

2nd-YEAR PhD REPORT

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October 11, 2021



THE UNIVERSITY *of* EDINBURGH

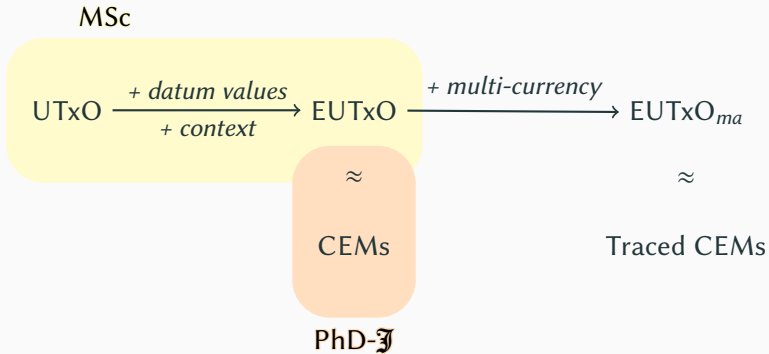


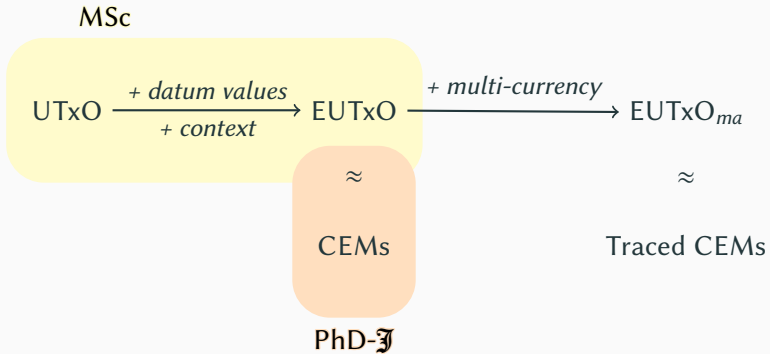
INPUT | OUTPUT

YEAR 3: *RECAP*

Mechanising the meta-theory of two separate objects of study:

- **BitML**: Bitcoin Modelling Language
- The (extended) **UTxO** model

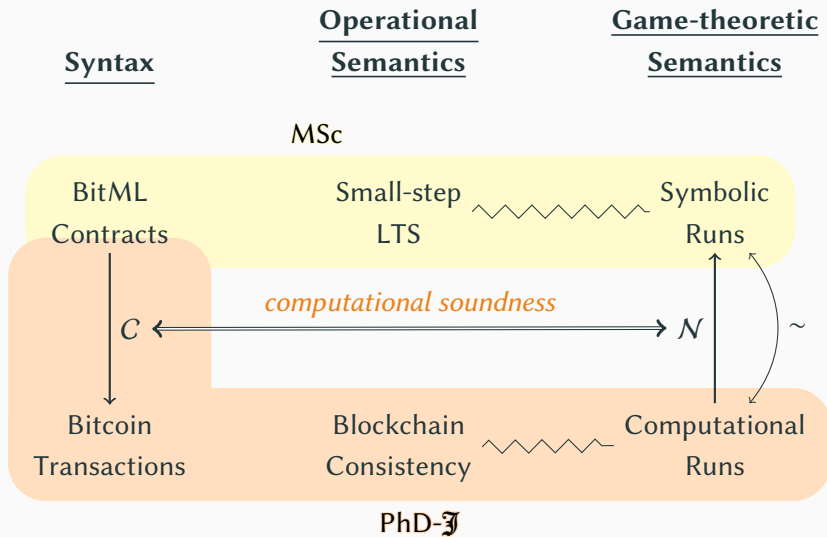




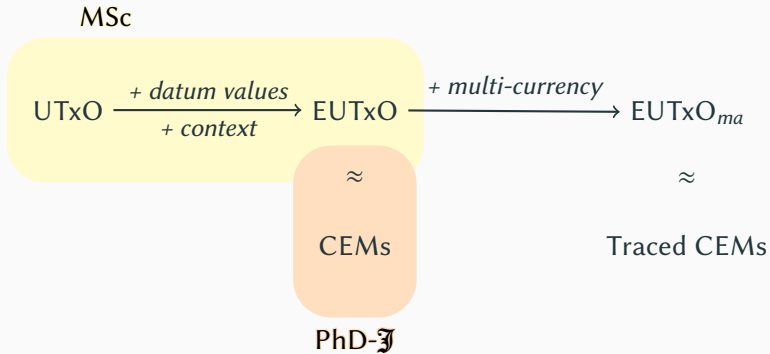
WTSC @ FC'20

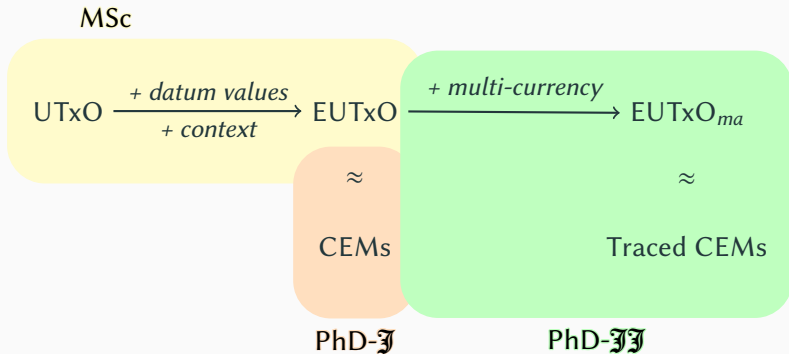
The Extended UTxO Model

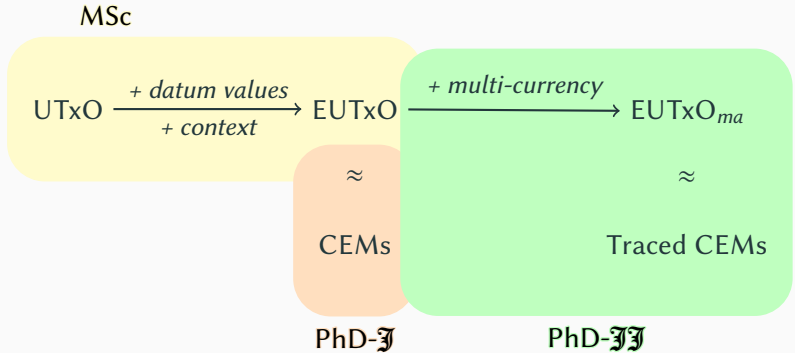
M.Chakravarty, J.Chapman, K.MacKenzie, O.Melkonian, M.P.Jones, P.Wadler



YEAR III: *WHERE I'VE BEEN...*







RSC @ ISoLA'20: *UTxO_{ma}: UTxO with Multi-Asset Support*

RSC @ ISoLA'20: *Native Custom Tokens in the Extended UTxO Model*

- In collaboration with W.Swierstra (UU) and J.Chapman (IOHK)

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| Blockchain | | Concurrency Theory |
|------------------|-------------------|---------------------------|
| ledgers | \leftrightarrow | computer memory |
| memory locations | \leftrightarrow | accounts |
| data values | \leftrightarrow | account balances |
| smart contracts | \leftrightarrow | programs accessing memory |

SEPARATION LOGIC FOR UTxO

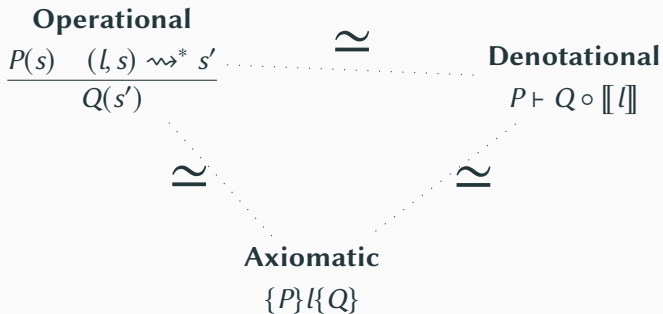
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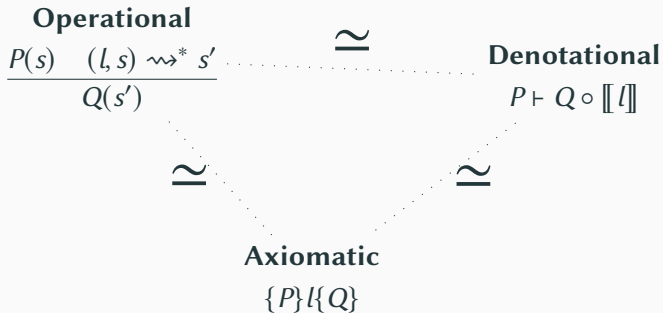


Transfer results from (Concurrent) Separation Logic!

HOARE-STYLE SEMANTICS AND CORRESPONDENCES



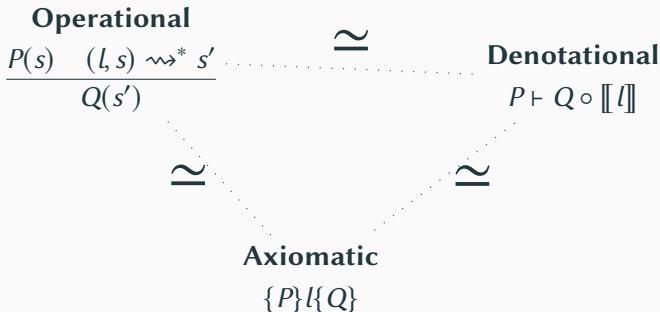
HOARE-STYLE SEMANTICS AND CORRESPONDENCES



SL: [FRAME] rule

$$\frac{l \# R \quad \{P\}l\{Q\}}{\{P * R\}l\{Q * R\}}$$

HOARE-STYLE SEMANTICS AND CORRESPONDENCES

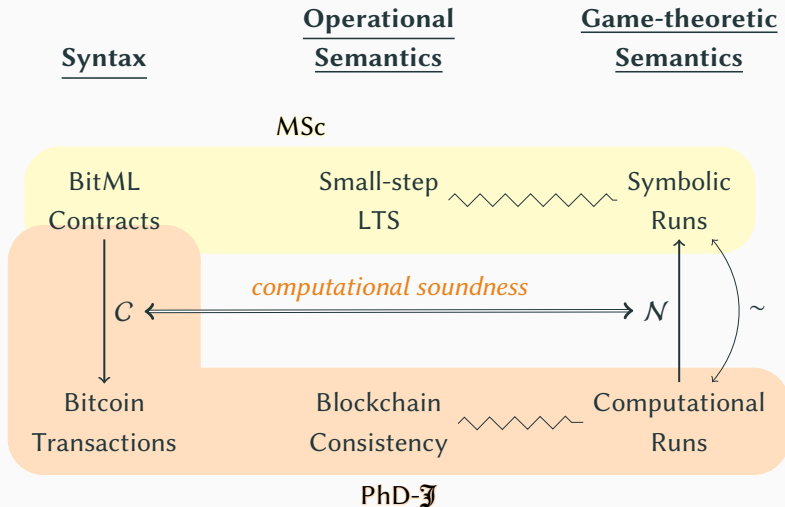


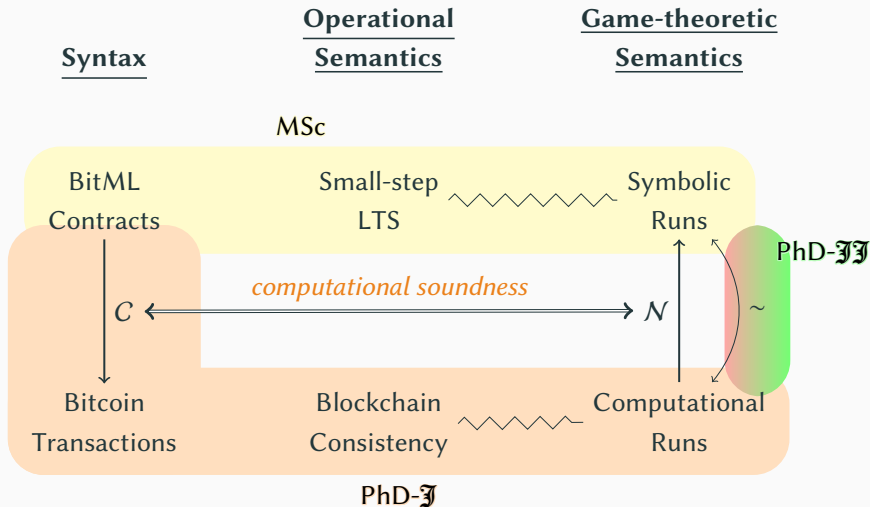
SL: [FRAME] rule

$$\frac{l \# R \quad \{P\} l \{Q\}}{\{P * R\} l \{Q * R\}}$$

CSL: [PARALLEL] rule

$$\frac{l_1 \parallel l_2 = l \quad l_1 \# P_2 \quad l_2 \# P_1 \quad \{P_1\} l_1 \{Q_1\} \quad \{P_2\} l_2 \{Q_2\}}{\{P_1 * P_2\} l \{Q_1 * Q_2\}}$$





BitML: COHERENCE

Definition 20 (Coherence). We inductively define the relation *coher*($R^s, R^c, r, txout, sechash, \kappa$) where (i) R^s is a symbolic run, (ii) R^c is a computational run, (iii) r is a randomness source, (iv) *txout* is an injective function from names x (occurring in R^s) to transaction outputs (T, o) (where T occurs in R^c), respecting values; (v) *sechash* is a mapping from secret names a (occurring in R^s) to bitstrings; (vi) κ maps triples $\{(\text{GIC}, D, A)\}$, where D is a subterm of C , to public keys.

Base case: *coher*($R^s, R^c, r, txout, sechash, \kappa$) holds if all the following conditions hold: (i) $R^s \xrightarrow{\tau} \Gamma \mid t, R^c \mathcal{R}, r, txout, sechash, \kappa$ holds if all the following conditions hold: (i) $R^s \xrightarrow{\tau} \Gamma \mid 0, with $R^c = T_0 \dots$ initial; (iii) all the public keys in R^c are generated from r , according to Definition 13; (iv) *txout* maps exactly the x of $(A, v)_x$ in Γ_0 to an output in T_0 of value $v\tilde{b}$, and spendable with $\tilde{K}_{A, (r_A)}$; (v) $\text{dom } sechash = \emptyset$; (vi) $\text{dom } \kappa = \emptyset$.$

Inductive case: *coher*($R^s \xrightarrow{\tau} \Gamma \mid t, R^c \mathcal{R}, r, txout, sechash, \kappa$) holds if *coher*($R^s, R^c, r, txout', sechash', \kappa'$) and one of the following cases applies.

- (1) $\alpha = \text{advertise}(\text{GIC})$, $\mathcal{R} = A \rightarrow * : C$, where C is obtained by encoding GIC as a bitstring, representing each x in it as the transaction output *txout'*(x). Further, *txout'* $\xrightarrow{\tau}$ *txout*, *sechash'* $\xrightarrow{\tau}$ *sechash*, and $\kappa' = \kappa$.
- (2) $\alpha = A : \text{GIC}, D$, where: (i) for some B, R^c contains $B \rightarrow * : C$, where C is obtained from GIC and *txout'* as in Item 1. Note that R^c might contain several such messages; below, we let C represent the first occurrence. (ii) for some B , $\mathcal{R} = B \rightarrow * : (C, \tilde{h}, \tilde{k})$ (signed by A), where \tilde{h} is a sequence comprising a bitstring h_i with $|h_i| = \eta$ for each secret a_i in A , and \tilde{k} is a sequence of keys, as the one produced by the stipulation protocol. We require that \mathcal{R} is the first occurrence, in the run R^c , of such a message after A . (iii) Let N_i be the length of a_i fixed in A . If $N_i \neq \pm$, we require that R^c contains, for some B , a query to the oracle $B \rightarrow O : m_i$, and a subsequent reply $O \rightarrow B : h_i$ such that $|m_i| = \eta + N_i$. Otherwise, if $N_i = \pm$, we require that h_i does not occur as a reply from O to any query of length $\geq \eta$. (iv) No hash is reused: the h_i are pairwise distinct, and also distinct from *sechash'*(b) for any $b \in \text{dom}(\text{sechash}')$. (v) *txout' = txout'*. (vi) *sechash* extends *sechash'* so that for each secret a_i we have *sechash*(a_i) = h_i . (vii) If $A \in \text{Hon}$, we define κ by extending κ' according to \tilde{k} , so to record the public keys of all participants occurring in G for each subterm D of C . If κ' already defines such keys, or $A \notin \text{Hon}$, we let $\kappa = \kappa'$.
- (3) $\alpha = A : \text{GIC}, x$, where: (i) $\mathcal{R} = B \rightarrow * : m$ for some B , where m is the signature of the transaction $T_{m,0}$ of $\mathcal{B}_{\text{adv}}(\text{GIC})$ relatively to the input x with $\tilde{K}_{A, (r_A)}$. The parameters of the compiler are set as follows: $\text{part}, \text{PartG}$ and val are inferred from G , we let *txout' = txout'*, *sechash' = sechash'*, and $\text{K}(B) = \tilde{R}_B^p(r_B)$, $\text{K}(D, B) = \kappa'(\text{GIC}, D, B)$ for each B ,

in $\mathcal{B}_{\text{adv}}(\text{GIC})$. The needed compiler parameters are obtained as in Item 3, (iii) *sechash' = sechash'*, $\kappa = \kappa'$, and *txout' extends txout'*, mapping z to $T_{m,0}$.

- (5) $\alpha = A : x, D$, where: (i) R^c contains $(C, v)_x$ with $C' = D + \sum_i D_i$, for some $D = A : D'$. (ii) In R^s , we find that $(C, v)_x$ has GIC as its ancestor advertisement. (iii) $\mathcal{R} = B \rightarrow * : m$, where m is a signature with key $\kappa'(\text{GIC}, D, A)$ of the first transaction T in $\mathcal{B}_0(D, D, T', o, v, \text{PartG}, 0)$, where $(T', o) = \text{txout}'(x)$. The compiler parameters are obtained as in Item 3, (iv) *txout' = txout'*, *sechash' = sechash'*, and $\kappa = \kappa'$. (v) R^c contains $B \rightarrow * : t$ for some B , and m is the first signature of T in $R^c \mathcal{R}$ after the first broadcast of T .
- (6) $\alpha = \text{put}(\tilde{x}, \tilde{a}, y)$, where: (i) $\tilde{x} = x_1 \dots x_k$. (ii) In Γ_{R^c} , the action α consumes $(D + C, v)_y$ and the deposits $(A_i, v_i)_{x_i}$ to produce $(C', v')_{y'}$, where $D = \dots : \text{put} \dots \text{reveal} \dots : C'$. Let t be the maximum deadline in α after in front of D , (iii) In R^s , we find that $(D + C, v)_y$ has GIC as its ancestor advertisement, for some G and C'' . (iv) $\mathcal{R} = T$ where T is the first transaction of $\mathcal{B}_0(C'', D, T', o, v', \tilde{x}, \text{PartG}, t)$, where $(T', o) = \text{txout}'(y)$. The compiler parameters are obtained as in Item 3, (v) *txout' extends txout'* so that y' is mapped to $(T, 0)$, *sechash' = sechash'*, and $\kappa = \kappa'$.
- (7) $\alpha = A : a$, where: (i) $\mathcal{R} = B \rightarrow * : m$ from some B with $|m| \geq \eta$. (ii) $R^c = \dots : (B \rightarrow O : m) (O \rightarrow B : \text{sechash}'(a)) \dots$, for some B . (iii) *txout' = txout'*, *sechash' = sechash'* and $\kappa = \kappa'$. (iv) In R^s we find an $A : \text{GIC}, D$ action, with a in G , with a corresponding broadcast in R^c of $m' = (C, \tilde{h}, \tilde{k})$. (v) \mathcal{R} is the first broadcast of m in R^c after the first broadcast of m' .
- (8) $\alpha = \text{split}(y)$, where: (i) In R^s , the action α consumes $(D + C, v)_y$ to obtain $(C_0, v_0)_{x_0} \mid \dots \mid (C_k, v_k)_{x_k}$ where $D = \dots : \text{split } \tilde{v} \rightarrow \tilde{C}$ and $\tilde{C} = C_0 \dots C_k$. Let t be the maximum deadline in α after in front of D . (ii) In R^s , we find that $(D + C, v)_y$ has GIC as its ancestor advertisement. (iii) $\mathcal{R} = T$ where T is the first transaction of $\mathcal{B}_{\text{par}}(\tilde{C}, D, T', o, \text{PartG}, t)$ where $(T', o) = \text{txout}'(y)$. The compiler parameters are obtained as for Item 3, (iv) *txout' extends txout'* mapping each x_i to (T, i) , *sechash' = sechash'*, and $\kappa = \kappa'$.
- (9) $\alpha = \text{withdraw}(A, v, y)$, where: (i) In R^s , the action α consumes $(D + C, v)_y$ to obtain $(A, v)_x$, where $D = \dots : \text{withdraw } A$. (ii) In R^s , we find that $(D + C, v)_y$ has GIC as its ancestor advertisement. (iii) $\mathcal{R} = T$ where T is the first transaction of $\mathcal{B}_0(D, D, T', o, v, \text{PartG}, 0)$ where $(T', o) = \text{txout}'(y)$. The compiler parameters are obtained as for Item 3, (iv) *txout' extends txout'* mapping x to $(T, 0)$, *sechash' = sechash'*, and $\kappa = \kappa'$.
- (10) $\alpha = A : x, x'$, where: (i) In R^s we find $(A, v)_x$ and $(A, v')_{x'}$. (ii) In R^c we find $B \rightarrow * : T$ for some B, T , where T has as its two inputs *txout'*(x) and *txout'*(x'), and a single output of

- (11) $\alpha = \text{join}(x, y)$, where: (i) In R^s the action α spends $(A, v')_{x'}$ to obtain $(A, v + v')_y$. (ii) $\mathcal{R} = T$ is an action having as inputs *txout'*(x) and *txout'*(x'), having one output of value $v + v'$ redeemable with κ . (iii) *txout' extends txout'* mapping y to $(T, 0)$, *sechash' = sechash'*, and $\kappa = \kappa'$.
- (12) $\alpha = A : x, v, v'$. Similar to Item 10.
- (13) $\alpha = \text{divide}(x, v, v')$. Similar to Item 11.
- (14) $\alpha = A : x, B$. Similar to Item 10.
- (15) $\alpha = \text{donate}(x, B)$. Similar to Item 11.
- (16) $\alpha = A : \tilde{g}, j$, where: (i) $\tilde{g} = g_1 \dots g_k$. (ii) In R^c $v = (B_i, v_i)_{y_i}$ for $i \in 1..k$, with $B_j = A$. (iii) In R^c $v = B \rightarrow * : T$ for some B, T , where T has as its inputs *txout'*(y_i) for $i \in 1..k$, and possibly others not in $\text{ran}(\text{txout}')$. (iv) $\mathcal{R} = B \rightarrow * : m$ from some B , where m is a signature of T with $\tilde{K}_{A, (r_A)}$, corresponding to the j -th. (v) \mathcal{R} is the first broadcast of m in R^c after the first cast of T . (vi) \mathcal{R} does not correspond to any of the cases, i.e. there is no other symbolic action α' for $R^s \mathcal{R}$ α' would be coherent with $R^c \mathcal{R}$. (vii) *txout' = txout'*, *sechash' = sechash'*, and $\kappa = \kappa'$.
- (17) $\alpha = \text{destroy}(x)$, where: (i) $\tilde{x} = x_1 \dots x_k$. (ii) In R^s , $\text{sums}(A_i, (v_i)_{x_i})$ to obtain 0. (iii) $\mathcal{R} = T$ from some B having as inputs *txout'*(x_1), ..., *txout'*(x_k), and possibly others not in $\text{ran}(\text{txout}')$. (iv) \mathcal{R} does not correspond to the other cases, i.e. there is no other symbolic action which $R^s \mathcal{R}$ α' would be coherent with $R^c \mathcal{R}$. (v) *txout' = txout'*, *sechash' = sechash'*, and $\kappa = \kappa'$.
- (18) $\alpha = \delta = \mathcal{R}$, and *txout' = txout'*, *sechash' = sechash'*, and $\kappa = \kappa'$.

Inductive case 2: the predicate *coher*($R^s, R^c \mathcal{R}, r, txout, sechash, \kappa$), and one of the following cases applies:

- (1) $\mathcal{R} = T$ where no input of T belongs to $\text{ran}(\text{txout})$.
- (2) $\mathcal{R} = A \rightarrow O : m$ or $\mathcal{R} = O \rightarrow A : m$, for some A, m .
- (3) $\mathcal{R} = A \rightarrow * : m$, where \mathcal{R} does not correspond to any of the cases, i.e. there is no other symbolic move, according to the first inductive cases.

We write $R^s \sim_{\mathcal{R}} R^c$ iff *coher*($R^s, R^c, r, txout, sechash, \kappa$) for $\text{txout}, \text{sechash}$, and κ .

The following lemma is the active contracts analogous of Lemma 5. Both results are proved by induction on the definition of *coher*.

Lemma 6. Let *coher*($R^s, R^c, r, txout, sechash, \kappa$). For each contract $(C, v)_x$ occurring in Γ_{R^c} , there exists a corresponding transaction output (T, o) in \mathcal{B}_{R^c} with value v . Further, T is generated by the invoking the compiler as $\mathcal{B}_0(C, D_p, T', o', v, \tilde{v}, \tilde{p}, t)$ for values of $D_p, T', o', \tilde{v}, \tilde{p}, t$, or as $\mathcal{B}_{\text{par}}(\tilde{C}, D_p, T', o', \tilde{v}, \tilde{p}, t)$ for values of $\tilde{C}, D_p, T', o', \tilde{v}, \tilde{p}, t$ such that $C = \tilde{C}_{\text{par}}$ and $v = \text{value parameters } txout, \text{sechash}, \kappa$.

```

data Tree {l u : Nat} : Set where
  Leaf  : {pf: l ≤ u} → Tree {l} {u}
  Node  : (x : Nat)
    → Tree {l} {x} → Tree {x} {u}
    → Tree {l} {u}
{-# COMPILER AGDA2HS Tree #-}

insert : {l u : Nat} (x : Nat)
  → Tree {l} {u}
  → {l ≤ x} → {x ≤ u}
  → Tree {l} {u}
insert x Leaf {l≤x} {x≤u} =
  Node x (Leaf {pf = l≤x}) (Leaf {pf = x≤u})
insert x (Node y l r) {l≤x} {x≤u} =
  case compare x y of λ where
    (LT {pf = x≤y}) → Node y (insert x l {l≤x} {x≤y}) r
    (EQ {pf = x=y}) → Node y l r
    (GT {pf = y≤x}) → Node y l (insert x r {y≤x} {x≤u})
{-# COMPILER AGDA2HS insert #-}

```

```

data Tree = Leaf
          | Node Natural Tree Tree

insert :: Natural -> Tree -> Tree
insert x Leaf = Node x Leaf Leaf
insert x (Node y l r)
  = case compare x y of
    LT -> Node y (insert x l) r
    EQ -> Node x l r
    GT -> Node y l (insert x r)

```

AGDA2HS: TYPECLASSES

```
record Show (a : Set) : Set where
  field show      : a → String
        showsPrec : Nat → a → ShowS
        showList  : List a → ShowS

record Show1 (a : Set) : Set where
  field showsPrec : Nat → a → ShowS
  show      : a → String
  show x = showsPrec 0 x ""
  showList : List a → ShowS
  showList = defaultShowList (showsPrec 0)

record Show2 (a : Set) : Set where
  field show      : a → String
        showsPrec : Nat → a → ShowS
  showsPrec _ x s = show x ++ s
  showList  : List a → ShowS
  showList = defaultShowList (showsPrec 0)

open Show {...}
{-# COMPILE AGDA2HS Show class Show1 Show2 #-}

instance
  ShowMaybe : {{Show a}} → Show (Maybe a)
  ShowMaybe {a = a} = record {Show1 s1}
    where
      s1 : Show1 (Maybe a)
      s1 . Show1.showsPrec n = λ where
        Nothing → showString "nothing"
        (Just x) → showParen true
          (showString "just " ∘ showsPrec 10 x)
  {-# COMPILE AGDA2HS ShowMaybe #-}
```

```
class Show a where
  show :: a -> String
  showsPrec :: Natural -> a -> ShowS
  showList :: [a] -> ShowS
  {-# MINIMAL showsPrec | show #-}
  show x = showsPrec 0 x ""
  showList = defaultShowList (showsPrec 0)
  showsPrec _ x s = show x ++ s

instance (Show a) => Show (Maybe a) where
  showsPrec n = \case
    Nothing -> showString "nothing"
    (Just x) -> showParen True
      (showString "just " . showsPrec 10 x)
```

```
record Show (a : Set) : Set where
  field show      : a → String
        showsPrec : Nat → a → ShowS
        showList  : List a → ShowS
record Show1 (a : Set) : Set where
  field showsPrec : Nat → a → ShowS
  show : a → String
  show x = showsPrec 0 x ""
```

CPP @ POPL'22

Reasonable Agda is Correct Haskell: Intrinsic Program Verification using AGDA2Hs

J.Cockx, O.Melkonian, J.Chapman, U.Norell + TU Delft students

```
showList = defaultShowList (showsPrec 0)
open Show {{...}}
{-# COMPILE AGDA2HS Show class Show1 Show2 #-}
instance
  ShowMaybe : {{Show a}} → Show (Maybe a)
  ShowMaybe {a = A} = record {Show1 s1}
    where
      s1 : Show1 (Maybe a)
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        Nothing → showString "nothing"
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          (showString "just " ∘ showsPrec 10 x)
{-# COMPILE AGDA2HS ShowMaybe #-}
```

```
showsPrec _ x S = show x ++ S
```

```
instance (Show a) => Show (Maybe a) where
  showsPrec n = \case
    Nothing -> showString "nothing"
    (Just x) -> showParen True
      (showString "just " . showsPrec 10 x)
```

setup-agda: CI INFRASTRUCTURE FOR AGDA

```
name: CI
on: push: {branches: master}
jobs:
  build-deploy:
    runs-on: ubuntu-latest
    steps:
      - uses: actions/checkout@v2.3.1
      - uses: omelkonian/setup-agda@v0.1
        with:
          agda-version: 2.6.1.3
          stdlib-version: 1.6
          libraries: |
            omelkonian/formal-prelude#92ef
            omelkonian/formal-bitcoin#0341
            omelkonian/formal-bitml#4382
    main: Main
    token: ${ secrets.GITHUB_TOKEN }
```

MODULAR AUTOMATIC SOLVERS FOR AGDA PROOFS

- define strategies for automatic proof search
- should be able to define solvers incrementally for specific types
- primarily achieved with Agda's **reflection**

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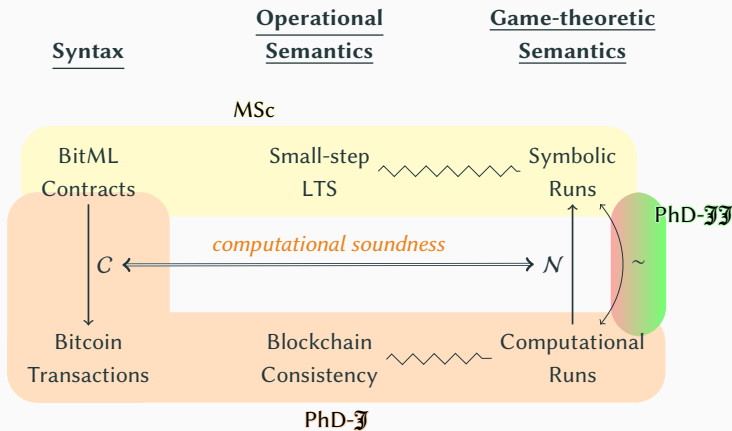
- define strategies for automatic proof search
- should be able to define solvers incrementally for specific types
- primarily achieved with Agda's **reflection**

```
open import Prelude.Init using (List)
open import Prelude.Semigroup
open import Prelude.Membership
open import Prelude.Solvers
```

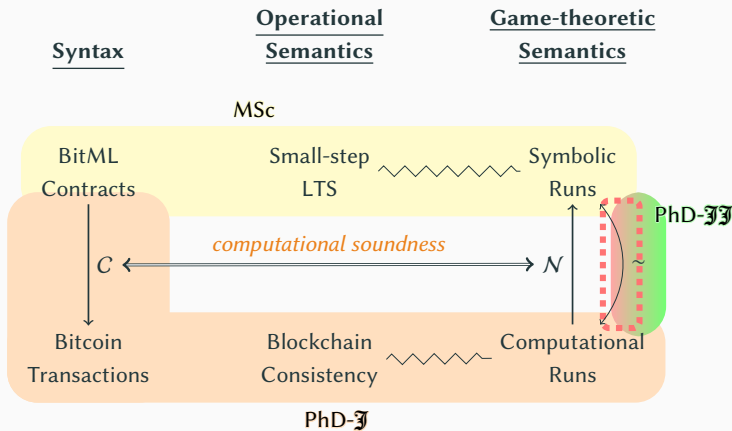
```
_ : ∀ {A : Set} {y : A} {xs ys zs : List A}
  → y ∈ ys → y ∈ xs ◇ ys ◇ zs
_ = solve
```

YEAR III: *WHERE I'M GOING...*

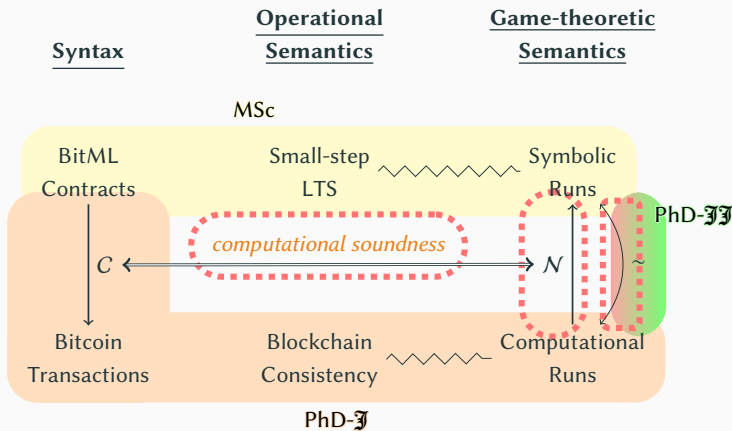
1. Finish up coherence
2. Symbolic \rightarrow computational runs
3. Prove **computational soundness**: compiler preserves coherence
4. Write a paper about it!



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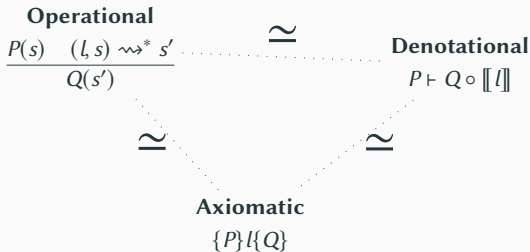


1. Finish up coherence
2. Symbolic \rightarrow computational runs
3. Prove **computational soundness**: compiler preserves coherence
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SEPARATION LOGIC FOR BLOCKCHAIN [2021 - MID 2022]

1. Obvious next step: extend results to UTxO ledgers
2. Write a paper about it!



THESIS WRITE-UP [MID 2022 - LATE 2022]



- Hopefully by then, enough material to fill a thesis
- Ideally, two more papers on BitML and UTxO at prestigious venues
- Realistically, UTxO exploration alongside thesis writing

- More ambitious directions (alas, no time)
 - **AGDA2HS**: extract executable programs from my mechanisations
 - **BitML**: improve/re-formulate (e.g. BitML \rightarrow EUTxO)
 - **EUTxO**: further extensions / state machine verification

DISCUSSION

- More ambitious directions (alas, no time)
 - **AGDA2HS**: extract executable programs from my mechanisations
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- Internship?
 - some interesting positions/projects so far
 - 🤔 is it worth it though?

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- More ambitious directions (alas, no time)
 - **AGDA2HS**: extract executable programs from my mechanisations
 - **BitML**: improve/re-formulate (e.g. BitML \rightarrow EUTxO)
 - **EUTxO**: further extensions / state machine verification
- Internship?
 - some interesting positions/projects so far
 is it worth it though?
- Extension?
 - a few more months would lead to more results
 is it worth it though?

DISCUSSION