

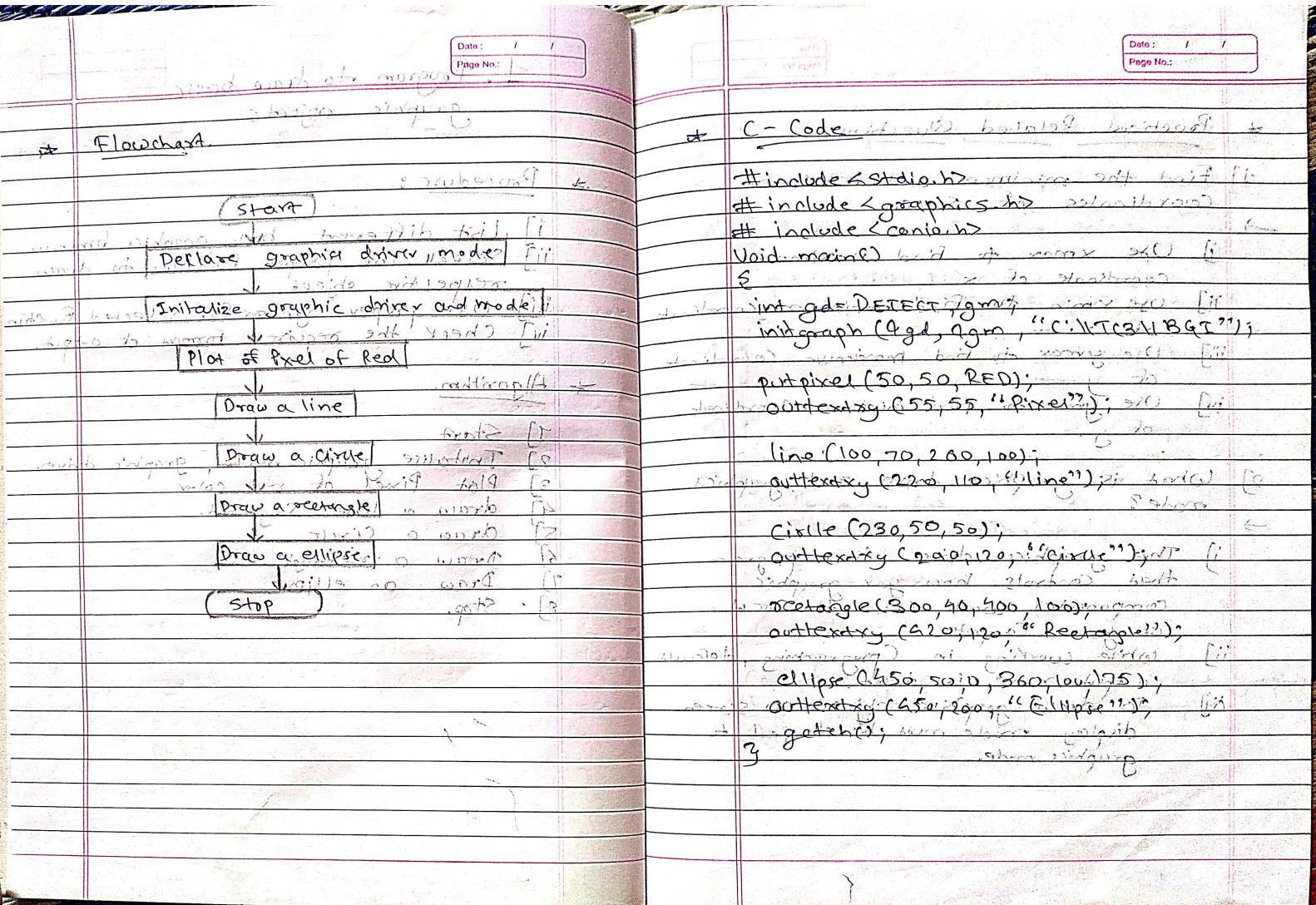
# 1. Program to draw basic graphic objects

## \* Procedure :

- i] List different basic graphic function.
- ii] Select the proper function to draw respective object.
- iii] Use proper syntax for selected function
- iv] Check the required format of output.

## \* Algorithm.

- 1] Start
- 2] Initialise graphic mode, graphic driver
- 3] Plot Pixel of red color
- 4] draw a line segment.
- 5] draw a circle
- 6] draw a rectangle
- 7] draw an ellipse
- 8] Stop.



## \* Practical Related Questions

- 1] Find the minimum and maximum coordinates of screen.  
→
  - i] Use  $x_{max}$  to find maximum coordinate of  $x$ .
  - ii] Use  $x_{min}$  to find minimum coordinate of  $x$ .
  - iii] Use  $y_{max}$  to find maximum coordinate of  $y$ .
  - iv] Use  $y_{min}$  to find minimum coordinate of  $y$ .
- 2] What is "graphics" driver and graphics mode?  
→
  - i] The "graphics driver" is a program that controls how your graphic components work with the rest of your computer.
  - ii] While working in programming, default output mode is text.
  - iii] To draw graphical objects on screen, display mode must be changed to graphics mode.

→ 3) what is part of graphics driver?

→ C:\L\TCB41\B&T\

1] Find error in following code:

```
2
3    putpixel(20,20);
    arrowatxy(25,25, "pixel");
```

→ In `putpixel`: Didn't specified color:  
Syntax error.

4] List four applications of Computer graphics.

- i] Computer Art.
- ii] Computer Aided Drawing
- iii] Education.
- iv] Visualisation

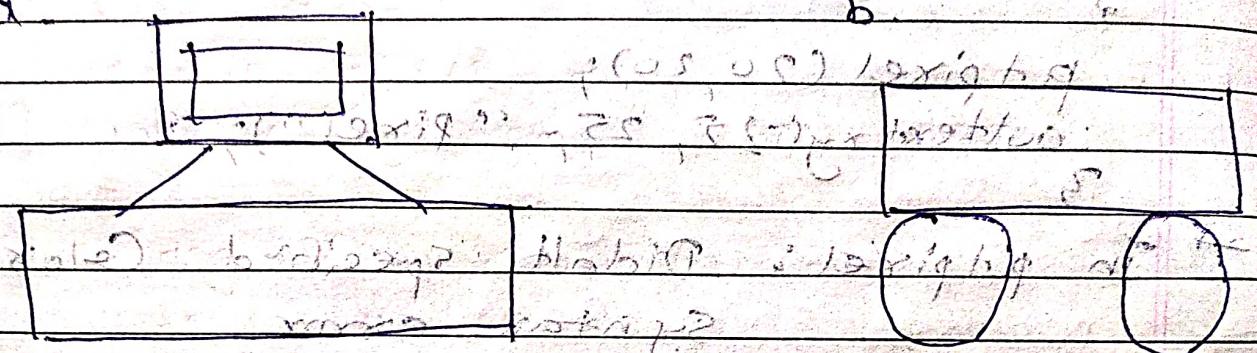
→ Conclusion:

Computer graphics provides different graphic functions to draw various graphic objects.

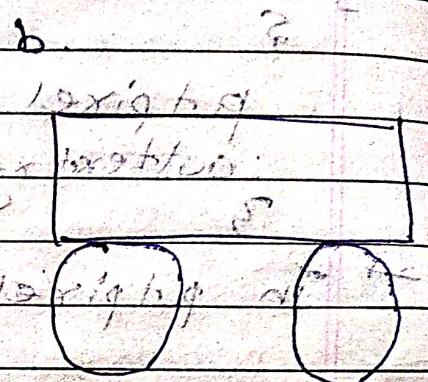
## Exercise writing to draw 2D shapes

1] Write a C program to display following objects.

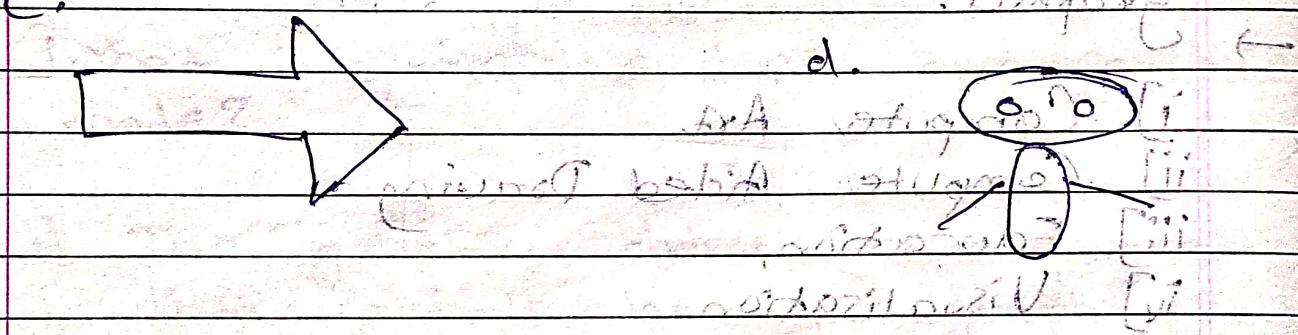
a.



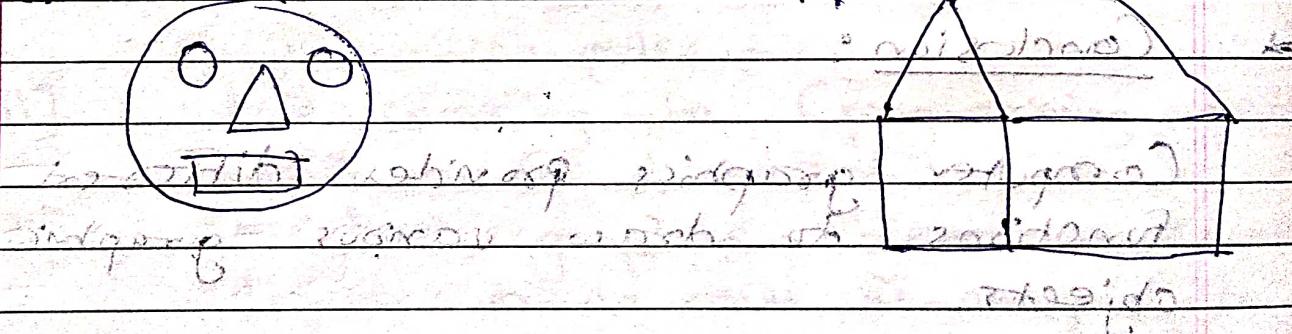
b.



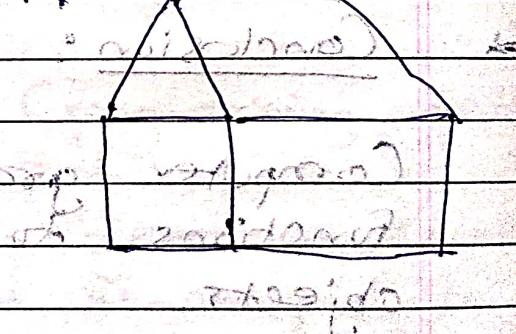
c.

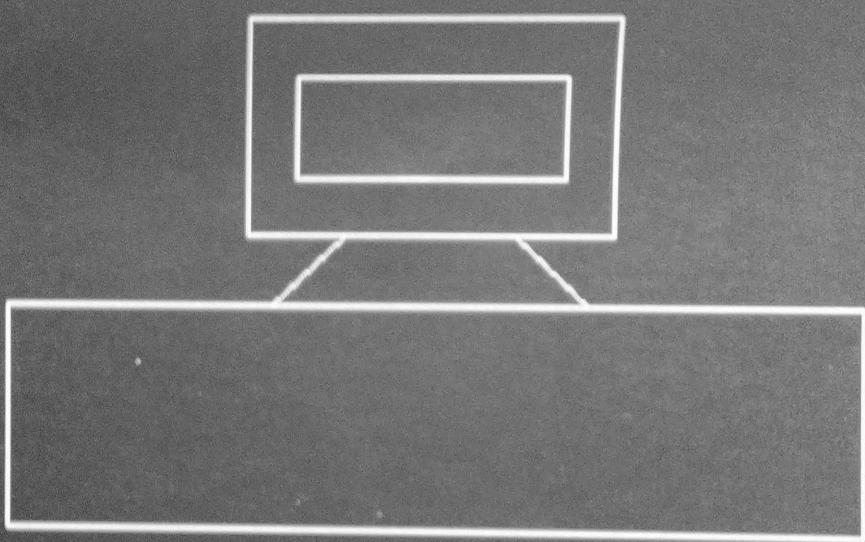


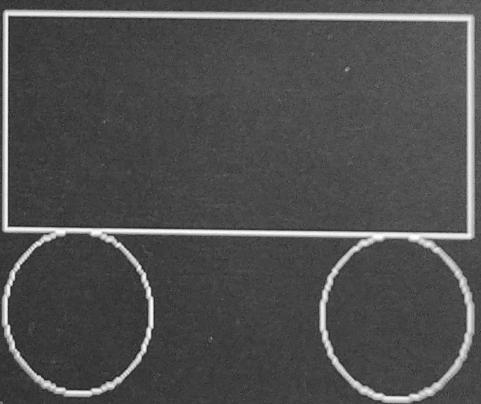
e.

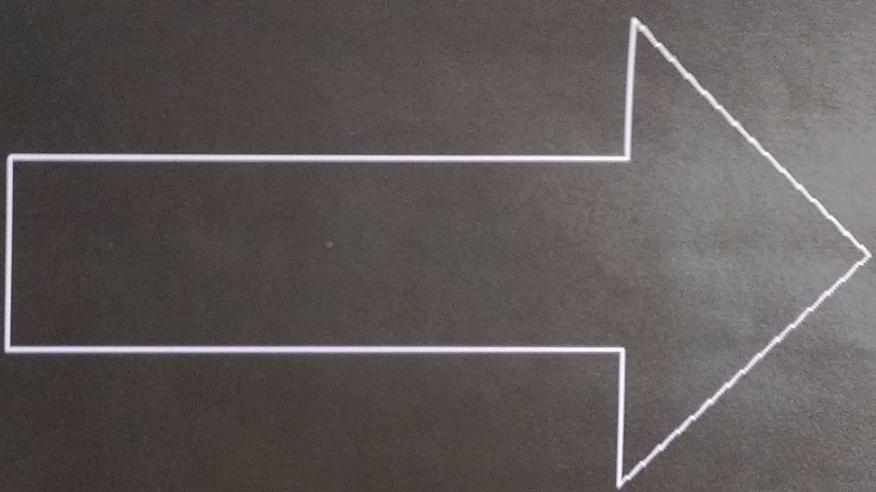


f.

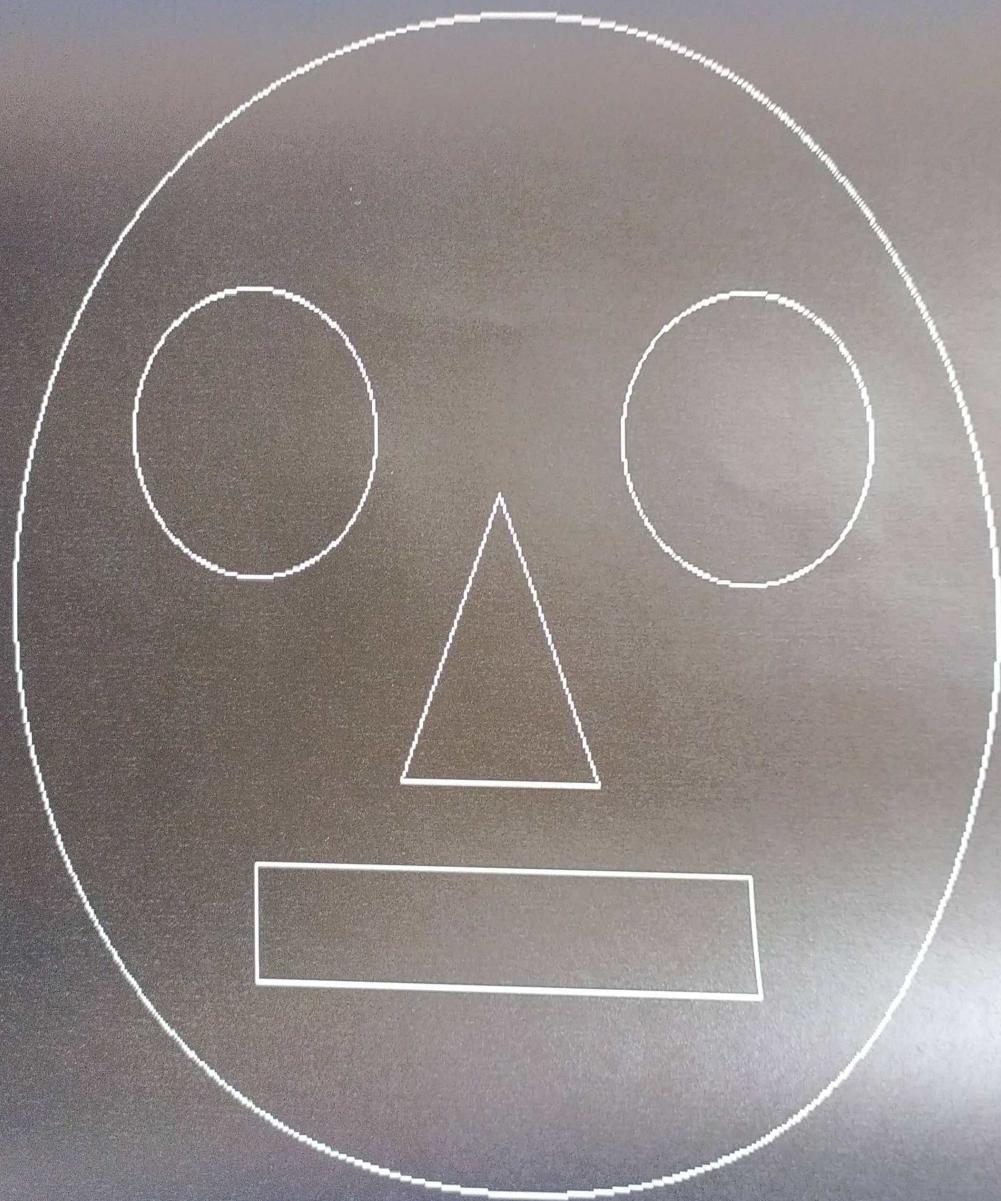


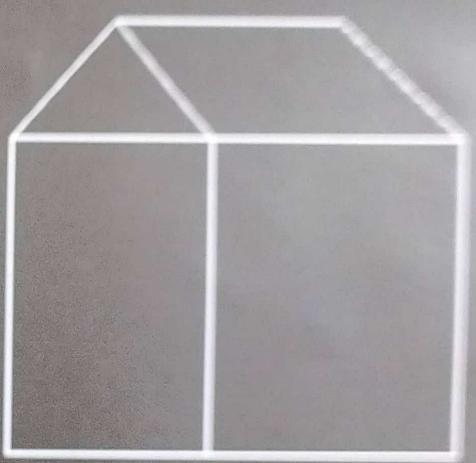












## 2. Program to draw line Using DDA algorithm

### Procedure:

- i] Read the input of the 2 end points of the line as  $(x_1, y_1)$  &  $(x_2, y_2)$   
such that  $x_1 \neq x_2$  and  $y_1 \neq y_2$
- ii] Calculate  $dx = x_2 - x_1$  and  $dy = y_2 - y_1$
- iii] if  $(dx >= dy)$   
 $\text{step} = dx + 1$  ;  $x = x_1$  ;  $y = y_1$   
 for  $k = 0$  to  $step - 1$   
 $x = x + 1$  ;  $y = y + 1$   
 $\text{put pixel}(x, y)$
- iv]  $x_{in} = dx / \text{step}$  &  $y_{in} = dy / \text{step}$
- v]  $x = x_1 + 0.5$  &  $y = y_1 + 0.5$
- vi] for ( $K = 0$ ;  $K < \text{step}$ ;  $K++$ )  
 $x = x + x_{in}$  ;  $y = y + y_{in}$   
 $\text{put pixel}(x, y)$

y

(i) straight  
(ii) diagonal

## 2. Program to draw line Using DDA algorithm

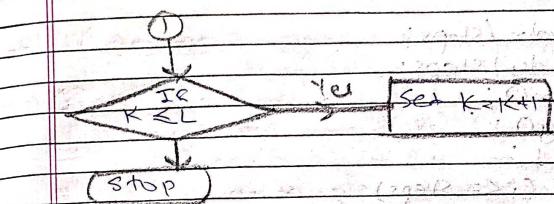
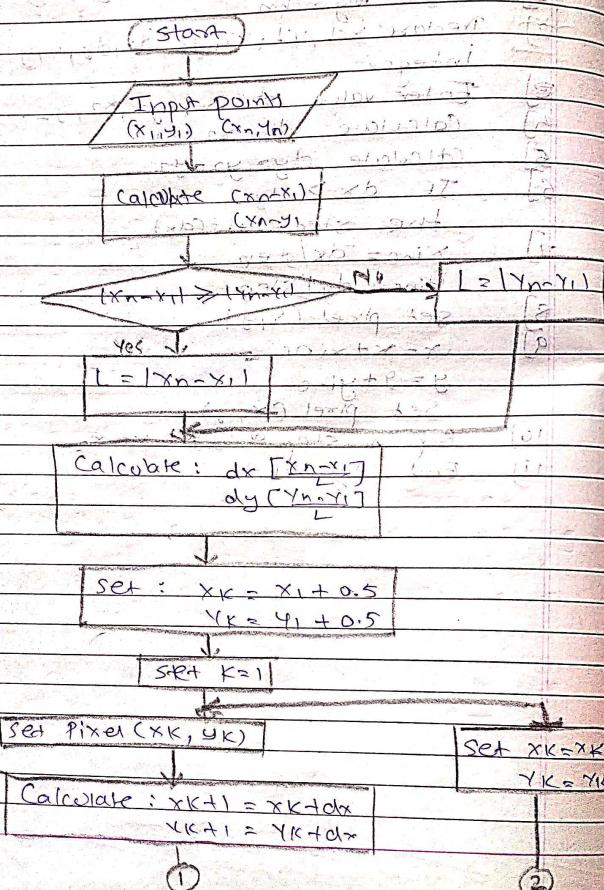
### Procedure:

- i) Read the input of the 2 end points of the line as  $(x_1, y_1)$  &  $(x_2, y_2)$  such that  $x_1 \neq x_2$  and  $y_1 \neq y_2$
- ii) Calculate  $dx = x_2 - x_1$  and  $dy = y_2 - y_1$
- iii) If  $(dx >= dy)$   
    step =  $dx$   
    else  
        step =  $dy$
- iv)  $x_{in} = dx / step$  &  $y_{in} = dy / step$
- v)  $x = x_1 + 0.5$  &  $y = y_1 + 0.5$
- vi) For ( $K = 0$ ;  $K < step$ ;  $K++$ )  
 $x = x + x_{in}$   
 $y = y + y_{in}$   
put pixel  $(x, y)$

### \* Algorithm:

- 1] Start Algorithm
- 2] Declare  $x_1, y_1, x_2, y_2, dx, dy, x, y$  as integer
- 3] Enter value of  $x_1, y_1, x_2, y_2$ .
- 4] calculate  $dx = x_2 - x_1$
- 5] calculate  $dy = y_2 - y_1$
- 6] If  $dx > dy$   
    then step =  $abs(dx)$
- 7]  $x_{inc} = dx / step$   
 $y_{inc} = dy / step$
- 8] set pixel  $(x, y)$
- 9]  $x = x + x_{inc}$   
 $y = y + y_{inc}$   
Set pixel  $(x, y)$
- 10] Repeat step 9 until  $x = x_2$
- 11] End Algorithm.

→ Flowchart:



\* C-Code

```

#include <graphics.h>
#include <conio.h>
#include <stdio.h>
Void main()
{
    gd = DETECT, gm;
    float x, y, dx, dy, steps;
    int x0, x1, y0, y1;
    initgraph(&gd, &gm, "C:\ITC\IBGT");
    setbkcolor(WHITE);
    x0 = -100, y0 = 200, x1 = 500, y1 = 300;
    dx (float) (x1 - x0);
    dy (float) (y1 - y0);
    if (dx) == dy)
    {
        if (steps == dx); // if steps = dx, then x = x0 + dx
        else
            steps = dy;
    }
}
    
```

y

steps = dy;

```

 $dx = dx / \text{steps};$ 
 $dy = dy / \text{steps};$ 
 $x = x_0;$ 
 $y = y_0;$ 
 $i = 1;$ 
while ( $i \leq \text{steps}$ )

```

```

    putpixel(x, y, red);
    x += dx;
    y += dy;
    i++;
getch();
closegraph();

```

### \* Practical Related Question on Rasterization

- 1] Define the term Rasterization.
- Rasterization is the task of taking an image described in a graphics format and converting it into a raster image  $(x \times h)$ .

- 2] Write slope intercept form of a line
- Slope intercept form of a line -
- $$y = mx + b$$

$m$  = slope of line

$b$  = y intercept of line

```
Enter the value of x1 and y1 : 100  
100  
Enter the value of x2 and y2: 150  
150
```



3) Write advantages and disadvantages of DDA Algorithm.



### Advantages:

- 1) It is a simple Algorithm
- 2) It is easy to implement.
- 3) Avoid using multiplication which is costly in term of time complexity.

### Disadvantages:

- 1) Points generated are not accurate.
- 2) Resulted lines are not smooth.
- 3) There is an increase in time complexity because of round off function.



### Conclusion:

- i) In Computer Graphics, a digital differential analyzer (DDA) is used for interpolation of variables over an interval between start and end point.
- ii) DDA's are used for rasterization of lines, triangles and polygons.

### \* Exercise

Q) Give following values for every iteration of DDA algorithm to draw a line from (3, 4) to (6, 8).

$$\rightarrow \begin{aligned} x_1 &= 3, y_1 = 4 \\ x_2 &= 6, y_2 = 8 \\ dx &= x_2 - x_1 \\ &= 6 - 3 \\ &= 3 \\ dy &= y_2 - y_1 \\ &= 8 - 4 \\ &= 4 \end{aligned}$$

$$dy > dx \text{ so } d = 4 \text{ and } ddx = 1$$

$$ddx = x_2 - x_1 / (dy - dx) \text{ initial}$$

$$d = 4, ddx = 1, ddy = 1, x = 3, y = 4$$

$$ddx = 0.75 \text{ rounded down to 1}$$

$$ddy = y_2 - y_1 / d \text{ rounded down to 1}$$

$$ddy = 4/4 = 1 \text{ rounded down to 1}$$

$$d = 1$$

$$x = 3 + 0.5 = 3.5$$

$$y = 4 + 0.5 = 4.5$$

$$i = 1$$

$$x = 3.5 + 0.75$$

$$= 4.25$$

$$y = 4.5 + 1$$

$$= 5.5$$

$$i = 2$$

$$x = 4.25 + 0.75$$

$$= 5$$

$$y = 5.5 + 1$$

$$= 6.5$$

$$i = 3$$

$$x = 5 + 0.75$$

$$= 5.75$$

$$y = 6.5 + 1$$

$$= 7.5$$

$$i = 4$$

$$x = 5.75 + 0.75$$

$$= 6.5$$

$$y = 7.5 + 1$$

$$= 8.5$$

I	X	Y
1	4.25	5.5
2	5	6.5
3	5.75	7.5
4	6.5	8.5

ii) Give following values of  $x$  every iteration of DDA Algorithm to draw a line from  $(-5, -5)$  to  $(-12, -12)$ .

$$\begin{aligned}x_1 &= -5 & y_1 &= -12 \\x_2 &= -12 & y_2 &= -12 \\dx &= x_2 - x_1 & dy &= y_2 - y_1 \\&= -12 - (-5) & &= -12 - (-5) \\&= -7 & &= 7\end{aligned}$$

$$\begin{aligned}dy &= y_2 - y_1 \\&= -12 - (-5) \\&= -12 + 5 \\&= -7\end{aligned}$$

$$dx < dy \Rightarrow d = 10 + 7 = 17$$

$$dx = x_2 - x_1 \quad d = 17 \\= -12 - (-5) \quad 1 + 2 \cdot 7 = 17 \\= -12 + 5 \quad 2 \cdot 7 = \\= -7$$

$$x = x_1 + \frac{dx}{d} \quad y = y_1 + \frac{dy}{d}$$

$$\begin{aligned}dy &= y_2 - y_1 \\&= -12 - (-5) \\&= -12 + 5 \\&= -7\end{aligned}$$

$$\begin{array}{|c|c|c|} \hline Y & X & T \\ \hline 1 & -5 & 1 \\ \hline 2 & -7 & 2 \\ \hline 3 & -10 & 3 \\ \hline 4 & -12 & 4 \\ \hline \end{array}$$

$$\begin{aligned}x &= 10 + 0 \cdot 5 = 10.5 \\y &= 0 + 0 \cdot 5 = 0.5\end{aligned}$$

i=1

$$\begin{aligned}x &= 10.5 + 1 = 11.5 \\y &= 0.5 + 0 = 0.5\end{aligned}$$

i=2

$$\begin{aligned}x &= 11.5 + 1 = 12.5 \\y &= 0.5 + 0 = 0.5\end{aligned}$$

i=3

$$\begin{aligned}x &= 12.5 + 1 = 13.5 \\y &= 0.5 + 0 = 0.5\end{aligned}$$

i=4

$$\begin{aligned}x &= 13.5 + 1 \\&= 14.5\end{aligned}$$

$$y = 0.5 + 0 = 0.5$$

T	X	Y
1	11.5	0.5
2	12.5	0.5
3	13.5	0.5
4	14.5	0.5

### 3. Program to draw line using Bresenham's algorithm.

#### \* Procedure :

- i) Input the two lines end-point, storing the left endpoint  $(x_0, y_0)$
- ii) Plot the point  $(x_0, y_0)$
- iii) Calculate the constants  $\Delta x, \Delta y, 2\Delta y$  and  $2(\Delta y - 2\Delta x)$  and get the first value for decision parameter at  $P_0 = 2\Delta y - \Delta x$
- iv) At each  $x_k$  along the line, starting at  $k=0$ , perform following test:  
 If  $p_k \leq 0$  then next point  $(x_{k+1}, y_k)$  and  $p_{k+1} = p_k + 2\Delta y$   
 Otherwise, the next point to plot is  $(x_{k+1}, y_{k+1})$  and  $p_{k+1} = p_k + 2\Delta y - 2\Delta x$
- v) Repeat step 4 ( $\Delta x$ ) times.

#### \* Algorithm :

- 1] Start
- 2] Input the two end-points of line,  
storing the left end-point in  $(x_0, y_0)$
- 3] Plot point  $(x_0, y_0)$
- 4] Calculate constant  $\Delta x, \Delta y, 2\Delta y$  and  $2\Delta y - \Delta x$  and get first value for  $P_0 = 2\Delta y - \Delta x$
- 5] At each  $x_k$  along the line, starting at  $k=0$ , perform following:

If  $p_k < 0$  next point is  $(x_{k+1}, y_k)$   
and  
 $x_{k+1} = p_k + 2dy$

otherwise,  $x_{k+1} = x_k$  and  $y_{k+1} = y_k$

$(x_k, y_{k+1})$  is now add to list

$p_k + 1 = p_k + 2dy - dx$  (if  $d > 0$ )

$p_k + 1 = p_k + 2dy + dx$  (if  $d < 0$ )

5) Repeat step 4 & check Hanoi

6) End

+ Flowchart for midpoint C-Y

Start  
Input  $x_1, y_1, x_2, y_2$   
 $x = x_1$   
 $y = y_1$   
 $\Delta x = \text{abs}(x_2 - x_1)$   
 $\Delta y = \text{abs}(y_2 - y_1)$   
 $S_1 = \text{Sign}(x_2 - x_1)$   
 $S_2 = \text{Sign}(y_2 - y_1)$

Interchange = No  
IF  $\Delta y > \Delta x$

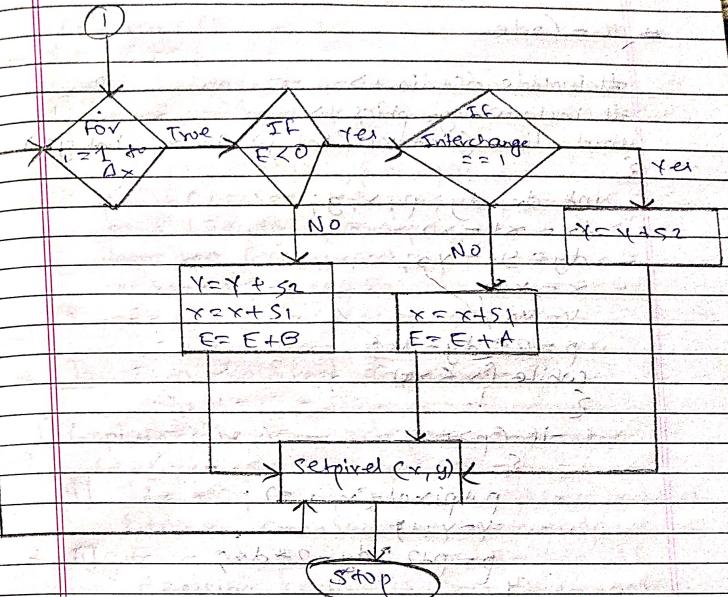
then  $E = 2\Delta y - \Delta x$  Interchange = Yes

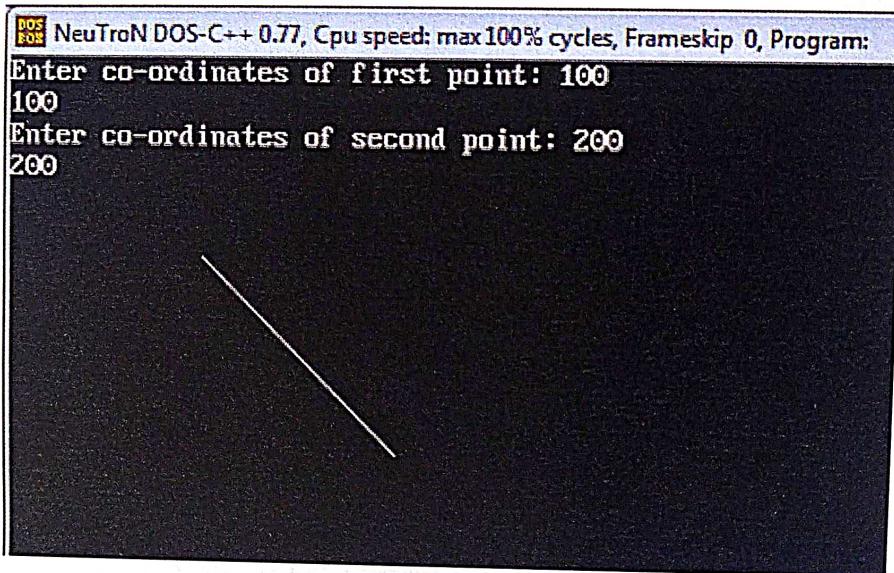
$A = 2\Delta y$   $B = -\Delta x$

$B = 2\Delta y - \Delta x$

Plot  $(x, y)$   $x = x_1$   $y = y_1$

Interchange = 1





## 2 C - Code

```
#include <stdio.h>
#include <graphics.h>
Void line( int x0, int y0, int x1, int y1)
{
    int dx, dy, p, x, y;
    dx = x1 - x0;
    dy = y1 - y0;
    x = x0;
    y = y0;
    p = 2 * dy - dx;
    while (x < x1)
    {
        if (p >= 0)
        {
            putpixel(x, y, 7);
            y = y + 1;
            p = p + 2 * dy - 2 * dx;
        }
        else
        {
            putpixel(x, y, 7);
            p = p + 2 * dy;
            y = y;
            x = x + 1;
        }
    }
}
```

```
int main()
```

```
    int gd = Detect(), mode = norm, x0, y0, x1, y1;
    initgraph(&gd, &mode, "C:\TURBO\BGI");
    printf("Enter 1st point:");
    scanf("%d,%d", &x0, &y0);
    printf("Enter 2nd point:");
    scanf("%d,%d", &x1, &y1);
    drawline(x0, y0, x1, y1);
    return 0;
```

## → Practical Related Questions

1] Explain the term decision parameter.

→ i] It is a criteria based on which further calculations are made.

ii] Ex. in bresenham algorithm if decision factor is  $> 0$  then action

is taken to place else not.

2] State advantages of Bresenham's algorithm over DDA.

→ i] Easy to Implement

ii] Fast and incremental

iii] More Accurate points than DDA

iv] Uses Fixed points only.

\* Exercise

i) Give following values for every iteration of Bresenham's algorithm to draw a line from (3, 4) to (6, 8)

$$\begin{aligned} x_1 &= 3, y_1 = 4 \\ x_2 &= 6, y_2 = 8 \\ \Delta x &= 3 \\ \Delta y &= 4 \end{aligned}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - 4}{6 - 3} = \frac{4}{3} = 1.3$$

$$p_k = 8 - 3 = 5$$

$$x_k, y_k \rightarrow p_k, x_{k+1}, y_{k+1}$$

$$\textcircled{1} \quad x_k, y_k \text{ and } p_k \text{ with } x_{k+1}, y_{k+1}$$

$$\textcircled{2} \quad (5, 6) \quad 4 \quad (6, 8)$$

$$\textcircled{3} \quad (5, 7) \quad 4 \quad (6, 8)$$

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ii) Given following values for every iteration of Bresenham's algorithm to draw a line from (-6, -6) to (-14, -14)

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-14 - (-6)}{-14 - (-6)} = \frac{-8}{-8} = 1$$

$$\Delta x = -8, \Delta y = -8$$

$$\Delta y = -16, 2\Delta y = -16$$

$$p_k = 7, p_{k+1} = -8$$

$$(5, -6) \quad 0 \quad (1, -5) \quad (1)$$

$$\textcircled{1} \quad (-6, -6) \quad 0 \quad (-8) + (-6) + 7 = (-6, -5) + 7 \\ p_{k+1} = -8 + (-16) - (-16) = -24$$

$$\textcircled{2} \quad (-6, -5) \quad -24 \quad (-6, -4) \\ p_{k+1} = -24 + (-16) - (-16) = -40$$

$$\textcircled{3} \quad (-6, -4) \quad -40 \quad (-6, -3) \\ p_{k+1} = -40 + (-16) - (-16) = -56$$

$$\textcircled{4} \quad (-6, -3) \quad -56 \quad (-6, -2) \\ p_{k+1} = -56 + (-16) - (-16) = -72$$

$$\begin{aligned}
 \textcircled{4} \quad & (-6, -2) \quad -12 \quad (-6, -1) \\
 p_k + 1 & = -72 + (-16) - (-16) + (-6 - (-6)) \\
 & = -88
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{5} \quad & (-6, -1) \quad -88 \quad (-6, 0) \\
 p_k + 1 & = -88 + (-16) - (-6) - (-6 - (-6)) \\
 & = -104
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{6} \quad & (-6, 0) \quad -104 \quad (-6, 1) \\
 p_k + 1 & = -104 + (-16) - (-8) - (-6 - (-6)) \\
 & = -120
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{7} \quad & (-6, 1) \quad -120 \quad (-6, -2) \\
 p_k + 1 & = -120 + (-16) - (-16) - (-6 - (-6))
 \end{aligned}$$

### Assessment Scheme

$$\begin{aligned}
 & \text{Omkar Savant} - 100 \\
 & \text{Akshara Raut} - 100
 \end{aligned}$$

### 4. Program to draw Circle

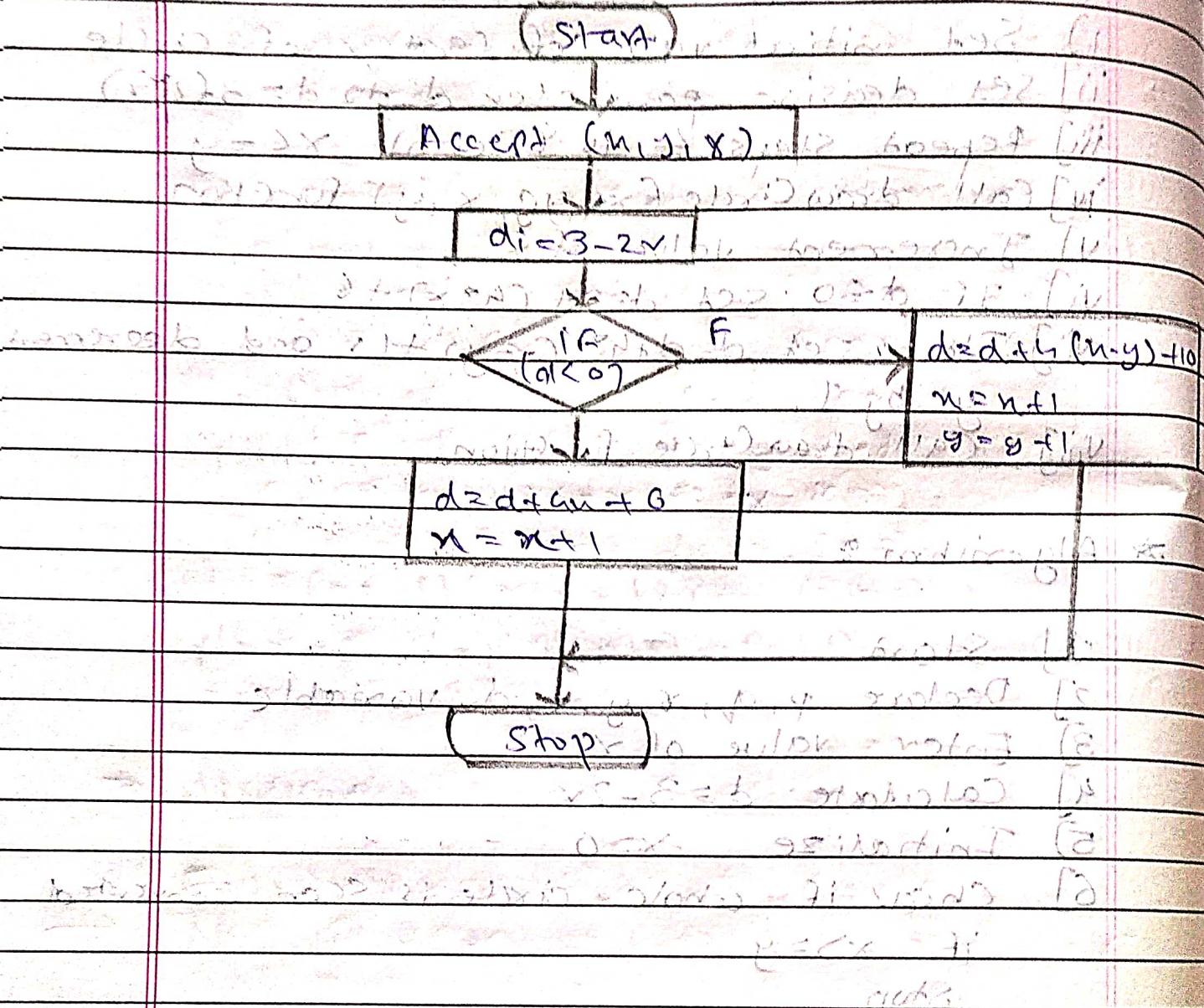
#### Procedure :

- i) Set initial value of center of circle
- ii) Set decision parameter  $d$  to  $d = 3 - 2r$
- iii) Repeat steps 4 to 8 until  $x = y$
- iv) Call drawCircle( $x_c, y_c, x, y$ ) function
- v) Increment value of  $x$
- vi) If  $d < 0$ , set  $d = d + (4x) + 6$
- vii) Else, set  $d = d + 4x + 4y + 10$  and decrease  $y$  by 1.
- viii) Call drawCircle function.

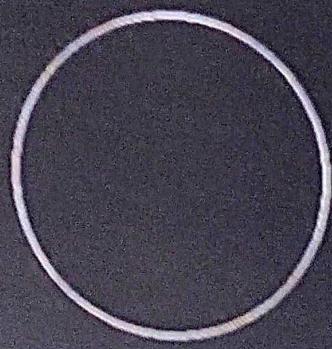
#### Algorithm :

- 1] Start
- 2] Declare  $p, q, x, y, r, d$  variable
- 3] Enter value of  $r$
- 4] Calculate  $d = 3 - 2r$
- 5] Initialize  $x = 0$
- 6] Check if whole circle is scan converted  
if  $x > y$   
Stop
- 7] Plot eight points by eight-way symmetry
- 8] Find location of next pixel to be scanned
- 9] Go to step 6
- 10] Stop

## Flowchart



**CIRCLE Using Graphics In C**



## \* C - Code :

```
#include <graphics.h>
#include <stdio.h>
void pixel(int xc, int yc, int x, int y);
int main()
{
    int gd, gm, xc, yc, x, y, p;
    initgraph(&gd, &gm, "C:\TURBO\BGI");
    printf("Enter Center of circle:");
    scanf("%d%d", &xc, &yc);
    printf("Enter radius of circle:");
    scanf("%d", &r);
    x = 0;
    y = r;
    p = 3 - 2 * r;
    pixel(xc, yc, x, y);
    while ((x < y))
    {
        if (p < 0)
            x++;
        else
            y--;
        p = p + 4 * x + 6;
    }
    if (y != 0)
        y--;
    p = p + 4 * (x - y) + 10;
    pixel(xc, yc, x, y);
}
```

4) ~~getch();~~  
~~closegraph();~~  
~~return 0;~~  
 void pixel (int xc, int yc, int x, int y)  
 {  
 putpixel (xc+x, yc+y, Red);  
 putpixel (xc+y, yc-x, Red);  
 putpixel (xc-x, yc+y, Red);  
 putpixel (xc-y, yc-x, Red);  
 putpixel (xc+x, yc+y, Red);  
 putpixel (xc+y, yc+x, Red);  
 putpixel (xc-x, yc+x, Red);  
 putpixel (xc-y, yc-x, Red);  
 }

- \* Practical Related Questions
- 1] Write equation of a circle.  
→ The equation of circle is  $x^2 + y^2 = r^2$
- 2] Write algorithm to draw 8-way symmetry of Circle  
→
- 1] Start
- 2] Declare p, q, x, y, r, d variable
- 3] Enter value of x, y, r  
4] Calculate  $d = 3 - 2x$

- 5) Initialize  $x = 0$   
 6) Check if whole circle is scan converted  
 7) Plot eight point by using concepts of eight-way symmetry  
 8) Find location of next pixel to be scanned.  
 a) Go to step 6.  
 b) Stop  
 → How the value of decision parameter (d) is calculated.  

$$d = 3 - 2x$$
  
 (where)  $x = (3 - d)$   
 (i) d = decision parameter  
 $r = \text{radius.}$

#### \* Conclusion

There are two popular algorithm for generating a circle -> Bresenham's Algorithm and Midpoint Circle Algorithm.

These algorithm are based on the idea of determining the subsequent points required to draw the circle.

### \* Exercise

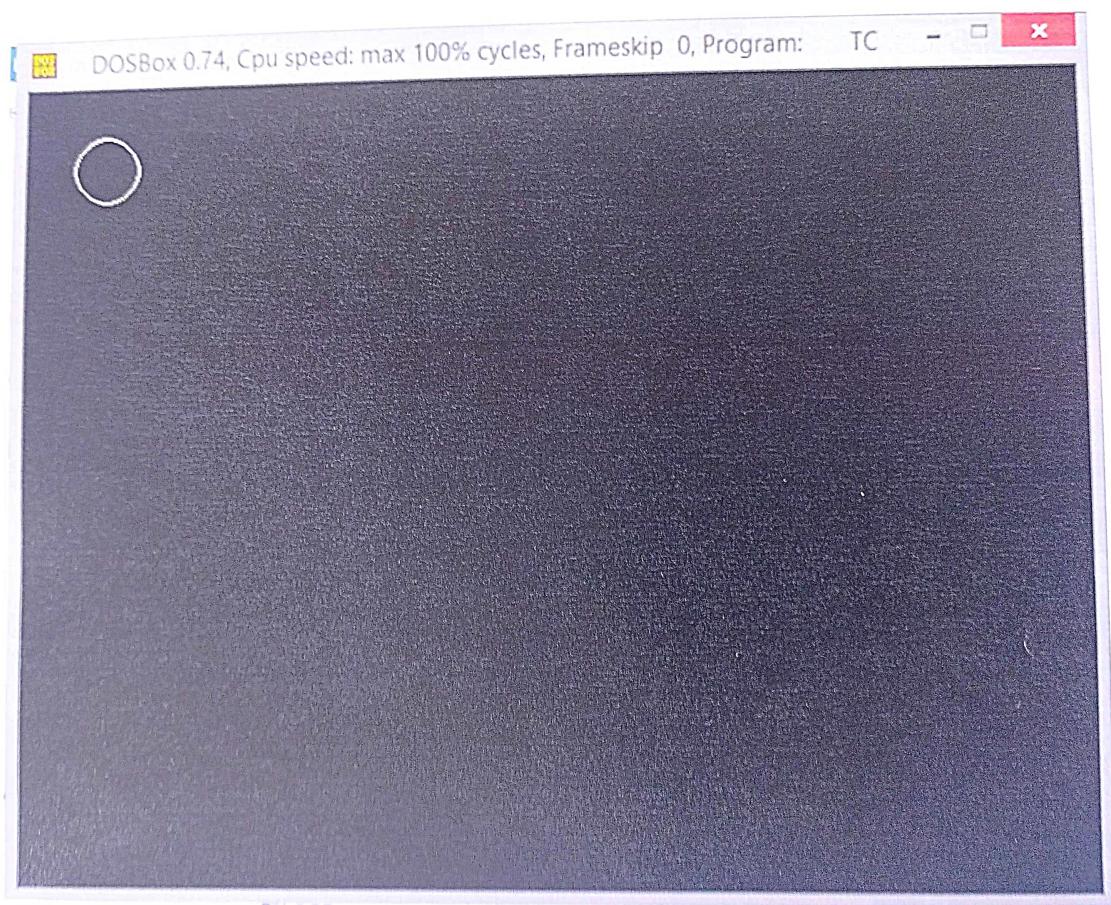
- 1) Calculate pixel for circle with radius 10 using Bresenham's Algorithm.



$P_k$	$P_{k+1}$	$(x_{k+1}, y_{k+1})$	$(x_{plot}, y_{plot})$
		$(0, 10)$	$(10, 20)$
-17	-7	$(1, 10)$	$(11, 20)$
-7	7	$(2, 10)$	$(12, 20)$
7	-7	$(3, 9)$	$(13, 19)$
-7	15	$(4, 9)$	$(14, 19)$
15	13	$(5, 8)$	$(15, 18)$
-13	19	$(6, 7)$	$(16, 17)$

- 2) Draw a circle with center  $(50, 50)$  and radius 20 by using Bresenham's Algorithm.

→ ~~multicolumn values must be 0 and 1~~



## 5. Program to fill polygon.

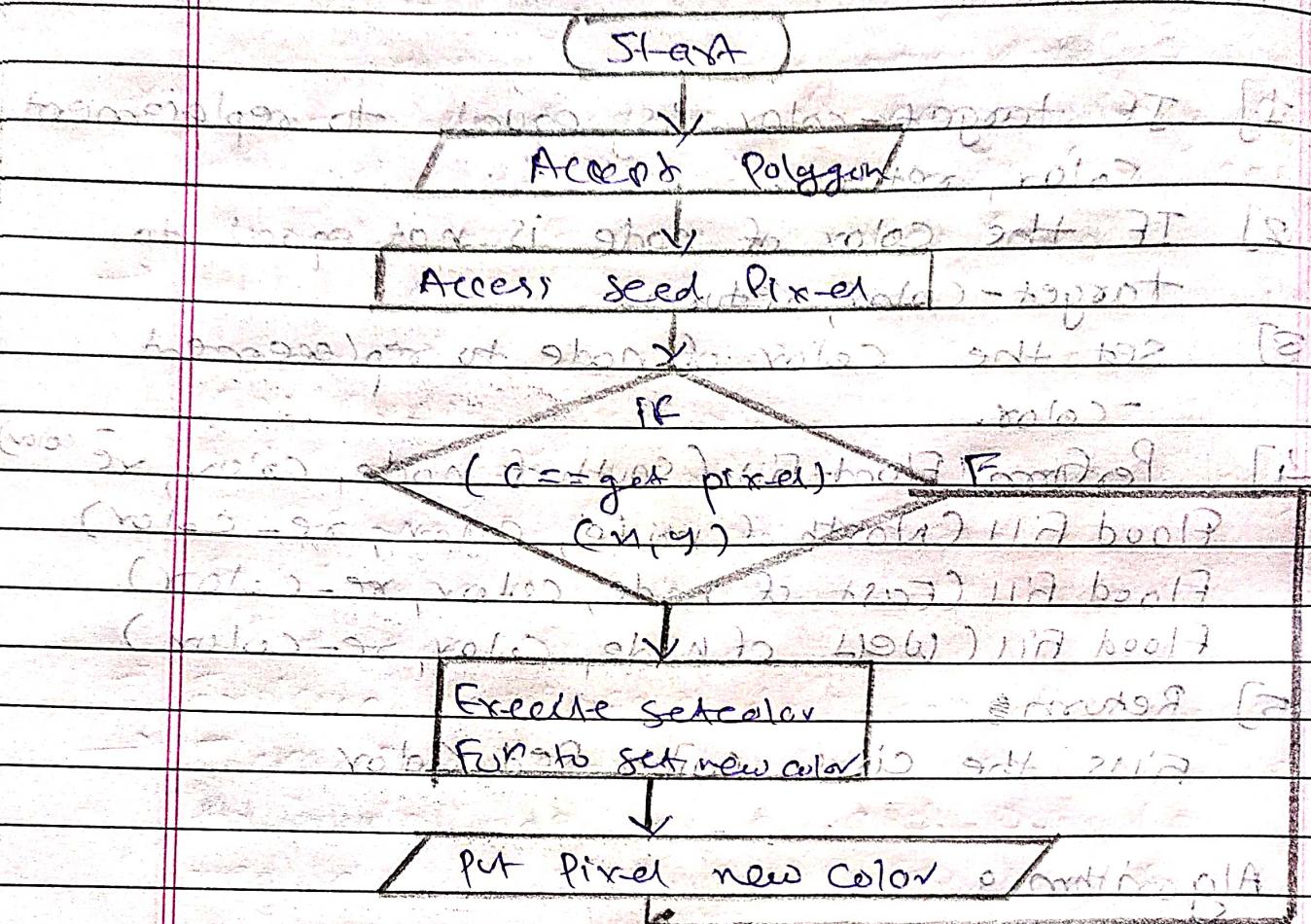
### \* Procedure :

- 1] IF target-color is equal to replacement color, return.
  - 2] IF the color of node is not equal to target-color, return.
  - 3] Set the color of node to replacement color.
  - 4] Perform Flood Fill (South of node, color, re-color)  
 Flood Fill (North of node, color, re-color)  
 Flood Fill (East of node, color, re-color)  
 Flood Fill (West of node, color, re-color)
  - 5] Return.
- Fills the circle with Red Color.

### \* Algorithm :

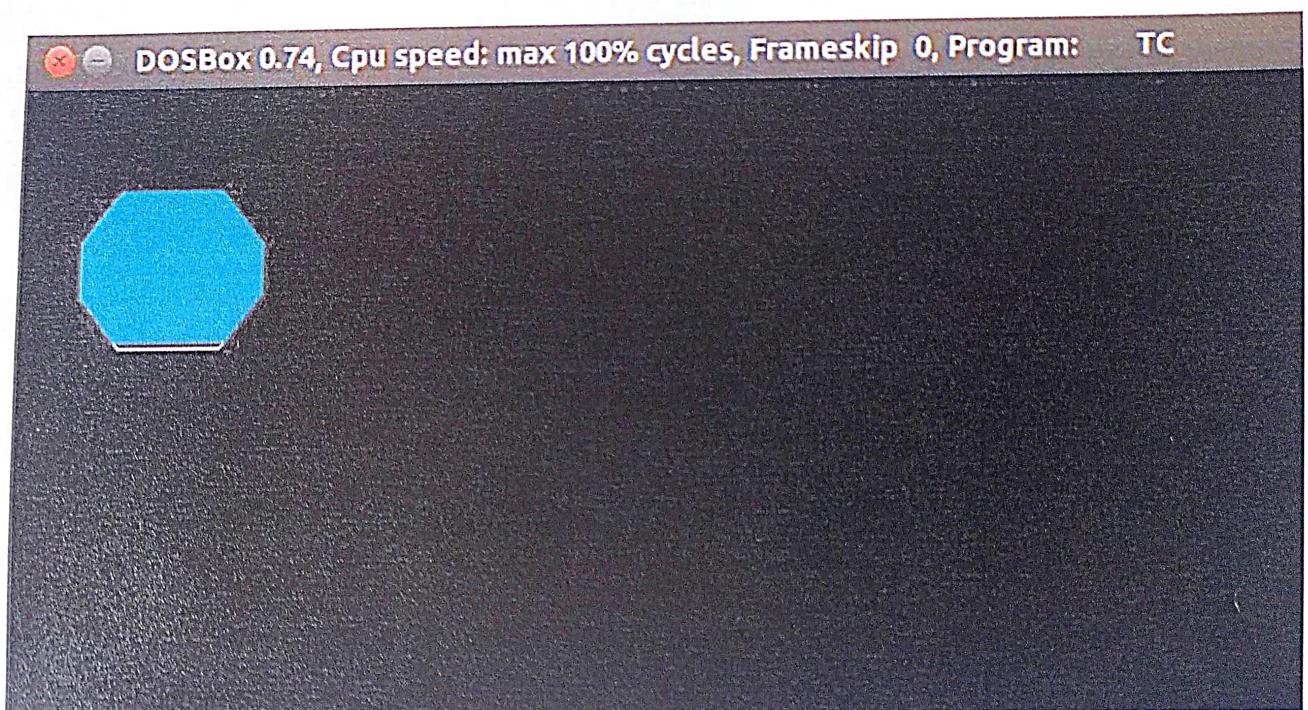
- 1] Initialize the value of seed point
- 2] Define the boundary values of polygon.
- 3] Check if the current seed point is of default color, then repeat steps 4 and 5 till the boundary pixels reached.
- 4] Change the default color with the fill color at the seed point.
- 5] Recursively follow the procedure with four neighbourhood points.
- 6] Exit.

## Flowchart



Flowchart for seed pixel coloring:

- Start**
- Check if seed pixel is black.
- If yes, set pixel to white and update neighbors.
- If no, set pixel to black and update neighbors.
- End**



## \* Practical Related Questions:

1) Define polygon.

→ A polygon is a plane figure with at least three straight sides and angles.

2) Explain types of polygon.

i) Regular Polygon:

A regular polygon has equal length sides, with equal angles between each side.

ii) Irregular Polygon:

It has unequal length sides and unequal angles between sides.

3) List coordinates of neighboring pixels in 8-connected method for seed pixel with coordinates  $(x, y)$ .

Putpixel  $(x, y, \text{color})$ ;

Fill  $(x-1, y, \text{color})$ ;

Fill  $(x+1, y, \text{color})$ ;

Fill  $(x, y-1, \text{color})$ ;

Fill  $(x, y+1, \text{color})$ ;

Fill  $(x+1, y+1, \text{color})$ ;

Fill  $(x-1, y+1, \text{color})$ ;

~~Fill(x-1, y-1, color);  
Fill(x+1, y+1, color);~~

4) List coordinates of neighbouring pixels in 4-connected method for seed pixel with co-ordinates  $(x,y)$ .

```
Putpixel(x,y,color);  
Fill(x+1,y,color);  
Fill(x,y+1,color);  
Fill(x-1,y,color);  
Fill(x,y-1,color);
```

5) Explain Inside-outside test of polygon.  
→ The Inside - outside test is used to find the inside and outside region of a polygon. Boundary fill is a recursive algorithm.

\* Conclusion Exercise (on [Lecture 2](#)) - 2

1] WAP to draw hexagon and fill hexagon with pink color using Flood Fill algorithm with 8-Connected method.

```
#include <stdio.h>
#include <graphics.h>
#include <conio.h>
```

void fill (int x, int y, int old, int new)

Int current : -

$\text{Ccurrent} = \text{getpixel}(Cx, Cy);$   
IE  $C_{x,y}$

If  $C_{\text{current}} = \text{old}_2$ , then  $\text{subscript} = 1$   
If  $C_{\text{current}} = \text{old}_1$ , then  $\text{subscript} = 2$

delay(5);

papixel(x,y,new);  
    Fill(x+1,y,old,new);

```
fill(x-1+y, old, new);  
fill(x+1+y, old, new);
```

~~fill(x,y-1,old,new);  
fill(x,y-1,old,new);~~

$\text{fill}(x+1, y+1, \text{old}, \text{new});$   
 $\text{fill}(x-1, y-1, \text{old}, \text{new});$

$\text{fill}(x-1, y-1, \text{old}, \text{new})$ ;  $\text{fill}(x+1, y-1, \text{old}, \text{new})$

fill(x-1, y+1, old, new);

then my work will begin to make your house

Void main(char \*c, int n) {  
 for (i = 0; i < n; i++) {  
 if (c[i] == '\n' || c[i] == '\r')  
 cout << "\n" << "\r";  
 else cout << c[i];  
 }  
}

int gd = DETECT, gm;

```
int graph (4 gd, 4 gm, "c:\1\1C371BGI");  
int a[5][300][150];
```

int arr[300, 150, 400, 750, 1350,

drawPoly(6, arr);

Floods((70,70,0,15),  
getch());

geton();  
closegraph();

3

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→ 5) Write a program to draw a triangle and fill it with blue color using flood fill algorithm with 4-connected method.

```
#include <stdio.h>
#include <graphics.h>
#include <conio.h>
void Fill(int, int, int, int);
Void main()
{
    int gd=DETECT, gm;
    initgraph(&gd, &gm, "C:\TURBO C\BGI");
    Triangle(120, 200, 120);
    Flood(55, 85, 10, 0);
    getch();
}
```

```
Void Fill(int x, int y, int new, int def)
{
    If (getpixel(x,y) == def)
        New = 1;
    Else
        New = 0;
    If (New == 1)
        Setpixel(x, y, new);
    Fill(x+1, y, new, def);
    Fill(x, y+1, new, def);
    Fill(x-1, y, new, def);
    Fill(x, y-1, new, def);
}
```

#### Conclusion:

Polygon is a chain of connected line segments. For filling polygons with particular colors, you need to determine the pixels falling on the border of the polygon and those which fall inside polygon.

#### Assessment Scheme:

Omkar Savant  
Atharva Rastogi

## 6. Program to Fill Polygon using boundary fill algorithm.

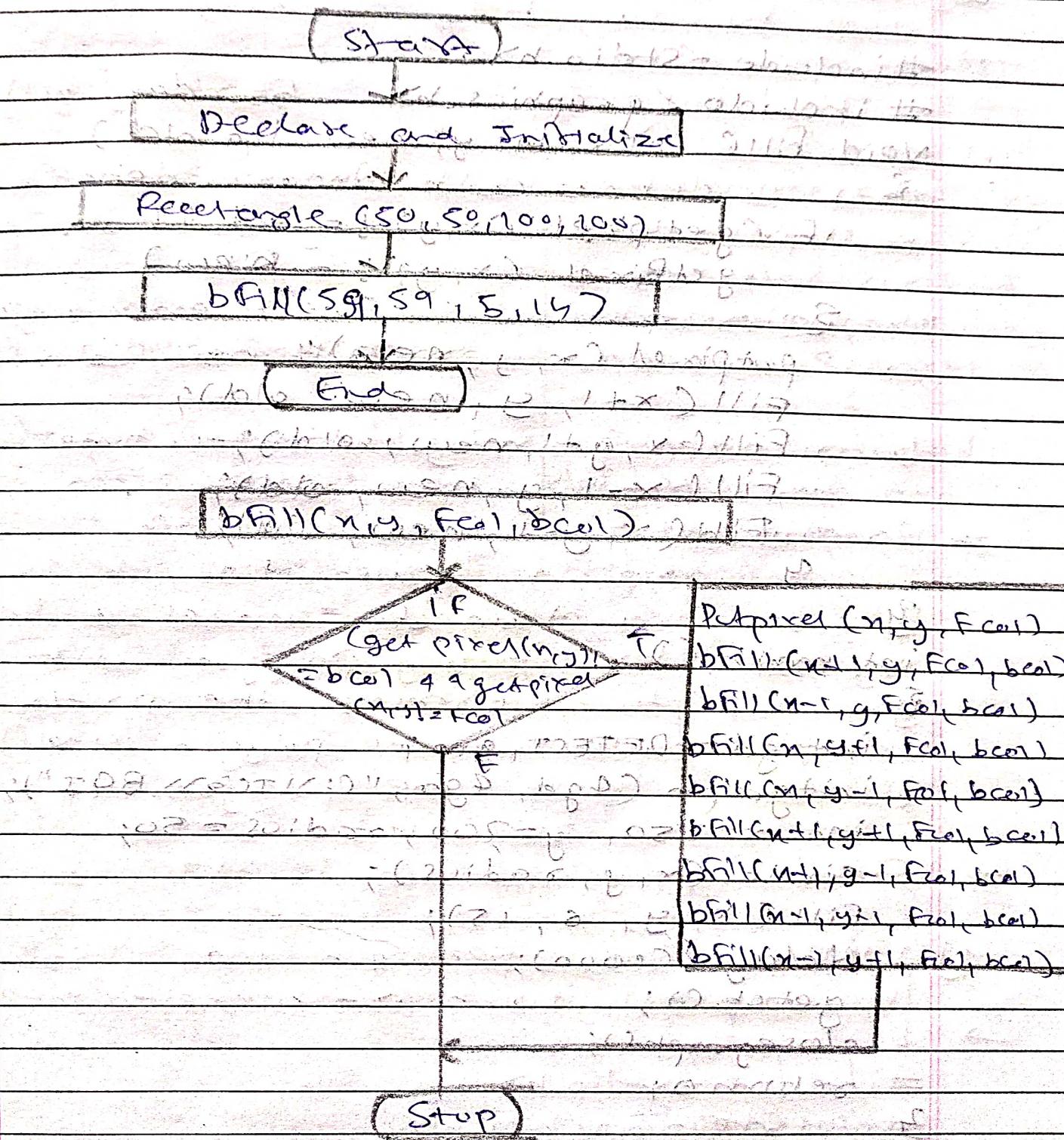
### \* Procedure :

- 1] Initialize the value of seed point.
- 2] Define the boundary values of polygon
- 3] Check if the current seed point is of default color, then ~~the~~ repeat the steps 4 and 5 till the boundary pixel reached.
- 4] Change the default color with the fill color at seed point.
- 5] Recursively follow the procedure with four neighbourhood points.
- 6] Exit.

### \* Algorithm :

- 1] Initialize the value of seed point.
- 2] Define the boundary value of polygon.
- 3] Check if the current seed point is of default color, then ~~the~~ repeat the steps 4 and 5 till boundary fill is reached.
- 4] Change the default color with the fill color at seed point.
- 5] Recursively follow the procedure with four neighbourhood points.
- 6] Exit.

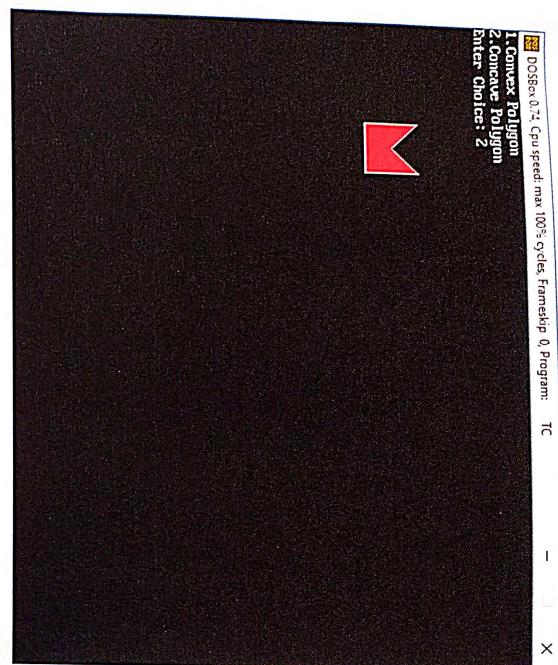
## \* Flowchart 8



\* Code :-

```
#include <stdio.h>
#include <graphics.h>
Void Fill( int x, int y, new, int old )
{
    If (getpixel(x,y) != old)
        getpixel(x,y) = old;
    putpixel(x,y, new);
    Fill(x+1, y, new, old);
    Fill(x, y+1, new, old);
    Fill(x-1, y, new, old);
    Fill(x, y-1, new, old);
}

int main()
{
    initgd = DETECT, gm;
    initgraph(&gd, &gm, "C:\TC3\BGI");
    int x=250, y=200, radius = 50;
    circle(x, y, radius);
    Fill(x, y, 6, 15);
    delay(1000);
    getch();
    closegraph();
    return 0;
}
```



## Practical Related Questions

1) Compare 4-connected and 8-connected methods to fill polygon.



### 4-connected

4-connected method, is where a pixel may have upto four neighbour.

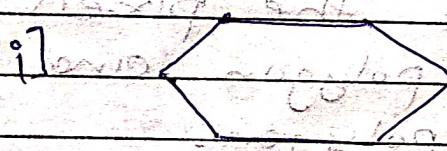
The pixels do not define a region since several pixels such as A and B are not connected.

### 8-connected

8-connected method, is where a pixel may have upto 8 neighbours.

Using 8-connected definition we can identify a specific region.

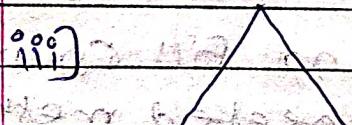
2) Identify type of polygon in following.



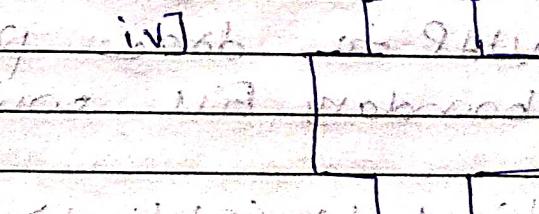
→ Hexagon  
— Regular



→ Irregular



→ Regular



→ Irregular

Q) Give basic difference between flood fill and boundary fill.



Flood Fill

Area is defined with multiple colors.

The interior is colored with any color.

It is time consuming.

\* Conclusion:

Boundary Fill

Area is defined with single color.

The interior is replaced with new color.

It is less time consuming.

Polygon is a chain of connected line segments. For filling polygon with color, you need to determine the pixels falling on the border of the polygon and those which fall inside the polygon.

\* Exercise.

Q) WAP to draw pentagon and fill color using boundary fill with 8-connected method.



```
#include <stdio.h>
```

```
#include <graphics.h>
```

3) (Five basic differences between Flood Fill and boundary Fill.)



### Flood Fill

Area is defined with multiple colors.

### Boundary Fill

Area is defined with single color.

The interior is colored. The interior is replaced with any color.

It is time consuming.

\* Conclusion:

Polygon is a chain of connected line segments. For filling polygon with color, you need to determine the pixels falling on the border of the polygon and those which fall inside the polygon.

\* Exercise.

1] WAP to draw pentagon and fill color using boundary fill with 8-connected method.



```
#include <stdio.h>
#include <graphics.h>
```

### Boundary Fill

Area is defined with single color.

The interior is colored. The interior is replaced with any color.

It is time consuming.

\* Conclusion:

Polygon is a chain of connected line segments. For filling polygon with color, you need to determine the pixels falling on the border of the polygon and those which fall inside the polygon.

```
Void fill(int x, int y, int new, int old)
```

```
{ if (getpixel(x,y) != old || getpixel(x,y) != new)
```

```
{
```

```
putpixel(x,y,new);
```

```
fill(x+1,y,new,old);
```

```
fill(x,y+1,new,old);
```

```
fill(x-1,y,new,old);
```

```
fill(x,y-1,new,old);
```

```
fill(x+1,y+1,new,old);
```

```
fill(x-1,y+1,new,old);
```

```
fill(x+1,y-1,new,old);
```

```
fill(x-1,y-1,new,old);
```

```
}
```

```
3 int main()
```

```
{
```

```
int gd=DETECT, gm;
```

```
initgraph(gd, gm, "C:\TC3\BGI");
```

```
int arr[4][4]={{120, 100, 240, 720}, {120, 720, 720, 120}}
```

```
drawpoly(5, arr);
```

```
fill(55, 55, 4, 15);
```

```
delay(10000);
```

```
getch();
```

```
closegraph();
```

```
return 0;
```

```
}
```

- 2) Write a program to draw trapezoid  
and fill it using boundary fill with  
B - connected method.

```
#include <stdio.h>
#include <graphics.h>
Void Fill (int x, int y, int new, int old)
{
    if (getpixel (x, y) != old) {
        getpixel (x, y) = new;
        putpixel (x, y, new);
        Fill (x+1, y, new, old);
        Fill (x, y+1, new, old);
        Fill (x-1, y, new, old);
        Fill (x, y-1, new, old);
    }
}
int main()
{
    Point gdev DETECT, gm;
    initgraph (&gdev, &gm, "C:\VTC\BGI");
    int arr = [100, 10, 350, 240, 100];
    draw poly (5, arr);
    fill (x, y, 6, 15);
    delay (1000);
    getch();
    closegraph();
    return 0;
}
```

## 7. Program for two dimensional transformations (translation and scaling)

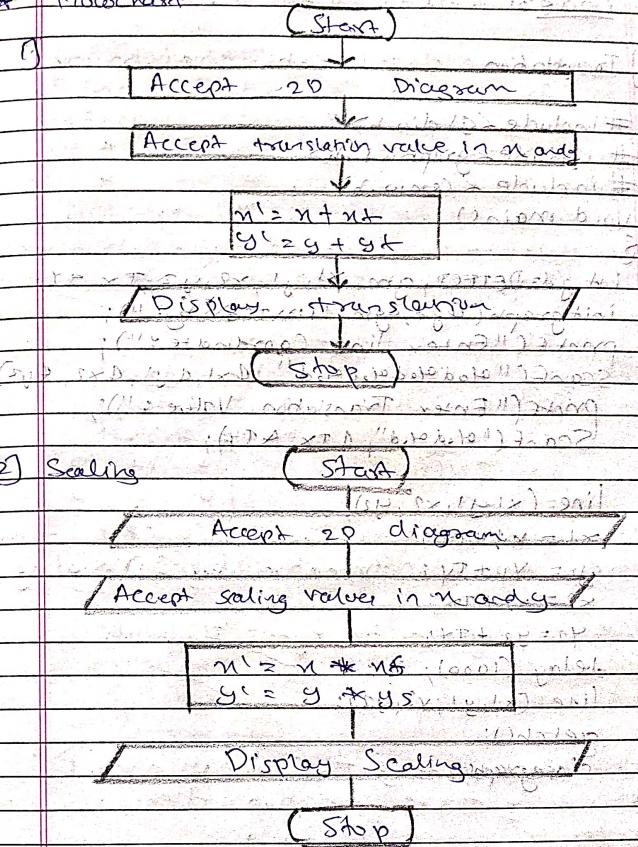
\* Procedure:

- 1] Start
- 2] Input object co-ordinate
- 3] For Translation
  - a] Enter translation factor
  - b] Move the original co-ordinate to a new position.
  - c] Display the object after translation
- 4] For Scaling
  - a] Input the scaled factor
  - b] Transform the co-ordinate
  - c] Display the object after scaling
- 5] Stop.

\* Algorithm.

- 1] Start
- 2] Input object coordinate
- 3] For Translation:
  - a] Enter translation factor
  - b] Move original to new position
  - c] Display translated object.
- 4] For Scaling:
  - a] Input Scaling factor
  - b] Scale the coordinate
  - c] Display scaled object
- 5] Stop.

\* Flowchart



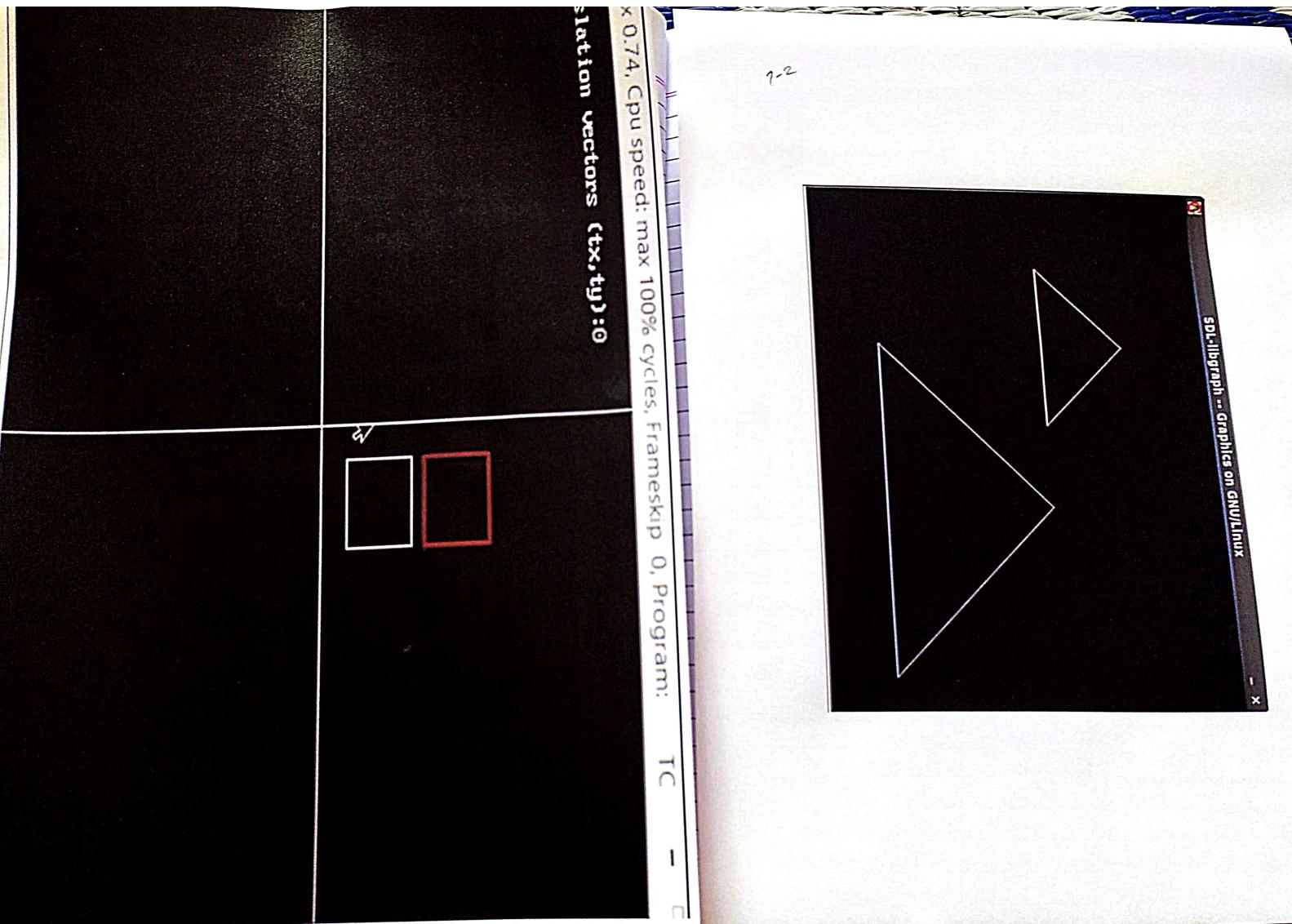
### \* Code:

```
i) Translation  
#include <stdio.h>  
#include <graphics.h>  
#include <conio.h>  
Void main()  
{  
    int gd=DETECT, gm, x1,y1,x2,y2, Tx, Ty;  
    initgraph(gd,gm, "C:\TURBO\BGI");  
    printf("Enter Line Co-ordinates : ");  
    scanf("%d%d%d%d", &x1,&y1, &x2,&y2);  
    printf("Enter Translation Value : ");  
    scanf("%d%d", &Tx, &Ty);  
  
    line(x1,y1,x2,y2);  
    x1 = x1 + Tx;  
    y1 = y1 + Ty;  
    x2 = x2 + Tx;  
    y2 = y2 + Ty;  
    delay(1000);  
    line(x1,y1,x2,y2);  
    getch();  
    closegraph();
```

3

### ii) Scaling

```
#include <stdio.h>  
#include <graphics.h>  
#include <conio.h>  
Void main()  
{  
    int gd=DETECT, gm, x1,y1,x2,y2;  
    int Tx, Ty;  
    initgraph(gd,gm, "C:\TURBO\BGI");  
    clrscr();  
    printf("Enter Co-ordinates : ");  
    scanf("%d%d%d%d", &x1, &y1, &x2, &y2);  
    printf("Enter Scaling Value : ");  
    scanf("%d", &Tx);  
    rectangle(x1,y1,x2,y2);  
    x1 = x1 * Tx;  
    y1 = y1 * Tx;  
    x2 = x2 * Tx;  
    y2 = y2 * Tx;  
    delay(1000);  
    rectangle(x1,y1,x2,y2);  
    getch();  
    closegraph();
```



\* Practical related questions:

1) Write the transformation matrix for

→ 2D Translation.

$$x' = x + t_x$$

$$y' = y + t_y$$

The pair  $(t_x, t_y)$  is called translation vector.  
The above equation can also be represented as:

$$P = \begin{bmatrix} x \\ y \end{bmatrix}, P' = \begin{bmatrix} x' \\ y' \end{bmatrix}, T = \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

$$\text{and } P' = P + T$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

→ 2) Write the transformation for 2D scaling.

$$\begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

→ 3) What does scaling transformation do?

→ A scaling transformation alters size of an object.

→ 1) Whether size of object remains same or changed in case of translation?  
→ The size remains in translation.

\* Conclusion:

Transformation are one of the primary vehicles used in Computer graphics used to manipulate 2D and 3D objects.

\* Exercise

1) Translate the polygon with co-ordinates  $A(2, 5), B(7, 10)$  and  $C(10, 25)$  by 3 units in  $x$  direction and 4 units in  $y$  direction.

$$\begin{array}{|c|c|c|} \hline & 2 & 5 & 1 \\ \hline & 7 & 10 & 1 \\ \hline & 10 & 2 & 1 \\ \hline \end{array} \quad \begin{array}{|c|c|c|} \hline & 1 & 0 & 0 \\ \hline & 0 & 1 & 0 \\ \hline & t_x & t_y & 1 \\ \hline \end{array}$$

$$\begin{array}{|c|c|c|} \hline & 2 & 5 & 1 \\ \hline & 7 & 10 & 1 \\ \hline & 10 & 2 & 1 \\ \hline \end{array} \quad \begin{array}{|c|c|c|} \hline & P_1 & 0 & 0 \\ \hline & 0 & 1 & 0 \\ \hline & 3 & 4 & 1 \\ \hline \end{array}$$

$$\rightarrow \begin{bmatrix} 5 & 9 & 1 \\ 10 & 14 & 1 \\ 13 & 6 & 1 \end{bmatrix} \quad A(5, 9) \\ B(10, 14) \\ C(13, 6)$$

9) Scale the polygon with coordinates  $A(2, 5)$ ,  $B(7, 10)$  and  $C(10, 2)$  by 2 units in x direction and 3 units in y direction.

			Sx	0	0
2	5	1	0	Sy	10
7	10	1	0	0	10
10	2	1	0	0	10

$\begin{array}{ c c c } \hline & 4 & 10 & 1 \\ \hline 1 & 4 & 20 & 1 \\ \hline 20 & 4 & 1 \\ \hline \end{array}$	$A(4,10)$
	$B(14,20)$
	$C(20,4)$

3) Give a  $3 \times 3$  homogeneous co-ordinate transformation matrix for each of the following translation.

i) Shift the image to the right 3 units

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 2 & 2 \\ 2 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 2 & 2 \\ 5 & 0 & 0 \end{bmatrix}$$

2) Shift the image up 2 units.

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & -2 & 1 \end{pmatrix}$$

10. The following table shows the number of hours worked by 1000 workers in a certain industry.

$$\begin{bmatrix} 1 & -2 & 1 \end{bmatrix}$$

2) Move image down  $\frac{1}{2}$  unit and right 7 units

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0.5 & 1 \end{pmatrix}$$

4) Move image down 2/3 unit and left 4 units

$$\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ -9 & 0.6 & 1 \end{array}$$

## 8. Program for 2 dimensional Translation (Rotation)

\* Procedure :

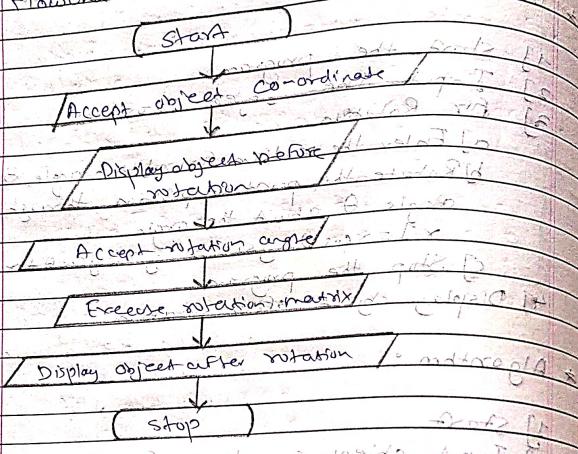
- 1] Start the program
- 2] Input the object coordinate
- 3] For Rotation
  - a] Enter the radian for rotation angle  $\theta$
  - b] Rotate the point at position through an angle  $\theta$  about the origin  

$$x_1 = x \cos \theta - y \sin \theta, y_1 = y \cos \theta + x \sin \theta$$
  - c] Stop the program.
- 4] Display object after rotation.

\* Algorithm :

- 1] Start
- 2] Input object coordinate from user.
- 3] Display the object before rotation.
- 4] Accept the rotation angle for user.
- 5] Execute rotation matrix
- 6] Display rotated object
- 7] Stop

\* Flowchart :



```
//8 -code
#include<stdio.h>
#include<graphics.h>
#include<math.h>
int main()
{
    int gd=0,gm,x1,y1,x2,y2;
    double s,c,angle;
    initgraph(&gd, &gm, "C:\\TC\\BGI");
    setcolor(RED);
    printf("Enter coordinates of line: ");
    scanf("%d%d%d%d",&x1,&y1,&x2,&y2);
    cleardevice();
    setbkcolor(WHITE);
    line(x1,y1,x2,y2);
    getch();
    setbkcolor(BLACK);
    printf("Enter rotation angle: ");
    scanf("%lf", &angle);
    setbkcolor(WHITE);
    c = cos(angle *3.14/180);
    s = sin(angle *3.14/180);
    x1 = floor(x1 * c + y1 * s);
    y1 = floor(-x1 * s + y1 * c);
    x2 = floor(x2 * c + y2 * s);
    y2 = floor(-x2 * s + y2 * c);
    cleardevice();
    line(x1, y1, x2, y2);
    getch();
    closegraph();
    return 0;
}
```

\* Practical Related Questions

- 1) Write the transformation matrix for 2D rotation.

→ 2) Matrix for 2D rotation for clockwise direction.

$$R = \begin{bmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

- 3) Matrix for 2D rotation for clockwise direction.

$$A = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

- eg) Write rotation matrix for a rotation angle  $30^\circ$

$$R = \begin{bmatrix} 0.86 & 0.5 \\ 0.5 & 0.86 \end{bmatrix}$$

One of the most important task in computer graphics is to transform the coordinate of object. It is a process by which the object can move to specific place.

- \* Exercise

1) Perform a counterclockwise  $45^\circ$  rotation of triangle A(2,3), B(5,5), C(4,3) about point (1,1).

$$A(2,3) \quad B(5,5) \quad C(4,3)$$

Angle of rotation =  $45^\circ$

$$\rightarrow \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 0.7 & 0.7 & 0 \\ -0.7 & 0.7 & 0 \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$\rightarrow \begin{bmatrix} 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 0 \\ 0 + 0.7 + 0 & 0 + 0.7 + 0 & 0 + 0 + 0 \\ 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0.7 & 0.7 & 0 \\ 0 & 0.7 & 0 \\ 1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0.7 & 0.7 & 0 \\ 0 & 0.7 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

\* Practical Related Questions

1] Write the transformation matrix for 2D rotation.

i] Matrix for 2D rotation for clockwise direction.

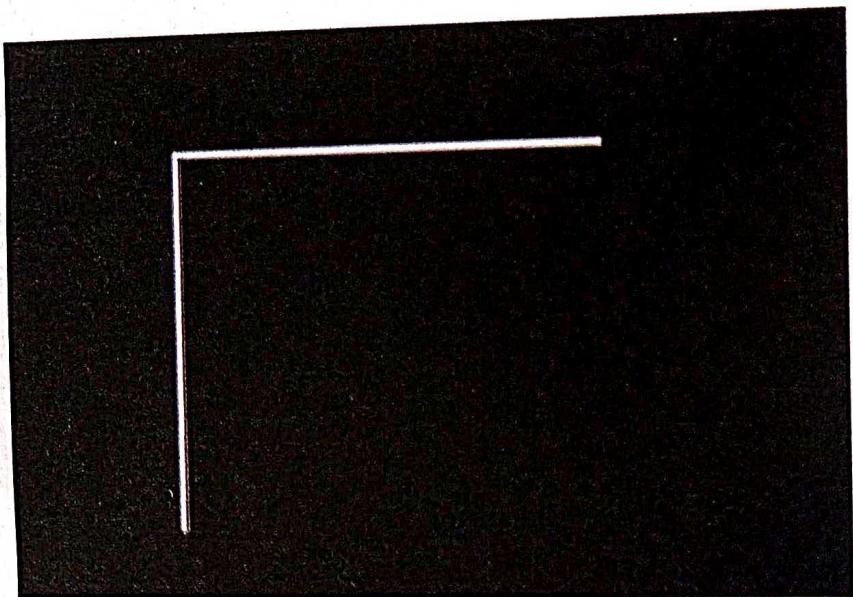
$$R_z = \begin{bmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

ii] Matrix for 2D rotation for clockwise direction

$$R = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

2] Write rotation matrix for a rotation angle  $30^\circ$ .

$$R = \begin{bmatrix} 0.86 & 0.5 \\ 0.5 & 0.86 \end{bmatrix}$$



## \* Conclusion :

One of the most important task in Computer Graphics is to transform the co-ordinates of object. It is a process by virtue of which the object can rotate to specific angle.

## \* Exercise.

- 1) Perform a counterclockwise  $45^\circ$  rotation of triangle  $A(2,3)$ ,  $B(5,5)$ ,  $C(4,3)$  about point  $(1,1)$ .

→

$$A(2,3) \quad B(5,5) \quad C(4,3)$$

$$\text{Angle of rotation} = 45^\circ$$

$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 0.7 & 0.7 & 0 \\ -0.7 & 0.7 & 0 \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 0 \\ 0 + 0.7 + 0 & 0 + 0.7 + 0 & 0 + 0 + 0 \\ 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 1 \end{bmatrix} * \begin{bmatrix} 5 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 0 \\ -0.7 + 0 + 0 & 0 + 0.7 + 0 & 0 + 0 + 0 \\ 0.7 + 0 + 0 & 0.7 + 0 + 0 & 0 + 0 + 1 \end{bmatrix} * \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0.7 & 0.7 & 0 \\ 0.7 & 0.7 & 0 \\ 1.7 & 1.7 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 3 & 1 \\ 5 & 5 & 1 \\ 4 & 3 & 1 \end{bmatrix} \quad \begin{bmatrix} 0.7 & 0.7 & 0 \\ -0.7 & 0.7 & 0 \\ 1.7 & 1.7 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1.4+2.1+1.7 & 1.4+2.1+1.7 & 0+0+1 \\ 3.5+3.5+1.7 & 3.5+3.5+1.7 & 0+0+1 \\ 2.8+2.1+1.7 & 2.8+2.1+1.7 & 0+0+1 \end{bmatrix}$$

$$= \begin{bmatrix} 5.2 & 5.2 & 1 \\ 7.2 & 7.2 & 1 \\ 6.6 & 6.6 & 1 \end{bmatrix}$$

\* Assessment Scheme

0.0	5.0	1.0
0.0	5.0	1.0
0.0	5.0	1.0

$$\begin{array}{|c|c|c|} \hline & 0.0 & 5.0 & 1.0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 1 & 0 & 0 & 0 \\ \hline \end{array}$$

$$\begin{array}{|c|c|c|} \hline & 0.0 & 5.0 & 1.0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 1 & 0 & 0 & 0 \\ \hline \end{array}$$

$$\begin{array}{|c|c|c|} \hline & 0.0 & 5.0 & 1.0 \\ \hline 0 & 0 & 0 & 0 \\ \hline 1 & 0 & 0 & 0 \\ \hline \end{array}$$

## 9. Program for two dimensional Transformation (Reflection & Shearing)

### \* Procedure:

- 1] Start the program
- 2] Input the object coordinate
- 3] For Shearing
  - a) Input Shearing factor.
  - b) Shearing related to x-axis
  - c) Shearing related to y-axis
  - d) Input the x-ref and y-ref value.
  - e) X shear related to reference line.
  - f) Y shear related to reference line.
  - g) Display object without transformation.
- 4] For reflection
  - a) Reflection about x-axis
  - b) Reflection about y-axis
  - c) Display the object after reflection.
- 5] Stop the Program.

### \* Algorithm

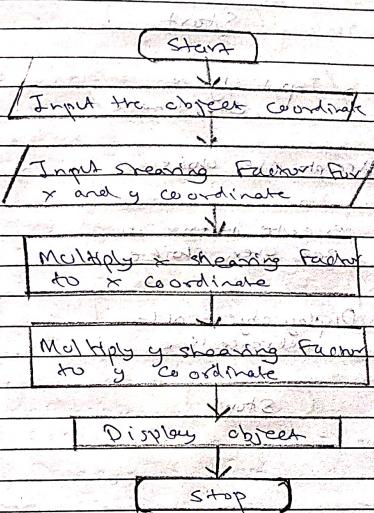
#### 1) Shear

- 1] Input object co-ordinates
- 2] Input Shearing Factor for x and y co-ordinates
- 3] Multiply y-shearing co-ordinate factor with y-coordinates.

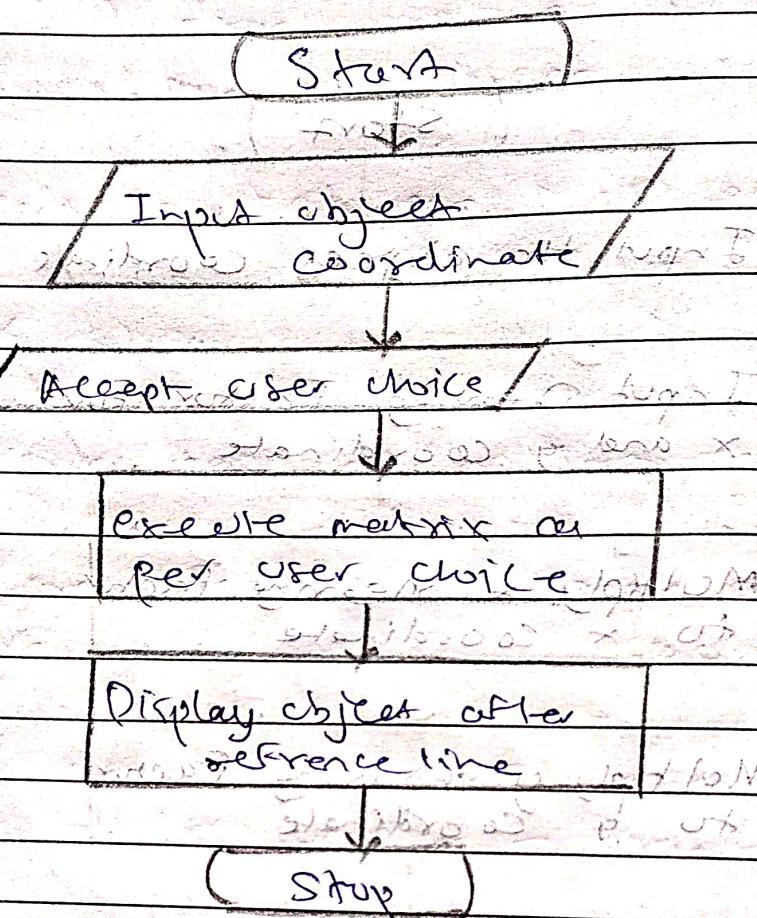
- Date: / /  
Page No: / /
- 4] display object after stretching  
 5] Stop
- 2) Reflection
- 1) Start
  - 2) Input object co-ordinates from user
  - 3) Ask the choice co-ordinate for user
  - a) about x-axis
  - b) about y-axis
  - c) about origin
  - d) x-y
  - e) -x-y
  - f) Perform matrix choose by user
  - g) display object after reflection
  - h) Stop

\* Flowchart

1) Shear



## 2) Reflection



```

//9 - reflection
#include <iostream.h>
#include <conio.h>
#include <graphics.h>
#include <math.h>
#include <stdlib.h>
#define pi 3.14
class arc
{
    float x[10],y[10],theta,ref[10][10],ang;
    float p[10][10],p1[10][10],x1[10],y1[10],xm,ym;
    int i,k,j,n;
public:
    void get();
    void cal ();
    void map ();
    void graph ();
    void plot ();
    void plot1();
};
void arc::get ()
{
    cout<<"\n ENTER ANGLE OF LINE INCLINATION AND Y INTERCEPT";
    cin>> ang >> b;
    cout <<"\n ENTER NO OF VERTICES";
    cin >> n;
    cout <<"\n ENTER";
    for (i=0; i<n; i++)
    {
        cout<<"\n x["<<i<<"] and y["<<i<<"]";
    }
    theta =(ang * pi)/ 180;
    ref [0] [0] = cos (2 * theta);
    ref [0] [1] = sin (2 * theta);
    ref [0] [2] = -b *sin (2 * theta);
    ref [1] [0] = sin (2 * theta);
    ref [1] [1] = -cos (2 * theta);
    ref [1] [2]= b * (cos (2 * theta)+1);
    ref [2] [0]=0;
    ref [2] [1]=0;
    ref [2] [2] = 1;
}
void arc :: cal ()
{
    for (i=0; i < n; i++)
    {
        p[0] [i] = x [i];
    }
}

```

```

    p1 [i] [j] = v [j];
    p1 [j] [i] = t;
}
for (i=0; i<n; i++)
{
    for (j=0; j<n; j++)
    {
        p1 [i] [j]=t;
        for (k=0;k<3; k++)
        {
            p1 [i] [j] += ref [i] [k] * p [k] [j];
        }
    }
    for (j=0; j<n; j++)
    {
        x1 [j]=p1 [0] [j];
        y1 [j] = p1 [1] [j];
    }
}
void arc :: map ()
{
    int gd = DETECT,gm;
    initgraph (&gd, &gm, " ");
    int errorcode = graphresult ();
    /* an error occurred */
    if (errorcode != grOK)
    {
        printf ("Graphics error: %s \n", grapherrmsg (errorcode));
        printf ("Press any key to halt:");
        getch ();
        exit (1); /* terminate with an error code */
    }
}
void arc :: graph ()
{
    xm=getmaxx ()/2;
    ym=getmaxy ()/2;
    line (xm, 0, xm+2*ym);
}
void arc :: plot 1 ()
{
    for (i=0; i <n-1; i++)
    {
        circle (x1[i]+xm, (-y1[i]+ym), 2);
        line (x1[i]+xm, (-y1[i]+ym), x1[i+1]+xm, (-y1[i+1]+ym));
    }
    line (x1[n-1]+xm, (-y1[n-1]+ym), x1[0]+xm, (-y1[0]+ym));
    getch();
}

```

```

    p [1] [i] = y [i];
    p [2] [i] = 1;
}
for (i=0; i<3;i++)
{
    for (j=0; j<n; j++)
    {
        p1 [i] [j]=0;
        for (k=0;k<3; k++)
    }
    p1 [i] [j] += ref [i] [k] * p [k] [j];
}
for (i=0; i<n; i++)
{
    x1 [i]=p1[0] [i];
    y1 [i] = p1 [1] [i];
}
void arc :: map ()
{
    int gd = DETECT,gm;
    initgraph (&gd, &gm, " ");
    int errorcode = graphresult ();
    /* an error occurred */
    if (errorcode != grOK)
    {
        printf ("Graphics error: %s \n", grapherrmsg (errorcode));
        printf ("Press any key to halt:");
        getch ();
        exit (1); /* terminate with an error code */
    }
}
void arc :: graph ()
{
    xm=getmaxx ()/2;
    ym=getmaxy ()/2;
    line (xm, 0, xm+2*ym);
}
void arc :: plot 1 ()
{
    for (i=0; i <n-1; i++)
    {
        circle (x1[i]+xm, (-y1[i]+ym), 2);
        line (x1[i]+xm, (-y1[i]+ym), x1[i+1]+xm, (-y1[i+1]+ym));
    }
    line (x1[n-1]+xm, (-y1[n-1]+ym), x1[0]+xm, (-y1[0]+ym));
    getch();
}

```

```
}

void arc :: plot ()
{
    for (i=0; i <n-1; i++)
    {
        circle (x1[i]+xm, (-y1[i]+ym, 2);
        line (x1[i]+xm, (-y1[i]+ym), x[i+1]+xm, (-y1[i+1]+ym));
    }
    line (x[n-1]+xm, (-y1[n-1]+ym), x[0]+xm, (-y[0]+ym));
    getch();
}
void main ()
{
    class arc a;
    clrscr();
    a.map();
    a.graph();
    a.get();
    a.cal();
    a.plot();
    a.plot1();
    getch();
}
```

```
//9 - shearing
#include<iostream.h>
#include<graphics.h>
#include<math.h>
#include<conio.h>
#include<dos.h>
void mul(int mat[3][3],int vertex[10][3],int n);
void shear(int vertex[10][3],int n);
void init(int vertex[10][3],int n);
int main()
{
    int i,x,y;
    int vertex[10][3],n;
    clrscr();
    cout<<"\nEnter the no. of vertex : ";
    cin>>n;
    for(i=0;i<n;i++)
    {
        cout<<"Enter the points (x,y): ";
        cin>>x>>y;
        vertex[i][0]=x;
        vertex[i][1]=y;
        vertex[i][2]=1;
    }
    shear(vertex,n);

    getch();
    return 0;
}
void init(int vertex[10][3],int n)
{
    int gd=DETECT,gm,i;
    initgraph(&gd,&gm,"C:\\turboc3\\bgi");
    setcolor(10);
    line(0,240,640,240);
    line(320,0,320,480);
    setcolor(3);
    line(450,20,490,20);
    setcolor(15);
    line(450,50,490,50);
    setcolor(6);
    outtextxy(500,20,"Original");
    outtextxy(500,50,"Transformed");
    setcolor(3);

    for(i=0;i<n-1;i++)
    {
```

```

        line(320+vertex[i][0],240+vertex[i][1],320+vertex[i+1][0],240+vertex[i+1][1]);
    }
    line(320+vertex[n-1][0],240+vertex[n-1][1],320+vertex[0][0],240+vertex[0][1]);
}

void mul(int mat[3][3],int vertex[10][3],int n)
{
    int i,j,k;
    int res[10][3];
    for(i=0;i<n;i++)
    {
        for(j=0;j<3;j++)
        {
            res[i][j]=0;
            for(k=0;k<3;k++)
            {
                res[i][j] = res[i][j] + vertex[i][k]*mat[k][j];
            }
        }
    }
    setcolor(15);
    for(i=0;i<n-1;i++)
    {
        line(320+res[i][0],240-res[i][1],320+res[i+1][0],240-res[i+1][1]);
    }
    line(320+res[n-1][0],240-res[n-1][1],320+res[0][0],240-res[0][1]);
}
}

void shear(int vertex[10][3],int n)
{
    int opt;
    int shear_array[3][3];
    cout<<"\n1.x-shear\n2.y-shear\nYour Choice: ";
    cin>>opt;
    switch(opt)
    {
        case 1: int xsh;
                  cout<<"\nEnter the x shear : ";
                  cin>>xsh;
                  shear_array[0][0]=1;
                  shear_array[1][0]=xsh;
                  shear_array[2][0]=0;
                  shear_array[0][1]=0;
                  shear_array[1][1]=1;
                  shear_array[2][1]=0;
                  shear_array[0][2]=0;
                  shear_array[1][2]=0;

```

```

                  shear_array[2][2]=1;
                  init(vertex,n);
                  mul(shear_array,vertex,n);
                  break;

        case 2:int ysh;
                  cout<<"\nEnter the y shear : ";
                  cin>>ysh;
                  shear_array[0][0]=1;
                  shear_array[1][0]=0;
                  shear_array[2][0]=0;
                  shear_array[0][1]=ysh;
                  shear_array[1][1]=1;
                  shear_array[2][1]=0;
                  shear_array[0][2]=0;
                  shear_array[1][2]=0;
                  shear_array[2][2]=1;
                  init(vertex,n);
                  mul(shear_array,vertex,n);
                  break;
    }
}

```

\* Practical Related Questions

1) Write the transformation matrix for 2D reflection.

$$\begin{bmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2) Write the transformation matrix for 2D shear

$\rightarrow X$  Shear:

$$\begin{bmatrix} 1 & 0 & 0 \\ Sx & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$\gamma$  Shear :

$$\begin{bmatrix} 1 & S\gamma & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

3) Define reflection and shearing.

$\rightarrow$  Reflection: It is the change in direction

of a wave at the boundary between two different media, so the wave moves back to its medium.

Shearing: A transformation which changes the shape of object.

4) Differentiate between x-shear and Y shear

$\rightarrow$  X shear      Y shear

1) It preserves the Y coordinate. It preserves the X coordinate with shear.

2) Change are made to X coordinates and change are made to Y coordinates.

3) Change cause the vertical. It causes horizontal line to tilt left or right to transform up or down.

\* Conclusion:

Thus, we learned the program of reflection and shearing of two dimensional object.

\* Exercise

1) A point (4,3) is rotated counter-clockwise by an angle of  $45^\circ$ . find the rotation matrix and the resultant point. Apply the Shearing transformation to a square with A(0,0), B(1,0) C(1,1) D(0,1) for below.

and then do it on blood

i) shear parameter value of 0.5 relative to line  $y_{ref} = \frac{1}{2}$

ii) A(0,0), B(1,0) C(1,1) D(0,1)  
shear parameter = 0.5  
and  $y_{ref} = -1$

$$\begin{bmatrix} 0 & 0 & 0 \\ 1 & 0 & 1 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0.5 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 1.5 & 0 & 1 \\ 2.5 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1.5 & 0 & 1 \\ 2 & 0 & 1 \\ 2.5 & 1 & 1 \end{bmatrix}$$

## 10. Program for three Dimensional Transformation

### 2.0 (Translation & Scaling)

#### \* Procedure :

- i) Start the program
- ii) Input object coordinate
- iii) For Translation
  - i) Enter translation factor  $t_x, t_y$  and  $t_z$
  - ii) Move original position to new position
  - iii) Display the object after translation.
- iv) For Scaling
  - i) Input the scaling factors  $s_x, s_y$ , and  $s_z$
  - ii) The transformed coordinate
  - iii) Display the object
- v) Stop the program.

#### \* Algorithm

##### 1) Translation

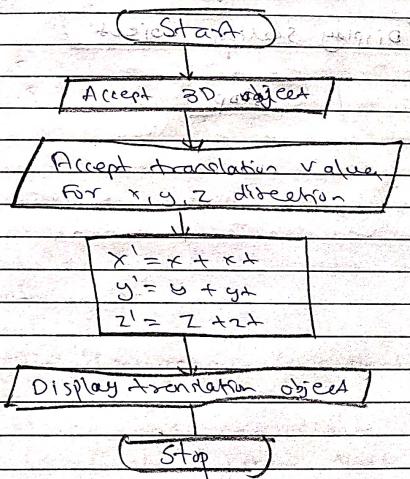
- i) Start
- ii) Accept object coordinate
- iii) Accept translation value.
- iv) Add translation value to original coordinate
- v) Display object after translation.
- vi) Stop

#### \* Scaling

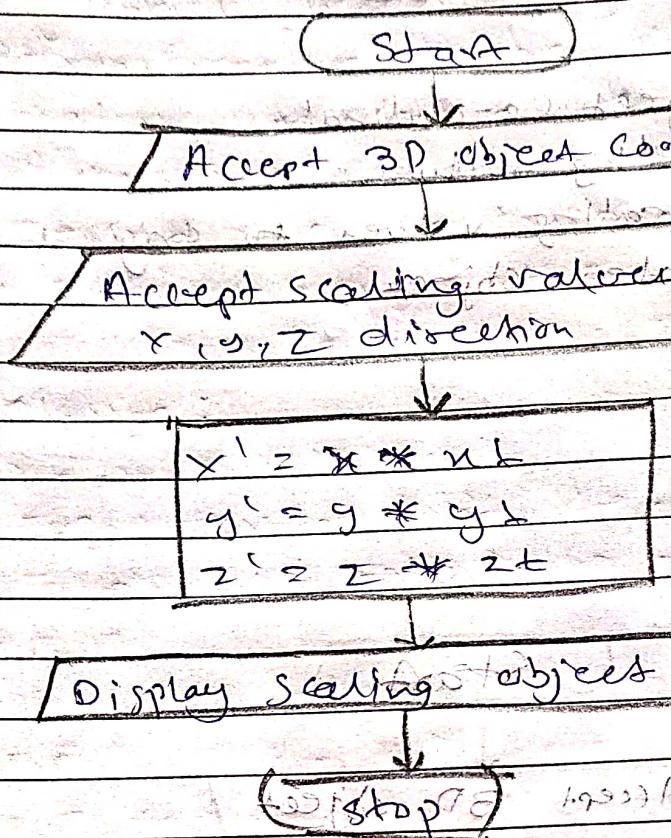
- i) Start
- ii) Accept object co-ordinate
- iii) Accept Scaling values
- iv) Multiply Scaling values to original coordinates
- v) Display Scaled object
- vi) Stop

#### \* Flowchart

##### 1) Translation



## 2) Scaling



$$s_x + x = X$$

$$s_y + y = Y$$

$$s_z + z = Z$$

Two methods exist

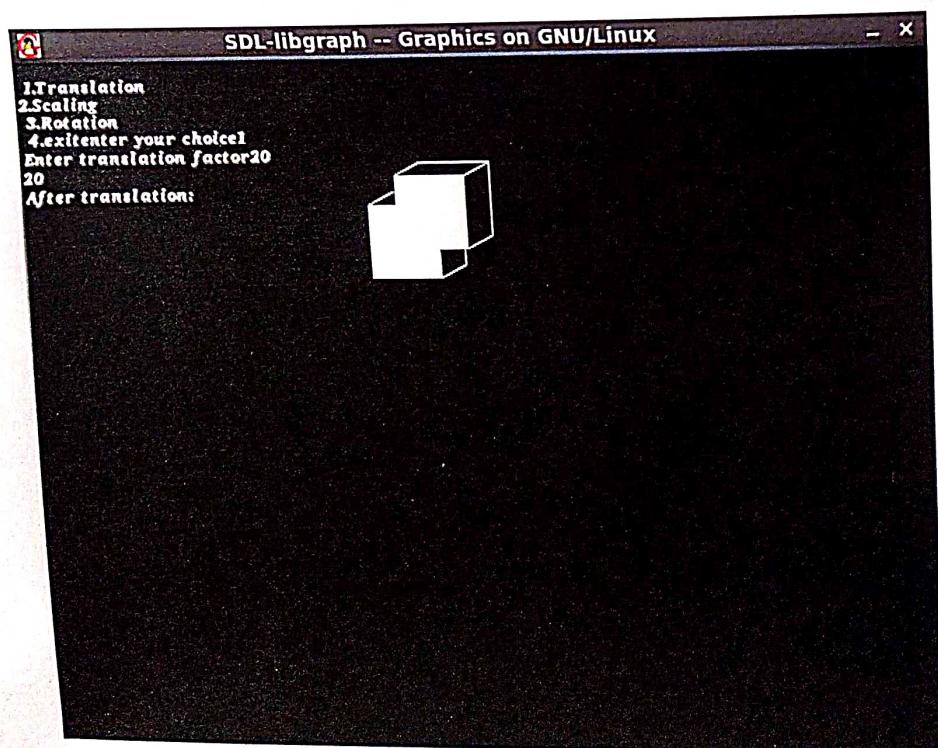
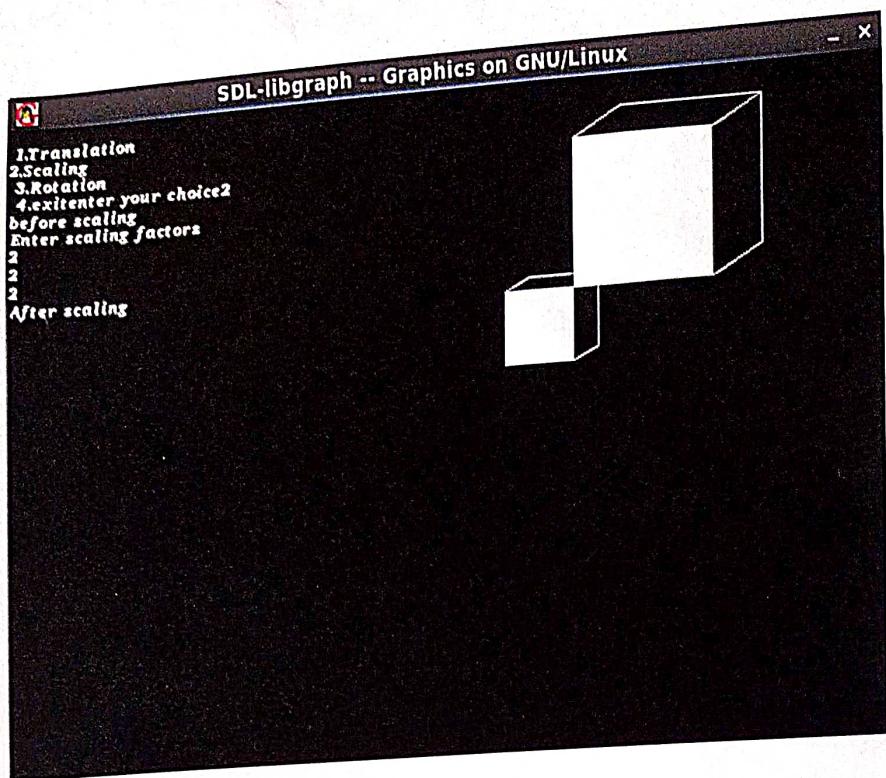
part 2

```
// 10 - translation
#include<stdio.h>
#include<conio.h>
#include<graphics.h>
#include<math.h>
int maxx,maxy,midx,midy;
void axis()
{
getch();
cleardevice();
line(midx,0,midx,maxy);
line(0,midy,maxx,midy);
}
void main()
{
int x,y,z,o,x1,x2,y1,y2;
int gd=DETECT,gm;
detectgraph(&gd,&gm);
initgraph(&gd,&gm,"c:\\tc\\bgi");
//setfillstyle(0,getmaxcolor());
maxx=getmaxx();
maxy=getmaxy();
midx=maxx/2;
midy=maxy/2;

axis();

bar3d(midx+50,midy-100,midx+60,midy-90,10,1);

printf("Enter translation factor");
scanf("%d%d",&x,&y);
//axis();
printf("After translation:");
bar3d(midx+x+50,midy-(y+100),midx+x+60,midy-(y+90),10,1);
getch();
closegraph();
}
```



\* Practical Related Questions:

1) Write the transformation matrix for 3D Translation.

$$\rightarrow \text{Translation matrix: } T = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ tx & ty & tz & 1 \end{bmatrix}$$

2) Write transformation matrix for 3D Scaling

$$\rightarrow \text{Scaling matrix: } S = \begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3] What Z-coordinate indicates in 3D transformation?

$\rightarrow$  Z - coordinate indicates rotation about front to back rotation in 3D object transformation.

4) Explain Homogeneous Coordinate

$\rightarrow$  i) Homogeneous coordinate is a coordinate system that algebraically treats all points in the projective plane equally.

- (ii) They are widely used in Computer graphics because they enable projective transformation to be described by matrix manipulation to in a different coordinate system.
- (iii) Homogeneous coordinate system is used in construction and design based applications.

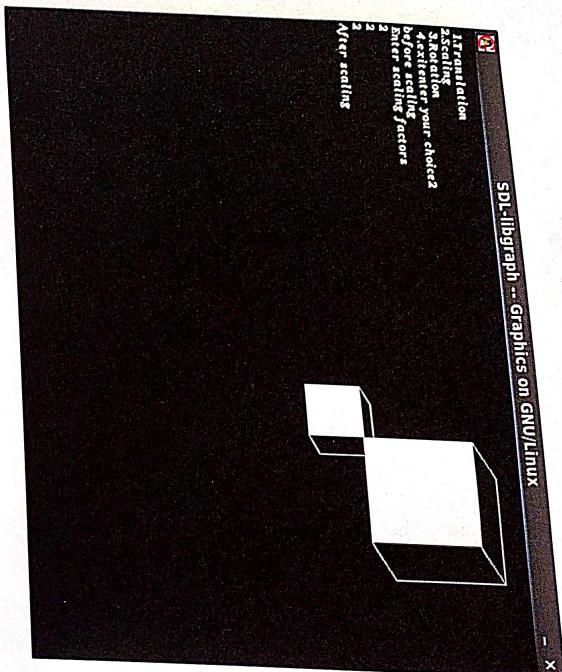
#### Conclusion:

Thus, we learned that the program to translate and scale the three dimensional object.

#### Exercise

- 1) Write a program to draw a cube in C by using base3d function. Translate the cube by 75 units in X, 75 units in Y and 75 units in Z direction.

$10^{-2}$



# 11. Program For three dimensional Transformation (Rotation)

## \* Procedure :

- 1] Start the program
- 2] Input the object co-ordinates
- 3] For rotation
  - a) Enter the Radian for rotation angle  $\theta$
  - b) Perform rotation about each axis.

### i) Z - Axis Rotation

$$x' = x * \cos \theta - y * \sin \theta$$

$$y' = x * \sin \theta + y * \cos \theta$$

$$z' = z$$

### ii) X - Axis Rotation

$$y' = y * \cos \theta - z * \sin \theta$$

$$z' = y * \sin \theta + z * \cos \theta$$

$$x' = x$$

### iii) Y - Axis Rotation

$$z' = z * \cos \theta - x * \sin \theta$$

$$x' = z * \sin \theta + x * \cos \theta$$

$$y' = y$$

g) Display the object after rotation.

h) Stop the program

\* Algorithm :-

- 1) Start
- 2) Input object coordinate.
- 3) Accept rotation angle.
- 4) For z-axis rotation
 
$$x' = x * \cos\theta - y * \sin\theta$$

$$y' = x * \sin\theta + y * \cos\theta$$

$$z' = z$$
- 5) For x-axis rotation
 
$$x' = x$$

$$y' = y * \cos\theta - z * \sin\theta$$

$$z' = y * \sin\theta + z * \cos\theta$$

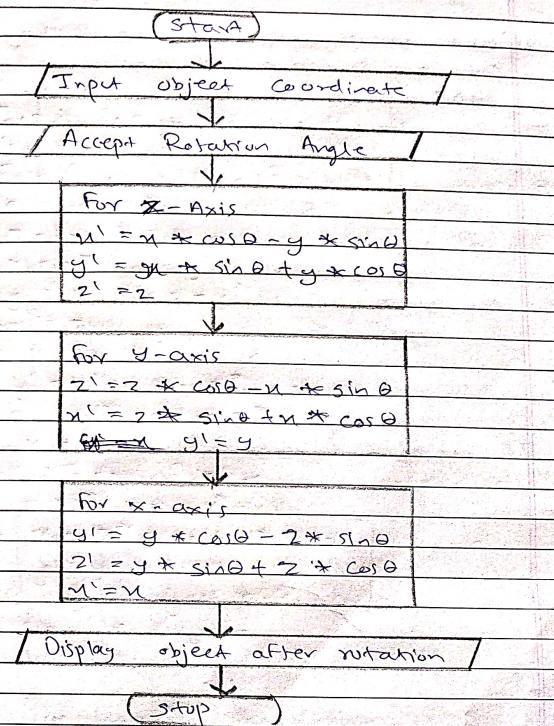
$$y = y$$
- 6) For y-axis rotation
 
$$x' = z * \cos\theta + y * \sin\theta$$

$$y' = y$$

$$z' = z * \sin\theta - y * \cos\theta$$

$$x = x$$
- 7) Display object after rotation.
- 8) Stop

\* Flowchart :-



```
// 11 - rotation
#include<stdio.h>
#include<conio.h>
#include<graphics.h>
#include<math.h>
int maxx,maxy,midx,midy;
void axis()
{
getch();
cleardevice();
line(midx,0,midx,maxy);
line(0,midy,maxx,midy);
}
void main()
{
int x,y,z,o,x1,y1,y2;
int gd=DETECT,gm;
detectgraph(&gd,&gm);
initgraph(&gd,&gm,"c:\\tc\\bgi");
//setfillstyle(0,getmaxcolor());
maxx=getmaxx();
maxy=getmaxy();
midx=maxx/2;
midy=maxy/2;
axis();
bar3d(midx+50,midy-100,midx+60,midy-90,5,1);
printf("Enter rotating angle");
scanf("%d",&o);
x1=50*cos(o*3.14/180)-100*sin(o*3.14/180);
y1=50*sin(o*3.14/180)+100*cos(o*3.14/180);
x2=60*cos(o*3.14/180)-90*sin(o*3.14/180);
y2=60*sin(o*3.14/180)+90*cos(o*3.14/180);
axis();
printf("After rotation about z axis");
bar3d(midx+x1,midy-y1,midx+x2,midy-y2,5,1);
axis();
printf("After rotation about x axis");
bar3d(midx+50,midy-x1,midx+60,midy-x2,5,1);
axis();
printf("After rotation about yaxis");
bar3d(midx+x1,midy-100,midx+x2,midy-90,5,1);
getch();
closegraph();
}
```

## \* Practical Related Questions

1) Write the transformation matrix for 3D

Rotation about Z-axis

$$R_z = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{bmatrix}$$

2) Write the transformation matrix for 3D

Rotation about X-axis

$$R_x = \begin{bmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{bmatrix}$$

3) Write the transformation matrix for 3D

Rotation about Y-axis

$$R_y = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

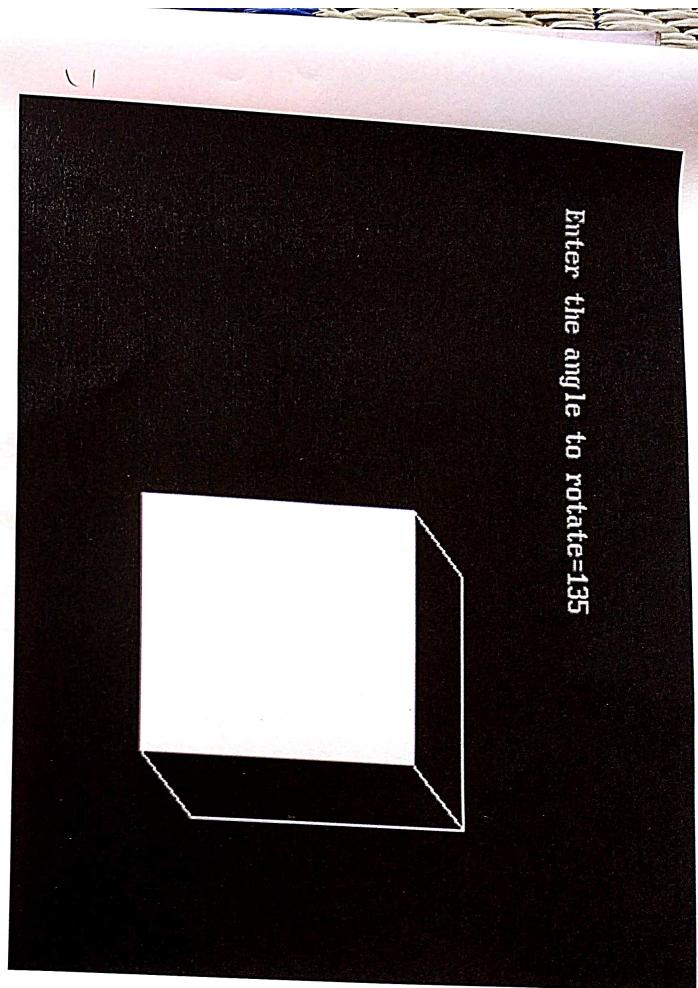
\* Conclusion :

Thus, we learned the program to rotate the 3 dimensional object.

\* Exercise:

1) WAP to draw a cube in C by using 'bar3d' function. Rotate the cube by  $45^\circ$  around x-axis.

Enter the angle to rotate=135



## 12. Program to Clip Line

Using Cohen Sutherland Line Clipping Algorithm.

Clipping Algorithm.

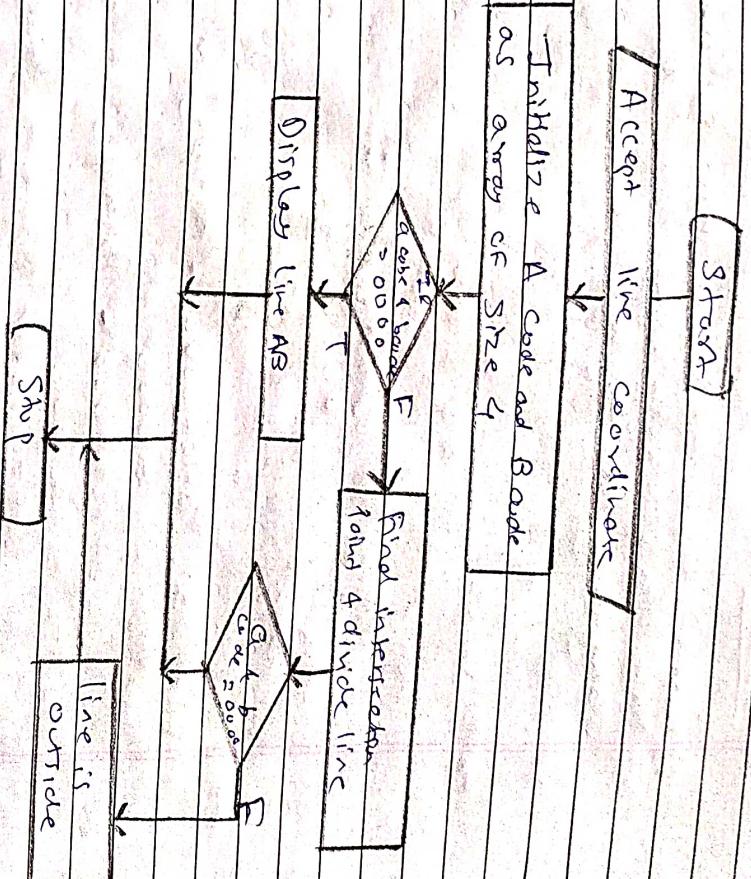
\* Procedure :

- 1) Given a line segment with endpoint  $P_1(x_1, y_1)$  and  $P_2(x_2, y_2)$ .
- 2) Compute the 4-bit code.
- 3) If both code are 0000, line lies completely inside the window.
- 4) If both code have 1 in same bit position, the line lies outside the border.
- 5) If a line cannot be trivially be accepted or rejected, at least one of the two endpoint must lie outside the window and the line segment crosses the window edge. This line must be clipped at the window edge, before being passed to the drawing routine.
- 6) Examining one of the endpoint, say  $P_1(x_1, y_1)$ . Read  $P_1$ 's 4 bit code.
- 7) When a set bit is found, compute the intersection I of the corresponding window edge with the line from  $P_1$  to  $P_2$ . Replace  $P_1$  with I and repeat the procedure.

## \* Algorithm

- 1) Calculate positions of both endpoints of the line or operations on both ends of screen or operations on both ends of line.
- 2) If both endpoints given are inside the window then line is visible.
- 3) If one endpoint given is outside the window then line is visible if it intersects the window else line is invisible.

## \* Flowchart



```
// 12 -code
#include<stdio.h>
#include<stdlib.h>
#include<math.h>
#include<graphics.h>
#include<dos.h>

typedef struct coordinate
{
    int x,y;
    char code[4];
}PT;

void drawwindow();
void drawline(PT p1,PT p2);
PT setcode(PT p);
int visibility(PT p1,PT p2);
PT resetendpt(PT p1,PT p2);

void main()
{
    int gd=DETECT,v,gm;
    PT p1,p2,p3,p4,ptemp;
    printf("\nEnter x1 and y1\n");
    scanf("%d %d",&p1.x,&p1.y);
    printf("\nEnter x2 and y2\n");
    scanf("%d %d",&p2.x,&p2.y);
    initgraph(&gd,&gm,"c:\\turboc3\\bgi");
    drawwindow();
    delay(500);
    drawline(p1,p2);
    delay(500);
    cleardevice();
    delay(500);
    p1=setcode(p1);
    p2=setcode(p2);
    v=visibility(p1,p2);
    delay(500);
    switch(v)
    {
        case 0: drawwindow();
                  delay(500);
                  drawline(p1,p2);
                  break;
        case 1:  drawwindow();
                  delay(500);
                  break;
    }
}
```

```

case 2: p3=resetendpt(p1,p2);
          p4=resetendpt(p2,p1);
          drawwindow();
          delay(500);
          drawline(p3,p4);
          break;
      }
      delay(5000);
      closegraph();
}
void drawwindow()
{
    line(150,100,450,100);
    line(450,100,450,350);
    line(450,350,150,350);
    line(150,350,150,100);
}
void drawline(PT p1,PT p2)
{
    line(p1.x,p1.y,p2.x,p2.y);
}
PT setcode(PT p)
{
    PT ptemp;
    if(p.y<100)
        ptemp.code[0]='1'; //Top
    else
        ptemp.code[0]='0';

    if(p.y>350)
        ptemp.code[1]='1'; //Bottom
    else
        ptemp.code[1]='0';

    if(p.x>450)
        ptemp.code[2]='1'; //Right
    else
        ptemp.code[2]='0';

    if(p.x<150)
        ptemp.code[3]='1'; //Left
    else
        ptemp.code[3]='0';
    ptemp.x=p.x;
}

    ptemp.y=p.y;
}
return(ptemp);
int visibility(PT p1,PT p2)
{
    int i,flag=0;
    for(i=0;i<4;i++)
    {
        if((p1.code[i]=='0') || (p2.code[i]=='0'))
            flag=1;
    }
    if(flag==0)
        return(0);
    for(i=0;i<4;i++)
    {
        if((p1.code[i]==p2.code[i]) && (p1.code[i]=='1'))
            flag='0';
    }
    if(flag=='0')
        return(1);
    return(2);
}
PT resetendpt(PT p1,PT p2)
{
    PT temp;
    int x,y;
    float m,k;
    if(p1.code[3]=='1')
        x=150;
    if(p1.code[2]=='1')
        x=450;
    if((p1.code[3]=='1') || (p1.code[2]=='1'))
    {
        m=(float)(p2.y-p1.y)/(p2.x-p1.x);
        k=(p1.y+(m*(x-p1.x)));
        temp.y=k;
        temp.x=x;
    }
}

```

```

        for(i=0;i<4;i++)
            temp.code[i]=p1.code[i];
        if(temp.y<=350 && temp.y>=100)
            return (temp);
    }
    if(p1.code[0]=='1')
        y=100;
    if(p1.code[1]=='1')
        y=350;
    if((p1.code[0]=='1') || (p1.code[1]=='1'))
    {
        m=(float)(p2.y-p1.y)/(p2.x-p1.x);
        k=(float)p1.x+(float)(y-p1.y)/m;
        temp.x=k;
        temp.y=y;
        for(i=0;i<4;i++)
            temp.code[i]=p1.code[i];
        return(temp);
    }
    else
        return(p1);
}

```

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**Practical Related Questions.**

- i) Define Clipping.  
→ Clipping is a method of discarding the unwanted part of image or object from view port.
- ii) How to calculate intersection points of a line  
→ If line is partially visible.  
→ Replace endpoint with the intersection point and update the region code.
- iii) Give 3 possible condition to clip line using algorithm.  
→ i) Completely Visible  
ii) Completely Invisible  
iii) Partially Visible

→ Conclusion:  $\text{Intersection} = \text{Line} \cap \text{View Port}$

Thus, we learned the program to clip line using Cohen Sutherland line clipping algorithm.

## 13. Program to Clip Line Using midpoint subdivision

### \* Exercise :

#### \* Procedure

- 1) Under four bit code Fix following line clipping
- 2) Under and determine categories of each line.
- 3) Give a line segment with endpoint P1P2 is partially visible
- 4) Divide line P1P2 at mid point P3 forming two segments P1P3 and P3P2, apply visibility test on both segments.
- 5) Both lines are partially visible category + so we have to divide it again and invisible line are formed.

### \* Algorithm

- 1) Start
- 2) Read two endpoints of line.
- 3) Assign region code using two endpoint by following steps:

initialise code with bit 0000

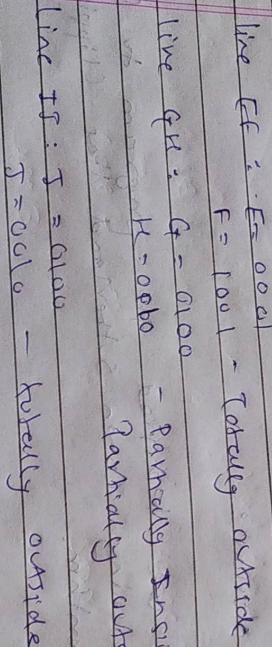
set bit 1 : if ( $x < w_n$ )

Set bit 2 : if ( $y < w_n$ )

Set bit 3 : if ( $y > w_n$ )

Set bit 4 : if ( $x > w_n$ )

$x_2 - x_1 = P_{1x}$



Line AB :  $A = B = 0000$  — Totaly Inside!

Line CD :  $C = 0000$

$D = 1000$  — Partially Visible

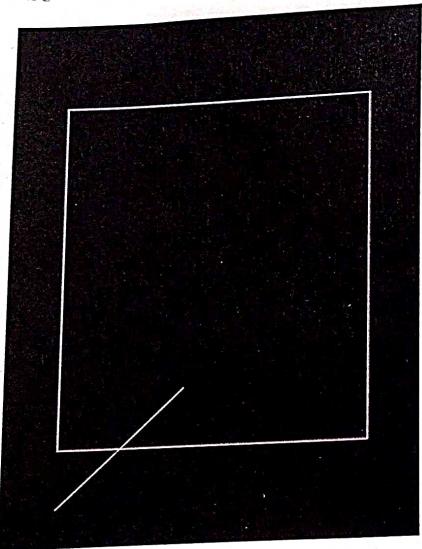
Line EF :  $E = 0001$   
 $F = 1001$  — Totaly outside

Line GH :  $G = 0100$   
 $H = 0000$  — Partially Inside

$G = 0000$   
 $H = 0000$  — Partially Outside

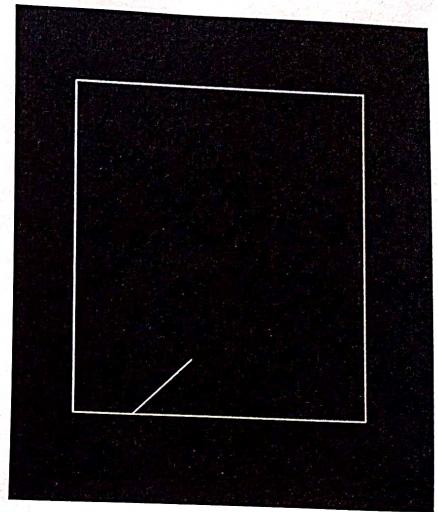
Line IJ :  $J = 0100$   
 $I = 0010$  — totally outside

before clipping



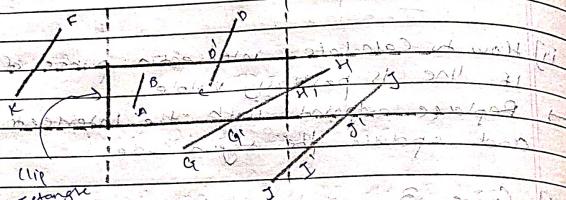
$n^2$

After clipping



### Exercises:

- 1) Write Four bit code for following lines and determine their clipping categories of each line.



Line AB :  $A = B = 0000$  - Totally inside

Line CD :  $C = 0000$  - Partially inside

$D = 1000$  - Partially visible

Line EF :  $E = 0001$

$F = 1001$  - Totally outside

Line GH :  $G = 0100$

$H = 0000$  - Partially Inside

Partially outside

Line IJ :  $I = 0100$

$J = 0010$  - totally outside

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### 13. Program to Clip Line

Using midpoint subdivision  
Line Clipping Algorithm

- \* Procedure
- 1] Give a line segment with endpoints
- 2] Four digit for points  $P_1$  and  $P_2$  are 1000, 4000 resp.
- 3] Clipping of four digit codes is done line  $P_1P_2$  is partially visible
- 4] Divide line  $P_1P_2$  at mid point  $P_3$  forming two segments  $P_1P_3$  and  $P_3P_2$ , apply visibility test on both segments.
- 5] Both lines are partially visible category, so we have to divide it again
- 6] This procedure continues until all the visible and invisible lines are formed.

#### Algorithm

1) Start

2) Read two endpoints of line

3) Assign region code using two endpoint by following steps:

initialise code with bit 0000

Set bit 1 : if ( $x < w_{x_1}$ )

Set bit 2 : if ( $x < w_{x_2}$ )

Set bit 3 : if ( $y < w_{y_1}$ )

Set bit 4 : if ( $y < w_{y_2}$ )

$w_{x_1} + w_{x_2} = P_1$  and  $w_{y_1} + w_{y_2} = P_2$

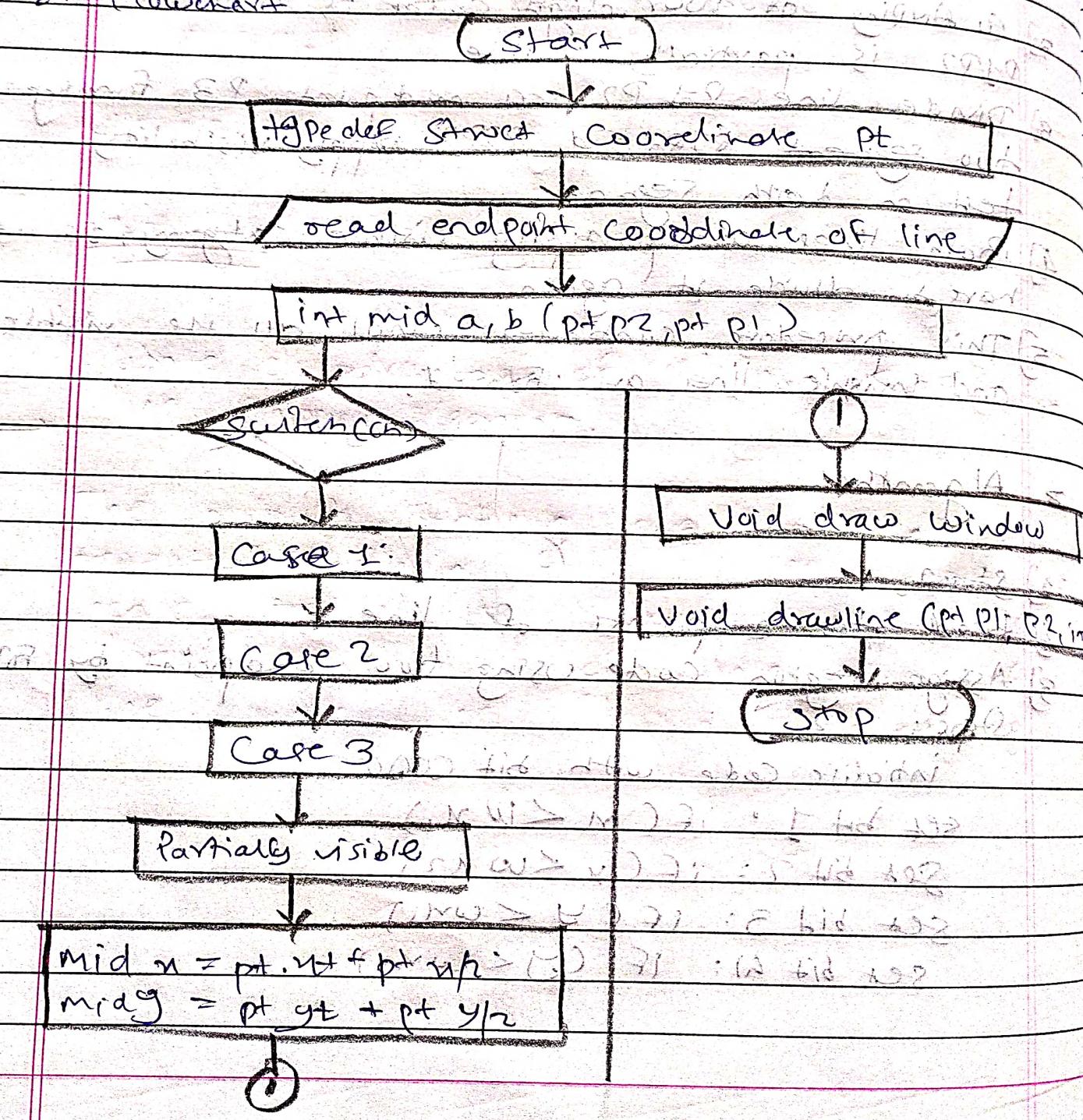
4) Check for visibility ad line.

a) if region code for both endpoints are zero  
b) if region code for both endpoints are not zero

5) Divide Partial line with you get a complete visible segment by using 3rd step.

c) End.

\* Flowchart



```
//13 - code
#include<stdio.h>
#include<conio.h>
#include<stdlib.h>
#include<dos.h>
#include<math.h>
#include<graphics.h>
typedef struct coordinate
{
    int x,y;
    char code[4];
}PT;
void drawwindow();
void drawline (PT p1,PT p2,int cl);
PT setcode(PT p);

int visibility (PT p1,PT p2);
PT resetendpt (PT p1,PT p2);
main()
{
    int gd=DETECT, gm,v;
    PT p1,p2,ptemp;
    initgraph(&gd,&gm,"C:\\TC\\BGI ");
    cleardevice();
    printf("\n\n\tENTER END-POINT 1 (x,y): ");
    scanf("%d,%d",&p1.x,&p1.y);
    printf("\n\n\tENTER END-POINT 2 (x,y): ");
    scanf("%d,%d",&p2.x,&p2.y);
    cleardevice();
    drawwindow();
    getch();
    drawline(p1,p2,15);
    getch();
    cleardevice();
    drawwindow();
    midsub(p1,p2);
    getch();
    closegraph();
    return(0);
}

midsub(PT p1,PT p2)
{
    PT mid;
    int v;
    p1=setcode(p1);
    p2=setcode(p2);
```

```

v=visibility(p1,p2);
switch(v)
{
    case 0: /* Line completely visible */
        drawline(p1,p2,15);
        break;
    case 1: /* Line completely invisible */
        break;
    case 2: /* line partly visible */
        mid.x = p1.x + (p2.x-p1.x)/2;
        mid.y = p1.y + (p2.y-p1.y)/2;
        midsub(p1,mid);
        mid.x = mid.x+1;
        mid.y = mid.y+1;
        midsub(mid,p2);
        break;
}
}

void drawwindow()
{
setcolor(RED);
line(150,100,450,100);
line(450,100,450,400);
line(450,400,150,400);
line(150,400,150,100);
}

void drawline (PT p1,PT p2,int cl)
{
setcolor(cl);
line(p1.x,p1.y,p2.x,p2.y);
}

PT setcode(PT p)
{
PT ptemp;
if(p.y<=100)
ptemp.code[0]='1'; /* TOP */
else
ptemp.code[0]='0';
if(p.y>=400)
ptemp.code[1]='1'; /* BOTTOM */
else
ptemp.code[1]='0';
if (p.x>=450)
ptemp.code[2]='1'; /* RIGHT */
}

```

```

else
ptemp.code[2]='0';
if (p.x<=150) /* LEFT */
ptemp.code[3]='1';
else
ptemp.code[3]='0';
ptemp.x=p.x;
ptemp.y=p.y;
return(ptemp);
}

int visibility (PT p1,PT p2)
{
int i,flag=0;
for(i=0;i<4;i++)
{
if((p1.code[i]!='0')||(p2.code[i]!='0'))
flag=1;
}
if(flag==0)
return(0);
for(i=0;i<4;i++)
{
if((p1.code[i]==p2.code[i]) &&(p1.code[i]=='1'))
flag=0;
}
if(flag==0)
return(1);
return(2);
}

```

## Practical Related Questions

1) Calculate coordinate of midpoint between two points  $P_1(-10, 20)$  and  $P_2(50, 10)$ .

$$(x_1, y_1) = (-10, 20)$$

$$(x_2, y_2) = (50, 10)$$

$$(x_{\min}, y_{\min}) = (100, 400)$$

$$(x_{\max}, y_{\max}) = (400, 400)$$

$$P_1 = -\Delta n = n_2 - n_1 = (50 - (-10)) = 60$$

$$P_2 = 60$$

$$P_3 = 10$$

$$P_4 = -10$$

$$q_1 = 110 \text{ (negative)} \rightarrow \text{downward shift}$$

$$q_2 = 410 \text{ (positive)} \rightarrow \text{upward shift}$$

$$q_3 = -80$$

$$q_4 = -38.4 \text{ (negative)} \rightarrow \text{downward shift}$$

$$\text{Ansatz: } q_1 + q_2 + q_3 + q_4 = 0 \rightarrow 110 + 410 - 80 - 38.4 = 391.6$$

$$q_1 = \frac{110}{60} = 1.8333 \rightarrow \text{upward shift}$$

$$q_2 = \frac{410}{60} = 6.8333 \rightarrow \text{upward shift}$$

$$q_3 = \frac{-80}{60} = -1.3333 \rightarrow \text{downward shift}$$

$$q_4 = \frac{-38.4}{60} = -0.64 \rightarrow \text{downward shift}$$

$$q_1 = \frac{-80}{10} = -8$$

$$q_2 = \frac{410}{10} = 41$$

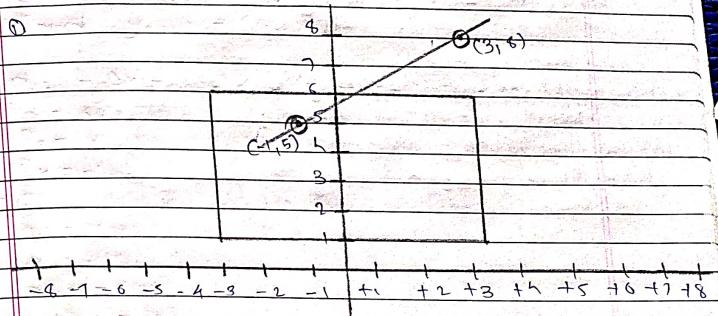
$$\begin{aligned}
 q_4 &= 3.80 = -3.80 \\
 p_4 &= -1.0 \\
 P &\leq 0+1 = \max(-3.8, -1) = -1 \\
 P &> 0+2 = \min(6.8233, 1.8233) \\
 N_1 &= N_1 + 1, N_2 \\
 &= -1.0+6 \rightarrow 8.333, 8.80 \\
 &= 3.9, 9
 \end{aligned}$$

2) Write disadvantages of Midpoint subdivision line clipping algorithm

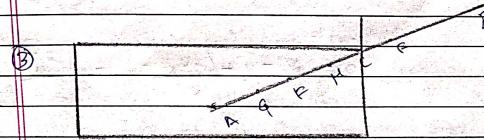
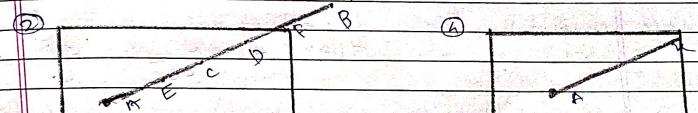
The midpoint subdivision algorithm requires repeated subdivision of the line segment and hence it is slower than using direct calculation of intersection of line with the clipping window edges.

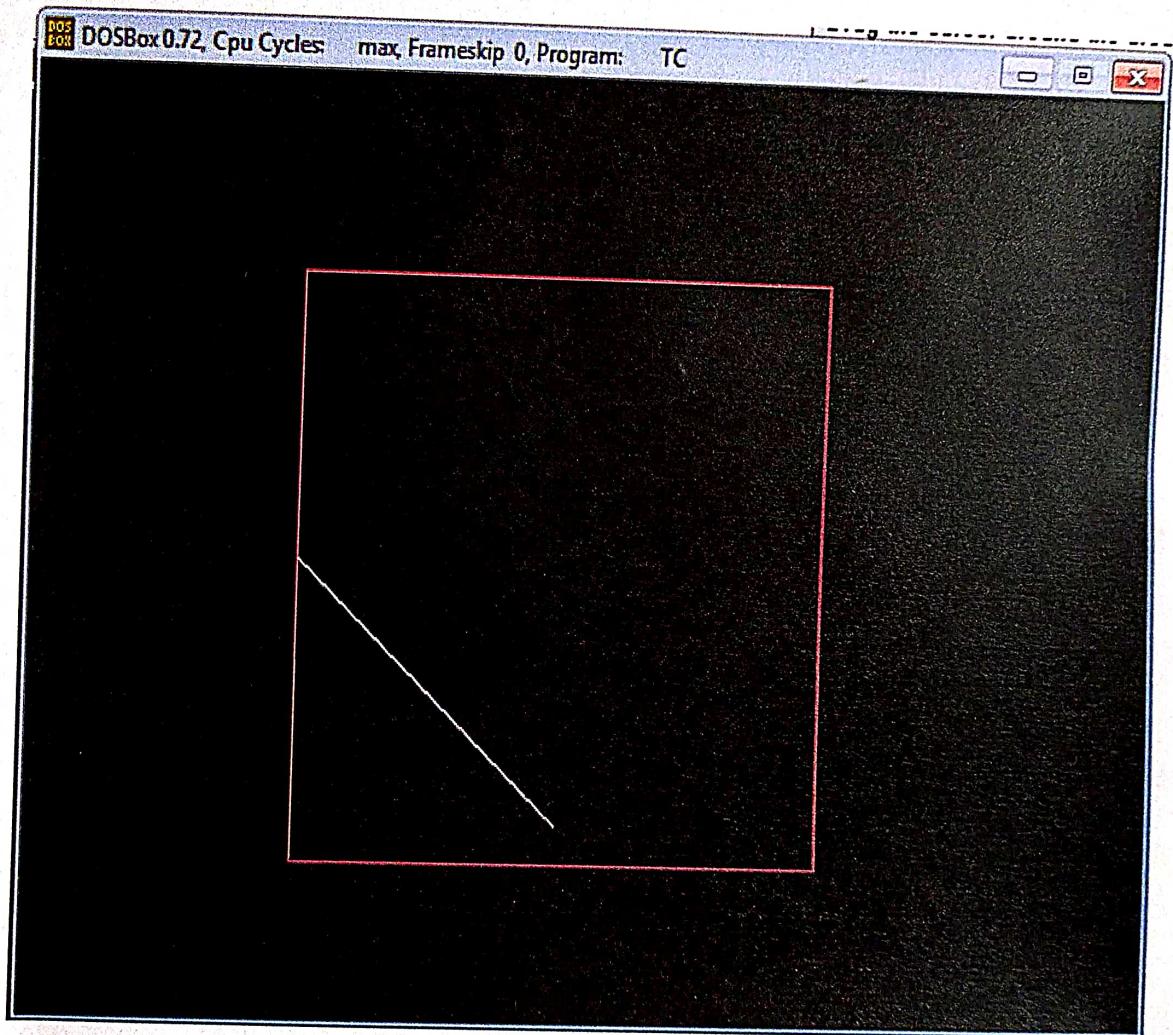
### Exercise:

- 1) Using midpoint subdivision line clipping algorithm illustrate a clipping of a line segment joining two end points A(1, 5) B(3, 8) by considering Clipping window with left corner at (-3, 4) and upper right corner at (2, 6)



-4 -3 -2 -1 0 1 2 3 4 5 6 7 8  
-4 -3 -2 -1 0 1 2 3 4 5 6 7 8





## 14. Program to Clip Polygon

Using Sutherland Hodgesman polygon

Clipping algorithm

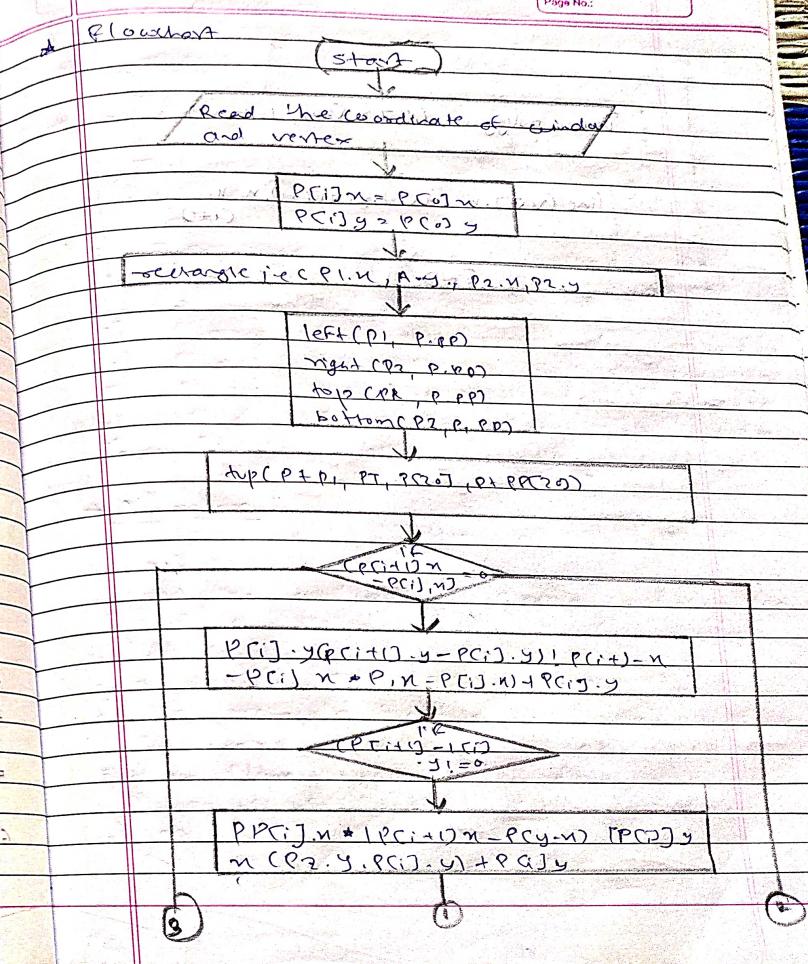
### \* Procedure :

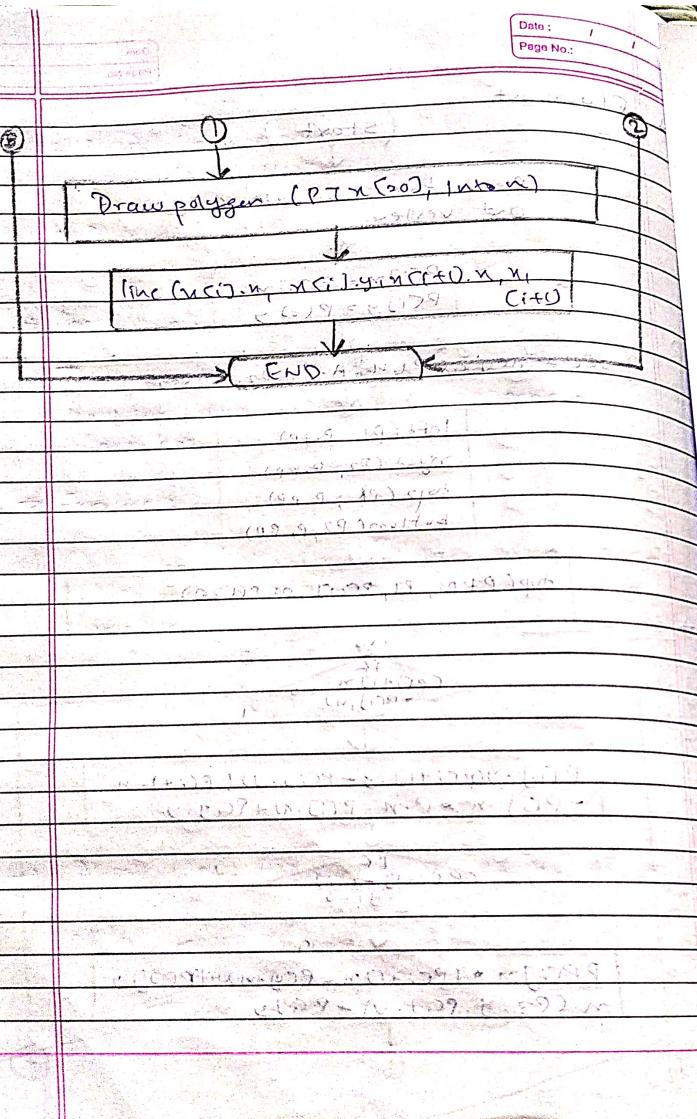
- 1] This algorithm performs a clipping of a polygon against each window edge in turn.
- 2] Every edge of polygon is compared with Clipping plane to find out the new vertex called output vertices.
- 3] Clipping against the left side of Clip window
- 4] Clipping against the top side of Clip window
- 5] Clipping against the right side of Clip window
- 6] Clipping against the bottom side of Clip window
- 7] These were the types of Clipping.

### \* Algorithm :

- 1] Start
- 2] Read the coordinates of clipping window then read the vertex coordinate of Clipping window.
- 3] Start with  $P[i]_x = P[0]_x$  and  $P[i]_y = P[0].y$
- 4] Use rectangle function to display window on screen
- 5] then draw polygon on window with the help of left( $P_1, \theta, pP$ ) right( $P_2, \Delta pP$ )
- 6] then call left function  
 $\text{left } (P_2, p\theta, P_1, P[20]; P + pP[P_2+1])$

- 7) If  $(P[i].n - P[i].y) \cdot n - P[i].x \cdot n > 0$  ( $P[i].n < P[i].y$ )  
 Then call right function  
 $\text{right}(P_1, P_2, P[i].x, P[i].y, P[i].n)$   
 8) If  $(P[i].n - P[i].y) \cdot n = 0$  ( $P[i].n = P[i].y$ )  
 $(P_1 \cdot n - P[i].y) + P[i].x = 0$   
 Then call the top function to clip triangle  
 of polygon  
 9) If  $(P[i+1].y - P[i].y) \cdot n = 0$  Then calculate  
 $(P_1 \cdot y - P[i].y) + P[i].x, n = 0$   
 10) If bottom  
 11) If  $(P[i+1].y - P[i].y) \cdot n < 0$  Then calculate  
 $P[i].n = P[i].d - P[i].y$  ( $P[i].d \cdot y - P[i].y$ )  
 $\rightarrow (P_2 \cdot y) \cdot P[i].d - P[i].y$   
 12) Draw polygon using draw polygon  
 13) End





```

//14 - code
#include<stdio.h>
#include<conio.h>
#include<graphics.h>
#include<math.h>
void dda(int,int,int,int,int,int,int,int);
void dda(int x1,int y1,int x2,int y2,int xmin,int ymin,int xmax,int ymax)
{
    float dx,dy;
    float steps,x=x1,y=y1;
    int i=0;
    dx=x2-x1;
    dy=y2-y1;
    if(abs(dx)>=abs(dy))
        steps=abs(dx);
    else
        steps=abs(dy);
    dx=dx/steps;
    dy=dy/steps;
    while(i++<=steps)
    {
        if(x>=xmin && x<=xmax && y>=ymin && y<=ymax)
        {
            line(x,y,x2,y2);
            return;
        }
        x=x+dx;
        y=y+dy;
    }
}
void main()
{
    int n, gd, gm, x1, x2, y1, y2, xRec, yRec, b1, b2, b3, b4, l, b, yMin, yMax, xMin, xMax;
    float m;
    int a[10][4], i, j, flag=0, in=0;
    gd=DETECT;
    gm=DETECT;
    initgraph(&gm, &gd, "C:\\TC\\BGI");
    printf("Enter the length and breadth of the clipping window:\n");
    scanf("%d%d", &l, &b);
    printf("Enter the starting co-ord of the rectangle\n");
    scanf("%d%d", &xRec, &yRec);
    clrscr();
    rectangle(xRec, yRec, xRec+l, yRec+b);
}

```

```

getch();
clrscr();

printf("Enter the no of lines\n");
scanf("%d",&n);

for(i=0;i<n;i++)
{
    printf("Enter the co-ord of line %d\n",i+1);
    for(j=0;j<2;j++)
    {
        scanf("%d",&a[i][j]);
    }
    a[i][2]=a[0][0];
    a[i][3]=a[0][1];
    if(i!=0)
    {
        a[i-1][2]=a[i][0];
        a[i-1][3]=a[i][1];
    }
}
clrscr();
rectangle(xRec,yRec,xRec+l,yRec+b);
for(i=0;i<n;i++)
{
    line(a[i][0],a[i][1],a[i][2],a[i][3]);
}
getch();
clrscr();
rectangle(xRec,yRec,xRec+l,yRec+b);

xMin=xRec;
yMin=yRec;
xMax=xRec+l;
yMax=yRec+b;

for(i=0;i<n;i++)
{
    flag=0;
    x1=a[i][0];
    x2=a[i][2];
    y1=a[i][1];
    y2=a[i][3];

    if(x1>=xMin && x1<=xMax && y1>=yMin && y1<=yMax)
        flag++;
}

```

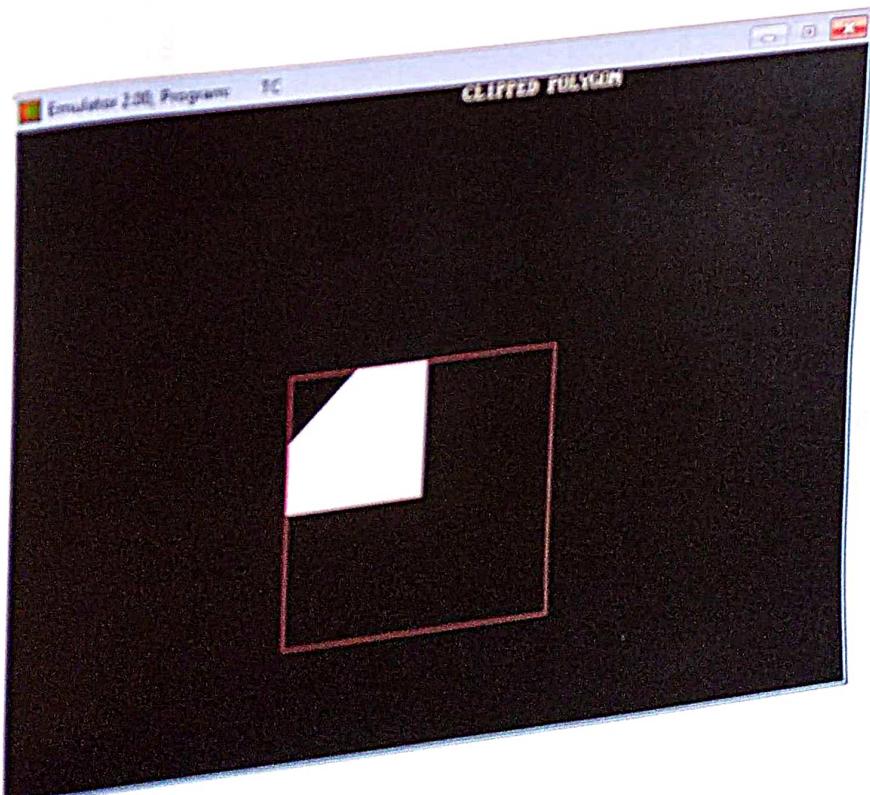
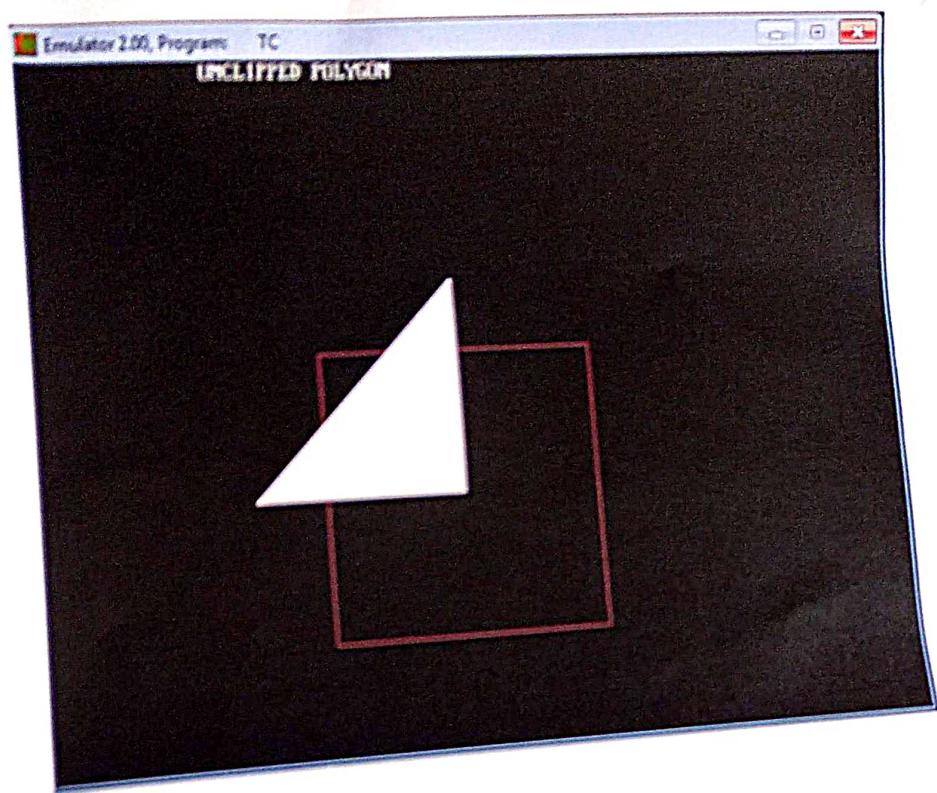
```

if(x2>=xMin && x2<=xMax && y2>=yMin && y2<=yMax)
    flag++;

switch(flag)
{
    case 0:
        break;
    case 1: if(x2>=xMin && x2<=xMax && y2>=yMin && y2<=yMax)
    {
        dda(x1,y1,x2,yMin,xMax,yMax);
    }
    else
    {
        dda(x2,y2,x1,yMin,xMax,yMax);
    }
    break;
    case 2: line(x1,y1,x2,y2);
    break;
}

getch();
closegraph();

```



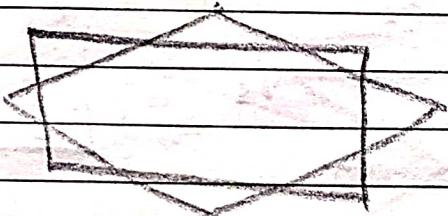
## \* Practical Related Questions

1) If vertex is outside the clipping window and second point is inside the clipping window, then write which points are added to output vertex list.

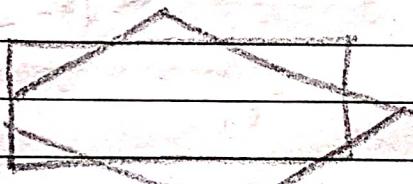
→ If the first vertex is outside the clipping window and second point is inside the clipping window, then both the intersection point of the polygon edge with window boundary and second vertex are added to OIP vertex list.

2) Write Procedure to Clip polygon using Sutherland and Hodgeson Polygon Clipping algorithm.

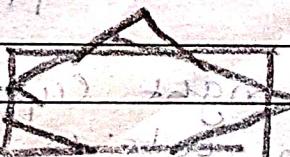
Before clipping :



1) After clipping against left side of window



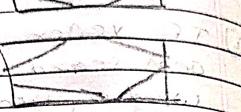
2) After Clipping against bottom side of window



2) After Clipping from top side of window



1] Polygon Clipped

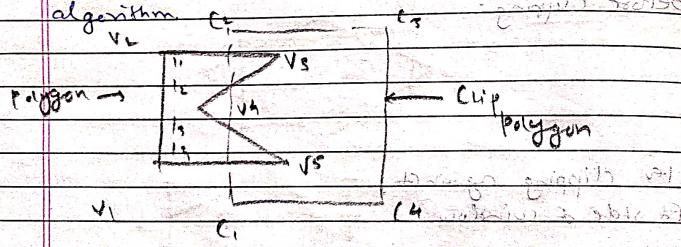


→ Conclusion:

Thus, we learned the program to clip polygon using Sutherland Hodgeman algorithm.

→ Exercise:

1] Clip the following polygon using Cohen Sutherland Polygon Clipping algorithm



→ After left Clipping :  $V_1, V_2, V_4, V_2, V_5'$

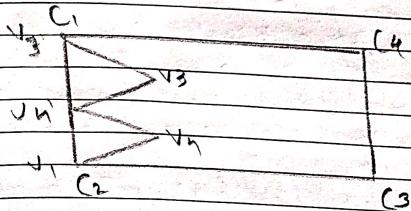
After right Clipping :  $V_1 = \text{outside}, V_2 = \text{inside}$

→ To save  $V_2$  and  $V_3$

$V_3 = \text{inside}$        $V_4 = \text{outside}$   
Save  $V_4$  and  $V_3$

$V_1 = \text{outside}$        $V_5 = \text{inside}$   
Save  $V_1$  and  $V_5$

Clipped Polygon,



## 15. Program to draw Hilbert's Curve

### \* Procedure

- 1) Hilbert subroutine draws the Hilbert curve
- 2) It takes as parameters the depth of recursion and dx and dy values that give the direction in which it should draw.
- 3) It recursively draws four smaller Hilbert curve and connects them with lines.

### \* Algorithm

- 1) Start
- 2) Initialize valid hilb (float a, b, c, d, ex, ey, end, hf)
- 3) Initialise the IF Condition
- 4) if (int > 1)
  - hilb (a, b, c, d, t[n][a], ty[b], end - 1, hf / 2)
  - hilb (a, d, c, b, t[n][b], ty[c], end - 1, hf / 2)
  - hilb (c, b, a, d, t[n][d], ty[d], end - 1, hf / 2)
- 5) Then, in main function use do while loop and use switch case.
- 6) For drawing hilbert curve read the limit of window
- 7) Enter no of iteration the hilbert curve is generated.
- 8) End

```

// 15 - code
#include <stdio.h>
#define N 32
#define K 3
#define MAX N * K

typedef struct { int x; int y; } point;

void rot(int n, point *p, int rx, int ry) {
    int t;
    if (!ry) {
        if (rx == 1) {
            p->x = n - 1 - p->x;
            p->y = n - 1 - p->y;
        }
        t = p->x;
        p->x = p->y;
        p->y = t;
    }
}

void d2pt(int n, int d, point *p) {
    int s = 1, t = d, rx, ry;
    p->x = 0;
    p->y = 0;
    while (s < n) {
        rx = 1 & (t / 2);
        ry = 1 & (t ^ rx);
        rot(s, p, rx, ry);
        p->x += s * rx;
        p->y += s * ry;
        t /= 4;
        s *= 2;
    }
}

int main() {
    int d, x, y, cx, cy, px, py;
    char pts[MAX][MAX];
    point curr, prev;
    for (x = 0; x < MAX; ++x)
        for (y = 0; y < MAX; ++y) pts[x][y] = ' ';
    prev.x = prev.y = 0;
    pts[0][0] = '.';
    for (d = 1; d < N * N; ++d) {
        d2pt(N, d, &curr);
        cx = curr.x * K;
        cy = curr.y * K;
        px = prev.x * K;

```

```
py = prev.y * K;
pts[cx][cy] = '.';
if (cx == px) {
    if (py < cy)
        for (y = py + 1; y < cy; ++y) pts[cx][y] = '|';
    else
        for (y = cy + 1; y < py; ++y) pts[cx][y] = '|';
}
else {
    if (px < cx)
        for (x = px + 1; x < cx; ++x) pts[x][cy] = '_';
    else
        for (x = cx + 1; x < px; ++x) pts[x][cy] = '_';
}
prev = curr;
}
for (x = 0; x < MAX; ++x) {
    for (y = 0; y < MAX; ++y) printf("%c", pts[y][x]);
    printf("\n");
}
return 0;
}
```

## \* Practical Topological Question

1) Define curve.

→ A curve is an infinitely large set of points. Each point has two neighbors except one point. Curve can be broadly classified into three categories.

2) Write topological and fractal dimension of hilbert curve.

→ Topological dimension is 1 and fractal dimension is 2 of hilbert curve.

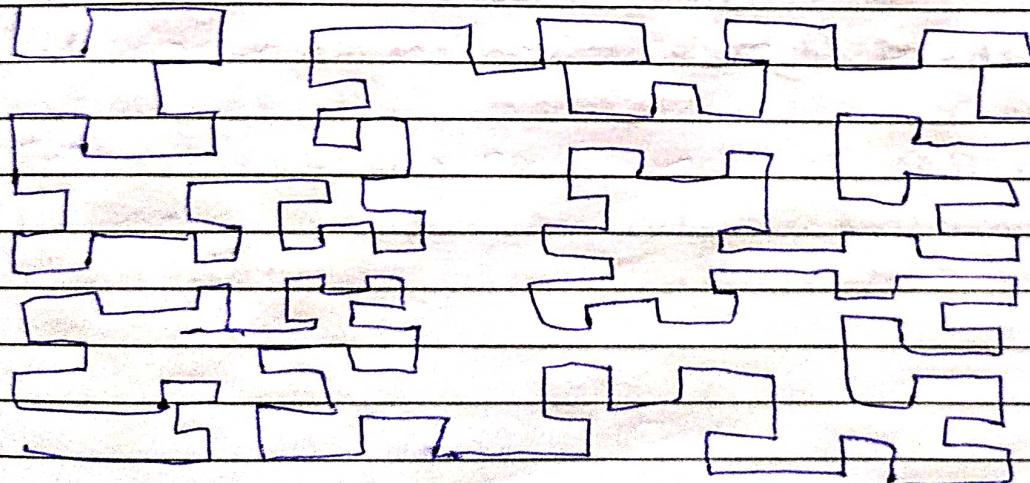
3) Conclusion

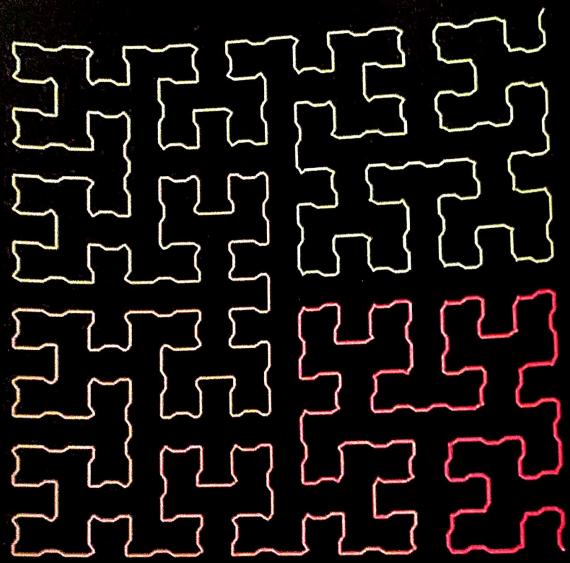
Thus, we learned to draw hilbert curve.

\* Exercise

1) Draw the hilbert curve

of





## 16. Program to draw Koch Curve and Bezier Curve

### \* Procedure

#### A) Koch curve

- 1] Start with a line segment.
- 2] Divide the line into 3 equal parts.
- 3] Trisect the line into 3 equal parts.
- 4] Form an equilateral triangle rising out of the middle segment.

#### 4] Repeat.

#### B) Bezier Curve :

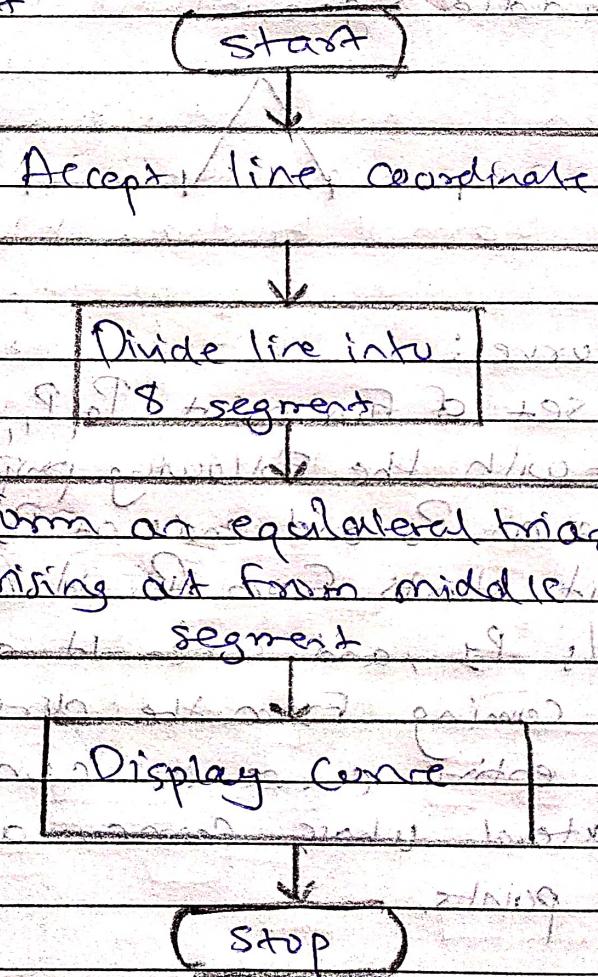
To each set of four points  $P_0, P_1, P_2, P_3$ , we associate a curve with the following properties:

- i] It starts at  $P_0$  and ends at  $P_3$ .
- ii] When it starts from  $P_0$ , it heads directly towards  $P_1$  and when it arrives at  $P_3$ , it is coming from the direction of  $P_2$ .
- iii] The entire curve is contained in the quadrilateral whose corners are the four given points.

## \* Algorithm

- 1) Start
- 2) Accept line coordinate
- 3) Divide line into 3 coordinate
- 4) Form a equilateral triangle rising out from middle segment
- 5) Repeat with newly formed segment.
- 6) Display Cores
- 7) Stop

## \* Flowchart



```
//18 - 1 - koch
#include <graphics.h>
#include <conio.h>
#include <math.h>

void koch(int x1, int y1, int x2, int y2, int it)
{
    float angle = 60*M_PI/180;
    int x3 = (2*x1+x2)/3;
    int y3 = (2*y1+y2)/3;

    int x4 = x3 + (x2-x3)*cos(angle)+(y2-y3)*sin(angle);
    int y4 = y3 - (x2-x3)*sin(angle)+(y2-y3)*cos(angle);

    if(it > 0)
    {
        koch(x1, y1, x3, y3, it-1);
        koch(x3, y3, x, y, it-1);
        koch(x, y, x4, y4, it-1);
        koch(x4, y4, x2, y2, it-1);
    }
    else
    {

        line(x1, y1, x3, y3);
        line(x3, y3, x, y);
        line(x, y, x4, y4);
        line(x4, y4, x2, y2);
    }
}

int main(void)
{
    int gd = DETECT, gm, i, n, x1 = 100, y1 = 100, x2 = 400, y2 = 400;
    initgraph(&gd, &gm, "C://TC3//BGI");
    printf("Enter number of interations");
    scanf("%d", &n);
    for(i=0; i<n; i++)
    {
        cleardevice();
        koch(x1, y1, x2, y2, i);
        getch();
    }
    return 0;
}
```

```

//16 - 1 - koch
#include<graphics.h>
#include<conio.h>
#include<math.h>

void koch(int x1, int y1, int x2, int y2, int it)
{
    float angle = 60*M_PI/180;
    int x3 = (2*x1+x2)/3;
    int y3 = (2*y1+y2)/3;

    int x4 = (x1+2*x2)/3;
    int y4 = (y1+2*y2)/3;

    int x = x3 + (x4-x3)*cos(angle)+(y4-y3)*sin(angle);
    int y = y3 - (x4-x3)*sin(angle)+(y4-y3)*cos(angle);

    if(it > 0)
    {
        koch(x1, y1, x3, y3, it-1);
        koch(x3, y3, x, y, it-1);
        koch(x, y, x4, y4, it-1);
        koch(x4, y4, x2, y2, it-1);
    }
    else
    {

        line(x1, y1, x3, y3);
        line(x3, y3, x, y);
        line(x, y, x4, y4);
        line(x4, y4, x2, y2);
    }
}

int main(void)
{
    int gd = DETECT, gm, i, n, x1 = 100, y1 = 100, x2 = 400, y2 = 400;
    initgraph(&gd, &gm, "C://TC3//BGI");
    printf("Enter number of interations");
    scanf("%d", &n);
    for(i=0; i<n; i++)
    {
        cleardevice();
        koch(x1, y1, x2, y2, i);
        getch();
    }
    return 0;
}

```

```
//16-2-code
#include<graphics.h>
#include<math.h>
#include<conio.h>
#include<stdio.h>
void main()
{
int x[4],y[4],i;
double put_x,put_y,t;
int gr=DETECT,gm;
initgraph(&gr,&gm,"C:\\TURBOC3\\BGI");
printf("\n***** Bezier Curve *****");
printf("\n Please enter x and y coordinates ");
for(i=0;i<4;i++)
{
scanf("%d%d",&x[i],&y[i]);
putpixel(x[i],y[i],3);           // Control Points
}

for(t=0.0;t<=1.0;t=t+0.001)      // t always lies between 0 and 1
{
put_x = pow(1-t,3)*x[0] + 3*t*pow(1-t,2)*x[1] + 3*t*t*(1-t)*x[2] + pow(t,3)*x[3]; // Formula to
draw curve
put_y = pow(1-t,3)*y[0] + 3*t*pow(1-t,2)*y[1] + 3*t*t*(1-t)*y[2] + pow(t,3)*y[3];
putpixel(put_x,put_y, WHITE);        // putting pixel
}
getch();
closegraph();
}
```

## Practical Related Question

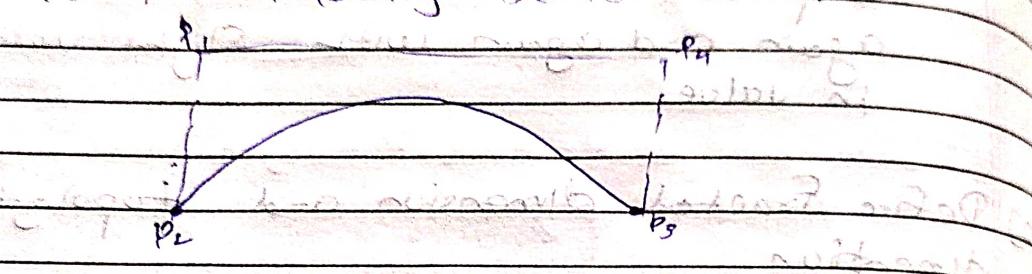
- 1) Define Fractal.
- Fractals are complex pictures generated by a computer from a single formula. They are created using repetitive steps. This means one formula is repeated again and again with slight validation in value.
- 2) Define fractal dimension and topological dimension.
- The objects which are having smooth surface and regular shape are generally described by using equation. But natural objects such as mountains, trees, oceans have irregular shape. It will be very difficult to draw those shapes by using the equation. Fractal is the most interesting form a mathematical perspective. So we can describe natural objects by using fractals.

### \* Conclusion

Thus we performed the program to form Koch curve and bezier curve.

### \* Exercise

1) Draw the following Bezier curve:



2) Draw the following Koch curve:



\*\*\*\*\* Bezier Curve \*\*\*\*\*  
Please enter x and y coordinates 200 300  
300 400  
300 300  
100 200

