Contents

1	Introduction	2
	1.1 Separation of concerns	2
	1.2 Computational	2
	1.3 Sets & maps	2
2	Cryptographic primitives	4
3	Base types	5
4	Token algebras	6
5	Addresses	7
6	Scripts	9
7	Governance actions	10
	7.1 Voting and ratification	11
	7.2 Protocol parameters and governance actions	12
	7.3 Enactment	12
8	Protocol parameters	16
9	Governance	18
10	Delegation	20
11	Transactions	25
12	UTxO	28
	12.1 Accounting	28
	12.2 Witnessing	33
13	Ledger State Transition	35
14	Ratification	37
	14.1 Ratification requirements	37
	14.2 Ratification restrictions	37
15	Blockchain layer	44
16	Properties	47
	16.1 UTxO	47

1 Introduction

Repository: https://github.com/input-output-hk/formal-ledger-specifications

This document describes the formalization of the Cardano ledger specification in the Agda programming language and proof assistant. The specification formalized here is that of the Conway era, described in detail in the Cardano Improvement Proposal (CIP) 1694, github.com/cardano-foundation/CIPs/CIP-1694.

1.1 Separation of concerns

The Cardano Node consists of three pieces:

- Networking layer, which deals with sending messages across the internet
- Consensus layer, which establishes a common order of valid blocks
- Ledger layer, which decides whether a sequence of blocks is valid

Because of this separation, the ledger gets to be a state machine:

$$s \xrightarrow{b} s'$$

More generally, we will consider state machines with an environment:

$$\Gamma \vdash s \xrightarrow{b} s'$$

These are modelled as 4-ary relations between the environment Γ , an initial state s, a signal b and a final state s'. The ledger consists of 25-ish (depending on the version) such relations that depend on each other, forming a directed graph that is almost a tree.

1.2 Computational

Since all such state machines need to be evaluated by the node and all nodes should compute the same states, the relations specified by them should be computable by functions. This can be captured by the following record, which is parametrized over the step relation.

```
record Computational (\_\vdash \_ \neg (\_, X) \_ : C \rightarrow S \rightarrow Sig \rightarrow S \rightarrow Set): Set where field compute : C \rightarrow S \rightarrow Sig \rightarrow Maybe S
\equiv -just \Leftrightarrow STS : compute \Gamma s b \equiv just s' \Leftrightarrow \Gamma \vdash s \neg (b, X) s'
nothing\Rightarrow \forall \neg STS : compute \Gamma s b \equiv nothing \Rightarrow \forall s' \Rightarrow \neg \Gamma \vdash s \neg (b, X) s'
```

1.3 Sets & maps

The ledger heavily uses set theory. For various reasons it was necessary to implement our own set theory (there will be a paper on this some time in the future). Crucially, the set theory is completely abstract (in a technical sense - Agda has an abstract keyword) meaning that implementation details of the set theory are irrelevant. Additionally, all sets in this specification are finite.

We use this set theory to define maps as seen below, which are used in many places. We usually think of maps as partial functions (i.e. functions not defined everywhere), but importantly they are not Agda functions.

2 Cryptographic primitives

We rely on a public key signing scheme for verification of spending.

```
Types & functions

SKey VKey Sig Ser: Set
  isKeyPair: SKey \rightarrow VKey \rightarrow Set
  isSigned: VKey \rightarrow Ser \rightarrow Sig \rightarrow Set
  sign: SKey \rightarrow Ser \rightarrow Sig

KeyPair = \Sigma[ sk \in SKey ] \Sigma[ vk \in VKey ] isKeyPair sk vk

Property of signatures

((sk, vk, _): KeyPair) (d: Ser) (\sigma: Sig) \rightarrow sign sk d \equiv \sigma \rightarrow isSigned vk d \sigma
```

Figure 1: Definitions for the public key signature scheme

3 Base types

```
Coin = N
Slot = N
Epoch = N
```

Figure 2: Some basic types used in many places in the ledger

```
record TokenAlgebra : Set<sub>1</sub> where
 field Value-CommutativeMonoid : CommutativeMonoid 0ℓ 0ℓ
 MemoryEstimate : Set
 {\tt MemoryEstimate = \mathbb{N}}
field coin
                                : Value → Coin
      inject
                                : Coin → Value
      policies
                                : Value → P PolicyId
                                : Value → MemoryEstimate
      size
      _≤<sup>t</sup>_
                                : Value → Value → Set
      AssetName
                                 : Set
      Assermant
specialAsset
                                 : AssetName
                                 : coin ∘ inject ≗ id
      coinIsMonoidHomomorphism : IsMonoidHomomorphism coin
sum<sup>v</sup> : List Value → Value
sum' = foldr _+'_ (inject 0)
```

Figure 3: Token algebras, used for multi-assets

4 Token algebras

5 Addresses

We define credentials and various types of addresses here.

```
Abstract types
   Network
   KeyHash
   ScriptHash
Derived types
 Credential = KeyHash ⊎ ScriptHash
 record BaseAddr : Set where
   field net : Network
        pay : Credential
         stake : Credential
 record BootstrapAddr : Set where
   field net
                   : Network
         pay
                   : Credential
         attrsSize: N
 record RwdAddr : Set where
   field net : Network
         stake : Credential
 VKeyBaseAddr
                    = Σ[ addr ∈ BaseAddr
                                               ] isVKey (addr .pay)
 VKeyBootstrapAddr = \Sigma[ addr \in BootstrapAddr ] isVKey (addr .pay)
 ScriptBaseAddr = \Sigma[ addr \in BaseAddr
                                              ] isScript (addr .pay)
 ScriptBootstrapAddr = \Sigma[ addr \in BootstrapAddr ] isScript (addr \cdot pay)
 Addr
            = BaseAddr
                             ⊎ BootstrapAddr
 VKeyAddr = VKeyBaseAddr ⊎ VKeyBootstrapAddr
 ScriptAddr = ScriptBaseAddr ⊎ ScriptBootstrapAddr
Helper functions
              : Addr → Credential
 payCred
             : Addr → Network
 netId
 isVKeyAddr : Addr → Set
 isScriptAddr : Addr → Set
 isVKeyAddr
                 = isVKey o payCred
                 = isScript o payCred
 isScriptAddr
 isScriptRwdAddr = isScript o RwdAddr.stake
```

Figure 4: Definitions used in Addresses

6 Scripts

We define Timelock scripts here. They can verify the presence of keys and whether a transaction happens in a certain slot interval. These scripts are executed as part of the regular witnessing.

```
data Timelock: Set where
                  : List Timelock
 RequireAllOf
                                         → Timelock
 RequireAnyOf : List Timelock
                                         → Timelock
 RequireMOf
                     : N → List Timelock → Timelock
 RequireSig
                     : KeyHash
                                         → Timelock
 RequireTimeStart : Slot
                                         → Timelock
 RequireTimeExpire : Slot
                                         → Timelock
module = (khs : P KeyHash) (I : Maybe Slot \times Maybe Slot) where
 data evalTimelock : Timelock → Set where
    evalAll: All evalTimelock ss
            → evalTimelock (RequireAllOf ss)
   evalAny : Any evalTimelock ss
            → evalTimelock (RequireAnyOf ss)
   evalMOf : ss'S.⊆ss → All evalTimelock ss'
            → evalTimelock (RequireMOf (length ss') ss)
   evalSig : x \in khs
            → evalTimelock (RequireSig x)
   evalTSt : I \cdot proj_1 \equiv just 1 \rightarrow a \le 1
            → evalTimelock (RequireTimeStart a)
   evalTEx: I.proj_2 \equiv just r \rightarrow r \leq a
            → evalTimelock (RequireTimeStart a)
```

Figure 5: Timelock scripts and their evaluation

7 Governance actions

We introduce three distinct bodies that have specific functions in the new governance framework:

- 1. a constitutional committee (henceforth called CC)
- 2. a group of delegate representatives (henceforth called DReps)
- 3. the stake pool operators (henceforth called SPOs)

```
GovActionID : Set
GovActionID = TxId × N
data GovRole: Set where
 CC DRep SPO: GovRole
data VDeleg: Set where
            : GovRole → Credential → VDeleg
 credVoter
 abstainRep
                                         VDeleg
 noConfidenceRep:
                                         VDeleg
record Anchor: Set where
 field url : String
       hash: DocHash
data GovAction: Set where
 NoConfidence
                                                         GovAction
 NewCommittee
               : Credential → Epoch → P Credential → Q → GovAction
 NewConstitution : DocHash → Maybe ScriptHash
 TriggerHF
                 : ProtVer
                                                       → GovAction
 ChangePParams : PParamsUpdate
                                                       → GovAction
 TreasuryWdrl
                 : (RwdAddr → Coin)
                                                       → GovAction
                                                         GovAction
actionWellFormed : GovAction → Bool
actionWellFormed (ChangePParams x) = ppdWellFormed x
actionWellFormed _
                                  = true
```

Figure 6: Governance actions

Figure 6 defines several data types used to represent governance actions including:

- GovActionID (governance action identifier)—a pair consisting of a TxId (transaction ID) and a natural number;
- GovRole (governance role)—one of three available voter roles defined above (CC, DRep, SPO);
- VDeleg (voter delegation)—one of three ways to delegate votes: by credential, abstention, or no confidence (credVoter, abstainRep, or noConfidenceRep);
- Anchor—a url and a document hash;
- GovAction (governance action)—one of seven possible actions (see Figure 7 for definitions).

¹There are many varying definitions of the term "hard fork" in the blockchain industry. Hard forks typically refer to non-backwards compatible updates of a network. In Cardano, we formalize the definition slightly more by calling any upgrade that would lead to *more blocks* being validated a "hard fork" and force nodes to comply with the new protocol version, effectively obsoleting nodes that are unable to handle the upgrade.

Action	Description
NoConfidence	a motion to create a state of no-confidence in the current
	constitutional committee
NewCommittee	changes to the members of the constitutional committee and/or to
	its signature threshold and/or term limits
NewConstitution	a modification to the off-chain Constitution, recorded as an on-chain
	hash of the text document
TriggerHF ¹	triggers a non-backwards compatible upgrade of the network;
	requires a prior software upgrade
ChangePParams	a change to one or more updatable protocol parameters, excluding
	changes to major protocol versions ("hard forks")
TreasuryWdrl	movements from the treasury, sub-categorized into small, medium or
-	large withdrawals (based on the amount of Lovelace to be withdrawn)
Info	an action that has no effect on-chain, other than an on-chain record

Figure 7: Types of governance actions

7.1 Voting and ratification

Every governance action must be ratified by at least two of these three bodies using their onchain *votes*. The type of action and the state of the governance system determines which bodies must ratify it. Ratified actions are then *enacted* on-chain, following a set of rules (see Section 7.3 and Figure 11). Figure 9 defines types that are used in ratification (for verifyPrev) where we check that the stored hash matches the one attached to the action we want to ratify.

- Ratification. An action is said to be ratified when it gathers enough votes in its favor (according to the rules described in Section 14).
- Expiration. An action that doesn't collect sufficient 'yes' votes before its deadline is said to have expired.
- Enactment. An action that has been ratified is said to be enacted once it has been activated on the network.

See Section 14 for more on the ratification process.

The data type Vote represents the different voting options: yes, no, or abstain. Each vote is recorded in a GovVote record along with the following data: a governance action ID, a role, a credential, and possibly an anchor.

A governance action proposal is recorded in a GovProposal record which includes fields for a return address, the proposed governance action, a hash of the previous governance action, a deposit (required to propose a governance action) and an anchor (see Figure 10).

To submit a governance action proposal to the chain one must provide a deposit which will be returned when the action is finalized (whether it is *ratified* or has *expired*). The deposit amount will be added to the *deposit pot*, similar to stake key deposits. It will also be counted towards the stake of the reward address it will be paid back to, to not reduce the submitter's voting power to vote on their own (and competing) actions.

Remarks.

- 1. A motion of no-confidence is an extreme measure that enables Ada holders to revoke the power that has been granted to the current constitutional committee.
- 2. A *single* governance action might contain *multiple* protocol parameter updates. Many parameters are inter-connected and might require moving in lockstep.

7.2 Protocol parameters and governance actions

Recall from Section 8, parameters used in the Cardano ledger are grouped according to the general purpose that each parameter serves (see Figure 13). Specifically, we have Network-Group, EconomicGroup, TechnicalGroup, and GovernanceGroup. This allows voting/ratification thresholds to be set by group, though we do not require that each protocol parameter governance action be confined to a single group. In case a governance action carries updates for multiple parameters from different groups, the maximum threshold of all the groups involved will apply to any given such governance action.

7.3 Enactment

Enactment of a governance action is carried out as an enact transition which requires an enact environment, an enact state representing the existing state (prior to enactment), the voted on governance action (that achieved enough votes to enact), and the state that results from enacting the given governance action (see Figure 11).

A record of type <code>EnactEnv</code> represents the environment for enacting a governance action. A record of type <code>EnactState</code> represents the state for enacting a governance action. The latter contains fields for the constitutional committee, constitution, protocol version, protocol parameters, withdrawals from treasury, and treasury balance.

The relation _____, ENACT)_ is the transition relation for enacting a governance action. It represents how the *EnactState* changes when a specific governance action is enacted (see Figure 12).

```
threshold: PParams → Maybe Q → GovAction → GovRole → Maybe Q
threshold pp ccThreshold' = \lambda where
    NoConfidence
                                                                  , vote Q1 >
                           → < noVote</p>
                                                   , vote P1
    (NewCommittee \_ \_ ) \rightarrow case ccThreshold' of \lambda where
                                                   , vote P2a
      (just _)
                           → < noVote</p>
                                                                  , vote Q2a >
                            → < noVote</p>
      nothing
                                                   , vote P2b
                                                                  , vote Q2b >
    (NewConstitution _ _) → ⟨ vote ccThreshold , vote P3
                                                                  , noVote >
    (TriggerHF _) \rightarrow ⟨ vote ccThreshold , vote P4 , vote Q4 ⟩ (ChangePParams x) \rightarrow ⟨ vote ccThreshold , vote (P5 x) , noVote ⟩
                                                                  , vote Q4 >
    (TreasuryWdrl _) → ⟨ vote ccThreshold , vote P6 , noVote ⟩
    Info
                            → < vote 2@</p>
                                                   , vote 2ℚ
                                                                  , vote 2\mathbb{Q}
  where
    open PParams pp
    open DrepThresholds drepThresholds
    open PoolThresholds poolThresholds
    -- Here, 2 can just be any number strictly greater than one. It just
    -- means that a threshold can never be cleared, i.e. that the action
    -- cannot be enacted.
    ccThreshold: 0
    ccThreshold = case ccThreshold' of \lambda where
      (just x) \rightarrow x
      nothing \rightarrow 20
    pparamThreshold: PParamGroup → ℚ
    pparamThreshold NetworkGroup = P5a
    pparamThreshold EconomicGroup = P5b
    pparamThreshold TechnicalGroup = P5c
    pparamThreshold GovernanceGroup = P5d
    P5 : PParamsUpdate → Q
    P5 ppu = maximum $ map s pparamThreshold (updateGroups ppu)
    noVote: Maybe ①
    noVote = nothing
    vote : \mathbb{Q} \rightarrow Maybe \mathbb{Q}
    vote = just
-- TODO: this doesn't actually depend on PParams so we could remove that argument,
          but we don't have a default ATM
canVote : PParams → GovAction → GovRole → Set
canVote pp \ a \ r = Is-just (threshold pp \ nothing a \ r)
```

Figure 8: Functions related to voting

Figure 9: NeedsHash and HashProtected types

```
data Vote: Set where
 yes no abstain: Vote
record GovVote : Set where
 field gid : GovActionID
               : GovRole
      role
      credential : Credential
      vote
              : Vote
      anchor : Maybe Anchor
record GovProposal : Set where
 field returnAddr : RwdAddr
      action : GovAction
      prevAction : NeedsHash action
      deposit : Coin
      anchor : Anchor
```

Figure 10: Governance action proposals and votes

```
record EnactEnv : Set where
    constructor [_,_,_]*
    field gid : GovActionID
        treasury : Coin
        epoch : Epoch

record EnactState : Set where
    field cc : HashProtected (Maybe ((Credential → Epoch) × ℚ))
        constitution : HashProtected (DocHash × Maybe ScriptHash)
        pv : HashProtected ProtVer
        pparams : HashProtected PParams
        withdrawals : RwdAddr → Coin

ccCreds : HashProtected (Maybe ((Credential → Epoch) × ℚ)) → P Credential
    ccCreds (just x , _) = dom (x .proj₁)
    ccCreds (nothing , _) = ∅
```

Figure 11: Enactment types

```
data _⊢_~(_,ENACT)_ : EnactEnv → EnactState → GovAction → EnactState → Set where
  Enact-NoConf :
    [gid, t, e]^e \vdash s \multimap (NoConfidence, ENACT)
                  record s { cc = nothing , gid }
  Enact-NewComm : let old = maybe proj_1 o^m (s .EnactState.cc .proj_1) in
    ∀[ term ∈ range new ] term ≤ (s .pparams .proj₁ .PParams.ccMaxTermLength +e e)
    [gid, t, e]^e \vdash s \rightarrow 0 NewCommittee new rem q, ENACTD
                record s \{ cc = just ((new U^{ml} old) | rem^c, q), gid \}
  Enact-NewConst:
    [gid, t, e]^e \vdash s \multimap (NewConstitution dh sh, ENACT)
                record s { constitution = (dh , sh) , gid }
  Enact-HF:
    [gid, t, e]^e \vdash s \multimap (TriggerHF v, ENACT)
                  record s { pv = v , gid }
  Enact-PParams :
    [gid, t, e]^e \vdash s \rightarrow \emptyset ChangePParams up, ENACTD
                record s { pparams = applyUpdate (s .pparams .proj<sub>1</sub>) up , gid }
  Enact-Wdrl : let newWdrls = s .withdrawals U* wdrl in
    \sum^{mv} [x \leftarrow newWdrls fm] x \leq t
    [gid, t, e]^e \vdash s \multimap TreasuryWdrl wdrl, ENACTD
                record s { withdrawals = newWdrls }
  Enact-Info:
    [gid, t, e]^e \vdash s \rightarrow (Info, ENACT) s
```

Figure 12: ENACT transition system

8 Protocol parameters

This section defines the adjustable protocol parameters of the Cardano ledger. These parameters are used in block validation and can affect various features of the system, such as minimum fees, maximum and minimum sizes of certain components, and more. ProtVer represents the protocol version used in the Cardano ledger. It is a pair of natural numbers, representing the major and minor version, respectively.

PParams contains parameters used in the Cardano ledger, which we group according to the general purpose that each parameter serves.

- NetworkGroup: parameters related to the network settings;
- EconomicGroup: parameters related to the economic aspects of the ledger;
- TechnicalGroup: parameters related to technical settings;
- GovernanceGroup: parameters related to governance settings.

The first three of these groups contain protocol parameters that were already introduced during the Shelley, Alonzo and Babbage eras. The new protocol parameters introduced in the Conway era (CIP-1694) belong to GovernanceGroup. These new parameters are declared in Figure 13 and denote the following concepts.

- drepThresholds: governance thresholds for DReps; these are rational numbers named P1, P2a, P2b, P3, P4, P5a, P5b, P5c, P5d, and P6;
- poolThresholds: pool-related governance thresholds; these are rational numbers named Q1, Q2a, Q2b, and Q4;
- ccMinSize: minimum constitutional committee size;
- ccMaxTermLength: maximum term limit (in epochs) of constitutional committee members;
- govActionLifetime: governance action expiration;
- govActionDeposit: governance action deposit;
- drepDeposit: DRep deposit amount;
- drepActivity: DRep activity period;
- minimumAVS: the minimum active voting threshold.

```
ProtVer : Set
 ProtVer = \mathbb{N} \times \mathbb{N}
 record Acnt: Set where
   field treasury reserves : Coin
 data PParamGroup: Set where
   NetworkGroup EconomicGroup TechnicalGroup GovernanceGroup: PParamGroup
 record DrepThresholds : Set where
   field P1 P2a P2b P3 P4 P5a P5b P5c P5d P6: 0
 record PoolThresholds : Set where
   field Q1 Q2a Q2b Q4: Q
 record PParams: Set where
   field
Network group
    maxBlockSize : N
                   : IN
    maxTxSize
    maxHeaderSize : N
    maxValSize : N
                   : ProtVer -- retired, keep for now
Economic group
                    : N
    а
    b
                    : N
    minUTxOValue : Coin
poolDeposit : Coin
Technical group
    Emax
                     : Epoch
    collateralPercent: N
Governance group
    drepThresholds : DrepThresholds
    poolThresholds : PoolThresholds
    govActionLifetime : N
    govActionDeposit : Coin
    ccMinSize
                    : IN
    ccMaxTermLength : N
    minimumAVS
                   : Coin
    -- Script
    -- costmdls
                          : Language →/¬ CostModel (Does not work with DecEq)
                  : CostModel
    costmdls
    prices
                    : Prices
    maxTxExUnits : ExUnits
    maxBlockExUnits : ExUnits
    coinsPerUTxOWord : Coin
    -- collateralPercent : N
    maxCollateralInputs : N
 paramsWellFormed : PParams → Set
 paramsWellFormed pp = 0 ∉ fromList
                                        17
   ( maxBlockSize :: maxTxSize :: maxHeaderSize :: maxValSize :: minUTxOValue :: poolDeposit
   :: drepDeposit :: [] )
```

9 Governance

```
Derived types
 record GovActionState : Set where
    field votes
                   : (GovRole × Credential) → Vote
          returnAddr : RwdAddr
          expiresIn : Epoch
                     : GovAction
          action
          prevAction : NeedsHash action
 GovState : Set
 GovState = List (GovActionID × GovActionState)
 record GovEnv : Set where
   constructor [_,_,_]t
   field txid : TxId
          epoch : Epoch
          pparams : PParams
Transition relation types
 _⊢_→d__,GOV'D_ : GovEnv × N → GovState → GovVote ⊌ GovProposal → GovState → Set
 _⊢_→d_,GOVD_: GovEnv → GovState → List (GovVote ⊌ GovProposal) → GovState → Set
Functions used in the GOV rules
  addVote: GovState → GovActionID → GovRole → Credential → Vote → GovState
  addVote s aid r kh v =
   modifyMatch
      (\lambda (x, \underline{\ }) \rightarrow aid \equiv^b x)
      (\lambda (gid, s') \rightarrow gid, record s' \{ votes = insert (votes s') (r, kh) v \}) s
 addAction: GovState
             \rightarrow Epoch \rightarrow GovActionID \rightarrow RwdAddr \rightarrow (a: GovAction) \rightarrow NeedsHash a
             → GovState
 addAction s e aid addr a prev = s :: r (aid , record
    { votes = \emptyset^m; returnAddr = addr; expiresIn = e; action = a; prevAction = prev })
```

Figure 14: Types and functions used in the GOV transition system

```
GOV-Vote: \forall \{x \ ast\} \rightarrow let \ open \ GovEnv \Gamma \ in
  (aid, ast) \in fromLists
  → canVote pparams (action ast) role
  let sig = inj<sub>1</sub> record { gid = aid ; role = role ; credential = cred
                               ; vote = v; anchor = x}
  in (\Gamma, k) \vdash s \multimap sig, GOV'  addVote s aid role cred v
GOV-Propose: \forall \{x\} \rightarrow \text{let open GovEnv } \Gamma; \text{ open PParams pparams hiding (a) in}
  actionWellFormed a \equiv true
  \rightarrow d \equiv govActionDeposit
  \rightarrow (∀ {new rem q} \rightarrow a \equiv NewCommittee new rem q
     \rightarrow ∀[ e ∈ range new ] epoch < e × dom new \(\cap \text{rem} \equiv^e \opi \))
  let sig = inj<sub>2</sub> record { returnAddr = addr ; action = a ; anchor = x
                               ; deposit = d ; prevAction = prev }
       s' = addAction s (govActionLifetime + e epoch) (txid, k) addr a prev
  in
  (\Gamma, k) \vdash s \multimap sig, GOV' \triangleright s'
_⊢_~(_,GOV)_ = SS⇒BS<sub>i</sub> _⊢_~(_,GOV')_
```

Figure 15: Rules for the GOV transition system

10 Delegation

```
record PoolParams : Set where
 field rewardAddr : Credential
data DCert: Set where
 delegate : Credential → Maybe VDeleg → Maybe Credential → Coin → DCert
 regpool : Credential → PoolParams → DCert
 retirepool : Credential → Epoch → DCert
 regdrep : Credential → Coin → Anchor → DCert
 deregdrep : Credential → DCert
 ccreghot : Credential → Maybe Credential → DCert
record CertEnv : Set where
 constructor [_,_,_]c
 field epoch : Epoch
       pp : PParams
       votes : List GovVote
record DState: Set where
 constructor [_,_,_]d
 field
   voteDelegs : Credential - VDeleg
   stakeDelegs : Credential - Credential
   rewards
              : RwdAddr → Coin
record PState: Set where
 constructor [_,_]p
 field pools : Credential → PoolParams
       retiring : Credential → Epoch
record GState : Set where
 constructor [_,_] v
 field dreps : Credential → Epoch
       ccHotKeys: Credential → Maybe Credential
record CertState : Set where
 constructor [_,_,_]c
 field dState: DState
       pState: PState
       gState: GState
GovCertEnv = CertEnv
DelegEnv = PParams
PoolEnv
          = PParams
```

Figure 16: Types used for CERTS transition system

```
cwitness : DCert → Credential
cwitness (delegate c - - ) = c
cwitness (regpool c _)
cwitness (retirepool c_{-}) = c_{-}
cwitness (regdrep c = c) = c
cwitness (deregdrep c)
                         = c
cwitness (ccreghot c _)
                          = c
requiredDeposit : {A : Set} → PParams → Maybe A → Coin
requiredDeposit pp (just _) = pp .poolDeposit
requiredDeposit pp nothing = 0
getDRepVote : GovVote → Maybe Credential
getDRepVote record { role = DRep ; credential = credential } = just credential
getDRepVote _
                                                           = nothing
```

Figure 17: Functions used for CERTS transition system

```
data _⊢_→(_,DELEG)_: DelegEnv → DState → DCert → DState → Set where
  DELEG-delegate:
    d ≡ requiredDeposit pp mv ⊔ requiredDeposit pp mc
    pp ⊢ [ vDelegs , sDelegs , rwds ] d → d delegate c mv mc d ,DELEGD
          [ insertIfJust c mv vDelegs , insertIfJust c mc sDelegs , rwds ] d
data _⊢_→(_,POOL)_: PoolEnv → PState → DCert → PState → Set where
  POOL-regpool: let open PParams pp; open PoolParams poolParams in
    c ∉ dom pools
    pp ⊢ [ pools , retiring ] p ¬( regpool c poolParams ,POOL)
          [\{c, poolParams\}^m \cup^{ml} pools, retiring]^p
  POOL-retirepool:
    pp ⊢ [ pools , retiring ] p → ( retirepool c e ,POOL)
          [ pools , { c , e }<sup>m</sup> ∪<sup>ml</sup> retiring ]<sup>p</sup>
data _⊢_→(_,GOVCERT)_: GovCertEnv → GState → DCert → GState → Set where
  GOVCERT-regdrep: let open PParams pp in
    (d \equiv drepDeposit \times c \notin dom \ dReps) \uplus (d \equiv 0 \times c \in dom \ dReps)
    [e, pp, vs]^c \vdash [dReps, ccKeys]^v \rightarrow (regdrep c d an, GOVCERT)
                         [ { c , e + drepActivity }<sup>m</sup> ∪<sup>ml</sup> dReps , ccKeys ]<sup>v</sup>
  GOVCERT-deregdrep :
    c \in dom \ dReps
    Γ⊢ [ dReps , ccKeys ] <sup>v</sup> → ( deregdrep c ,GOVCERT)
         \llbracket \ dReps \mid \{ \ c \ \}^c \ , \ ccKeys \ \rrbracket^v
  GOVCERT-ccreghot:
    (c, nothing) ∉ ccKeys
    Γ⊢ [ dReps , ccKeys ] <sup>v</sup> → ( ccreghot c mc ,GOVCERT)
         [ dReps , singleton<sup>m</sup> c mc ∪<sup>ml</sup> ccKeys ]<sup>v</sup>
```

Figure 18: Auxiliary DELEG and POOL rules

```
data _⊢_→(_,CERT)_: CertEnv → CertState → DCert → CertState → Set where
  CERT-deleg :
     pp \vdash st^d \neg \emptyset dCert , DELEG  st^d'
       \  \  \, [\hspace{.1cm} e \hspace{.1cm}, pp \hspace{.1cm}, vs \hspace{.1cm}]^{\hspace{.05cm} c} \vdash [\hspace{.1cm} st^d \hspace{.1cm}, \hspace{.1cm} st^p \hspace{.1cm}, \hspace{.1cm} st^g \hspace{.1cm}]^c \rightharpoonup (\hspace{.1cm} dCert \hspace{.1cm}, \hspace{.1cm} CERT) \hspace{.1cm} [\hspace{.1cm} st^{d \hspace{.1cm} \prime} \hspace{.1cm}, \hspace{.1cm} st^p \hspace{.1cm}, \hspace{.1cm} st^g \hspace{.1cm}]^c 
   CERT-pool :
      pp \vdash st^p \multimap (dCert, POOL) st^p'
      \llbracket e, pp, vs \rrbracket^c \vdash \llbracket st^d, st^p, st^g \rrbracket^c \rightarrow \emptyset dCert, CERTD \llbracket st^d, st^p', st^g \rrbracket^c
   CERT-vdel :
      \Gamma \vdash st^g \neg (dCert, GOVCERT) st^g'
      \Gamma \vdash [st^d, st^p, st^g]^c \rightarrow (dCert, CERT) [st^d, st^p, st^g]^c
data _⊢_→d_,CERTBASED_: CertEnv → CertState → T → CertState → Set where
   CERT-base :
      let open PParams pp; open CertState st; open GState gState
             refresh = mapPartial getDRepVote (fromList vs)
      in T -- TODO: check that the withdrawals are correct here
      \llbracket e, pp, vs \rrbracket^c \vdash st \neg \emptyset \_, CERTBASED record st
         { gState = record gState
            { dreps = mapValueRestricted (const (e + drepActivity)) dreps refresh } }
_⊢_→(_,CERTS)_: CertEnv → CertState → List DCert → CertState → Set
\bot-\bot-\bigcirc, CERTS\bigcirc = SS\RightarrowBS^b \bot-\bot-\bigcirc, CERTBASE\bigcirc \bot-\bot-\bigcirc, CERT\bigcirc
```

Figure 19: CERTS rules

11 Transactions

Transactions are defined in Figure 20. A transaction is made up of a transaction body, a collection of witnesses and some optional auxiliary data. Some key ingredients in the transaction body are:

- A set of transaction inputs, each of which identifies an output from a previous transaction. A transaction input consists of a transaction id and an index to uniquely identify the output.
- An indexed collection of transaction outputs. The TxOut type is an address paired with a coin value.
- A transaction fee. This value will be added to the fee pot.
- The size and the hash of the serialized form of the transaction that was included in the block.

```
Abstract types
     Ix TxId AuxiliaryData : Set
Derived types
     TxIn = TxId \times Ix
     TxOut = Addr × Value × Maybe DataHash
     UTx0 = TxIn \rightarrow TxOut
     Wdrl = RwdAddr → Coin
     RdmrPtr : Set
     RdmrPtr = Tag \times Ix
     ProposedPPUpdates = KeyHash → PParamsUpdate
     Update
                                                           = ProposedPPUpdates × Epoch
Transaction types
     record TxBody : Set where
                                                 : P TxIn
          field txins
                            txouts
                                                                  : Ix → TxOut
                            txfee
                                                                  : Coin
                            mint
                                                                  : Value
                           txvldt : Maybe Slot × Maybe Slot
txcerts : List DCert
                           txwdrls
                                                                  : Wdrl
                           txvote
txprop
txpr
                           txdonation : Coin
                                                 : Maybe Update
                           txup
                           txADhash : Maybe ADHash netwrk : Maybe Network
                                                                  : Maybe Network
                            txsize
                                                                   : IN
                            txid
                                                                   : TxId
                            collateral : P TxIn
                            reqSigHash : P KeyHash
                            scriptIntHash : Maybe ScriptHash
     record TxWitnesses: Set where
          field vkSigs : VKey → Sig
                            scripts : P Script
                            txdats : DataHash → Datum
                            txrdmrs : RdmrPtr - Redeemer x ExUnits
          scriptsP1 : ℙ P1Script
          scriptsP1 = mapPartial isInj<sub>1</sub> scripts
     record Tx : Set where
          field body : TxBody
                            wits : TxWitnesses
                            -- isValid : Bool
                            txAD : Maybe AuxiliaryData
Abstract functions
                                                                                                                            26
```

Figure 20: Definitions used in the UTxO transition system

```
getValue : TxOut → Value
getValue (_{-}, v,_{-}) = v
txinsVKey : \mathbb{P} \text{ TxIn} \rightarrow \text{UTxO} \rightarrow \mathbb{P} \text{ TxIn}
txinsVKey txins\ utxo = txins \cap dom\ (utxo \ ' to-sp\ (isVKeyAddr? \circ proj_1))
scriptOuts : UTxO → UTxO
scriptOuts utxo = filter<sup>m</sup> (sp-o (to-sp isScriptAddr?)
                                    \lambda \{ (\_, addr, \_) \rightarrow addr \}) utxo
txinsScript : \mathbb{P} \text{ TxIn} \rightarrow \text{UTxO} \rightarrow \mathbb{P} \text{ TxIn}
txinsScript \ txins \ utxo = txins \cap dom \ (proj_1 \ (scriptOuts \ utxo))
lookupScriptHash : ScriptHash → Tx → Maybe Script
lookupScriptHash sh tx =
  if sh \in map^s proj_1 (m^s) then
    just $ lookup<sup>m</sup> m sh
  else
    nothing
  where m = setToHashMap $ tx .Tx.wits .TxWitnesses.scripts
isP2Script : Script → Bool
isP2Script = is-just o isInj2
```

12 UTxO

12.1 Accounting

Figure 21 defines functions needed for the UTxO transition system. Figure 22 defines the types needed for the UTxO transition system. The UTxO transition system is given in Figure 24.

- The function outs creates the unspent outputs generated by a transaction. It maps the transaction id and output index to the output.
- The balance function calculates sum total of all the coin in a given UTxO.

```
outs : TxBody → UTxO
 outs tx = mapKeys (tx .txid ,_) (tx .txouts)
 balance : UTxO → Value
 balance utxo = \sum^{mv} [x \leftarrow utxo f^{m}] getValue x
  cbalance : UTxO → Coin
 cbalance utxo = coin (balance utxo)
 coinPolicies : P ScriptHash
 coinPolicies = policies (inject 1)
  isAdaOnly<sup>b</sup> : Value → Bool
  isAdaOnly<sup>b</sup> v = L (policies v) \equiv<sup>e</sup>? coinPolicies J
 minfee : PParams → Tx → Coin
  minfee pp tx = pp .a * tx .body .txsize + pp .b
               + txscriptfee (pp .prices) (totExUnits tx)
 data DepositPurpose : Set where
   CredentialDeposit: Credential → DepositPurpose
   PoolDeposit : Credential → DepositPurpose
   DRepDeposit : Credential → DepositPurpose
   GovActionDeposit : GovActionID → DepositPurpose
  certDeposit : PParams → DCert → Maybe (DepositPurpose × Coin)
  certDeposit _ (delegate c - v) = just (CredentialDeposit c \cdot v)
 certDeposit _ _
                                     = nothing
 certDeposit<sup>™</sup>: PParams → DCert → DepositPurpose → Coin
  certDeposit<sup>m</sup> pp cert = case certDeposit pp cert of λ where
    (just (p, v)) \rightarrow \{p, v\}^m
   nothing
                → Ø<sup>m</sup>
 propDeposit<sup>m</sup> : PParams → GovActionID → GovProposal → DepositPurpose → Coin
 propDeposit<sup>m</sup> pp gaid record { returnAddr = record { stake = c } }
   = { GovActionDeposit gaid , pp .govActionDeposit }<sup>m</sup>
 certRefund : DCert → Maybe DepositPurpose
 certRefund (delegate c nothing nothing x) = just (CredentialDeposit c)
                                            = just (DRepDeposit c)
 certRefund (deregdrep c)
 certRefund _
                                              = nothing
 certRefund<sup>s</sup> : DCert → P DepositPurpose
 certRefunds = partialToSet certRefund
-- this has to be a type definition for inference to work
data inInterval (slot : Slot) : (Maybe Slot × Maybe Slot) → Set where
 both : \forall \{l \ r\} \rightarrow l \leq slot \times slot \leq r \rightarrow inInterval \ slot \ (just \ l \ , just \ r)
                                → inInterval slot (just 1 , nothing)
 lower: \forall \{1\} \rightarrow 1 \leq slot
 upper: \forall \{r\} \rightarrow slot \leq r
                                      → inInterval slot (nothing, just r)
                                          inInterval slot (nothing , nothing)
-- Boolean Functions
```

Rooloan Implication

```
Derived types
 Deposits = DepositPurpose → Coin
UTxO environment
 record UTx0Env : Set where
   field slot : Slot
         ppolicy : Maybe ScriptHash
         pparams : PParams
UTxO states
 record UTxOState : Set where
   constructor [_,_,_,_] u
   field utxo : UTxO
         fees
                 : Coin
         deposits : Deposits
         donations : Coin
UTxO\ transitions
 _⊢_~(_,UTXO)_ : UTxOEnv → UTxOState → Tx → UTxOState → Set
```

Figure 22: UTxO transition-system types

```
updateCertDeposits : PParams → List DCert → DepositPurpose → Coin
 → DepositPurpose → Coin
updateCertDeposits pp [] deposits = deposits
updateCertDeposits pp (cert :: certs) deposits
 = updateCertDeposits pp certs deposits ∪* certDeposit™ pp cert
  | certRefunds cert c
updateProposalDeposits : PParams → TxId → List GovProposal → DepositPurpose → Coin
 → DepositPurpose → Coin
updateProposalDeposits pp txid [] deposits = deposits
updateProposalDeposits pp txid (prop :: props) deposits
 = updateProposalDeposits pp txid props deposits
 U* propDeposit<sup>m</sup> pp (txid, length props) prop
updateDeposits : PParams → TxBody → DepositPurpose → Coin → DepositPurpose → Coin
updateDeposits pp txb
 = updateCertDeposits pp (txb .txcerts)
 updateProposalDeposits pp (txb .txid) (txb .txprop)
depositsChange : PParams → TxBody → DepositPurpose → Coin → Z
depositsChange pp txb deposits
 = getCoin (updateDeposits pp txb deposits)
 depositRefunds : PParams → UTxOState → TxBody → Coin
depositRefunds pp st txb = negPart (depositsChange pp txb (st .deposits))
newDeposits : PParams → UTxOState → TxBody → Coin
newDeposits pp st txb = posPart (depositsChange pp txb (st .deposits))
consumed : PParams → UTxOState → TxBody → Value
consumed pp st txb
 = balance (st .utxo | txb .txins)
 + txb .mint
 + inject (depositRefunds pp st txb)
produced : PParams → UTxOState → TxBody → Value
produced pp st txb
 = balance (outs txb)
 + inject (txb .txfee)
 + inject (newDeposits pp st txb)
 + inject (txb .txdonation)
```

Figure 23: Functions used in UTxO rules, continued

```
UTXO-inductive:
  let open Tx tx renaming (body to txb); open TxBody txb
       open UTxOEnv Γ renaming (pparams to pp)
       open UTxOState s
  in
     txins ≠ Ø
                                                      → txins c dom utxo
  → inInterval slot txvldt
                                                      \rightarrow minfee pp tx \leq txfee
  \rightarrow consumed pp s txb \equiv produced pp s txb \rightarrow coin mint \equiv 0
  → txsize ≤ maxTxSize pp
  \rightarrow \forall [(, txout) \in txouts.proj_1]
       inject (utxoEntrySize txout * minUTxOValue pp) ≤ t getValue txout
  \rightarrow \forall [ (\_, txout) \in txouts .proj_1 ]
       serSize (getValue txout) ≤ maxValSize pp
  \rightarrow \forall [(a, \_) \in \text{range txouts}]
       Sum.All (const \tau) (\lambda \alpha \rightarrow \alpha .BootstrapAddr.attrsSize \leq 64) \alpha
  \rightarrow ∀[ (\alpha, _) ∈ range txouts ] netId \alpha ≡ networkId
  \rightarrow ∀[ a \in \text{dom txwdrls}] a \cdot \text{RwdAddr.net} \equiv \text{networkId}
  -- Add deposits
     \Gamma \vdash s \multimap \emptyset tx, UTXOD \llbracket (utxo \mid txins \circ) \cup^{ml} (outs txb) \rrbracket
                             , fees + txfee
                             , updateDeposits pp txb deposits
                             , donations + txdonation
                             ] u
```

Figure 24: UTXO inference rules

12.2 Witnessing

Figure 25: Functions used for witnessing

```
_⊢_→①_,UTXOWD_ : UTxOEnv → UTxOState → Tx → UTxOState → Set
```

Figure 26: UTxOW transition-system types

```
UTXOW-inductive:

let open Tx tx renaming (body to txb); open TxBody txb; open TxWitnesses wits open UTxOState s; open UTxOEnv \( \infty\)

witsKeyHashes = map \(^s\) hash (dom vkSigs)

witsScriptHashes = map \(^s\) hash scripts

in

\[
\forall \( (vk \), \( \sigma \)) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma \)) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( \sigma \) isSigned \( vk \) (txidBytes txid) \( \sigma \)

\[
\forall \( (vk \), \( \sigma ) \infty vkSigs \( (vk \)) is vkSeyHashes

\[
\forall \( vk \) is vkSeyHashes

\[
\forall \( vk \)
```

Figure 27: UTXOW inference rules

13 Ledger State Transition

The entire state transformation of the ledger state caused by a valid transaction can now be given as a combination of the previously defined transition systems.

```
record LEnv : Set where
constructor [_,_,_]<sup>le</sup>
field slot : Slot
ppolicy : Maybe ScriptHash
pparams : PParams

record LState : Set where
constructor [_,_,_]<sup>l</sup>
field utxoSt : UTxOState
govSt : GovState
certState : CertState

txgov : TxBody → List (GovVote ⊌ GovProposal)
txgov txb = map inj₁ txvote ++ map inj₂ txprop
where open TxBody txb
```

Figure 28: Types and functions for the LEDGER transition system

```
_⊢_¬(_,LEDGER)_: LEnv → LState → Tx → LState → Set
```

Figure 29: The type of the LEDGER transition system

```
LEDGER : let open LState s; txb = tx .body; open TxBody txb; open LEnv Γ in
    record { LEnv Γ } ⊢ utxoSt → ( tx ,UTXOW) utxoSt'
    → [ epoch slot , pparams , txvote ] c ⊢ certState → ( txcerts ,CERTS) certState'
    → [ txid , epoch slot , pparams ] L ⊢ govSt → ( txgov txb ,GOV) govSt'
    → map s stake (dom txwdrls) ⊆ dom (certState' .dState .voteDelegs)
    Γ ⊢ s → ( tx ,LEDGER) [ utxoSt' , govSt' , certState' ] l
```

Figure 30: LEDGER transition system

```
_⊢_→①_,LEDGERSD_ : LEnv → LState → List Tx → LState → Set
_⊢_→①_,LEDGERSD_ = SS⇒BS _⊢_→①_,LEDGERD_
```

Figure 31: LEDGERS transition system

14 Ratification

Governance actions are *ratified* through on-chain voting actions. Different kinds of governance actions have different ratification requirements but always involve *two of the three* governance bodies, with the exception of a hard-fork initiation, which requires ratification by all governance bodies. Depending on the type of governance action, an action will thus be ratified when a combination of the following occurs:

- the *constitutional committee* (CC) approves of the action; for this to occur, the number of CC members who vote yes must meet the CC vote threshold;
- the *delegation representatives* (DReps) approve of the action; for this to occur, the stake controlled by the DReps who vote yes must meet the DRep vote threshold as a percentage of the *total participating voting stake* (totalStake);
- the stake pool operators (SPOs) approve of the action; for this to occur, the stake controlled by the SPOs who vote yes must meet a certain threshold as a percentage of the *total registered voting stake* (totalStake).

Warning. Different stake distributions apply to DReps and SPOs.

A successful motion of no-confidence, election of a new constitutional committee, a constitutional change, or a hard-fork delays ratification of all other governance actions until the first epoch after their enactment. This gives a new constitutional committee enough time to vote on current proposals, re-evaluate existing proposals with respect to a new constitution, and ensures that the in principle arbitrary semantic changes caused by enacting a hard-fork do not have unintended consequences in combination with other actions.

14.1 Ratification requirements

Figure 32 details the ratification requirements for each governance action scenario. The columns represent

- GovAction: the action under consideration;
- CC: a \checkmark indicates that the constitutional committee must approve this action; a symbol means that constitutional committee votes do not apply;
- DRep: the vote threshold that must be met as a percentage of totalStake;
- SPO: the vote threshold that must be met as a percentage of the stake held by all stake pools; a symbol means that SPO votes do not apply.

Each of these thresholds is a governance parameter. The two thresholds for the Info action are set to 100% since setting it any lower would result in not being able to poll above the threshold.

14.2 Ratification restrictions

As mentioned earlier, each GovAction must include a GovActionID for the most recently enacted action of its given type. Consequently, two actions of the same type can be enacted at the same time, but they must be *deliberately* designed to do so.

Figure 33 defines three more types and some helper functions used in the ratification transition system.

- StakeDistrs represents a map relating each voting delegate to an amount of stake;
- RatifyEnv denotes an environment with data required for ratification;

GovAction		DRep	SP0	
1. Motion of no-confidence	-	P1	Q1	
2a. New committee/threshold (normal state)	-	P2a	Q2a	
2b. New committee/threshold (state of no-confidence)	-	P2b	Q2b	
3. Update to the Constitution	✓	P3	-	
4. Hard-fork initiation	✓	P4	Q4	
5a. Changes to protocol parameters in the NetworkGroup	✓	P5a	-	
5b. Changes to protocol parameters in the	✓	P5b	-	
EconomicGroup				
5c. Changes to protocol parameters in the	✓	P5c	-	
TechnicalGroup				
5d. Changes to protocol parameters in the	✓	P5d	-	
GovernanceGroup				
6. Treasury withdrawal	✓	P6	-	
7. Info	✓	100	100	

Figure 32: Ratification requirements

```
record StakeDistrs : Set where
 field stakeDistr : VDeleg - Coin
record RatifyEnv : Set where
 field stakeDistrs : StakeDistrs
       currentEpoch : Epoch
       dreps : Credential → Epoch
       ccHotKeys : Credential → Maybe Credential
       treasury : Coin
record RatifyState : Set where
 constructor [-,-,-]^r
 field es
             : EnactState
       removed : P (GovActionID × GovActionState)
       delay : Bool
CCData: Set
CCData = Maybe ((Credential → Epoch) × ℚ)
isCC : VDeleg → Bool
isCC (credVoter CC _) = true
isCC _
                    = false
isDRep : VDeleg → Bool
isDRep (credVoter DRep _) = true
isDRep (credVoter _ _) = false
isDRep abstainRep
                       = true
isDRep noConfidenceRep = true
isSPO: VDeleg → Bool
isSPO (credVoter SPO _) = true
isSPO_
                      = false
```

Figure 33: Types and functions for the RATIFY transition system

- RatifyState denotes an enactment state that exists during ratification;
- CCData stores data about the constitutional committee.
- isCC, isDRep, and isSPO, which return true if the given delegate is a CC member, a DRep, or an SPO (resp.) and false otherwise.

The code in Figure 34 defines some of the types required for ratification of a governance action.

- Assuming a ratification environment Γ ,
 - cc contains constitutional committee data;
 - votes is a relation associating each role-credential pair with the vote cast by the individual denoted by that pair;
 - ga denotes the governance action being voted upon.
- roleVotes filters the votes based on the given governance role.
- actualCCVote determines how the vote of each CC member will be counted; specifically, if a CC member has not yet registered a hot key, has expired, or has resigned, then actualCCVote returns abstain; if those none of these conditions is met, then
 - if the CC member has voted, then that vote is returned;
 - if the CC member has not voted, then the default value of no is returned.
- actualCCVotes uses actualCCVote to determine how the votes of all CC members will be counted.
- actualPDRepVotes determines how the votes will be counted for DReps; here, abstainRep is mapped to abstain and noConfidenceRep is mapped to either yes or no, depending on the value of ga.
- actualDRepVotes determines how the votes of DReps will be counted; activeDReps that didn't vote count as a no.
- actualVotes is a partial function relating delegates to the actual vote that will be counted on their behalf; it accomplishes this by aggregating the results of actualCCVotes, actualPDRepVotes, and actualDRepVotes.

The code in Figure 35 defines votedHashes, which returns the set of delegates who voted a certain way on the given governance role. The code in Figure 36 defines yet more types required for ratification of a governance action.

- getStakeDist computes the stake distribution based on the given governance role and the corresponding delegations;
- acceptedStake calculates the sum of stakes for all delegations that voted yes for the specified role;
- totalStake calculates the sum of stakes for all delegations that didn't vote abstain for the given role;
- activeVotingStake computes the total stake for the role of DRep for active voting; it calculates the sum of stakes for all active delegates that have not voted (i.e., their delegation is present in CC but not in the *votes* mapping);
- accepted checks if an action is accepted for the CC, DRep, and SPO roles and whether it meets the minimum active voting stake (meetsMinAVS);

```
actualVotes : RatifyEnv → CCData → (GovRole × Credential) → Vote → GovAction → PParams
              → VDeleg → Vote
actualVotes\ \Gamma\ cc\ votes\ ga\ pparams
  = mapKeys (credVoter CC) actualCCVotes
  U<sup>ml</sup> actualPDRepVotes U<sup>ml</sup> actualDRepVotes
  U<sup>ml</sup> actualSPOVotes
  where
    open RatifyEnv Γ
    open PParams pparams
    roleVotes : GovRole → VDeleg ¬ Vote
    roleVotes r = mapKeys (uncurry credVoter) (filter<sup>m</sup>? ((r^2_-) \circ proj_1 \circ proj_1) votes)
    activeCC activeDReps : P Credential
    activeCC = case cc of \lambda where
      (just (cc, \_)) \rightarrow dom (filter^{mb} (is-just \circ proj_2) (ccHotKeys | dom cc))
      nothing
    activeDReps = dom (filter<sup>m</sup>? (\lambda x \rightarrow \text{currentEpoch} \le ? (\text{proj}_2 x)) dreps)
    actualCCVote : Credential → Epoch → Vote
    actualCCVote c e =
      case \dot{c} currentEpoch \leq e \dot{c}^b, lookup<sup>m</sup>? ccHotKeys c of \lambda where
        (true , just (just c')) → maybe id Vote.no $ lookup<sup>m</sup>? votes (CC , c')
                                    → Vote.abstain -- expired, no hot key or resigned
    actualCCVotes : Credential → Vote
    actualCCVotes = case cc , \dot{c} ccMinSize \leq length ^{s} activeCC \dot{c}^{b} of \lambda where
      (just (cc, \_), true) \rightarrow mapWithKey actualCCVote cc
      (just (cc, \_), false) \rightarrow constMap (dom cc) Vote.no
      (nothing
                    , _)
    actualPDRepVotes
      = { abstainRep , Vote.abstain }<sup>m</sup>
      U^{ml} { noConfidenceRep , (case ga of \lambda where NoConfidence \rightarrow Vote.yes
                                                                         → Vote.no) }<sup>m</sup>
    actualDRepVotes
      = roleVotes GovRole.DRep
      U<sup>ml</sup> constMap (map<sup>s</sup> (credVoter DRep) activeDReps) Vote.no
    actualSPOVotes
         roleVotes GovRole.SPO
      U<sup>ml</sup> constMap spos (if isHF then Vote.no else Vote.abstain)
      where
        spos : P VDeleg
        spos = filter* isSPOProp $ dom (StakeDistrs.stakeDistr stakeDistrs)
        isHF: Bool
        isHF = case ga of \lambda where
           (TriggerHF _) → true
                           → false
```

Figure 34: Types and proofs for the ratification of governance actions

```
votedHashes: Vote \rightarrow (VDeleg \rightarrow Vote) \rightarrow GovRole \rightarrow P VDeleg votedHashes v votes r = votes^{-1} v votedYesHashes: (VDeleg \rightarrow Vote) \rightarrow GovRole \rightarrow P VDeleg votedYesHashes = votedHashes Vote.yes votedAbstainHashes participatingHashes: (VDeleg \rightarrow Vote) \rightarrow GovRole \rightarrow P VDeleg votedAbstainHashes = votedHashes Vote.abstain participatingHashes votes r = votedYesHashes votes r U votedHashes Vote.no votes r
```

Figure 35: Calculation of the votes as they will be counted

```
getStakeDist: GovRole → P VDeleg → StakeDistrs → VDeleg → Coin
getStakeDist CC cc _
                                                        = constMap (filter s isCCProp cc) 1
getStakeDist DRep _ record { stakeDistr = dist } = filterKeys isDRepProp dist
getStakeDist SPO _ record { stakeDistr = dist } = filterKeys isSPOProp dist
acceptedStakeRatio : GovRole → P VDeleg → StakeDistrs → (VDeleg → Vote) → ℚ
acceptedStakeRatio r cc dists votes = acceptedStake /o totalStake
  where
    acceptedStake totalStake : Coin
    acceptedStake = \sum^{mv} [x \leftarrow (getStakeDist \ r \ cc \ dists \ | \ votedYesHashes \ votes \ r)]^{fm}]x
    totalStake = \Sigma^{mv} [ x \in \text{getStakeDist } r \text{ } cc \text{ } dists \text{ | votedAbstainHashes } votes \text{ } r \text{ } c \text{ } fm \text{ ] } x
acceptedBy : RatifyEnv → EnactState → GovActionState → GovRole → Set
acceptedBy \Gamma (record { cc = cc , _; pparams = pparams , _ }) gs role =
  let open GovActionState gs
      votes' = actualVotes \Gamma cc votes action pparams
              = maybe id Q.OQ $ threshold pparams (proj<sub>2</sub> <$> cc) action role
  in acceptedStakeRatio role (dom votes') (RatifyEnv.stakeDistrs Γ) votes' ℚ.≥ t
accepted : RatifyEnv → EnactState → GovActionState → Set
accepted \Gamma es gs = accepted By \Gamma es gs CC \wedge accepted By \Gamma es gs DRep \wedge accepted By \Gamma es gs SPO
expired : Epoch → GovActionState → Set
expired current record { expiresIn = expiresIn } = expiresIn < current</pre>
```

Figure 36: Calculation of stake distributions

• expired checks whether a governance action is expired in a given epoch.

The code in Figure 37 defines still more types required for ratification of a governance action.

- verifyPrev takes a governance action, its NeedsHash, and EnactState and checks whether the ratification restrictions are met;
- delayingAction takes a governance action and returns true if it is a "delaying action" (NoConfidence, NewCommittee, NewConstitution, TriggerHF) and returns false otherwise;
- delayed checks whether a given GovAction is delayed.

Figure 38 defines three rules, RATIFY-Accept, RATIFY-Reject, and RATIFY-Continue, along with the relation $_\vdash_\neg \bigcirc_$, RATIFYD. The latter is the transition relation for ratification of a GovAction.

```
verifyPrev : (a : GovAction) \rightarrow NeedsHash a \rightarrow EnactState \rightarrow Set
verifyPrev NoConfidence h = s = h = es .cc .proj_2
verifyPrev (NewCommittee _ _ _) h es = h ≡ es .cc .proj₂
verifyPrev (NewConstitution _ _) h = s = h \equiv es .constitution .proj<sub>2</sub>
verifyPrev (TriggerHF _) h \ es = h \equiv es .pv .proj_2
verifyPrev (ChangePParams _) h \ es = h \equiv es .pparams .proj_2
verifyPrev (TreasuryWdrl _)
                                       _ _ = T
verifyPrev Info
delayingAction : GovAction → Bool
delayingAction NoConfidence
                                             = true
delayingAction (NewCommittee _ _ _) = true
delayingAction (NewConstitution _ _) = true
delayingAction (TriggerHF _)
delayingAction (ChangePParams _)
                                           = false
delayingAction (TreasuryWdrl _)
                                           = false
delayingAction Info
                                             = false
delayed: (a : GovAction) \rightarrow NeedsHash a \rightarrow EnactState \rightarrow Bool \rightarrow Set
delayed a h es d = \neg \text{ verifyPrev } a \text{ h es } \forall d \equiv \text{ true}
```

Figure 37: Determination of the status of ratification of the governance action

```
RATIFY-Accept: let open RatifyEnv \Gamma; st = a .proj<sub>2</sub>; open GovActionState st in
    accepted \Gamma es st
  \rightarrow ¬ delayed action prevAction es d
  \rightarrow [ a .proj<sub>1</sub> , treasury , currentEpoch ] ^{e} \vdash es \rightarrow ( action ,ENACT) es'
    Γ⊢[es , removed
                                   , d
                                                                \mathbb{I}^r \rightarrow \emptyset a ,RATIFY'D
        [es', \{a\} \cup removed, delayingAction action]^r
RATIFY-Reject : let open RatifyEnv \Gamma; st = a \cdot proj_2 in
    ¬ accepted Γ es st
  → expired currentEpoch st
    \Gamma \vdash [es, removed, d]^r \multimap [a, RATIFY'] [es, {a} \cup removed, d]^r
RATIFY-Continue: let open RatifyEnv \Gamma; st = a .proj<sub>2</sub>; open GovActionState st in
    ¬ accepted Γ es st × ¬ expired currentEpoch st
  ⊎ accepted Γ es st
    × ( delayed action prevAction es d
      \forall (\forall es' \rightarrow \neg [\alpha .proj_1, treasury, currentEpoch]^e \vdash es \neg (action, ENACT) es'))
  \Gamma \vdash [es, removed, d]^r \rightarrow (a, RATIFY') [es, removed, d]^r
_⊢_⊸(_,RATIFY) : RatifyEnv → RatifyState → List (GovActionID × GovActionState)
                    → RatifyState → Set
_⊢_~(_,RATIFY)_ = SS⇒BS _⊢_~(_,RATIFY')_
```

Figure 38: The RATIFY transition system

• RATIFY-Accept checks if the votes for a given GovAction meet the threshold required for acceptance, that the action is accepted and not delayed, and RATIFY-Accept ratifies the

action.

- RATIFY-Reject asserts that the given GovAction is not accepted and expired; it removes the governance action.
- RATIFY-Continue covers the remaining cases and keeps the GovAction around for further voting.

Note that all governance actions eventually either get accepted and enacted via RATIFY-Accept or rejected via RATIFY-Reject. If an action satisfies all criteria to be accepted but cannot be enacted anyway, it is kept around and tried again at the next epoch boundary.

We never remove actions that do not attract sufficient yes votes before they expire, even if it is clear to an outside observer that this action will never be enacted. Such an action will simply keep getting checked every epoch until it expires.

15 Blockchain layer

```
record NewEpochEnv : Set where
 field stakeDistrs : StakeDistrs
   -- TODO: compute this from LState instead
record NewEpochState : Set where
 constructor [-,-,-,-]^{ne}
 field lastEpoch : Epoch
             _poci
: Acnt
. .
       acnt
               : LState
               : EnactState
       fut : RatifyState
record ChainState : Set where
 field newEpochState : NewEpochState
record Block : Set where
 field ts : List Tx
       slot : Slot
```

Figure 39: Definitions for the NEWEPOCH and CHAIN transition systems

```
NEWEPOCH-New : \forall \{\Gamma\} \rightarrow let
  open NewEpochState nes hiding (es)
  open RatifyState fut using (removed) renaming (es to esW)
  -- ^ this rolls over the future enact state into es
  open LState ls; open UTxOState utxoSt
  open CertState certState
  open PState pState; open DState dState; open GState gState
  open Acnt acnt
  trWithdrawals = esW .EnactState.withdrawals
  totWithdrawals = \sum^{m \, v} [ \ x \leftarrow trWithdrawals \ ^{\text{fm}} \ ] \ x
  removedGovActions = flip concatMap<sup>s</sup> removed \lambda (gaid, gaSt) \rightarrow
      map s (GovActionState.returnAddr gaSt ,_)
            ((deposits | { GovActionDeposit gaid }) s)
  govActionReturns = aggregate_{+} $ map ^{s} (\lambda (\alpha, _ , d) \rightarrow a , d) removedGovActions <math>^{fs}
           = record esW { withdrawals = \emptyset<sup>m</sup> }
  retired = retiring -1 e
  refunds = govActionReturns ∪* trWithdrawals | dom rewards
  unclaimed = govActionReturns ∪* trWithdrawals | dom rewards c
  govSt' = filter (\lambda x \rightarrow i proj_1 x \notin map^s proj_1 removed i) govSt
  gState' = record gState { ccHotKeys = ccHotKeys | ccCreds (es .EnactState.cc) }
  certState' = record certState {
      pState = record pState
        { pools = pools | retired c; retiring = retiring | retired c};
      dState = record dState
        { rewards = rewards U* refunds };
      gState = if not (null govSt') then gState' else record gState'
        { dreps = mapValues suce dreps }
  utxoSt' = record utxoSt
      \{ fees = 0 \}
      ; deposits = deposits | map<sup>s</sup> (proj<sub>1</sub> o proj<sub>2</sub>) removedGovActions <sup>c</sup>
      ; donations = 0
  1s' = record ls
      { govSt = govSt'; utxoSt = utxoSt'; certState = certState'}
  acnt' = record acnt
      { treasury = treasury + fees + getCoin unclaimed + donations - totWithdrawals }
  in
  e \equiv suc^e lastEpoch
  → record { currentEpoch = e; treasury = treasury; GState gState; NewEpochEnv \( \Gamma \) }
      ⊢ [ es , ∅ , false ] r → ( govSt' ,RATIFY) fut'
  \Gamma \vdash nes \neg (e, NEWEPOCH) [e, acnt', ls', es, fut']^{ne}
NEWEPOCH-Not-New : \forall \{\Gamma\} \rightarrow \text{let open NewEpochState nes in}
  e ≢ suc<sup>e</sup> lastEpoch
  \Gamma \vdash nes \multimap \emptyset e , NEWEPOCH \emptyset nes
                                               45
```

Figure 40: NEWEPOCH transition system

```
_⊢_→ℂ_,CHAIND_ : τ → ChainState → Block → ChainState → Set
```

Figure 41: Type of the CHAIN transition system

```
CHAIN:

let open ChainState s; open Block b; open EnactState (newEpochState .NewEpochState.es) in record { stakeDistrs = calculateStakeDistrs (newEpochState .NewEpochState.ls) }

⊢ newEpochState → ( epoch slot ,NEWEPOCH) nes

→ [ slot , constitution .proj₁ .proj₂ , pparams .proj₁ ] le

⊢ nes .NewEpochState.ls → ( ts ,LEDGERS) ls'

_ ⊢ s → ( b ,CHAIN) record s { newEpochState = record nes { ls = ls' } }
```

Figure 42: CHAIN transition system

16 Properties

16.1 UTxO

Here, we state the fact that the UTxO relation is computable.

```
UTXO-step: UTxOEnv → UTxOState → Tx → Maybe UTxOState
UTXO-step = compute

UTXO-step-computes-UTXO: UTXO-step \( \tau \) utxoState tx \( \equiv \) just utxoState'

\[
\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{\text{
```

Figure 43: Computing the UTXO transition system

Property 16.1 (Preserve Balance)

```
For all env ∈ UTxOEnv, utxo, utxo' ∈ UTxO, fees, fees' ∈ Coin and tx ∈ Tx,
   if

tx .body .txid ∉ map * proj₁ (dom utxo)

and

Γ ⊢ [ utxo , fees , deposits , donations ] " ¬ ( tx ,UTXO)
      [ utxo' , fees' , deposits' , donations' ] "

then

getCoin [ utxo , fees , deposits , donations ] "

≡ getCoin [ utxo' , fees' , deposits' , donations' ] "
```