

Globalization and Prosperity Lab

## Computational Model: Data

July 30, 2021

## Agenda

- Data, Principles and Definitions
- Missing Production
- Overlay of Final Uses
- Mutual Imputation of Missing Flows
- Disaggregating Use Activities to Use Industries

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## Data

- WIOT for trade, input-output flows and uses in 2014
- ITPD-E for proportions of bilateral trade by industry  
Mean of years 2013-15
- WIOT flow data  $W_{sdab}$   
with source country  $s$ , destination  $d$ , supply activity  $a(i)$ , use  $b(j)$
- ITPD-E trade and self-trade data  $X_{sdi}$   
with source country  $s$ , destination country  $d$ , supply industry  $i$

## Bilateral Trade Flows by Supply Industry and Use

- $X_{sdij}$ : Trade or self-trade flow from source country  $s$  and supply industry  $i$  to destination country  $d$  (including  $d = s$ ) and use  $j$
- General principles of data handling:
  1. use WIOD for  $b$  uses within  $sdi$  and totals to preserve value added: 38 aggregate activities  $b(j)$ , 5 final uses  $b$
  2. use ITPD for proportional imputations of  $sdi$ : 170 industries  $i$
  3. use flows reported in either data set to complete the other
  4. take production function of industries to be identical within activity

## Definitions

- Countries:** 43 and ROW (rest of world).  
 Mutual consistency between ITPD and WIOD
- Industries:** 170 ITPD-based industries.  
 Aggregation for WIOD consistency, plus non-traded sector.  
 Called GPL industries (Globalization and Prosperity Lab)
- Activities:** 38 aggregate WIOD activities (including HH and international organization activities), plus 5 final uses (total 43): final consumption expenditure  $C_{sdi}^{HH}$  by households and non-profit organisations serving households (NPISH)  $C_{sdi}^{NPISH}$ , final expenditure by government  $G_{sdi}$ , gross fixed capital formation  $I_{sdi}^K$ , and changes in inventories and valuables  $I_{sdi}^{IV}$ .

## GPL Country Groups

- Country group  $\mathbb{G}_c$  based on World Development Indicators (WDI): High, Upper middle, Lower middle, Low income
- Regroup WDI countries for consistent per-capita GDP ranking 2014  
Top Upper middle income country Equatorial Guinea at \$19.4k GDP p.c.; reassign High-income countries with less GDP p.c. to Upper middle; similarly for Lower middle (top Iran with \$5.6k) and Low income (top Yemen with \$1.7k GDP)
- WIOD sample countries (43): pop weighted mean GDP p.c. \$14.9k  
ROW (173 WDI countries): pop wgt'd mean \$4.3k (**Lower middle**)  
WIOD: 28 High, 12 Upper middle, 2 Lower middle, 1 Low income  
India single low-income country in WIOD, grouped with lower middle income  
ROW: 30 High, 43 Upper middle, **49 Lower middle**, 43 Low income

## Aggregate Variables

- **Production** (output, not value added):  $Y_{si} = \sum_d \sum_j X_{sdij} = X_{s \cdot i}$ .  
self trade included ( $s = d$  in sum)
- **Market size** (expenditure):  $X_{di} = \sum_s \sum_j X_{sdij} = X_{\cdot di}$ .  
self trade included ( $s = d$  in sum)
- **Exports**  $EX_{si} = \sum_{d \neq s} \sum_j X_{sdij}$   
**Imports**  $IM_{di} = \sum_{s \neq d} \sum_j X_{sdij}$
- **Trade balance** country  $c$ :  $TB_{ci} = EX_{ci} - IM_{ci}$



## Value Added (JUNYUAN TO CHECK)

- **Production:**  $Y_{ci} = \sum_d \sum_j X_{cdij} = X_{c \cdot i}$   
self trade included ( $c = d$  in sum)
- **Intermediate inputs:**  $M_{dj} = \sum_s \sum_i X_{sdij} = X_{\cdot d \cdot j}$   
self trade included ( $s = d$  in sum)  
Restated:  $M_{ci} = \sum_s \sum_k X_{scki} = X_{\cdot c \cdot i}$
- **Value added:**  $V_{ci} = Y_{ci} - M_{ci}$   
Underlying  $X_{sdij}$  combines ITPD and WIOD information  
after disaggregation (extending Lindner, Legault & Guan 2012)  
Problem cases: XXX

## Capital and Labor Shares (JUNYUAN TO COMPLETE))

- SEA: Results from comparison value-added shares WIOD and SEA
- Winsorize the extremely low VA shares
- ROW as mean of sector-specific world average for lower middle income countries
- XXX

## Current Account Balance (FOR LATER)

- **Current Account balance** country  $c$ :  $CA_c = TB_c + r_c \cdot B_c$   
(cross-border foreign net wealth position  $B_c$ , no cross-border labor movements)
- To be calibrated. Proposal:
  - Use CPIS (Coordinated Portfolio Investment Survey) 2014 to find  $B_c$ , use WDI 2014 to find  $r_c B_c$ , and compute  $CA_c = TB_c + r_c B_c$  using WDI and  $r_c = (CA_c - TB_c) / B_c$  using WDI and CPIS
  - Problem to be addressed: United States  $B_{US} < 0$  but  $r_{US} B_{US} > 0$  because interest rate on gross foreign credit exceeds interest rate on gross foreign debt

## Activity Aggregation

- Aggregate activities  $a$  from WIOD and GPL industries  $i$  defined so that strict nesting  $a(i)$
- Set of industries within activity  $a$ :  $i \in \mathbb{I}_a = \{i : a(i)\}$ ,  $j \in \mathbb{J}_b = \mathbb{I}_a$ .  
Universe of industries:  $\bigcup_a \mathbb{I}_a$
- **Production** (self trade included):  $Y_{sa} = \sum_{i \in \mathbb{I}_a} X_{s \cdot i}$ .  
**Market size** (self trade included):  $X_{da} = \sum_{i \in \mathbb{I}_a} X_{\cdot di}$ .
- **Intermediate inputs**:  $M_{db} = \sum_{j \in \mathbb{J}_b} X_{\cdot d \cdot j}$   
**Value added**:  $V_{sa} = Y_{sa} - M_{sa}$

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## Data With Non-zero Production After Mutual Imputations

- Combined ITPD 2013-15 and WIOD 2014 data  $X_{sdi}$   
10,848,350 observations (corresponding to 269,277 at  $X_{sdi}$  level)
- In ITPD 2013-15 (mean): 256,985  $X_{sdi}$  observations (some self trade)  
Appended non-zero production: 133  $X_{ssi}$  observations  
Resulting total: 257,118 observations
- Unmatched ITPD 2013-15  $X_{sdi}$  in WIOD 2014 after imputations: 226  $X_{sdi}$  observations  
(less than 1/1,000 of 1 percent of total trade)
- Imputation: Append 9,115  $X_{sdi}$  observations, resulting: 269,277  $X_{sdi}$

## Disaggregating Use Activities to Use Industries (JUNYUAN)

- Wolsky (1984) and Lindner, Legault & Guan (2012):  
Disaggregate  $X_{sdab}$  into  $X_{sdi j}$  under multiplicity of possibilities  

$$\left( X_{sdab} = \gamma_{sdab} \cdot \sum_{i \in \mathbb{I}_a} X_{sdi}^{ITPD} \right)$$
- We know:  $X_{sdib}$   
Single consistent disaggregation of  $b(j)$  into  $j$  given observed  $i$   

$$\left( X_{sdib} = \gamma_{sdab} \cdot X_{sdi}^{ITPD} \right)$$
- Rationale, Main assumptions, Plausibility of assumptions

## *APPENDIX*

## Reverse Imputations as Alternative to Main Approach

- $X_{sdij}$ : Trade or self-trade flow from source country  $s$  and supply industry  $i$  to destination country  $d$  (including  $d = s$ ) and use  $j$
- Alternative principles of data handling:
  1. use ITPD for  $sdi$  totals: 170 industries  $i$
  2. use WIOD for proportional imputations, especially of  $j$  within  $sdi$ : 38 aggregate activities  $b(j)$ , 5 final uses  $b$
  3. use flows reported in either data set to complete the other
- **Problem:** Pervasive cases of negative value added  
*Likely cause:* ITPD flows out of proportion for input-output relations

## Missing Production: All Industries Produce in All Countries

- ITPD data incomplete for production  $Y_{si} = \sum_d \sum_j X_{sdij} = X_{s \cdot i}$ .  
(WIOD suggests 1 no-production case of 133 only: media reproduction in Russia)
  - 7,480 square observations expected: 44 source countries (including ROW)  $\times$  170 supply industries
  - 44 missing: nontraded sector missing from ITPD for 44 countries
  - 20 missing: 5 WIOD aggregate activities missing for some countries (e.g. rental services in 11 countries, publishing in 3)
  - 69 missing: GPL industries within WIOD aggregates missing (e.g. rice in Taiwan, live cattle in Japan, prepared vegetables in Canada)

## Imputation of Missing Production *within* Activity Level

- In 69 cases of missing production, some ITPD industries  $i$  within WIOD activity  $a$  for a source country  $s$  non-missing but others missing

- From ITPD, define production share of industry by activity:

$$\beta_{si|a}^{ITPD, \mathbb{G}} = \frac{Y_{\cdot i}^{ITPD, \mathbb{G}}}{\sum_{i \in \mathbb{I}_a} Y_{\cdot i}^{ITPD, \mathbb{G}}}, \quad \text{where } Y_{\cdot i}^{ITPD, \mathbb{G}} = \sum_{s \in \mathbb{G}_s} Y_{si}$$

for three groups  $\mathbb{G}_s$  by income p.c. 2014 (WDI)

- Imputation:  $Y_{si}^{ITPD} = \beta_{si|a}^{ITPD, \mathbb{G}} Y_{sa}^{ITPD} = \beta_{si|a}^{ITPD, \mathbb{G}} \beta_{sa}^{WIOD} Y_{s\cdot}^{ITPD}$ ,  
where  $Y_{sa}^{ITPD} = \beta_{sa}^{WIOD} Y_{s\cdot}^{ITPD}$  given below.

## Imputation of Missing Production *at* Activity Level

- From WIOD, supply activity share in total (38 activities) by country:

$$\beta_{sa}^{WIOD} = Y_{sa}^{WIOD} / Y_{s.}^{WIOD}.$$

- Intended imputation:  $Y_{sa}^{ITPD} = \beta_{sa}^{WIOD} Y_{s.}^{ITPD}$ , but  $Y_{s.}^{ITPD}$  unobserved

- Known:  $\tilde{Y}_{s.}^{ITPD} = \left( 1 - \sum_{i \in \mathbb{M}_s} \beta_{si|a}^{ITPD, \mathbb{G}} \beta_{sa}^{WIOD} \right) Y_{s.}^{ITPD}$

where  $\mathbb{M}_s$  is set of industries missing from ITPD by country  $s$

- Complete **imputation**:  $Y_{si}^{ITPD} = \frac{\beta_{si|a}^{ITPD, \mathbb{G}} \beta_{sa}^{WIOD}}{1 - \sum_{i \in \mathbb{M}_s} \beta_{si|a}^{ITPD, \mathbb{G}} \beta_{sa}^{WIOD}} \tilde{Y}_{s.}^{ITPD}$

## Manual Flow Corrections: Reset zero to \$100k

- In ITPD data (2013-2015 mean), 25,172 zero trade flows. Zero kept
- Of the 133 imputations into ITPD, WIOD suggests one zero trade flow: Russian self-trade in reproduced media, set to \$100k  
133 *i* industries imputed into ITPD, corresponding to 72 *a* activities
- Some imputations may be implausibly large under above method, so manually reduce to \$100k: Soybeans in Cyprus and Norway; Tobacco leaves and cigarettes in Finland; Cocoa and cocoa products in Cyprus, Ireland, Latvia, Malta and Slovakia; Cotton in Malta; Live swine in Turkey.



## Final Uses in WIOD 2014

- In WIOD 2014, there are 73,568  $W_{sda}$  flow observations (with non-zero or zero values)
  - 48 w/ negative investment (gross fixed capital formation  $I_{sda}^K < 0$ )
  - 1,516 w/ negative inventory and valuables change ( $I_{sda}^{IV} < 0$ )
  - no other use or final use categories exhibit negative values
- To prevent negative changes from inducing implausible flows, we use time aggregation for steady-state final-use shares in total

## Time Aggregation of Final Uses in WIOD 2000-2014

- WIOD 2000-14 to measure steady-state share of final uses in total  $W_{sdabt}$ : 43 countries plus ROW  $s, d$ ; 38 activities  $a(i), b(j)$ ;  $t = 2000, \dots, 2014$
- In steady state, gross investment or inventory change non-negative
  - But time and use aggregation  $\sum_t \sum_b W_{sdabt} = W_{sda..} < 0$  in 14 cases (with ROW destination) and  $\sum_t \sum_{b \in \mathbb{F}} W_{sdabt} < 0$  in 110 cases (where  $\mathbb{F}$  is set of final uses): impacts of negative inventory changes (and five cases of negative investment), mostly for ROW destination, publishing and basic metals activities
- For final use shares, we set final use share **to zero when otherwise negative** (positive total) and **to unity when otherwise in excess of unity** (negative total).
  - 292 zero final use shares (from 190), 73 unitary final use shares (from 65)

## Use Activity Shares from WIOD in ITPD

- Combine WIOD activities with ITPD flows by industry  $i$  (for  $a(i)$ ).  
38 supply activities  $a(i)$ , 38+5 use activities plus final uses  $b(j)$

- Final use share:  $\bar{\gamma}_{sda}^{finl} = \frac{\sum_t \sum_{b \in \mathbb{F}} W_{sdabt}}{\sum_t \sum_b W_{sdabt}}$ .

Time aggregation of WIOD 2000-14, where  $\mathbb{F}$  is set of final uses

- For 38 use activities  $b \notin \mathbb{F}$ :  $\gamma_{sdab} = \left(1 - \bar{\gamma}_{sda}^{finl}\right) \frac{W_{sdab,2014}}{\sum_{b \notin \mathbb{F}} W_{sdab,2014}}$

$$\text{For 5 final uses } b \in \mathbb{F}: \gamma_{sdab} = \bar{\gamma}_{sda}^{finl} \frac{W_{sdab,2014}}{\sum_{b \in \mathbb{F}} W_{sdab,2014}}$$

Set  $W_{sdab,2014} = 0$  if  $< 1$  cent of \$1 (20,389 of 3,236,992 obs.)

Cap  $I_{sdi}^K, I_{sdi}^{IV}$  below so  $\sum_{b \in \mathbb{F}} W_{sdab,2014} \geq 0$  (815 of 3,236,992 obs.)

- Overlay uses on bilateral flows by industry:**  $X_{sdib} = \gamma_{sdab} \cdot X_{sdi}^{ITPD}$

## Excess and Unaccounted Trade Flows in WIOD 2014

- In 2014 (final sample year), WIOD reports 70,802 non-zero trade flows  $W_{sda}$  by source country  $s$ , destination  $d$ , supply activity  $a(i)$   
Set  $W_{sdab} = 0$  if  $< 1$  cent of \$1 (20,389 of 3,236,992 obs.), then aggregate uses  $b$ .
- In 2014, ITPD reports 55,939 non-zero flows  $X_{sda} = \sum_{i \in \mathbb{I}_a} X_{sdi}$  by source-country  $s$ , destination  $d$ , supply activity  $a(i)$  after imputing non-zero production for all activities and countries
- 16,325 excess trade flows  $W_{sda}$  in WIOD (not in ITPD)
- 1,462 *unaccounted* trade flows  $X_{sda}$  in ITPD (not in WIOD)

## Treating *Excess* WIOD-2014 Flows

- 16,325  $W_{sda}$  flows (617 self-trade  $s = d$ ) in WIOD but not in ITPD  
Excess self-trade (617) accounts for 40.1% of self trade and 35.0% of total in WIOD

- Proportion missing  $d$  to all non-missing:  $\zeta_{sdab}^{WIOD} = \frac{W_{sdab}}{\sum_{c \in \mathbb{G}_{ITPD}} W_{scab}}$   
 $\mathbb{G}_{ITPD}$ : non-missing destinations in WIOD *and* ITPD (cover all but 23 of 16,325)  
 Remove if  $I_{sdi}^{IV} < 0$  dominant so that no  $\sum_{c \in \mathbb{G}_{ITPD}} W_{scab} < 0$  (drop 15 of 16,325)

Share of industry  $i$  in activity  $a$  by country group:  $\gamma_{sdi|a}^{ITPD, \mathbb{G}}$  (next page)

- **Impute excess WIOD flows into ITPD** (16,287 successes)

$$X_{sdab} = \zeta_{sdab}^{WIOD} X_{s \cdot a}^{ITPD} \quad \text{and} \quad X_{sdib} = \gamma_{sdi|a}^{ITPD, \mathbb{G}} X_{sdab},$$

where  $X_{s \cdot a}^{ITPD} = \sum_{i \in \mathbb{I}_a} \sum_{c \in \mathbb{G}_{ITPD}} X_{sci}^{ITPD}$  is observed ITPD flow

## Treating *Excess* WIOD Flows: Industry Shares 2013-15

- For 7,172 of 16,287 observations industry shares directly observed.  
Share of industry  $i$  in activity  $a$  by country pairs and  $i \in \mathbb{I}_a$ :

$$\gamma_{sdi|a}^{ITPD, \mathbb{G}} = \frac{X_{sdi}^{ITPD, 13-15}}{\sum_{i \in \mathbb{I}_a} X_{sdi}^{ITPD, 13-15}}$$

- For 8,257 of 16,287 observations industry shares require imputation.  
Share of industry  $i$  in activity  $a$  by country **group** pairs and  $i \in \mathbb{I}_a$ :

$$\gamma_{sdi|a}^{ITPD, \mathbb{G}} = \frac{\sum_{s \in \mathbb{G}_s} \sum_{d \in \mathbb{G}_d} X_{sdi}^{ITPD, 13-15}}{\sum_{s \in \mathbb{G}_s} \sum_{d \in \mathbb{G}_d} \sum_{i \in \mathbb{I}_a} X_{sdi}^{ITPD, 13-15}}$$

- For 868 of 16,287 observations no pair flows, **reuse**  $\beta_{si|a}^{ITPD, \mathbb{G}}$  above

## Treating *Unaccounted* ITPD Trade Flows

- 1,462 *unaccounted*  $X_{sda}$  flows in ITPD (not in WIOD) concentrated: mostly printing, publishing, basic metals, and repair and installation

- To preserve WIOD I-O structure, assume flows only to 5 final uses.

For 5 final uses  $b \in \mathbb{F}$ :  $\gamma_{sdab}^{\mathbb{F}, \mathbb{G}} = \frac{\sum_{s \in \mathbb{G}_s} \sum_{d \in \mathbb{G}_d} \sum_{i \in \mathbb{I}_a} X_{sdib}}{\sum_{s \in \mathbb{G}_s} \sum_{d \in \mathbb{G}_d} \sum_{i \in \mathbb{I}_a} \sum_{b \in \mathbb{F}} X_{sdib}},$

for three groups  $\mathbb{G}_c$  by income p.c. 2014 (WDI) and  $X_{sdib}$  as imputed

Some industries show no cases of cross-group shipments into final uses

34 of 1,462 flows therefore not imputable

- **Impute**  $X_{sdab} = \gamma_{sdab}^{\mathbb{F}, \mathbb{G}} X_{sda}$  (1,428 successes)

## Data Quality Assessments (JUNYUAN)

- Value added comparisons between WIOD, SEA and COMPLETE DATA after imputation
- XXX