

# Simulation Studies of Liquid Slag Flow Patterns at High Temperatures

**BTP-2 (MTY401U4M)**

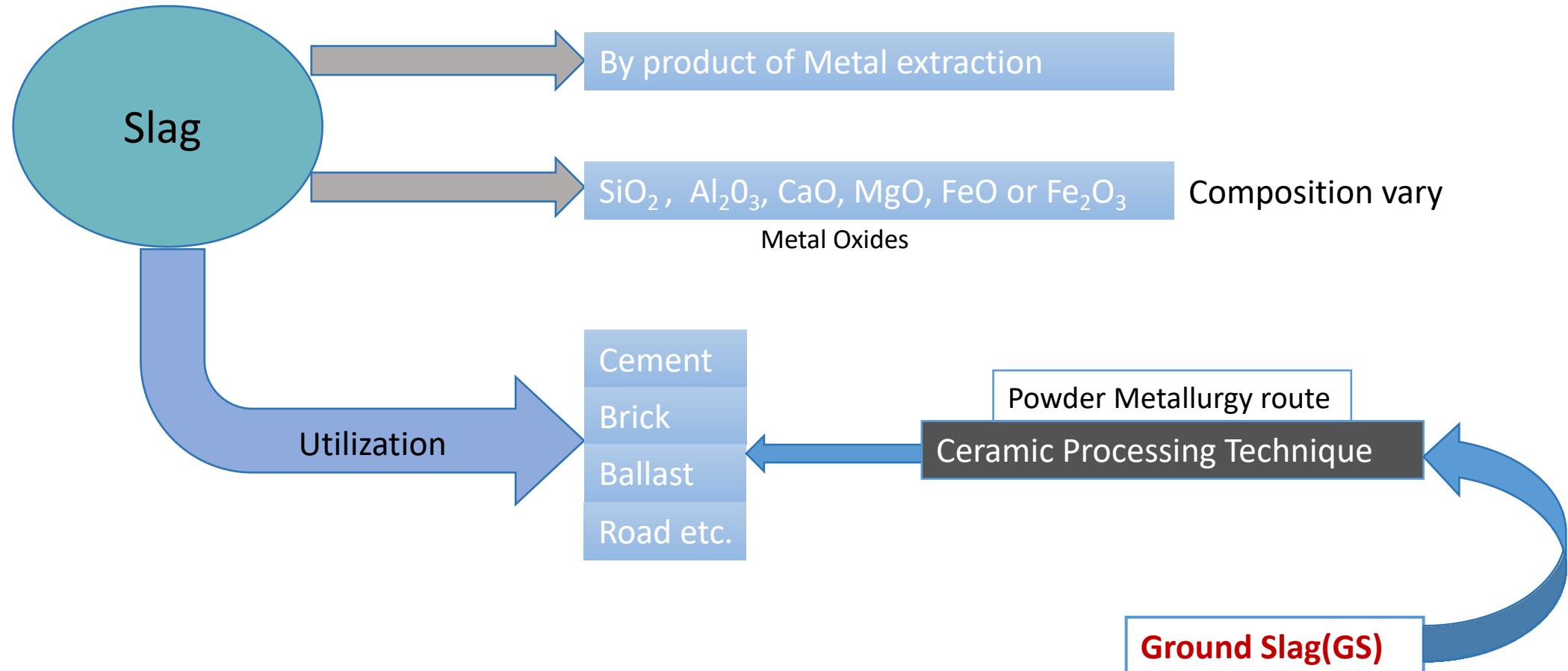
Under the Guidance of:

Dr. Srishilan C

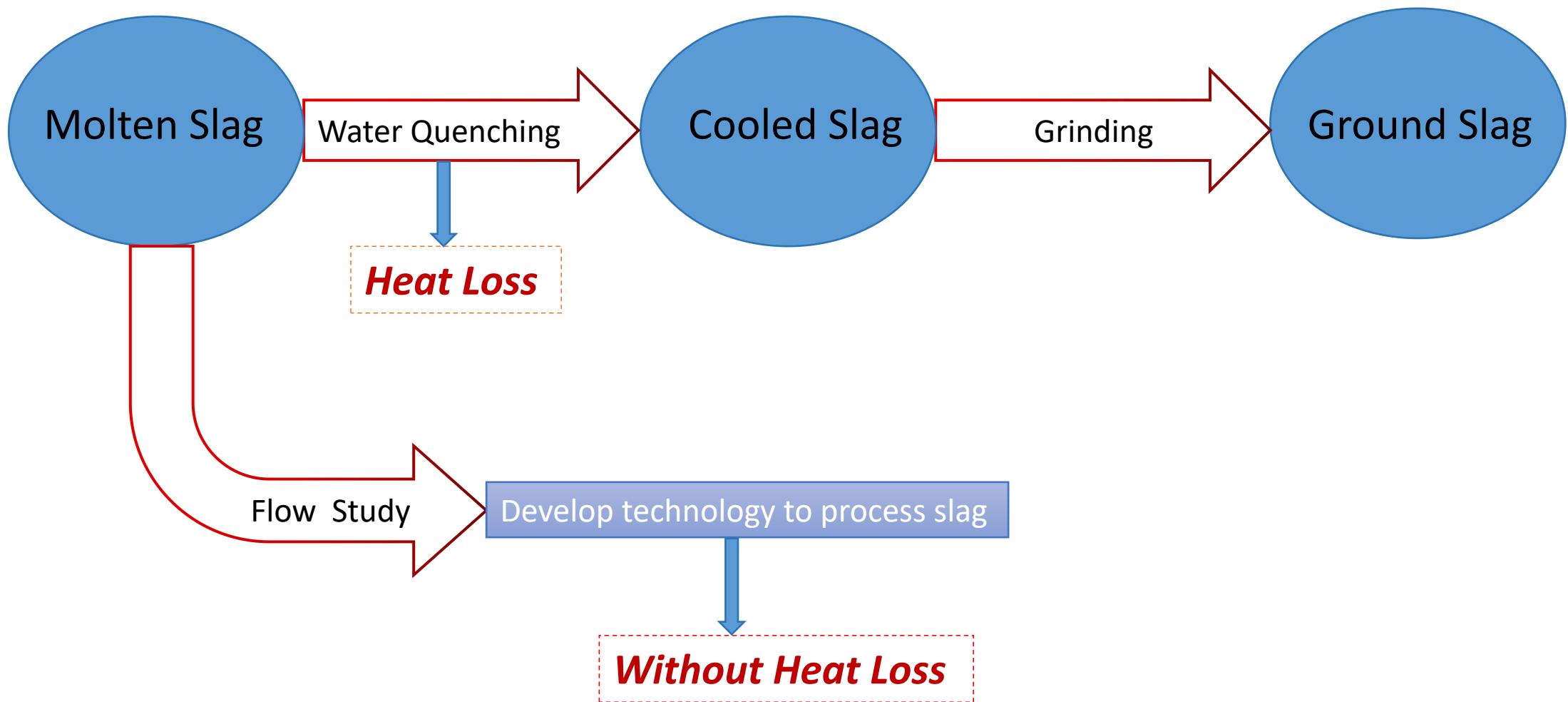
Presented by:

Om Prakash Gadhwal  
2021umt0183

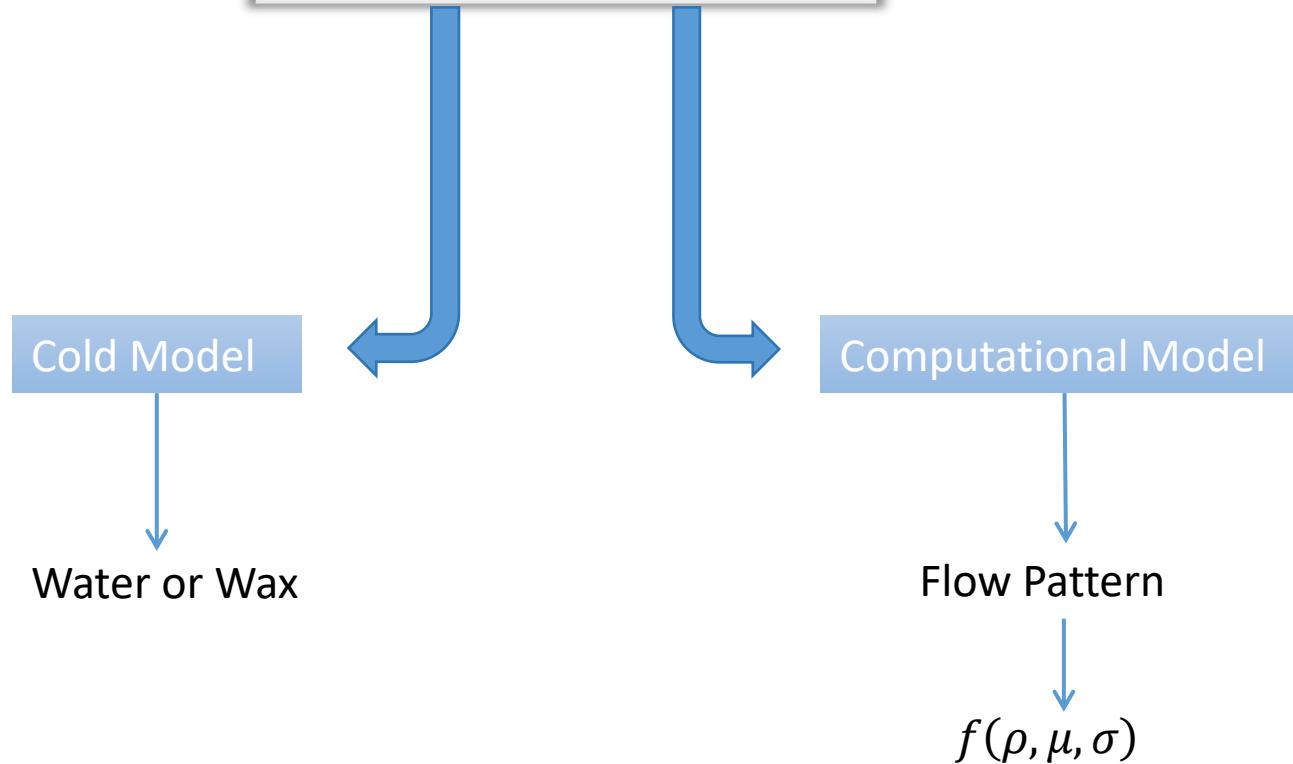
# Background



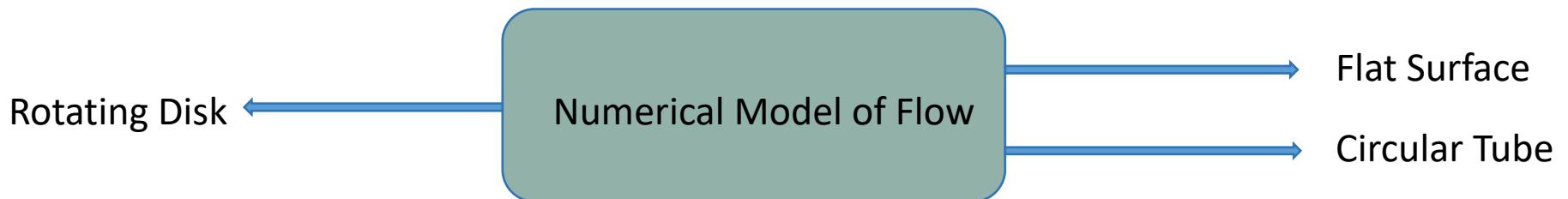
# Objective



# Study



where  $\rho$  = Density of slag( $\text{kg/m}^3$ )  
 $\mu$  = Viscosity of slag( $\text{Pa.s}$ )  
 $\sigma$  = Surface tension( $\text{N/m}$ )



## Literature Data

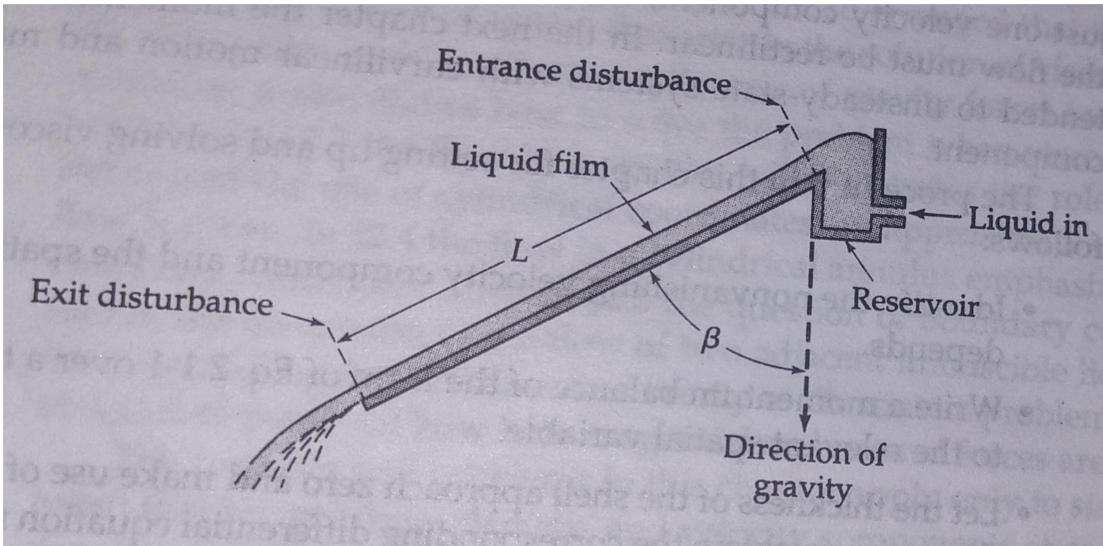
Research Paper	Model	Equation	Viscosity Range(Pa.s)
Jia, 2019, pp. 2-3	Arrhenius Temperature Model	$\eta = A \exp(E_\eta/RT)$	1.3 - 2.6
Hurst, 2000, pp. 1-2	Arrhenius Temperature Model	$\eta = e^A \cdot e^{\frac{B}{T}}$	0.7 - 32
Arman, 2017, pp. 2-7	Urbain composition model	$\eta = a \cdot T \cdot e^{\frac{b \cdot 10^3}{T}}$	0 - 15

# 1. Flat Surface

After Applying Shell Momentum Balance to Steady Flow

Second-order differential equation:

$$\frac{d^2 v_z}{dx^2} = -\frac{\rho g \cos \beta}{\mu}$$



Ref:- Transport Phenomena(R.Byron Bird, Warren E. Stewart, Edwin N. Lightfoot)

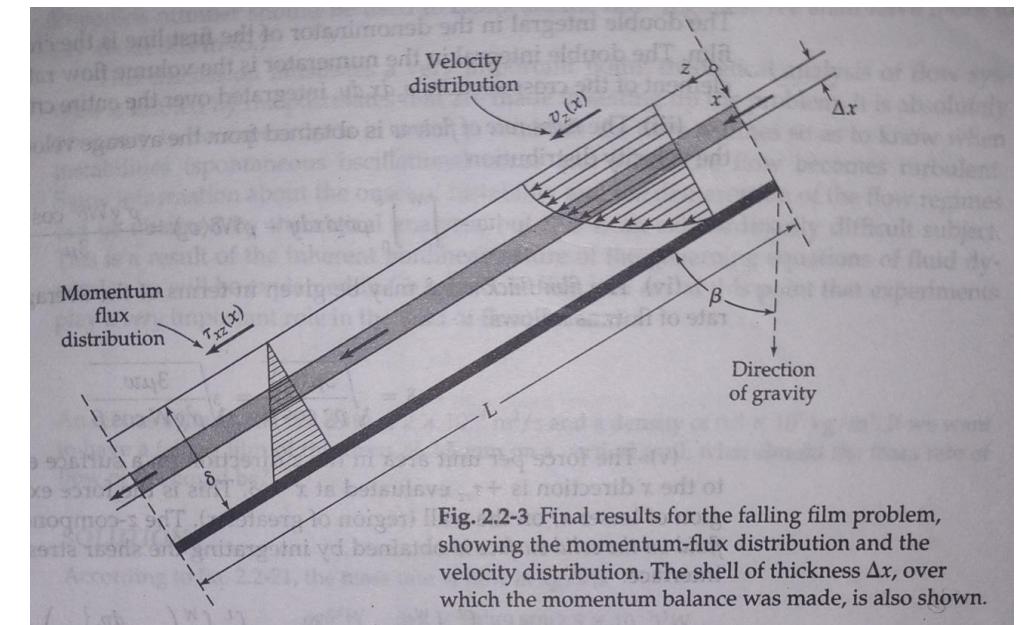
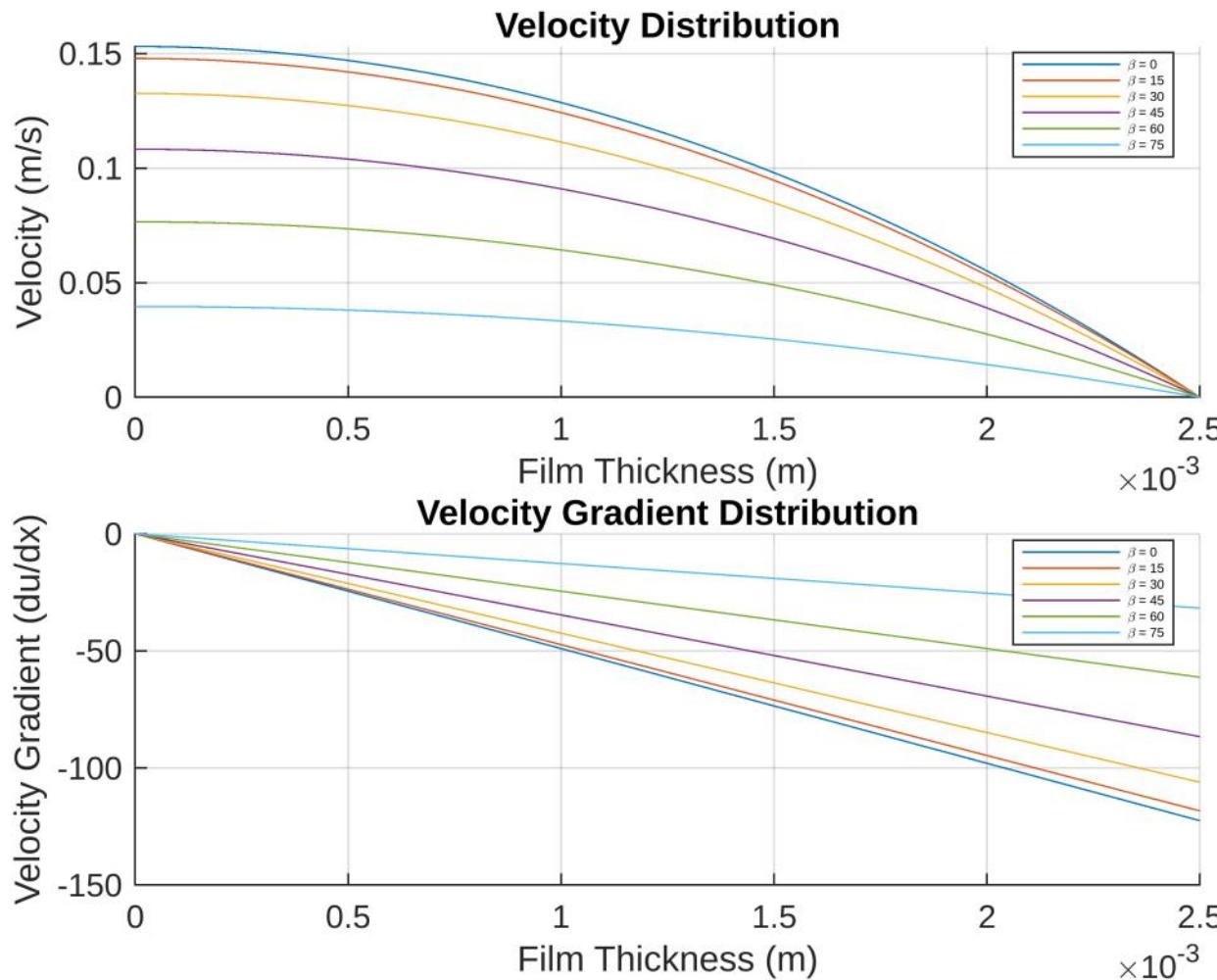
Boundary Conditions:

- $\frac{dv_z}{dx} = 0$  at  $x = 0$  (No shear at the fluid surface)
- $v_z = 0$  at  $x = \delta$  (No-slip condition at the solid surface)

Used Parameters:

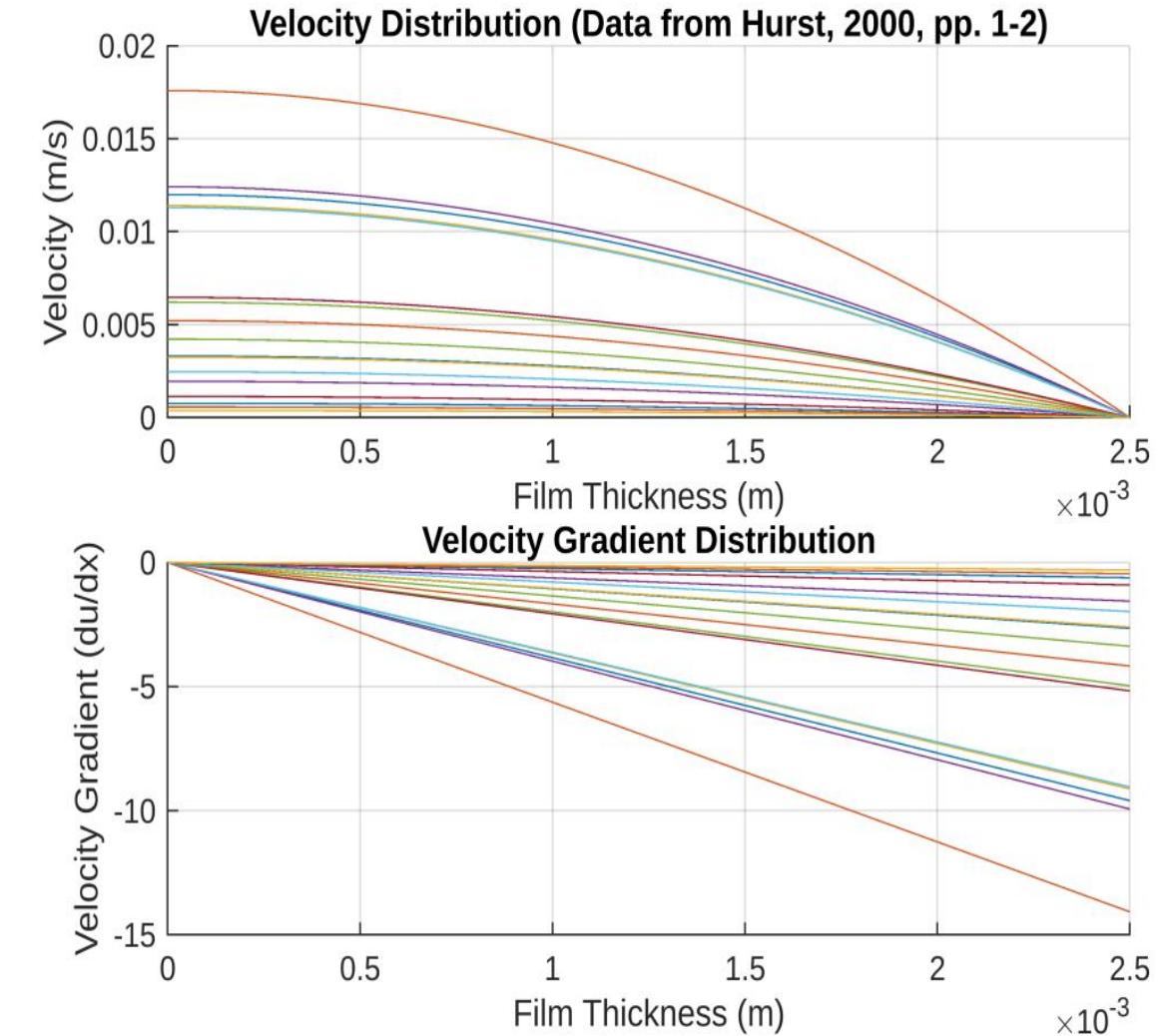
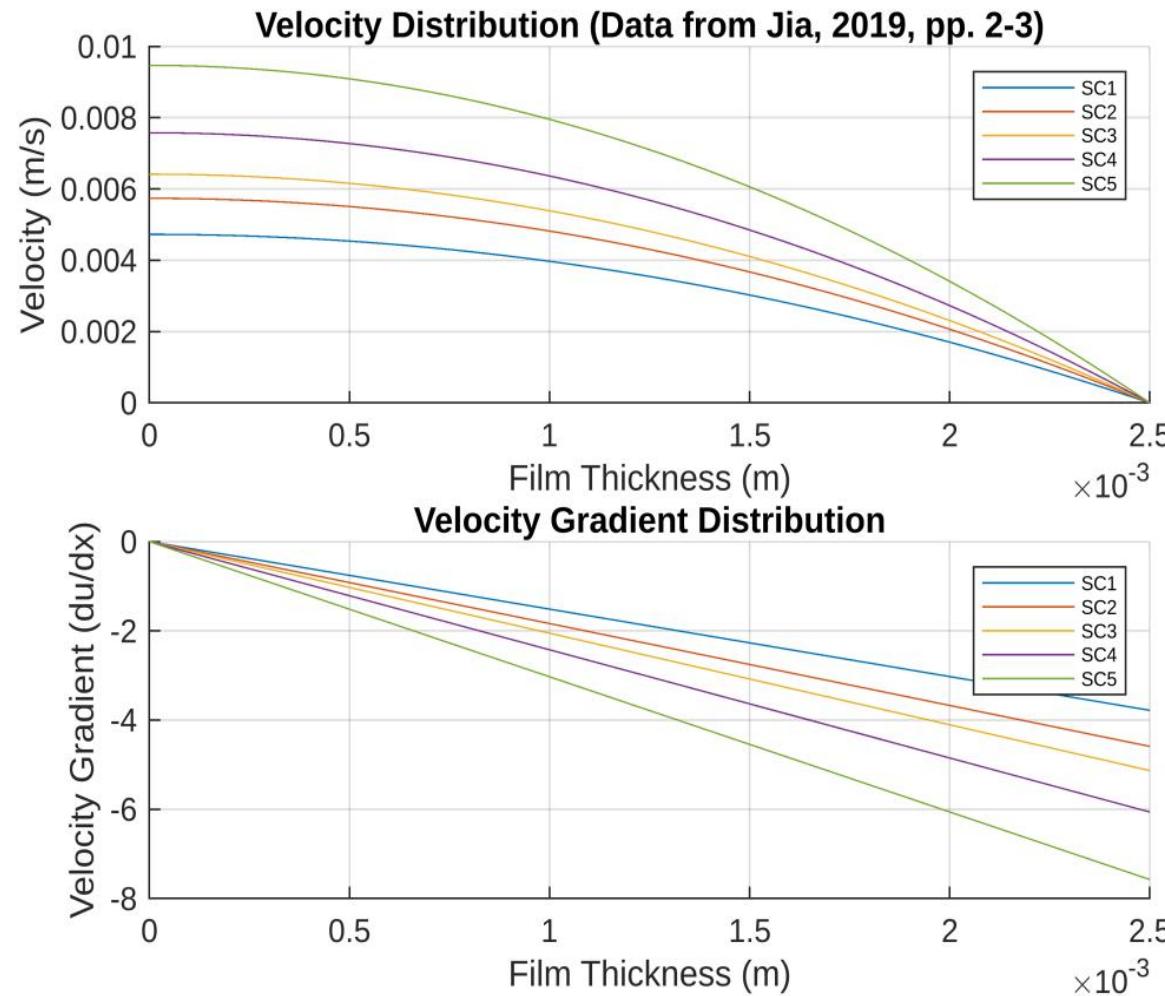
- Density ( $\rho$ ) =  $800 \text{ kg/m}^3$
- Gravitational Acceleration ( $g$ ) =  $9.8 \text{ m/s}^2$
- Inclination Angle ( $\beta$ ) =  $60^\circ$
- Film Thickness ( $\delta$ ) =  $2.5 \times 10^{-3} \text{ m}$
- Viscosity ( $\mu$ ) =  $0.16 \text{ Pa.s}$

# Velocity Distribution due to Variation in Geometry



Ref:- Transport Phenomena(R.Byron Bird, Warren E. Stewart, Edwin N. Lightfoot)

# Velocity Distribution due to Variation in Viscosity



## 2. Circular Tube

Second-order differential equation:

After Applying Shell Momentum Balance to Steady Flow

$$\frac{d^2v_z}{dr^2} = -\frac{(P_0 - P_L)}{L\mu} + \frac{1}{r} \frac{dv_z}{dr}$$

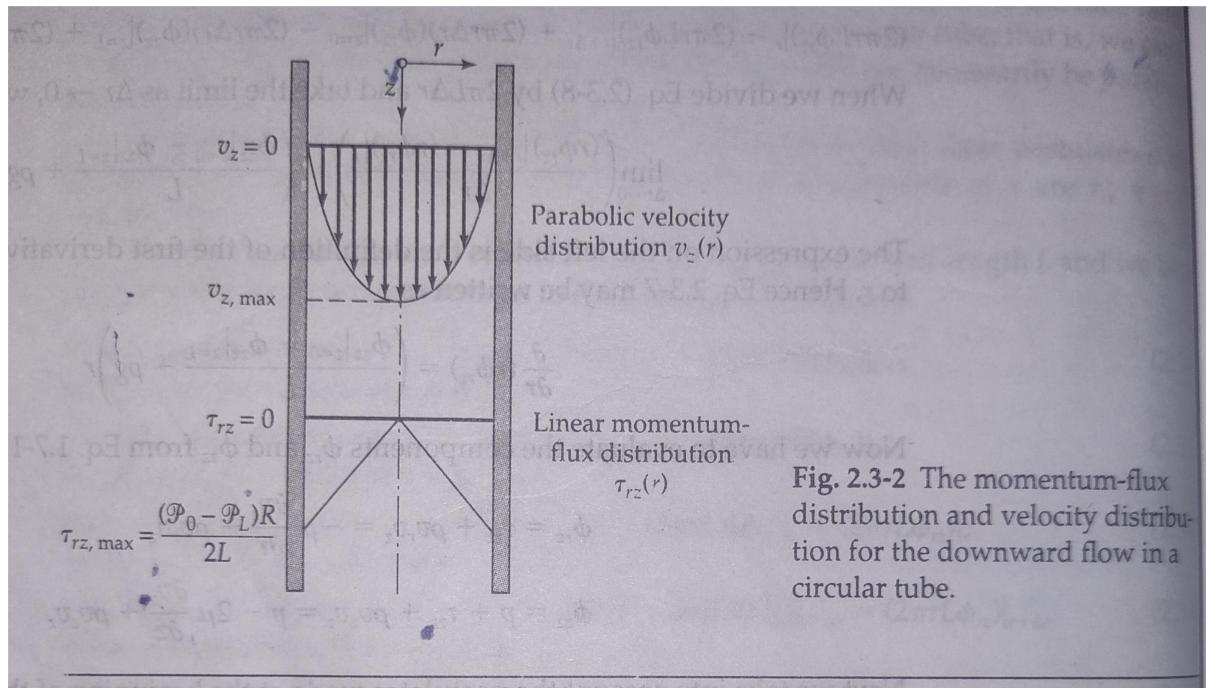


Fig. 2.3-2 The momentum-flux distribution and velocity distribution for the downward flow in a circular tube.

Ref:- Transport Phenomena(R.Byron Bird, Warren E. Stewart, Edwin N. Lightfoot)

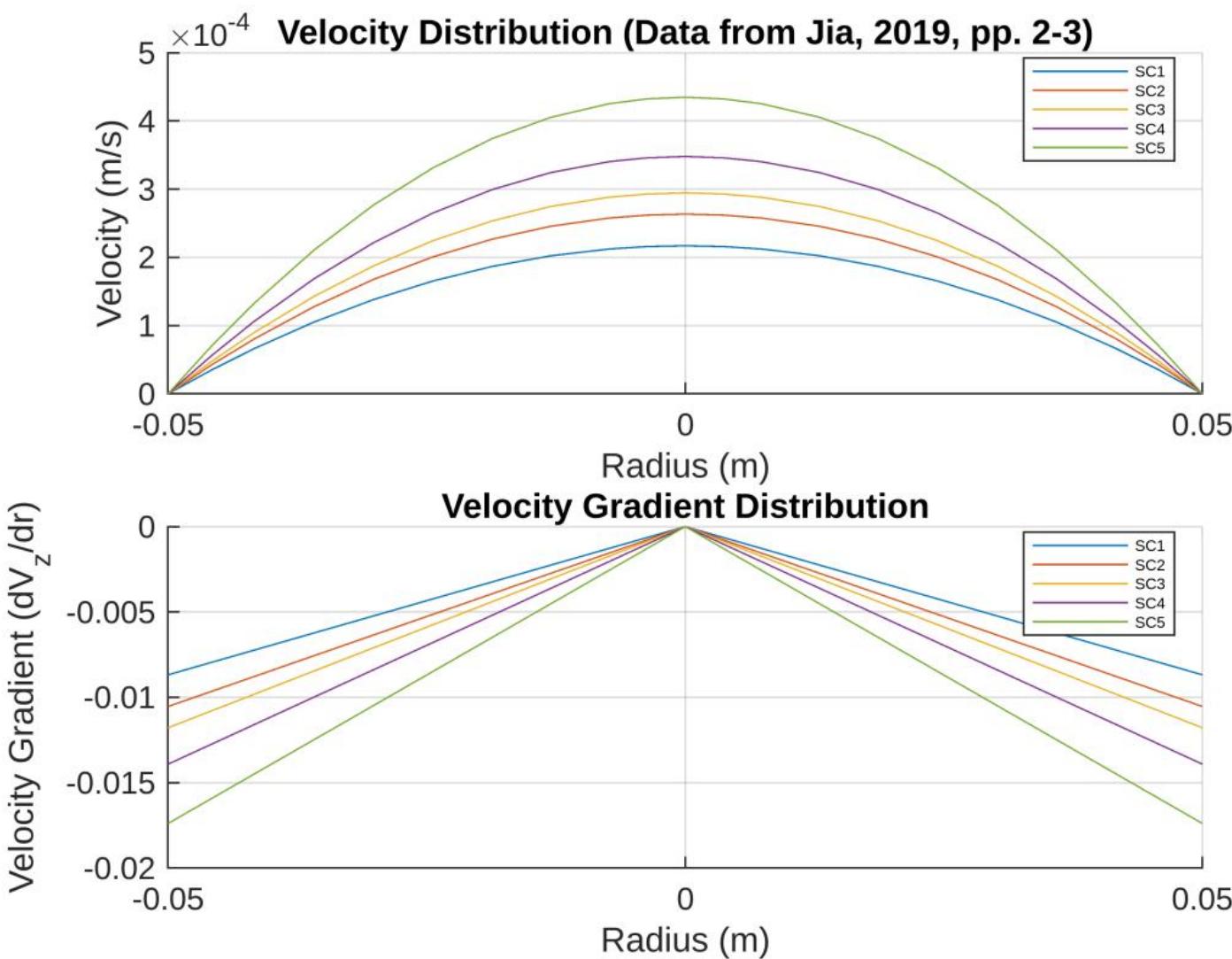
Boundary Conditions:

- $\frac{dv_z}{dr} = 0$  at  $r = 0$  (No shear at the tube center)
- $Vz = 0$  at  $r = R$  (No-slip condition at the wall)

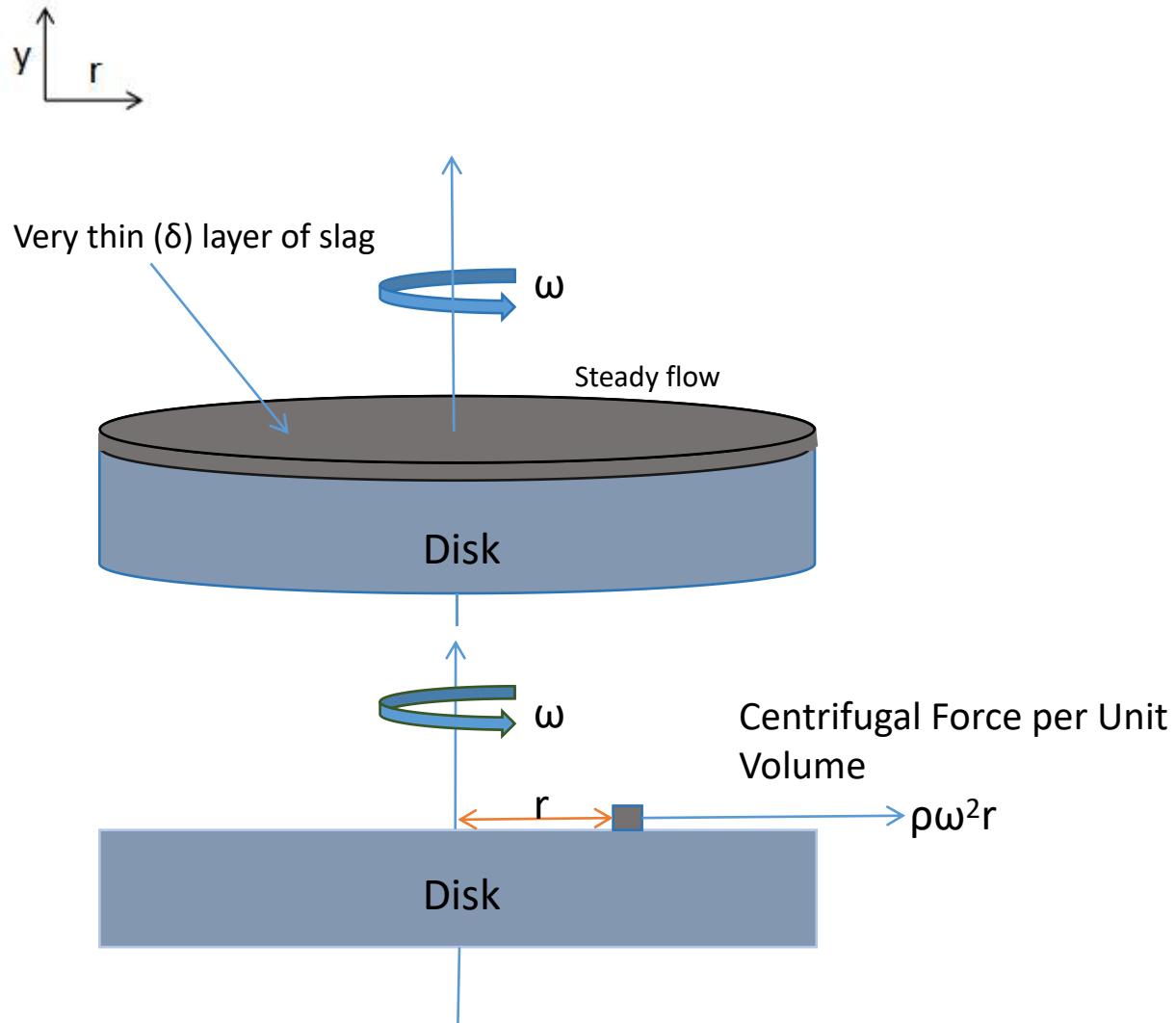
Used Parameters:

- Pressure at Start ( $P_0$ ) = 1.0 Pa
- Pressure at End ( $P_L$ ) = 0.1 Pa
- Tube Length ( $L$ ) = 1.0 m
- Density ( $\rho$ ) = 800 kg/m<sup>3</sup>
- Gravitational Acceleration ( $g$ ) = 9.8 m/s<sup>2</sup>
- Tube Radius ( $R$ ) = 0.05 m

## Velocity Distribution due to Variation in Viscosity



### 3. Rotating Disk



#### Navier–Stokes equations:

Cauchy momentum equation (*convective form*)

$$\rho \frac{D\mathbf{u}}{Dt} = -\nabla p + \nabla \cdot \boldsymbol{\tau} + \rho \mathbf{a}$$

$$\left[ \begin{array}{l} \boldsymbol{\tau} = -\mu \frac{du}{dy} \quad (\text{Newton's law of viscosity}) \\ \mathbf{a} = \omega^2 \mathbf{r} \end{array} \right]$$

Final Form of the Navier-Stokes Equation  
for a Rotating Disk :-

$$\frac{d^2 v_r}{dy^2} = - \frac{\rho \omega^2 r}{\mu}$$

# Velocity Distribution due to Radial Variation

**Second-order differential equation:**

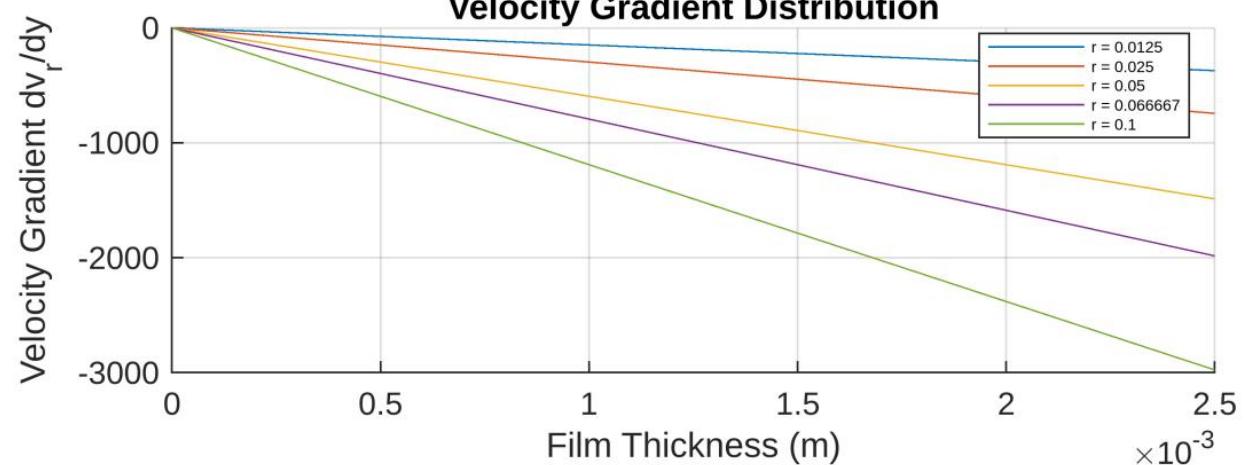
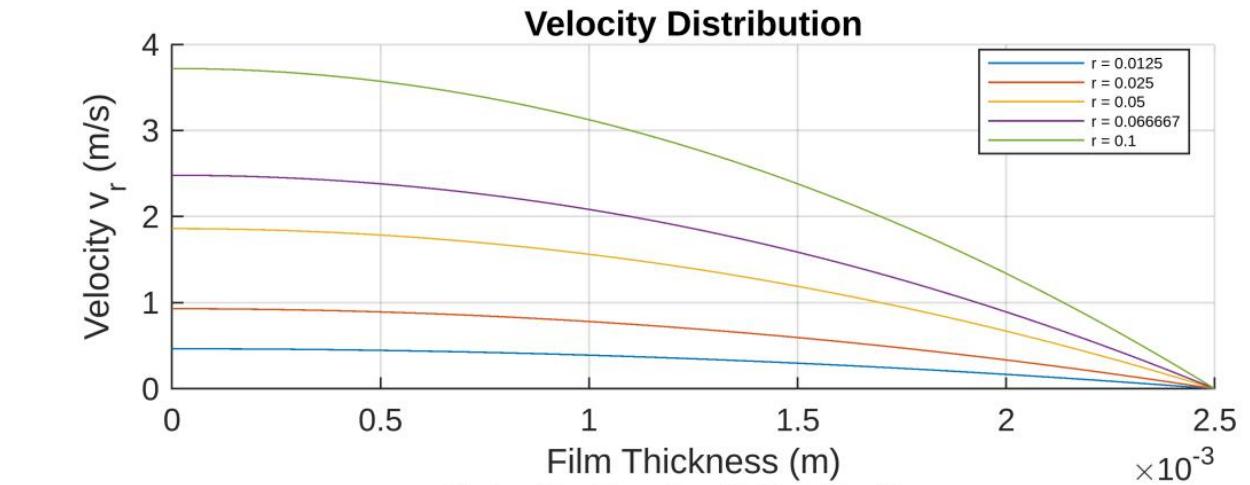
$$\frac{d^2v_r}{dy^2} = \frac{\rho\omega^2r}{\mu}$$

**Boundary Conditions:**

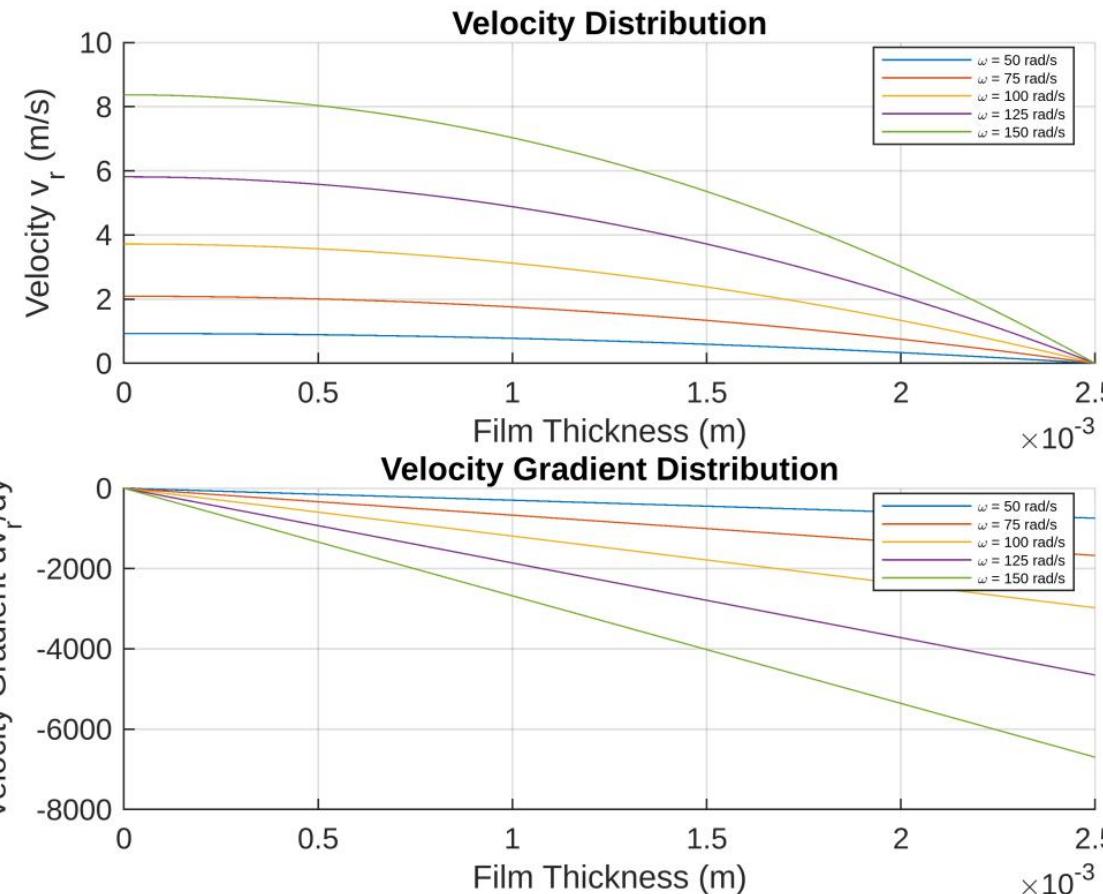
- $\frac{dv_r}{dy} = 0$  at  $y = 0$  (No shear at the fluid surface)
- $v_r = 0$  at  $y = \delta$  (No-slip condition at the disk surface)

**Used Parameters:**

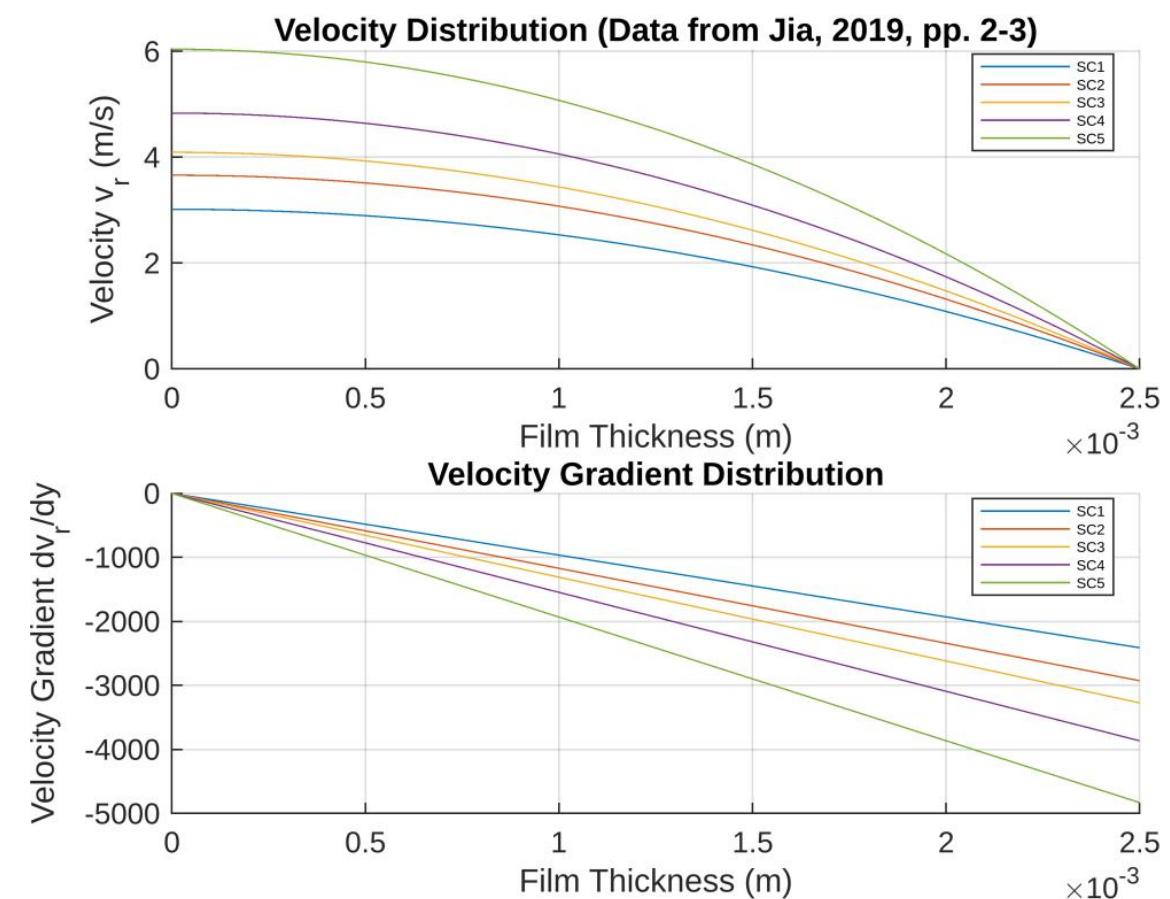
- Density ( $\rho$ ) =  $2.5 \times 10^3$  kg/m<sup>3</sup>
- Gravitational Acceleration ( $g$ ) = 9.8 m/s<sup>2</sup>
- Film Thickness ( $\delta$ ) =  $2.5 \times 10^{-3}$  m
- Viscosity ( $\mu$ ) = 2.1 Pa.s
- Rotational Speed ( $\omega$ ) = 100 rad/s
- Disk Radius ( $R$ ) = 0.1 m



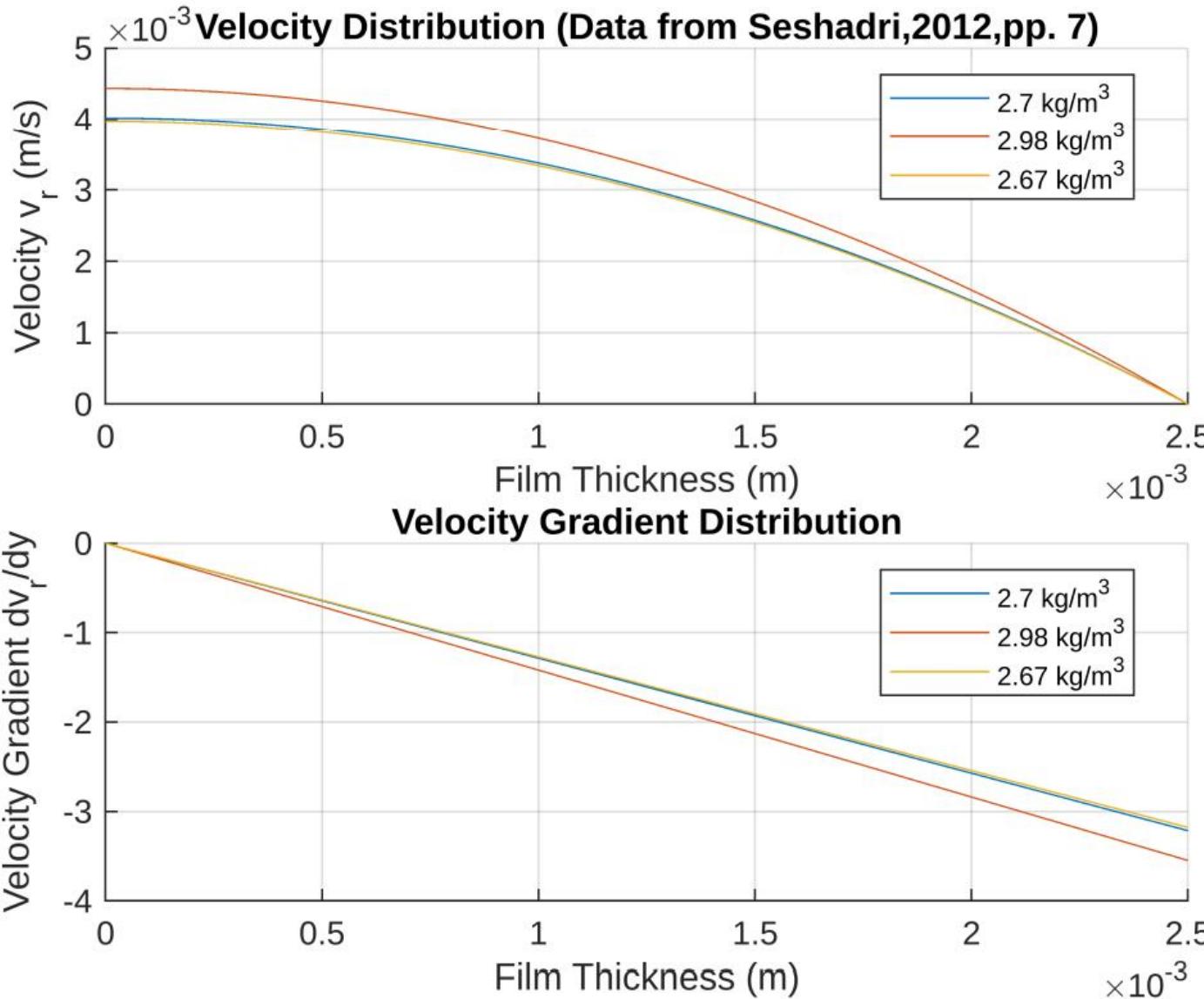
Velocity Distribution for Different Rotational Speeds ( $\omega$ )



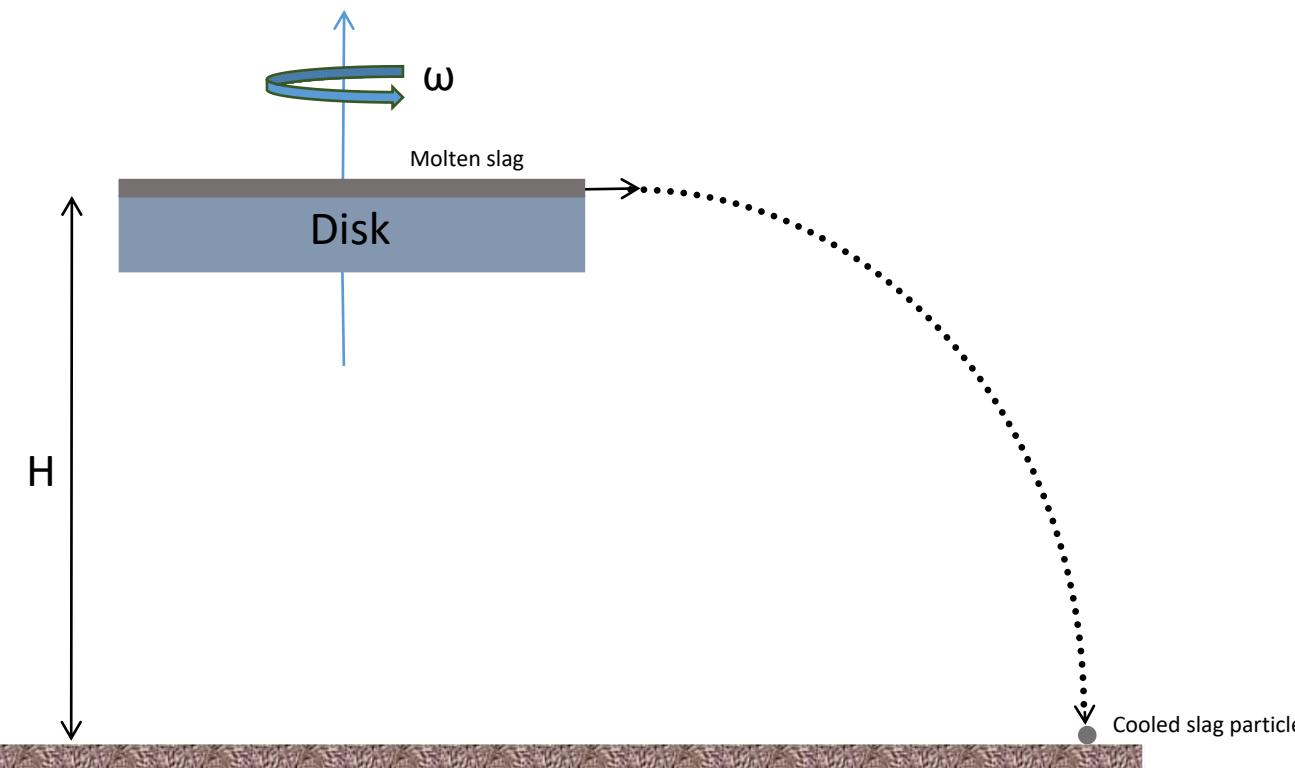
Velocity Distribution due to Variation in Viscosity



## Velocity Distribution due to Variation in Density



# Setup



**vertical height of the disc from the ground**

$$H = \frac{1}{2}gt_{\text{flight}}^2 \quad t_{\text{flight}} \geq t_{\text{cool}}$$

$$H \geq \frac{1}{2}gt_{\text{cool}}^2$$

According to Newton's Law of Cooling-

$$\frac{dQ}{dt} = -aA(T_p - T_g) - \varepsilon\sigma_0 A(T_p^4 - T_g^4)$$

$$Q = \boxed{mc_p\Delta T} + \boxed{m\Delta H_f}$$

Sensible Heat      Latent Heat

$$\frac{dT_p}{dt} = \frac{\Delta H_f}{c_p} \cdot \frac{df}{dt} - \frac{6 [\alpha(T_p - T_g) + \sigma_0 \varepsilon (T_p^4 - T_g^4)]}{\rho c_p d_p}$$

$$\frac{df}{dt} = 22.11 \left[ \exp\left(\frac{-2643.68}{T_p}\right) - \exp\left(\frac{-4165.83}{T_p}\right) \right]$$

Variable	Description	Unit
$\frac{dT_p}{dt}$	Rate of change of particle temperature	— K/s
$\Delta H_f$	Latent heat of fusion	$209.2 \times 10^3$ J/kg
$c_p$	Specific heat capacity of the particle	$1.247 \times 10^3$ J/(kg·K)
$df/dt$	Solid fraction change rate	— 1/s
$\alpha$	Convective heat transfer coefficient	372 W/(m <sup>2</sup> ·K)
$T_p$	Temperature of the particle	1723 K
$T_g$	Temperature of the surrounding gas	293 K
$\sigma_0$	Stefan-Boltzmann constant	$5.67 \times 10^{-8}$ W/(m <sup>2</sup> ·K <sup>4</sup> )
$\varepsilon$	Emissivity of the particle surface	0.9
$\rho$	Density of the particle	$2.5 \times 10^3$ kg/m <sup>3</sup>
$d_p$	Particle diameter	— m

Modified Kitamura equation for particle diameter in the ligament breakup regime: -

$$d_p = 1.9 \times 1.6 \times R \left( \left( \frac{4\rho Q}{\pi \mu R} \right)^{0.26} \cdot \left( \frac{\rho \omega^2 R^3}{\sigma} \right)^{-0.42} \cdot \left( \frac{\mu}{\sqrt{\rho \sigma R}} \right)^{0.38} \right) + C$$

$$Q = 2\pi R \delta \cdot \frac{2}{3} V_{z,\max} \quad C=61 \text{ } \mu\text{m}$$

Variable	Description	Values
$d_p$	Particle diameter	— m
R	Radius of disk	0.1 m
Q	Volumetric flow rate	— m <sup>3</sup> /s
$\rho$	Density of fluid	$2.5 \times 10^3$ kg/m <sup>3</sup>
$\mu$	Dynamic viscosity	2.1 Pa·s
$\delta$	Film thickness	$2.5 \times 10^{-3}$ m
$V_{z,\max}$	Maximum velocity	3.72024 m/s
$\omega$	Angular velocity	100 rad/s
$\sigma$	Surface tension	0.45 N/m

Ref:- Li, Jun Guo, Hong Wei Lu, and Yu Zhu Zhang. "Cooling Mechanism of the Steel Slag Droplet Granulated by Gas Quenching Method." Advanced Materials Research 233 (2011): 870-876.

Ref:- Prather, Cody A., et al. "Experimental and theoretical investigation of rotary atomization dynamics for control of microparticle size during spray congealing process." Powder Technology 418 (2023): 118278.

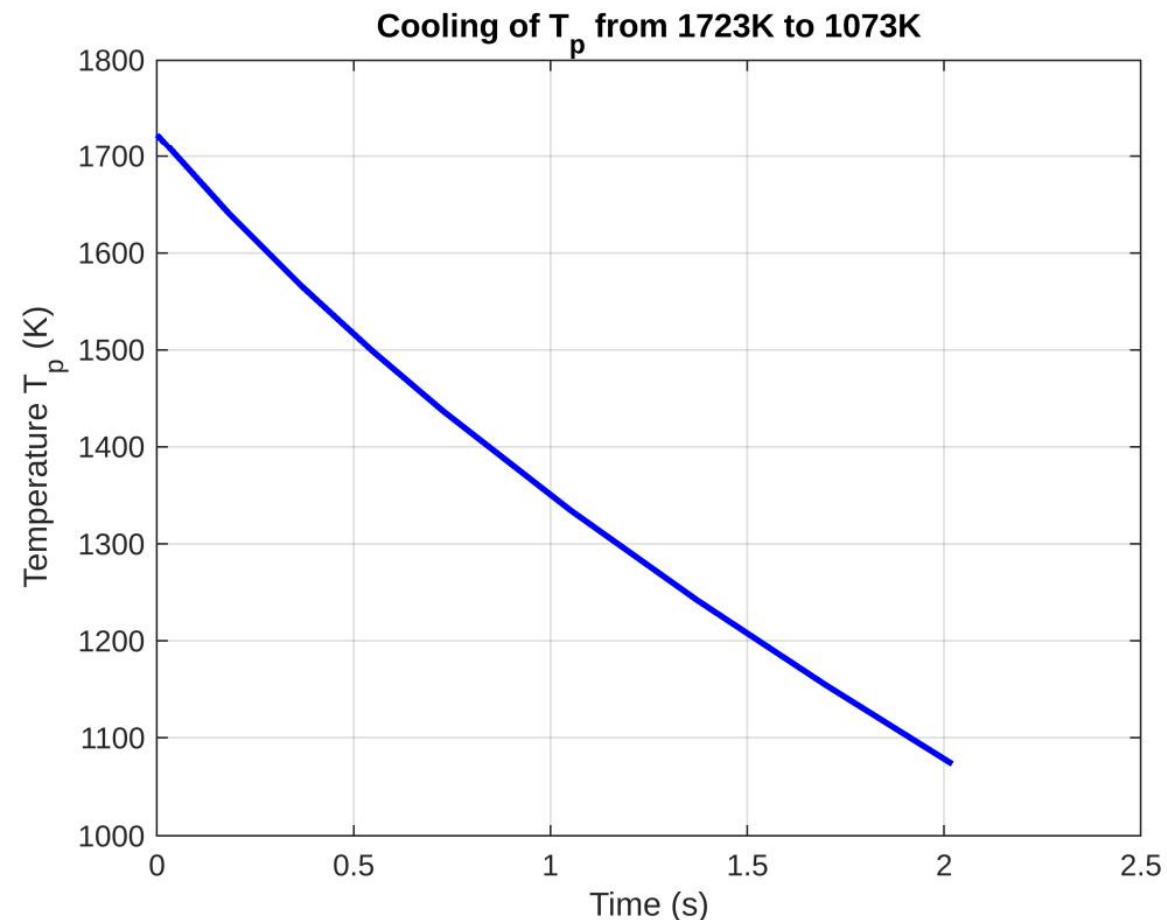
particle diameter  $d_p = 4.884$  mm

*First-Order Droplet Solidification ODE :-*

$$\frac{dT_p}{dt} = 3709.2 \left[ \exp\left(\frac{-2643.68}{T_p}\right) - \exp\left(\frac{-4165.83}{T_p}\right) \right] + 43.1 - 0.47T_p - 2.01 \times 10^{-11}T_p^4$$

$$T_{cool} = 2.021 \text{ s}$$

Therefore, the minimum required height of the disc from the ground is:  $H_{min} = 20.01$  m





# Work Plan

	BTP – I (Till Mid-Sem)	BTP – I (Till End-Sem)	BTP – II (Till Mid-Sem)	BTP – II (Till End-Sem)
Problem Identification				
Literature				
Model Framework				
Model Enhancement				
Variation Geometry				
Variation $\mu$				
Variation $\rho$				
Simulation Debugging				
Documentation and Report				

Completed

Not Started

*Thank You*

## References:

- Jia, Ruidong, et al. "Effects of SiO<sub>2</sub>/CaO ratio on viscosity, structure, and mechanical properties of blast furnace slag glass ceramics." *Materials Chemistry and Physics* 233 (2019): 155-162.
- Hurst, H. J., J. H. Patterson, and A. Quintanar. "Viscosity measurements and empirical predictions for some model gasifier slags—II." *Fuel* 79.14 (2000): 1797-1799.
- Tsuruda, Arata, Lukmanul Hakim Arma, and Hiromichi Takebe. "Viscosity measurement and prediction of gasified and synthesized coal slag melts." *Fuel* 200 (2017): 521-528.
- Seetharaman, Seshadri, et al. "Understanding the properties of slags." *ISIJ international* 53.1 (2013): 1-8.
- Li, Jun Guo, Hong Wei Lu, and Yu Zhu Zhang. "Cooling Mechanism of the Steel Slag Droplet Granulated by Gas Quenching Method." *Advanced Materials Research* 233 (2011): 870-876.
- Prather, Cody A., et al. "Experimental and theoretical investigation of rotary atomization dynamics for control of microparticle size during spray congealing process." *Powder Technology* 418 (2023): 118278.
- Doering, Charles R., and John D. Gibbon. *Applied analysis of the Navier-Stokes equations.* No. 12. Cambridge university press, 1995.