

Simulation Lab(MC503)

Assignment7

Try to solve all the problems

1. The PDF and CDF of Burr type III distribution is given by

$$PDF : f(x, \alpha, \beta) = \alpha \beta x^{-(\beta+1)} (1 + x^{-\beta})^{-(\alpha+1)}; x > 0, \alpha > 0, \beta > 0.$$
$$CDF : F(x, \alpha, \beta) = (1 + x^{-\beta})^{-\alpha}$$

Use the probability integral transform to generate 2000 samples from this distribution when $\alpha = 1$ & $\beta = 1.5$. Calculate mean and Variance for the generated samples. Plot this PDF and CDF for $\alpha=1, \beta=1, \alpha=1.5, \beta=3$, where the range of x is $0.01 \leq x \leq 5$ with step-size 0.01. You can use different colours to identify the PDF and CDF for different parameter values.

2. Generate 1000 random samples from the discrete uniform distribution

The PMF is: $p(x) = \frac{1}{j-i+1}; x=i, i+1, \dots, j$.

Algorithm:

Simulate $U \sim U[0,1]$. Return $X = i + [(j-i+1)U]$.

Find its means and variance and verify the sample mean and variance from the exact distribution mean.

3. Generate 1000 random samples from the Bernoulli (p) Distribution

Algorithm:

Simulate $U \sim U[0,1]$. If $U \leq p$, return $X=1$, else return $X=0$.

..... end