Lasso and Ridge Regression



Act like my Machine Learning teacher and teach me Lasso Regression and a complete guide and maths intuition and 25 mcg questions and answers

Absolutely! Let's dive into Lasso Regression, step by step. I'll structure the lesson like this:

🌀 What You'll Learn:

- 1. Introduction to Lasso Regression
- 2. Need for Regularization
- 3. Mathematical Intuition
- 4. Lasso vs Ridge vs Linear Regression
- 5. Geometric View of Lasso
- 6. Advantages & Disadvantages
- 7. Python Implementation
- 8. 25 MCQs with Answers

1. Introduction to Lasso Regression

Lasso (Least Absolute Shrinkage and Selection Operator) is a type of linear regression that includes L1 regularization. It helps prevent overfitting and can also shrink some coefficients to exactly zero, effectively performing feature selection.



1 2. Why Regularization?

When you train a model with many features, there's a chance it will fit too closely to the training data (overfit) and perform poorly on new data.

Regularization:

- Adds a penalty term to the loss function.
- Forces the model to keep weights (coefficients) small.

3. Mathematical Intuition

Standard Linear Regression:

Loss Function:

$$ext{RSS} = \sum_{i=1}^n (y_i - \hat{y}_i)^2 = \sum_{i=1}^n (y_i - eta_0 - \sum_{j=1}^p eta_j x_{ij})^2$$

Lasso Regression adds L1 penalty:

$$ext{Loss} = \underbrace{\sum_{i=1}^n (y_i - eta_0 - \sum_{j=1}^p eta_j x_{ij})^2}_{ ext{Residual Sum of Squares (RSS)}} + \lambda \underbrace{\sum_{j=1}^p |eta_j|}_{ ext{L1 Penalty}}$$

Where:

- $\lambda \geq 0$ is the **regularization strength**.
- Higher λ means more penalty (more shrinkage of coefficients).

4. Lasso vs Ridge vs Linear

Feature	Linear Regression	Ridge (L2)	Lasso (L1)
Penalty Term	None	$\lambda \sum eta_j^2$	(\lambda \sum
Coefficients Shrink?	No	Yes	Yes (some to zero)
Feature Selection	X	×	V

📊 5. Geometric Intuition

- Lasso uses an **L1-norm constraint**, which forms a **diamond-shaped region** in the coefficient space.
- Because of the sharp corners of the diamond, the optimization often "sticks" at corners → some coefficients = 0.

🔽 6. Advantages & Disadvantages

Advantages:

- Feature selection
- Reduces overfitting
- Simple and interpretable

X Disadvantages:

- Can be unstable when features are highly correlated
- Doesn't perform group selection (only picks one of many correlated variables)



🔪 7. Lasso in Python

```
python
from sklearn.linear model import Lasso
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_squared_error
# Sample data
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2)
# Apply Lasso
lasso = Lasso(alpha=1.0)
lasso.fit(X_train, y_train)
# Predict
y pred = lasso.predict(X test)
# Evaluate
print("MSE:", mean_squared_error(y_test, y_pred))
print("Coefficients:", lasso.coef_)
```

8. 25 MCQs on Lasso Regression

Q1. What is the penalty used in Lasso Regression?

a) L2

b) L1

c) L0

d) None

Ans: b)

Q2. Lasso can shrink some coefficients to:

a) Zero

b) Infinity

c) Negative values only

d) Mean of data

Ans: a)

Q3. In Lasso regression, increasing λ leads to:

a) Larger coefficients

b) Smaller coefficients

c) No change

d) Overfitting

Ans: b)

Q4. Lasso helps in:

- a) Model selection
- b) Feature selection
- c) Clustering
- d) Normalization

Ans: b)

Q5. Lasso regression reduces:

- a) Bias
- b) Variance
- c) Both bias and variance
- d) None

Ans: b)

Q6. Which norm is used in Lasso?

- a) L1
- b) L2
- c) Frobenius
- d) Manhattan

Ans: a)

Q7. When $\lambda=0$, Lasso becomes:

- a) Ridge
- b) Linear Regression
- c) Logistic Regression
- d) SVM

Ans: b)

Q8. Lasso prefers:

- a) All features equally
- b) Dense models
- c) Sparse models
- d) Random features

Ans: c)

Q9. Lasso works well when:

- a) Many correlated features
- b) Few non-zero features
- c) All features are relevant
- d) Data is non-linear

Ans: b)



Q10. The main difference between Lasso and Ridge is:

- a) Type of data used
- b) Loss function
- c) Type of penalty
- d) Use of cross-validation

Ans: c)

Q11. Lasso is best for:

- a) Dimensionality reduction
- b) Time series
- c) Classification
- d) Feature extraction

Ans: a)

Q12. What happens to irrelevant features in Lasso?

- a) Grows large
- b) Becomes NaN
- c) Shrunk to zero
- d) Stays constant

Ans: c)

Q13. Lasso's objective function is:

$$\min_{eta} \sum (y - Xeta)^2 + \lambda \sum |eta|$$

True / False?

Ans: True

Q14. Does Lasso perform variable selection?

Ans: Yes

Q15. Does Ridge perform variable selection?

Ans: No

Q16. Lasso penalty is:

- a) Convex
- b) Non-convex
- c) Linear

Ans: a) (but also note: L1 is convex but not differentiable at 0)

Q17. Which of the following can be zero in Lasso?

- a) Error
- b) Intercept
- c) Coefficients
- d) X-values

Ans: c)

Q18. What's the typical result of Lasso on high-dimensional data?

- a) Dense models
- b) Models with all features
- c) Models with few selected features
- d) Logistic models

Ans: c)

Q19. In Lasso, what does a very high lambda do?

- a) Fit well
- b) Selects all features
- c) Makes model too simple
- d) Enhances accuracy

Ans: c)

Q20. Lasso regression is primarily used for:

- a) Classification
- b) Regression with irrelevant features
- c) Clustering
- d) PCA

Ans: b)

Q21. Lasso can't handle:

- a) Sparse data
- b) Multicollinearity well
- c) Linear relationships
- d) Overfitting

Ans: b)

Q22. What's the role of alpha in Lasso in sklearn?

- a) It's learning rate
- b) It's max iterations
- c) It's the regularization strength
- d) None

Ans: c)

Q23. Lasso selects features by:

- a) Correlation
- b) Randomness
- c) Shrinking less useful coefficients to zero
- d) Clustering

Ans: c)

Q24. If we use StandardScaler with Lasso, it is to:

- a) Normalize target
- b) Scale inputs
- c) Increase speed
- d) Nothing

Ans: b)

Q25. Which regression shrinks some coefficients to zero?

- a) Ridge
- b) OLS
- c) Lasso
- d) None

Ans: c)

Would you like:

- A PDF of this guide?
- A small dataset to try Lasso yourself?
- A notebook to test the MCQs interactively?

Let me know how you'd like to proceed.