

Lab 3

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Q2. Write Java Code solution to improve bubble sort for the scenario in which the input is already sorted.

```
public class BubbleSort {  
  
    public static void main(String[] args) {  
        // TODO Auto-generated method stub  
        int[] result = bubbleSortOptimizationByNotCheckingLastSortedElement(new int[] {9,5,6,4,7,3,8,2,1});  
        int[] result2 = bubbleSortOptimizationForSortedArray(new int[] {9,5,6,4,7,3,8,2,1});  
        System.out.println(Arrays.toString(result));  
    }  
  
    static int[] bubbleSortOptimizationForSortedArray(int[] arr) {  
        int n = arr.length;  
        boolean isSwapped = false;  
        for(int i = 0; i < n ;i++){  
            isSwapped = false;  
            for(int j = 0; j < n-1; j++){  
                if(arr[j] > arr[j+1]){  
                    int temp = arr[j];  
                    arr[j] = arr[j+1];  
                    arr[j+1] = temp;  
                    isSwapped = true;  
                }  
            }  
            if(!isSwapped) break;  
        }  
        return arr;  
    }  
}
```

Time Complexity: If the array is sorted then, it runs only the inner loop. Complexity is $O(n)$.
Here, n is $O(n)$, If $f(n) \leq cg(n)$

$n \leq cn$, for all $c > 2$, this is always true. So, n is $O(n)$

Therefore, the complexity is $O(n)$

Q3. Write JavaCode solution for improving Bubble sort by cutting the running time for every ith pass.

```
public class BubbleSort {

    public static void main(String[] args) {
        // TODO Auto-generated method stub
        int[] result = bubbleSortOptimizationByNotCheckingLastSortedElement(new int[] {9,5,6,4,7,3,8,2,1});
        int[] result2 = bubbleSortOptimizationForSortedArray(new int[] {9,5,6,4,7,3,8,2,1});
        System.out.println(Arrays.toString(result));
    }

    static int[] bubbleSortOptimizationByNotCheckingLastSortedElement(int[] arr) {
        int n = arr.length;

        for(int i = 0; i < n ;i++){
            for(int j = 0; j < n-1-i; j++){
                if(arr[j] > arr[j+1]){
                    int temp = arr[j];
                    arr[j] = arr[j+1];
                    arr[j+1] = temp;
                }
            }
        }
        return arr;
    }
}
```

Time Complexity: $O(n) * O(n(n-1)/2) = O(n^2(n-1)/2)$;
Which is half of the Bubble Sort Time complexity.

Q4. Given array of n, integers that belong to the set {0,1, 2}. Write an sorting algorithm to sort the array and explain why it runs in O(n) time.

```
public static void main(String[] args) {
    int[] inputArr = new int[]{2, 2, 1, 0, 0, 1, 2, 0, 1, 2, 1, 1};
    int[] sortedArr = sortSetOf3Integers(inputArr);
    System.out.println(Arrays.toString(sortedArr));
}

public static int[] sortSetOf3Integers(int[] arr) {
    int[] resultArr = new int[arr.length];
    int aCount = 0, bCount = 0, cCount = 0;
    // Counting numbers of 0's , 1 and 2
    for (int i = 0; i < arr.length; i++) { // O(n)
        if (arr[i] == 0) aCount++;
        if (arr[i] == 1) bCount++;
        if (arr[i] == 2) cCount++;
    }
    // Creating sorted resultArr using numbers count (start-end)
    for (int i = 0; i < resultArr.length; i++) { // O(n)
        if (i < aCount) {
            resultArr[i] = 0;
        } else if (i < (aCount+bCount)) {
            resultArr[i] = 1;
        } else {
            resultArr[i] = 2;
        }
    }
    return resultArr;
}
```

Complexity: $O(n) + O(n) = 2*O(n) = O(n)$

$2n$ is $O(n)$, If $f(n) \leq cg(n)$

$2n \leq cn$, for all $c > 2$, this is always true. So, $2n$ is $O(n)$

Therefore, the complexity is $O(n)$