

## Regularization's

$$y = 15 + 1.2x_1 + 2x_2 + 39x_3$$

$x_3$  is very important to determine  
y / output variable / dependent variable

bcz  $x_3$  has highest coefficient.  
or  $x_3$  has highest Regression Coefficient.

&  $x_1$  is least imp.

∴ Value of  $x_3$  is too high,  
working of datasets becomes  
very much computationally expensive.

∴ Model becomes very complex.

∴ To reduce the complexity of  
the Model, we use

Regularization.

$$\therefore y = 0.9 + 0.7x_1 + 2x_2 + 5x_3$$

∴ this becomes a computationally  
easy task.

Regularization Types:

① Ridge

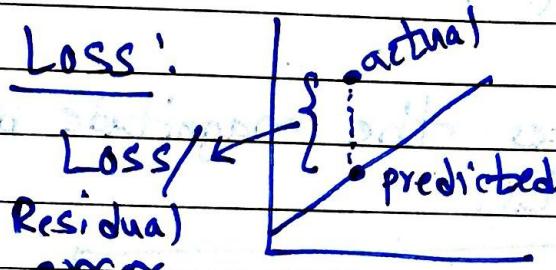
② Lasso

① Ridge: (It uses L2 Regularization Technique).

$$\text{Ridge regression} = \text{LOSS} + \lambda \|\mathbf{w}\|^2$$

minimum  
penalty

Loss:



(actual - predicted)

Greater the diff, greater the Loss.

Penalty: It is imposed to reduce the loss.

i.e. we try to compensate here for the loss i.e. reduce the loss.

Also, it helps to scale down the magnitude of the coefficient.

$\lambda$ : It is any constant value.

$$\|\mathbf{w}\|^2 = w_1^2 + w_2^2 + w_3^2 + \dots + w_n^2$$

$\mathbf{w}$  - It is a vector of coefficients

Now, let's understand, how does adding penalty reduces the loss.

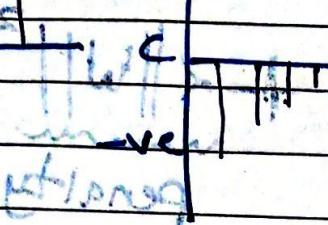
$$\lambda = 0.01$$

$$\lambda = 1$$

$$\lambda = 2$$

coeff  
-ve

suppose  $y = 5 + 2x_1 + 3x_2 + 5x_3$  (true)



variables (v)

(v)

(v)

~~value~~ of value modulates the magnitude of the coefficients.

Greater  $\lambda \rightarrow$  Lesser value of coefficient

Note: ① More computationally efficient ② Penalizes large nos. more ③ More popular ④ Good when encountering collinearity.

• 2. Lasso: (It uses L1 Reg. Technique)

• Lasso R. = Loss +  $\lambda ||w||_1$

•  $||w||_1 = |w_1| + |w_2| + |w_3| + \dots + |w_n|$

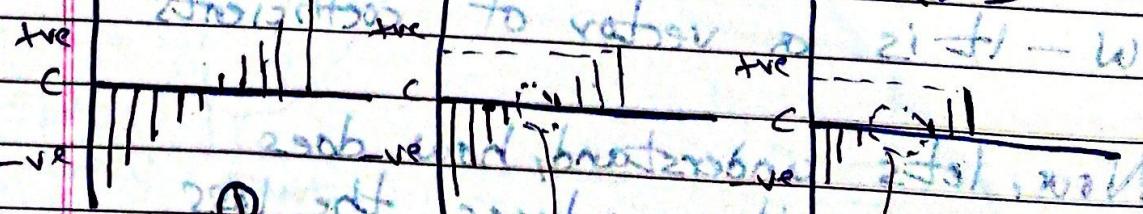
$$y = 15 + 1.2x_1 + 20x_2 + 39x_3$$

$$\Rightarrow y = 0.9 + 0x_1 + 0x_2 + 5x_3$$

$$\lambda = 0.001$$

$$\lambda = 1$$

$$\lambda = 5$$



Note: Lasso R. also acts as Feature Selection. That's how

① Lasso is diff. from Ridge R.  
② Also, it is more robust to outliers.

### ③ Elastic Net Regression

It is taking advantages of both Ridge & Lasso Regression.

$$\text{Ridge R.} = \text{Loss} + \lambda \|\mathbf{w}\|^2$$

$$\text{Lasso R.} = \text{Loss} + \lambda \|\mathbf{w}\|$$

$$\text{Elastic Net R.} = \text{Loss} + \lambda_1 \|\mathbf{w}\|^2 + \lambda_2 \|\mathbf{w}\|$$

\* Ridge R. is used in datasets which have Multicollinearity Problem i.e. when the independent variables are highly correlated with each other.

\* Lasso R. is used for Feature Selection.

\* Elastic Net R. inherits advantages of both.  
 ∵ It is elastic i.e. flexible.  
 ∵ E-N Reg' is a hybrid of RR & LR.

## # Naive Bayes Variants

① Bernoulli Distribution

- Used when feature values is of Binary nature

$$P(\text{Success}) = p$$

$$P(\text{Failure}) = q = (1-p)$$

Let  $X$  be a random variable.

∴ Random Var.

$X = 1 \rightarrow$  It Signifies Success

$X = 0 \rightarrow$  It Signifies Failure

∴ Random Var.  $X$  has Bernoulli Distribution.

$$P(X=x) = p^x \cdot (1-p)^{1-x}$$

where  $x = 0$  or  $1$

OR

$$P(X) = \begin{cases} p & \text{if } X=1 \\ q & \text{if } X=0 \end{cases}$$

## ② Multinomial NB:

It is usually used in Natural Lang. Processing.

∴ MNB is basically used when we are interested to find the occurrence-times / frequency of a particular word in a Text Document.

### Multinomial Distribution:

MNB is used when we are interested in finding combined probability.

Blood Group	O	A	B	AB
Probability	0.44	0.42	0.10	0.04

So, now we hv a big population among which we are randomly picking "6 Indians" i.e. random sampling & we hv to find the following:  
What is the probability that in the given

1 Person is with Blood Group ①

2 Ppl. are ——— A

2 ——— B

1 Person is ——— AB

Formula:

$$P(X_1=x_1, \dots, X_k=x_k) = \frac{n!}{x_1! \dots x_k!} \cdot P_1^{x_1} \cdots P_k^{x_k}$$

$$\therefore P(X_1=1, X_2=2, X_3=2, X_4=1) = \frac{6!}{1! 2! 2! 1!} \cdot (0.44^1 \cdot 0.42^2 \cdot 0.10^2 \cdot 0.04^1)$$

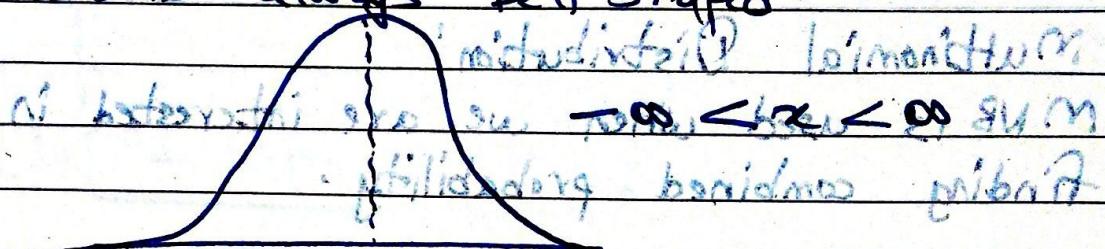
### ③ Gaussian/Normal Distribution

Warning: Don't use it if your data is DISCRETE.

For discrete counts, use Multinomial.

Gaussian NB is used when features are CONTINUOUS.

It is always Bell Shaped.



Gaussian NB can be used on Iris dataset.

PDF is  $f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$

$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$

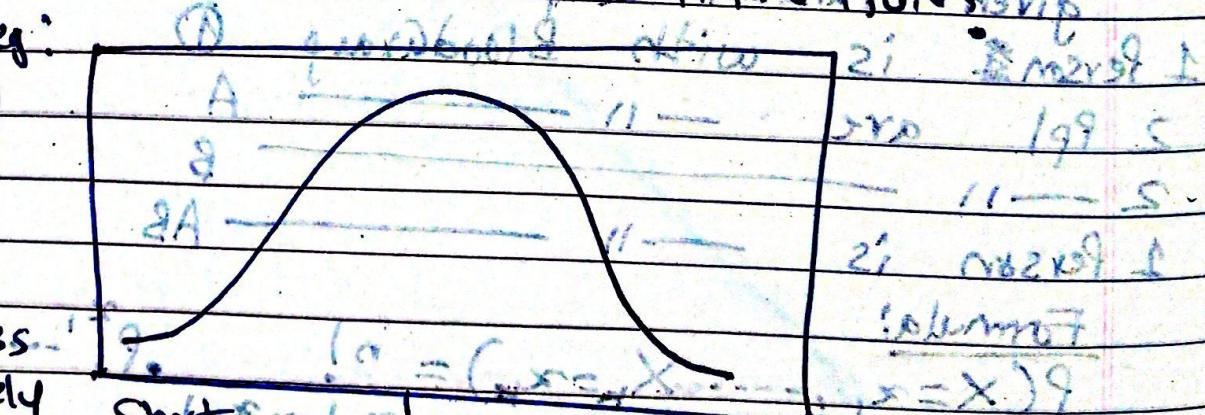
Above formula has 3 input Parameters

mean, SD, & Variance

# What is NORMAL DISTRIBUTION?

More eg:

Likely

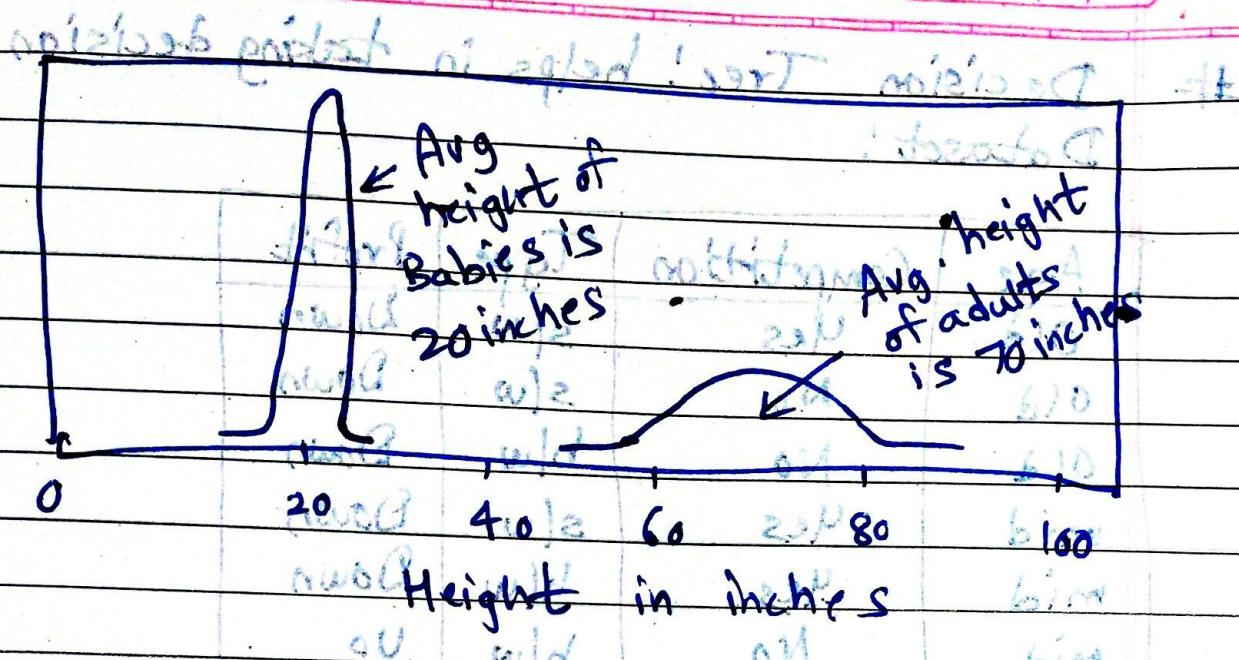


Average

Height

Tall

$\mu = \frac{1}{n} \sum x_i$



Normal Distributions are always centered on the average value.

Just by looking at the graph, we can tell that there is a high probability that a newborn baby will be between 19 & 21 inches tall.

In contrast, adults are between

60 - 80 inches tall.

Also, we can notice that the curve for babies is way tall compared to curve for adults. This is because there are many more possibilities for adult height than for babies.

∴ Babies have relatively small SD compared

to adults.

$$\sigma_{\text{babies}} = 0.6 \quad \sigma_{\text{adults}} = 4$$

such that 95% of the measurements

Normal Curves are always around  $\pm 2$  around the Mean i.e. 95% of babies fall b/w  $20 \pm 1.2$  inches & 95% of adults fall b/w  $70 \pm 8$  inches.