

Q1 Train decision tree without pruning and observe model overfitting.

- Size of the tree: **442**
- Training error $error_D = \frac{\text{incorrectly classified instances}}{\text{Total number of instances}}$

$$= \frac{30}{30 + 5670} = \frac{30}{5700} = \mathbf{0.005263}$$
- Test error $error_S = \frac{\text{incorrectly classified instances}(r)}{\text{Total number of instances}(n)}$

$$= \frac{456}{456 + 1968} = \frac{456}{2424} = \mathbf{0.188118}$$
- 95% confidence interval of the true error on future data

$$error_D = error_S \mp 1.96 * \sqrt{(error_S * (1 - error_S)) / n}$$

$$= 0.188118 \mp 1.96 * 0.00793$$

$$= 0.188118 \mp 0.0155579$$

Lower bound = 0.1725601**Upper bound = 0.2036759****Q2 Decision pruning and model selection by cross validation.**

Range for MinNumObj = 1 to 5

Range for NumFolds = 2 to 6

MAE value(%error)	m = 1	m = 2	m = 3	m = 4	m = 5
N = 2	0.0454(3.0877)	0.0475(3.1754)	0.049(3.1404)	0.0509(3.1404)	0.0537(3.3509)
N = 3	0.0476(2.8947)	0.0488(3)	0.0499(3.0351)	0.0511(3.1053)	0.0531(3.2632)
N = 4	0.0444(2.8246)	0.0455(2.8947)	0.0473(2.9825)	0.0496(3.2281)	0.0515(3.3158)
N = 5	0.0455(2.9474)	0.0465(3.0351)	0.0482(3.0877)	0.0501(3.1754)	0.0511(3.193)
N = 6	0.0495(3.1579)	0.0496(3.1228)	0.0511(3.1754)	0.0518(3.2105)	0.0534(3.2982)

- Parameter setting used to retrain a j48 tree on entire training data:
 MinNumObj = 1, NumFolds = 4, reducedErrorPruning = True, Unpruned = False,
 numDecimalPlaces = 2, seed = 1, batchSize = 100.
- Size of tree = **122** and number of leaves = 73
- Training error $error_D = \frac{\text{incorrect classified instances}}{\text{Total number of instances}} = \frac{105}{105+5595} = \frac{105}{5700} = \mathbf{0.018142}$
- Test error $error_S = \frac{\text{incorrect classified instances}(r)}{\text{Total number of instances}(n)} = \frac{481}{481+1943} = \frac{481}{2424} = \mathbf{0.19843}$
- The 95% confidence interval of the true error on future data

$$\begin{aligned} error_D &= error_S \pm 1.96 * \sqrt{(error_S * (1 - error_S)) / n} \\ &= 0.19843 \pm 1.96 * \sqrt{0.19843 * (1 - 0.19843) / 2424} \\ &= 0.19843 \pm 1.96 * 0.0081 \\ &= 0.19843 \pm 0.015876 \end{aligned}$$

Upper bound = 0.214306

Lower bound = 0.182554

Q3 Compare learning algorithms by cross validations.

Average error of NBC models resulted in 10-fold cross validation: $\frac{1410}{5700} * 100 = \mathbf{24.7368\% (0.2418 \text{ MAE})}$.

J48, 10-fold cross validation error: $\frac{161}{5700} * 100 = \mathbf{2.8245\% (0.0444 \text{ MAE})}$

Comparing results with J48, J48 is better as there is significant difference in average error of 10-fold cross validation.

1. Finally selected model is J48,

$$\text{Test error } error_S = \frac{\text{incorrectly classified instances}(r)}{\text{Total number of instances}(n)} = \mathbf{0.19843}$$

2. Test error of other model, NBC is

$$error_S = \frac{\text{incorrectly classified instances}(r)}{\text{Total number of instances}(n)} = \frac{664}{664 + 1760} = \frac{664}{2424} = \mathbf{0.27392}$$

3. Yes, as per selection of J48 the average error is low and hence prediction of the model will work more efficiently than NBC for independent data set.