

Optimal Task Assignment by Learning Members' Abilities (MURI)

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November 3, 2015

1 Problem Setup

Consider we have a group of people and there is a sequence of tasks. Suppose each person has a set of skills and each task requires some of these tasks to a extent.

$people = \{p_1, p_2, \dots, p_n\}$, $tasks = \{t_1, t_2, \dots, t_T\}$

Each person $p = (s_1, s_2, \dots, s_m)$ and task $t = (r_1, r_2, \dots, r_m)$ has m skills set and requirements. We suppose that skill values fall in $[0, b]$ and b is a configuration parameter which directly affects problem's complexity.

2 Problem Definition

Suppose we know task requirements; however, people's skills are unknown. We need to learn the values of their abilities through payoff function. We also consider that for handling each task, merely one person is needed. The goal is maximizing of the performance in long run. Additionally, payoff function f for person p and task t is defined as follows

$$f(p, t) = \begin{cases} 1, & s_1 \geq r_1 \wedge s_2 \geq r_2 \wedge \dots \wedge s_m \geq r_m \\ 0, & otherwise \end{cases} \quad (1)$$

3 Proposed Method

To maximize the performance, we have to learn people's skills. If we know everybody's expertises, we assign best people to their matching task to a great extent To learn, we propose a simple rule-based learning approach. If agent handles successfully the task, it conveys:

$s_1 \geq r_1 \wedge s_2 \geq r_2 \wedge \dots \wedge s_m \geq r_m$

and he or she fails it means:

$s_1 < r_1 \vee s_2 < r_2 \vee \dots \vee s_m < r_m$

1 In this method, we can learn, and hence, limit the boundaries for each per-
 2 son’s skills with assigning more tasks to him or her.

3 One goal in this study could be finding a lower bound of numbers task
 4 assignment to a single person with m different skills that vary in $[0, b]$ to ensure
 5 that more than 90% of his or her skill values are uncovered so far.

6 First we start with no knowledge about people’s skills and initialize skill
 7 values with 0s. To learn actual values there are two important power which are
 8 defined in the following descriptively.

9 3.1 Exploration

In exploration phase, we choose one person who is completely unknown and has
 all 0s in his or her skills. If there is no one left unknown in people, then we will
 choose that person has the largest boundary distance (who is more unknown).
 To do this, we define a boundary $[x, y]$ such that $x \geq 0$ and $y \leq b$ for each skill
 in every person. Boundary distance is defined as

$$dist = \sqrt{\sum_{i=1}^m (x_i - y_i)^2} \quad (2)$$

10 If there are more than one person having the largest distance, then we choose
 11 one of them by random.

12 3.2 Exploitation

13 In exploitation phase, we choose one of known people (they have skills values
 14 greater than 0) who is more appropriate for the task and his or her skills are
 15 more promising for handling successfully. The selection method for task $t =$
 16 (r_1, r_2, \dots, r_m) and if each person such as $p = (s_1, s_2, \dots, s_m)$ is

$$\arg \max_p o(t, p); \quad o(t, p) = \begin{cases} \sqrt{\sum_{i=1}^m (s_i - r_i)^2}, & \text{if } s_1 \geq r_1 \wedge s_2 \geq r_2 \wedge \dots \wedge s_m \geq r_m \\ 0, & \text{otherwise} \end{cases} \quad (3)$$

17 3.3 Exploration and exploitation trade-off

There are different methods in Multi Armed Bandits literature [1, 3]; however,
 for the sake of simplicity and soundness, we will stick with the following method,

$$P_{exploration} = \frac{c}{t} \quad (4)$$

18 where c is a constant and t is the time-step variable. In the beginning exploration
 19 power is very high; however, since t increases over time; as a consequence, the
 20 exploitation power gradually increases and exploration decays. This concept is
 21 inspired since in the beginning we do not have enough knowledge and is better

1 to explore more; nonetheless, as time passes, we know more and hence it is
2 better to exploit more and refine the available solutions.

3 4 Extensions

- 4 1. Find a group of people instead of just one person to handle a task.
- 5 2. We suppose there is a prior knowledge regarding each person; however, this
6 prior probability gradually change through time with a Bayesian learning.
3. The payoff could be continuous instead of binary. Also it cannot be euclidean distance for all, thus:

$$f(p, t) = \sqrt{\sum_{i=1}^m u_i}; \quad u_i = \begin{cases} (r_i - s_i)^2, & \text{if } r_i \geq s_i \\ 0, & \text{otherwise} \end{cases} \quad (5)$$

4. The payoff function could be stochastic as follows:

$$f(p, t) = \begin{cases} 1, & \text{if } s_1 + \mathcal{N}(1, \sigma^2) \geq r_1 \wedge s_2 + \mathcal{N}(1, \sigma^2) \geq r_2 \wedge \dots \wedge s_m + \mathcal{N}(1, \sigma^2) \geq r_m \\ 0, & \text{otherwise} \end{cases} \quad (6)$$

- 7 5. We can use some other multi armed bandits algorithms (contextual MAB)
8 and for instance Soft Max to facilitate exploration and exploitation trade-
9 off [2, 3].
- 10 6. If we consider that tasks are decomposable then we can have a group of
11 people handling a task instead of solely one person. Therefore, to solve
12 this problem, we will use solutions for multiple knapsack problem [4].

13 References

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