Lecture 12: Design Theory II

Today's Lecture

- 1. Boyce-Codd Normal Form
 - ACTIVITY
- 2. Decompositions & 3NF
 - ACTIVITY
- 3. MVDs
 - ACTIVITY

1. Boyce-Codd Normal Form

What you will learn about in this section

- 1. Conceptual Design
- 2. Boyce-Codd Normal Form
- 3. The BCNF Decomposition Algorithm
- 4. ACTIVITY

Conceptual Design طراحی مفہومی

Back to Conceptual Design

Now that we know how to find FDs, it's a straight-forward process:

- 1. Search for "bad" FDs دنبال وابستگی تابعی های بد میگردیم
- 2. If there are any, then keep decomposing the table into sub-tables until no more bad FDs اگر پیدا کردیم، جدول رو تجزیه می کنیم تا آن وابستگی تابعی های بد حذف شوند بد حذف شوند

Recall: there are several normal forms...

3. When done, the database schema is *normalized – شمای پایگاهدادهی شما*

Boyce-Codd Normal Form (BCNF)

• Main idea is that we define "good" and "bad" FDs as follows:

- $X \rightarrow A$ is a "good FD" if X is a (super)key
 - In other words, if A is the set of all attributes
- X → A is a "bad FD" otherwise
- We will try to eliminate the "bad" FDs!
 - سعی می کنیم که وابستگی تابعیهای بد را حذف کنیم.

Boyce-Codd Normal Form (BCNF)

- Why does this definition of "good" and "bad" FDs make sense?
- If X is *not* a (super)key, it functionally determines *some* of the attributes; therefore, those other attributes can be duplicated
 - Recall: this means there is <u>redundancy</u>
 - And redundancy like this can lead to data anomalies!

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

Boyce-Codd Normal Form

BCNF is a simple condition for removing anomalies from relations:

A relation R is in BCNF if:

if $\{A_1, ..., A_n\} \rightarrow B$ is a non-trivial FD in R

then $\{A_1, ..., A_n\}$ is a superkey for R

Equivalently: \forall sets of attributes X, either (X⁺ = X) or (X⁺ = all attributes)

In other words: there are no "bad" FDs

Example

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

{SSN} → {Name,City}

This FD is *bad* because it is **not** a superkey

 \Rightarrow **Not** in BCNF

What is the key? {SSN, PhoneNumber}

Example

Name	SSN	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Madison

SSN	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

Now in BCNF!

{SSN} → {Name,City}

This FD is now good because it is the key

Let's check anomalies:

- Redundancy?
- Update?
- Delete ?

BCNFDecomp(R):		

BCNFDecomp(R):

Find a set of attributes X s.t.: X⁺ ≠ X and X⁺ ≠ [all attributes]

Find a set of attributes X which has non-trivial "bad" FDs, i.e. is not a superkey, using closures

BCNFDecomp(R):

Find a set of attributes X s.t.: $X^+ \neq X$ and $X^+ \neq X$ [all attributes]

if (not found) then Return R

If no "bad" FDs found, in BCNF!

BCNFDecomp(R):

Find a set of attributes X s.t.: $X^+ \neq X$ and $X^+ \neq X$ [all attributes]

if (not found) then Return R

let
$$Y = X^+ - X$$
, $Z = (X^+)^C$

Let Y be the attributes that X functionally determines (+ that are not in X)

And let Z be the complement, the other attributes that it doesn't

BCNFDecomp(R):

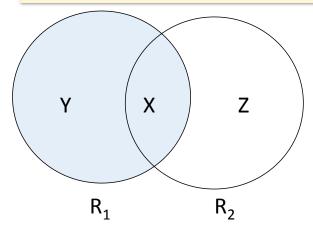
Find a set of attributes X s.t.: $X^+ \neq X$ and $X^+ \neq X$ [all attributes]

if (not found) then Return R

$$\underline{\mathsf{let}}\;\mathsf{Y}=\mathsf{X}^{\scriptscriptstyle{+}}-\mathsf{X},\;\;\mathsf{Z}=(\mathsf{X}^{\scriptscriptstyle{+}})^{\scriptscriptstyle{\complement}}$$

decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

Split into one relation (table) with X plus the attributes that X determines (Y)...



BCNFDecomp(R):

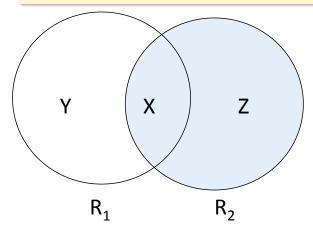
Find a set of attributes X s.t.: $X^+ \neq X$ and $X^+ \neq X$ [all attributes]

if (not found) then Return R

let
$$Y = X^{+} - X$$
, $Z = (X^{+})^{C}$

decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

And one relation with X plus the attributes it *does not* determine (Z)



BCNFDecomp(R):

Find a *set of attributes* X s.t.: X⁺ ≠ X and X⁺ ≠ [all attributes]

if (not found) then Return R

<u>let</u> $Y = X^+ - X$, $Z = (X^+)^C$ decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

Return BCNFDecomp(R₁), BCNFDecomp(R₂)

Proceed recursively until no more "bad" FDs!

Example

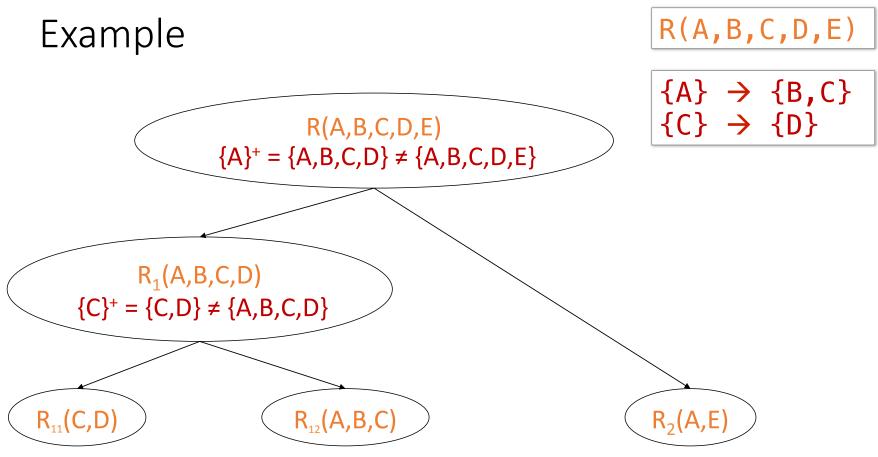
BCNFDecomp(R):

Find a set of attributes X s.t.: $X^+ \neq X$ and $X^+ \neq$ [all attributes]

if (not found) then Return R

let
$$Y = X^+ - X$$
, $Z = (X^+)^C$
decompose R into $R_1(X \cup Y)$ and $R_2(X \cup Z)$

Return BCNFDecomp(R₁), BCNFDecomp(R₂)



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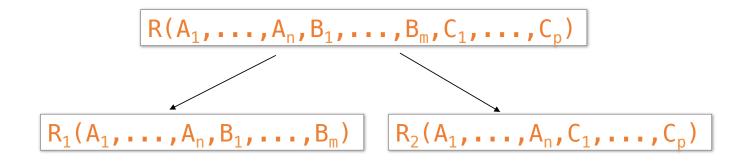
2. Decompositions

Recap: Decompose to remove redundancies

- 1. We saw that **redundancies** in the data ("bad FDs") can lead to data anomalies
- 2. We developed mechanisms to detect and remove redundancies by decomposing tables into BCNF
 - 1. BCNF decomposition is *standard practice* very powerful & widely used!
- 3. However, sometimes decompositions can lead to **more subtle** unwanted effects...

When does this happen?

Decompositions in General



 R_1 = the *projection* of R on A_1 , ..., A_n , B_1 , ..., B_m

 R_2 = the *projection* of R on A_1 , ..., A_n , C_1 , ..., C_p

Theory of Decomposition

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera

Sometimes a decomposition is "correct"

I.e. it is a <u>Lossless</u> <u>decomposition</u>

Name	Price
Gizmo	19.99
OneClick	24.99
Gizmo	19.99

Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Lossy Decomposition

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
Gizmo	19.99	Camera

However sometimes it isn't

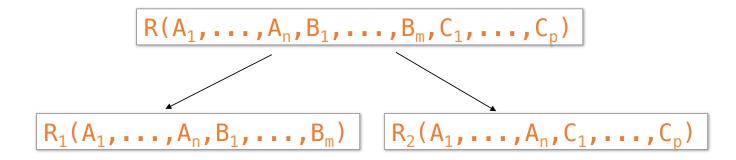
What's wrong here?



Name	Category
Gizmo	Gadget
OneClick	Camera
Gizmo	Camera

Price	Category
19.99	Gadget
24.99	Camera
19.99	Camera

Lossless Decompositions



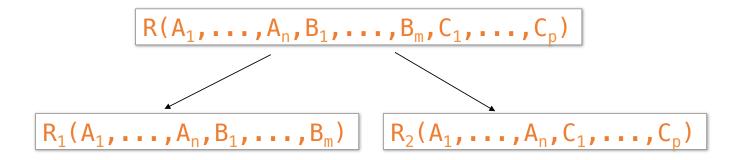
What (set) relationship holds between R1 Join R2 and R if lossless?



It's lossless if we have equality!

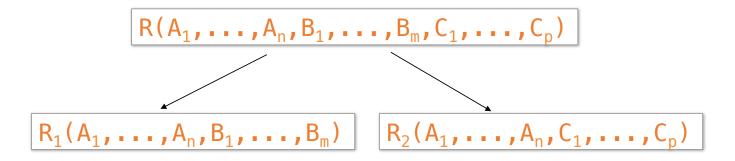
Hint: Which tuples of R will be present?

Lossless Decompositions



A decomposition R to (R1, R2) is <u>lossless</u> if R = R1 Join R2

Lossless Decompositions



If
$$\{A_1, ..., A_n\} \rightarrow \{B_1, ..., B_m\}$$

Then the decomposition is lossless

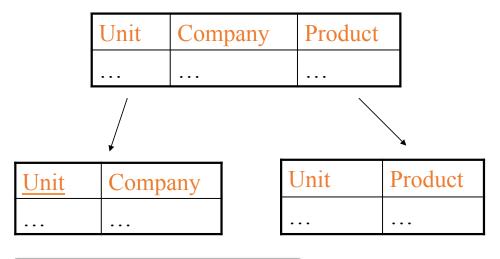
Note: don't need
$$\{A_1, ..., A_n\} \rightarrow \{C_1, ..., C_p\}$$

BCNF decomposition is always lossless. Why?

A problem with BCNF

<u>Problem</u>: To enforce a FD, must reconstruct original relation—on each insert!

A Problem with BCNF



```
{Unit} → {Company}
{Company, Product} → {Unit}
```

We do a BCNF decomposition
on a "bad" FD:
{Unit}+ = {Unit, Company}

```
{Unit} → {Company}
```

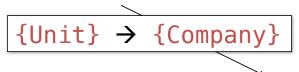
We lose the FD {Company, Product} → {Unit}!!

So Why is that a Problem?

<u>Unit</u>	Company
Galaga99	UW
Bingo	UW

Unit	Product
Galaga99	Databases
Bingo	Databases

No problem so far. All *local* FD's are satisfied.



Unit	Company	Product
Galaga99	UW	Databases
Bingo	UW	Databases

Let's put all the data back into a single table again:

Violates the FD {Company, Product} → {Unit}!!

The Problem

- We started with a table R and FDs F
- We decomposed R into BCNF tables R_1 , R_2 , ... with their own FDs F_1 , F_2 , ...
- We insert some tuples into each of the relations—which satisfy their local FDs but when reconstruct it violates some FD **across** tables!

<u>Practical Problem</u>: To enforce FD, must reconstruct R—on each insert!

Possible Solutions

- Various ways to handle so that decompositions are all lossless / no FDs lost
 - For example 3NF- stop short of full BCNF decompositions. See Bonus Activity!
- Usually a tradeoff between redundancy / data anomalies and FD preservation...

BCNF still most common- with additional steps to keep track of lost FDs...

3NF

- R is in *Third Normal Form (3NF)* if for every nontrivial FD X → A, either:
 - X is a superkey of R, or
 - A is a member of at least one key of R
- Tradeoff:
 - We can check all FD's in the decomposed relation
 - But now we might have redundancy due to FD's
 - Example: (Unit, Company, Product) is in 3NF, but not in BCNF

وابستگیهای چند مقداری -3. MVDs

What you will learn about in this section

1. MVDs

2. ACTIVITY

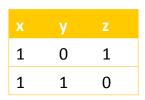
Multi-Value Dependencies (MVDs)

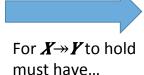
- A multi-value dependency (MVD) is another type of dependency that could hold in our data, which is not captured by FDs
- Formal definition:
 - Given a relation **R** having attribute set **A**, and two sets of attributes $X,Y\subseteq A$
 - The *multi-value dependency (MVD) X->> Y* holds on R if
 - for any tuples $t1,t2 \in R$ s.t. t1[X]=t2[X], there exists a tuple t_3 s.t.:
 - $t_1[X] = t_2[X] = t_3[X]$
 - t₁[Y] = t₃[Y]
 - t₂[A\Y] = t₃[A\Y]
 - Where A \ B means "elements of set A not in set B"

Multi-Value Dependencies (MVDs)

- One less formal, literal way to phrase the definition of an MVD:
- The MVD X->> Y holds on R if for any pair of tuples with the same X values, the "swapped" pair of tuples with the same X values, but the other permutations of Y and A\Y values, is also in R

Ex:
$$X = \{x\}, Y = \{y\}$$
:





X	У	Z	
1	0	1	
1	1	0	
1	0	0	
1	1	1	

Note the connection to a local *cross-product...*

Multi-Value Dependencies (MVDs)

- Another way to understand MVDs, in terms of conditional independence:
- The MVD X→Y holds on R if given X, Y is conditionally independent of A \ Y and vice versa...

Here, given x = 1, we know for ex. that: $y = 0 \rightarrow z = 1$

I.e. z is conditionally *dependent* on y given x

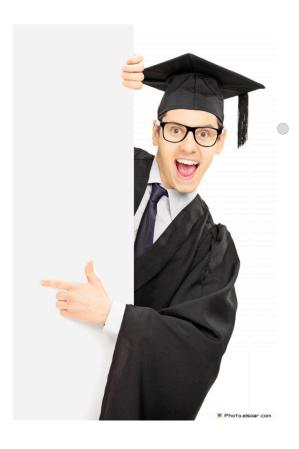
х	У	z	
1	0	1	
1	1	0	

Here, this is not the case!

I.e. z is conditionally *independent* of y given x

x	У	z
1	0	1
1	1	0
1	0	0
1	1	1

Multiple Value Dependencies (MVDs)



A "real life" example...

Grad student CA thinks:

"Hmm... what is real life??

Watching a movie over the weekend?"

Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

Are there any functional dependencies that might hold here?

No...

And yet it seems like there is some pattern / dependency...

Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

Movie_theater	film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

Given a set of movies and snacks...

Movie_theat	ter film_name	snack
Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
Rains 216	Star Trek: The Wrath of Kahn	Burrito
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
Rains 218	Star Wars: The Boba Fett Prequel	Ramen
Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

For a given movie theatre...

Given a set of movies and snacks...

Any movie / snack combination is possible!

	Movie_theater (A)	film_name (B)	Snack (C)
t_1	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t ₂	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write $\{A\} \rightarrow \{B\}$ if for any tuples t_1, t_2 s.t. $t_1[A] = t_2[A]$

	Movie_theater (A)	film_name (B)	Snack (C)
t_1	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
t ₃	Rains 216	Star Trek: The Wrath of Kahn	Burrito
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t ₂	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write $\{A\} \rightarrow \{B\}$ if for any tuples t_1, t_2 s.t. $t_1[A] = t_2[A]$ there is a tuple t_3 s.t.
• $t_3[A] = t_1[A]$

	Movie_theater (A)	film_name (B)	Snack (C)
t_1	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
t₃	Rains 216	Star Trek: The Wrath of Kahn	Burrito
3			
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t ₂	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write $\{A\} \rightarrow \{B\}$ if for any tuples t_1, t_2 s.t. $t_1[A] = t_2[A]$ there is a tuple t_3 s.t.

- $t_3[A] = t_1[A]$
- $t_3[B] = t_1[B]$

	Movie_theater (A)	film_name (B)	Snack (C)
t_1	Rains 216	Star Trek: The Wrath of Kahn	Kale Chips
t₃	Rains 216	Star Trek: The Wrath of Kahn	Burrito
- 5			
	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Kale Chips
t ₂	Rains 216	Lord of the Rings: Concatenated & Extended Edition	Burrito
	Rains 218	Star Wars: The Boba Fett Prequel	Ramen
	Rains 218	Star Wars: The Boba Fett Prequel	Plain Pasta

More formally, we write $\{A\} \rightarrow \{B\}$ if for any tuples t_1, t_2 s.t. $t_1[A] = t_2[A]$ there is a tuple t_3 s.t.

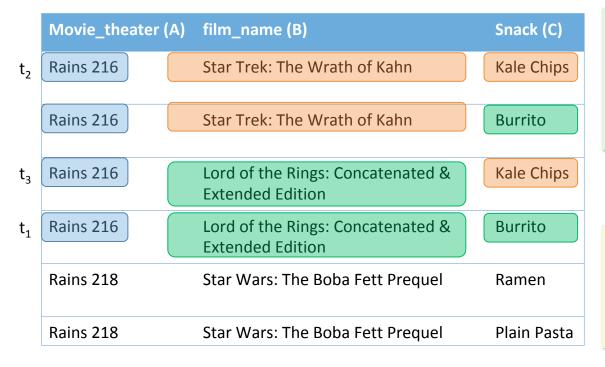
- $t_3[A] = t_1[A]$
- $t_3[B] = t_1[B]$
- and $t_3[R\backslash B] = t_2[R\backslash B]$

Where R\B is "R minus B" i.e. the attributes of R not in B



Note this also works!

Remember, an MVD holds over a relation or an instance, so defn. must hold for every applicable pair...



This expresses a sort of dependency (= data redundancy) that we can't express with FDs

*Actually, it expresses conditional independence (between film and snack given movie theatre)!

Activity-12-2.ipynb

Summary

- Constraints allow one to reason about **redundancy** in the data
- Normal forms describe how to remove this redundancy by decomposing relations
 - Elegant—by representing data appropriately certain errors are essentially impossible
 - For FDs, BCNF is the normal form.
- A tradeoff for insert performance: 3NF