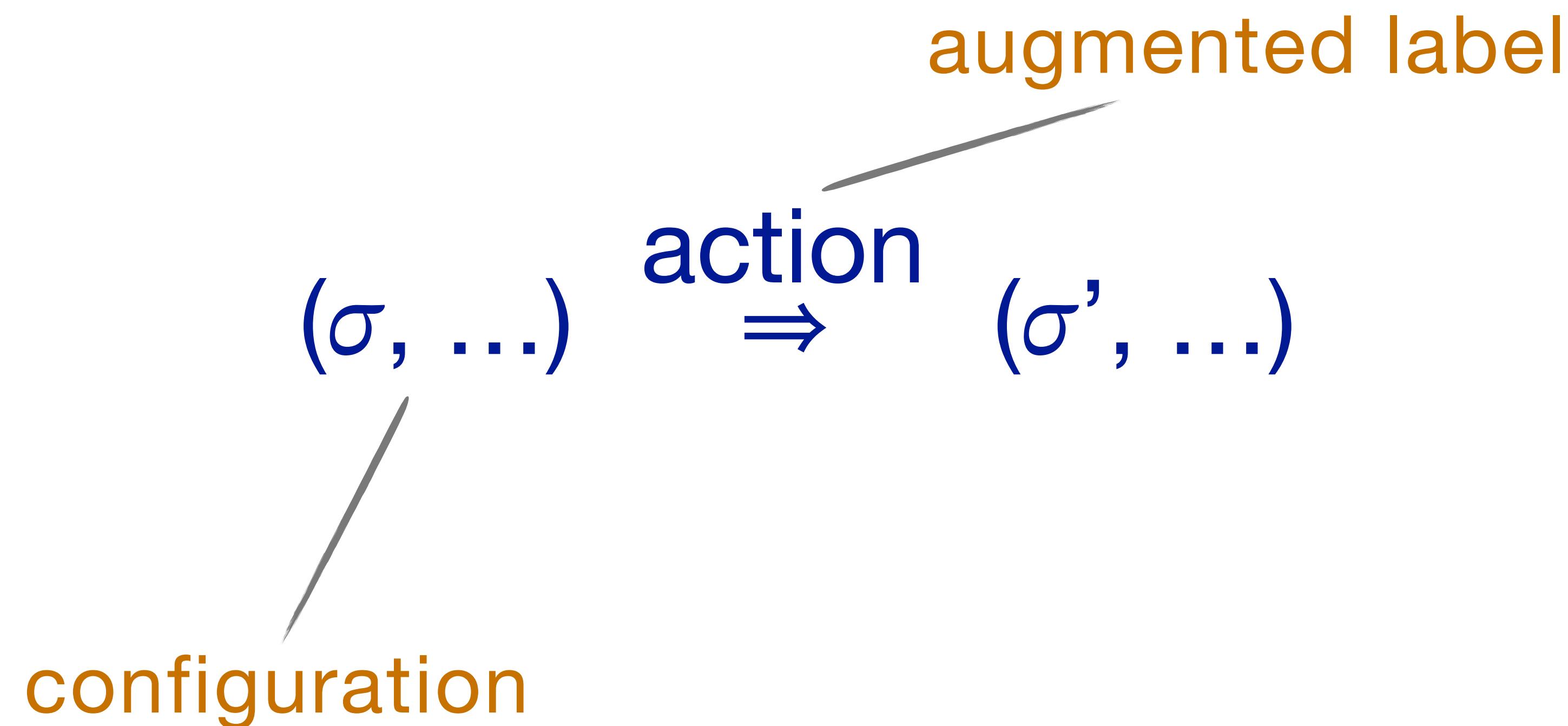


configuration

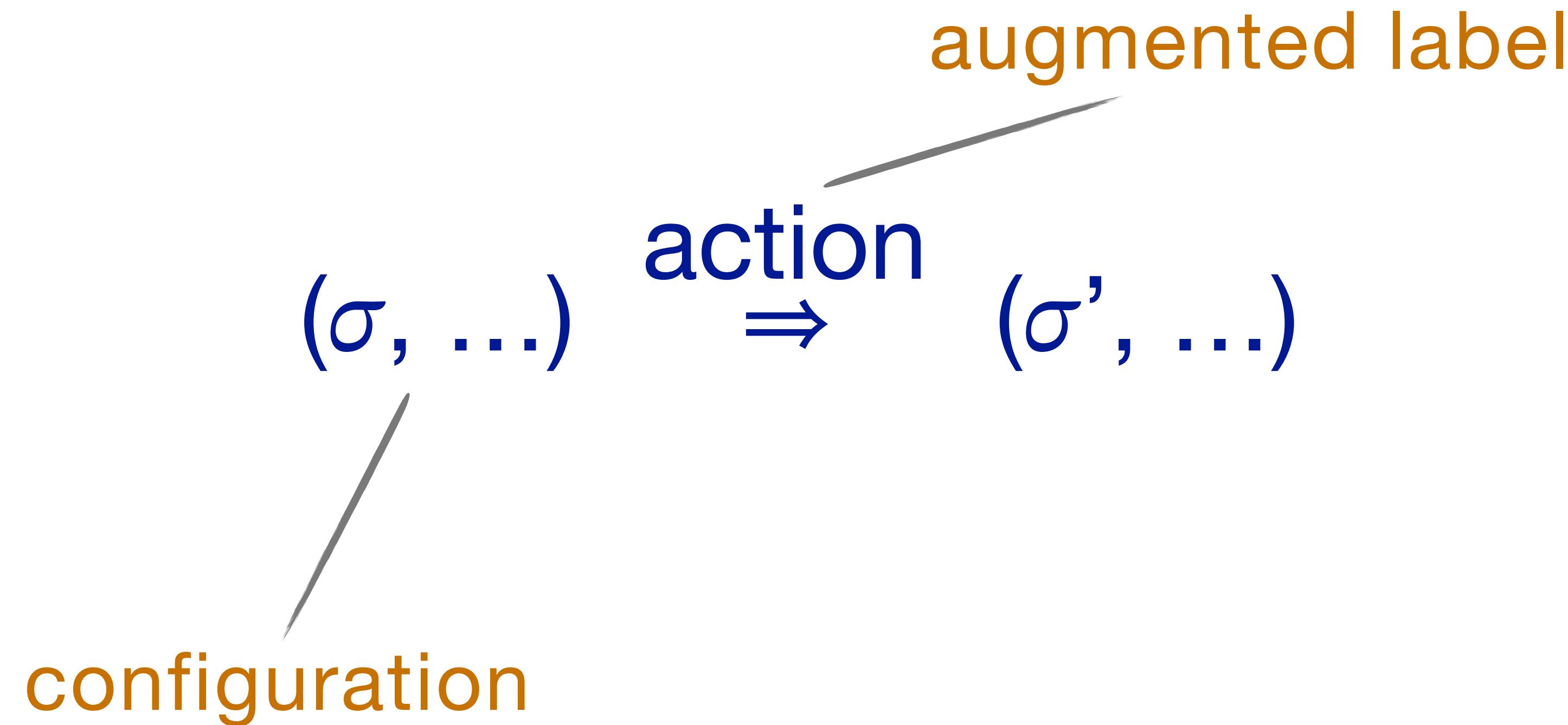
# Configuration Relation



# Configuration Relation



# Configuration Relation



```
(=>) : Conf state * Action label * Conf (Transition state label)
```

# Configuration Relation

# Configuration Relation

```
(=>) : Conf state * Action label * Conf (Transition state label)
```

# Configuration Relation

( $\Rightarrow$ ) : Conf state \* Action label \* Conf (Transition state label)

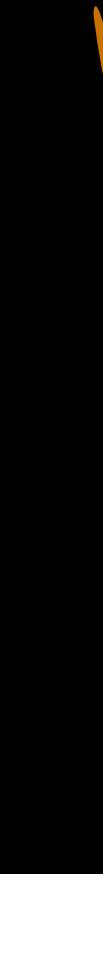
c { state = Holding, value }

means: inputs = [], outputs = [],  
and durations & signers are arbitrary

# Configuration Relation

$(\Rightarrow) : \text{Conf state} * \text{Action label} * \text{Conf} (\text{Transition state label})$

```
c { state = Holding, value }  
=> { Propose payment }
```



means: inputs = [], outputs = [],  
and durations & signers are arbitrary

# Configuration Relation

$(\Rightarrow) : \text{Conf state} * \text{Action label} * \text{Conf} (\text{Transition state label})$

```
c { state = Holding, value }  
=> { Propose payment }  
c' { state = Collecting payment {}, value }
```

means: inputs = [], outputs = [],  
and durations & signers are arbitrary

# Configuration Relation

( $\Rightarrow$ ) : Conf state \* Action label \* Conf (**Transition state label**)

```
c { state = Holding, value }  
=> { Propose payment }  
c' { state = Collecting payment {}, value }  
where
```

means: inputs = [], outputs = [],  
and durations & signers are arbitrary

# Configuration Relation

( $\Rightarrow$ ) : Conf state \* Action label \* Conf (Transition state label)

```
c { state = Holding, value }
=> { Propose payment }
c' { state = Collecting payment {}, value }
where
  0 < payment.amount <= value
```

means: inputs = [], outputs = [],  
and durations & signers are arbitrary

# Configuration Relation

( $\Rightarrow$ ) : Conf state \* Action label \* Conf (**Transition state label**)

```
c { state = Holding, value }
=> { Propose payment }
c' { state = Collecting payment {}, value }
where
  0 < payment.amount <= value
  payment.deadline > c'.duration.endTime
```

means: inputs = [], outputs = [],  
and durations & signers are arbitrary



c { state = Collecting payment keys, value }

```
c { state = Collecting payment keys, value }
=> { Add key }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Add key }
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```
c { state = Collecting payment keys, value }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
c' { state = Holding, value - payment.value }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
c' { state = Holding, value - payment.value
  , outputs = [PayTo payment.value payment.recipient]
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
c' { state = Holding, value - payment.value
     , outputs = [PayTo payment.value payment.recipient]
   }
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
c' { state = Holding, value - payment.value
     , outputs = [PayTo payment.value payment.recipient]
   }
where
  c'.duration.endTime <= payment.deadline
```

```
c { state = Collecting payment keys, value }
=> { Add key }
c' { state = Collecting payment ({key} ∪ keys), value }
where
  key ∈ authorisedKeys
```

```
c { state = Collecting payment keys, value }
=> { Pay }
c' { state = Holding, value - payment.value
     , outputs = [PayTo payment.value payment.recipient]
   }
where
  c'.duration.endTime <= payment.deadline
  |keys| > noRequiredSignatures
```

```
c { state = Collecting payment keys, value }
=> { Cancel }
c' { state = Holding, value }
where
  c'.duration.startTime > payment.deadline
```

# Configuration Relation: Wellformedness

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Given  $c_1 \Rightarrow^a c_2$ , we require

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- $c_1.\text{state}.\text{label} \xrightarrow[a.\text{label}]{} c_2.\text{state}.\text{label}$

DFA transition

# Configuration Relation: Wellformedness

Given  $c_1 \Rightarrow^a c_2$ , we require

- $c_1.\text{state.label} \xrightarrow{a.\text{label}} c_2.\text{state.label}$
- $c_1.\text{duration.endTime} < c_2.\text{duration.endTime}$

DFA transition

# Configuration Relation: Wellformedness

Given  $c_1 \Rightarrow^a c_2$ , we require

- $c_1.\text{state.label} \xrightarrow{a.\text{label}} c_2.\text{state.label}$
- $c_1.\text{duration.endTime} < c_2.\text{duration.endTime}$

DFA transition

Anything else?

# Contract Implementation

# Contract Implementation

```
transition :: Conf (state :: State)
```

# Contract Implementation

```
transition :: Conf (state :: State)
-> Action (label :: Label)
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
validate    :: ConfState (state :: State)
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
validate    :: ConfState (state :: State)
  -> Action (label :: Label)
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
validate    :: ConfState (state :: State)
  -> Action (label :: Label)
  -> Conf (Transition state label)
```

# Contract Implementation

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
validate   :: ConfState (state :: State)
  -> Action (label :: Label)
  -> Conf (Transition state label)
  -> Bool
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
&& deadline payment > standardInterval
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
  && deadline payment > standardInterval
= Just $
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
  && deadline payment > standardInterval
= Just $
  ( state      = Collecting payment Set.empty
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
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= Just $
  ( state      = Collecting payment Set.empty
  , value      = value conf
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
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transition conf{ state = Holding } (Propose payment) [] time
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  , value      = value conf
  , inputs     = []
```

```
transition :: Conf (state :: State)
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  -> [ReceiveFrom]           - inputs to consume
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= Just $
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  , value      = value conf
  , inputs     = []
  , outputs    = []
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
  && deadline payment > standardInterval
= Just $
  ( state      = Collecting payment Set.empty
  , value      = value conf
  , inputs     = []
  , outputs    = []
  , duration   = (time, time + standardInterval)
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Holding } (Propose payment) [] time
| 0 < amount payment && amount payment <= value conf
  && deadline payment > standardInterval
= Just $
  ( state      = Collecting payment Set.empty
  , value      = value conf
  , inputs     = []
  , outputs    = []
  , duration   = (time, time + standardInterval)
  , signers   = Set.empty
  )
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
| key `Set.elem` authorisedKeys
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
  = Just $
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
= Just $
  conf{ state      = Collecting payment }
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
  = Just $
    conf{ state      = Collecting payment
          (Set.addElement key keys)}
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
= Just $
  conf{ state      = Collecting payment
        (Set.addElement key keys)
  , duration = (time, time + standardInterval)
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
= Just $
  conf{ state      = Collecting payment
        (Set.addElement key keys)
  , duration = (time, time + standardInterval)
  , signers  = Set.unit key}
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
= Just $
  conf{ state      = Collecting payment
        (Set.addElement key keys)
  , duration = (time, time + standardInterval)
  , signers  = Set.unit key
  }
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  (Add key) [] time
  | key `Set.elem` authorisedKeys
= Just $
  conf{ state      = Collecting payment
        (Set.addElement key keys)
  , duration = (time, time + standardInterval)
  , signers  = Set.unit key
  }
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay [] time
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
| Set.count keys >= noRequiredSignatures
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
  && time < deadline payment
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                     - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
    && time < deadline payment
  = Just $
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
  && time < deadline payment
  = Just $
    ( state      = Holding
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
    && time < deadline payment
  = Just $
    ( state      = Holding
    , value      = value conf - amount payment
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
| Set.count keys >= noRequiredSignatures
&& time < deadline payment
= Just $
  ( state      = Holding
  , value      = value conf - amount payment
  , inputs     = [] )
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
| Set.count keys >= noRequiredSignatures
&& time < deadline payment
= Just $
  ( state      = Holding
  , value      = value conf - amount payment
  , inputs     = []
  , outputs    = [PayTo (amount payment)]
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
    && time < deadline payment
  = Just $
    ( state      = Holding
    , value      = value conf - amount payment
    , inputs     = []
    , outputs    = [PayTo (amount payment)
                  (recipient payment)]
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay [] time
| Set.count keys >= noRequiredSignatures
  && time < deadline payment
= Just $
  ( state      = Holding
  , value      = value conf - amount payment
  , inputs     = []
  , outputs    = [PayTo (amount payment)
                (recipient payment)]
  , duration   = (time, (time + standardInterval))
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys } Pay []
  | Set.count keys >= noRequiredSignatures
    && time < deadline payment
  = Just $
    ( state      = Holding
    , value      = value conf - amount payment
    , inputs     = []
    , outputs    = [PayTo (amount payment)
                  (recipient payment)]
    , duration   = (time, (time + standardInterval)
                   `min` deadline payment)
```

```
transition :: Conf (state :: State)
  -> Action (label :: Label)
  -> [ReceiveFrom]           - inputs to consume
  -> Time                    - current time
  -> Maybe (Conf (Transition state label))
```

```
transition conf{ state = Collecting payment keys }
  -> Cancel [] time
  | time > deadline payment
= Just $
  ( state      = Holding
  , value      = value conf
  , inputs     = []
  , outputs    = []
  , duration   = (time, time + standardInterval)
  , signers   = Set.empty
  )
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

validate Holding (Propose payment)

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate Holding (Propose payment)
conf{ state = Collecting payment keys, outputs = [] }
```

```
validate    :: ConfState (state :: State)
-> Action (label :: Label)
-> Conf (Transition state label)
-> Bool
```

```
validate Holding (Propose payment)
  conf{ state = Collecting payment keys, outputs = [] }
| 0 < amount payment && amount payment <= value conf
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate Holding (Propose payment)
  conf{ state = Collecting payment keys, outputs = [] }
  | 0 < amount payment && amount payment <= value conf
  && deadline payment > snd (duration conf)
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate Holding (Propose payment)
  conf{ state = Collecting payment keys, outputs = [] }
  | 0 < amount payment && amount payment <= value conf
  && deadline payment > snd (duration conf)
  && Set.isEmpty keys
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate Holding (Propose payment)
            conf{ state = Collecting payment keys, outputs = [] }
| 0 < amount payment && amount payment <= value conf
&& deadline payment > snd (duration conf)
&& Set.isEmpty keys
= true
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate Holding (Propose payment)
  conf{ state = Collecting payment keys, outputs = [] }
  | 0 < amount payment && amount payment <= value conf
  && deadline payment > snd (duration conf)
  && Set.isEmpty keys
  = true
validate (Collecting payment keys) (Add key)
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate Holding (Propose payment)
  conf{ state = Collecting payment keys, outputs = [] }
  | 0 < amount payment && amount payment <= value conf
  && deadline payment > snd (duration conf)
  && Set.isEmpty keys
  = true
validate (Collecting payment keys) (Add key)
  conf{ state = Collecting payment keys, outputs = [] }
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate Holding (Propose payment)
            conf{ state = Collecting payment keys, outputs = [] }
| 0 < amount payment && amount payment <= value conf
  && deadline payment > snd (duration conf)
  && Set.isEmpty keys
= true
validate (Collecting payment keys) (Add key)
            conf{ state = Collecting payment keys, outputs = [] }
| key `Set.elem` signers conf
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate Holding (Propose payment)
            conf{ state = Collecting payment keys, outputs = [] }
            | 0 < amount payment && amount payment <= value conf
              && deadline payment > snd (duration conf)
              && Set.isEmpty keys
            = true
validate (Collecting payment keys) (Add key)
            conf{ state = Collecting payment keys, outputs = [] }
            | key `Set.elem` signers conf
              && key `Set.elem` authorisedKeys && key `Set.elem` keys
            = true
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

validate (Collecting payment keys) Pay

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
| Set.count keys >= noRequiredSignatures
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
| Set.count keys >= noRequiredSignatures
&& snd (duration conf) =< payment.deadline
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
| Set.count keys >= noRequiredSignatures
&& snd (duration conf) =< payment.deadline
&& paidAmount == amount payment
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
| Set.count keys >= noRequiredSignatures
&& snd (duration conf) =< payment.deadline
&& paidAmount == amount payment
&& paidRecipient == recipient payment
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Pay
conf{ state = Holding,
      outputs = PayTo paidAmount paidRecipient : _ }
| Set.count keys >= noRequiredSignatures
  && snd (duration conf) =< payment.deadline
  && paidAmount == amount payment
  && paidRecipient == recipient payment
= true
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate    :: ConfState (state :: State)
-> Action (label :: Label)
-> Conf (Transition state label)
-> Bool
```

validate (Collecting payment keys) Cancel

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate (Collecting payment keys) Cancel
conf{ state = Holding, outputs = [] }
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Cancel
          conf{ state = Holding, outputs = [] }
| fst (duration conf) > payment.deadline
```

```
validate    :: ConfState (state :: State)
             -> Action (label :: Label)
             -> Conf (Transition state label)
             -> Bool
```

```
validate (Collecting payment keys) Cancel
          conf{ state = Holding, outputs = [] }
| fst (duration conf) > payment.deadline
= true
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate (Collecting payment keys) Cancel
          conf{ state = Holding, outputs = [] }
| fst (duration conf) > payment.deadline
= true
validate _ _ _
```

```
validate    :: ConfState (state :: State)
              -> Action (label :: Label)
              -> Conf (Transition state label)
              -> Bool
```

```
validate (Collecting payment keys) Cancel
          conf{ state = Holding, outputs = [] }
| fst (duration conf) > payment.deadline
= true
validate _ _ _
= false
```

# Correctness

For all configurations  $c$ , labels  $l$ , actions  $a :: \text{Action } l$ , inputs  $is$ , time  $t$ , we have

if transition  $c \ a \ is \ t = \text{Just } c'$ ,  
then  $c \Rightarrow^a c'$  and  $c'.\text{inputs} \subseteq is$

# Correctness

For all configurations  $c$ , labels  $l$ , actions  $a :: \text{Action } l$ , inputs  $is$ , time  $t$ , we have

if transition  $c \ a \ is \ t = \text{Just } c'$ ,  
then validate  $c.\text{state } a \ c' = \text{True}$

# Completeness

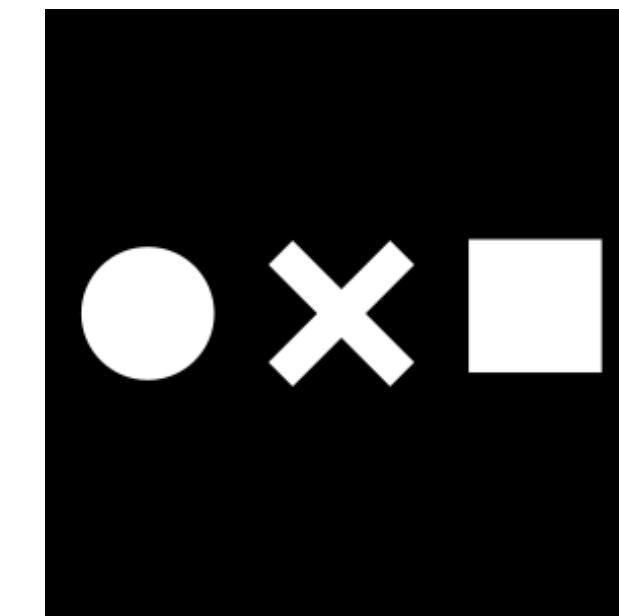
???

Thank you!

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