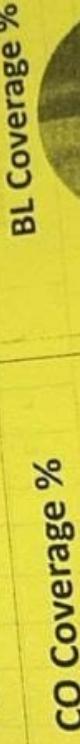


CO1	problems in Science and Engineering.	4	1	3
CO2	Analyze vector differentiation and vector integration and related Theorems.	4	1	3
CO3	Apply Laplace Transforms techniques in solving Engineering problems.	4	1	3
CO4	Extend their knowledge apply multiple integrals in solving problems in Science and Engineering. Of the Fundamentals of analytic functions.	4	1	3
COS	Utilize Complex Integrals and Power series in solving Engineering problems.	4	1	3

Q. No	Questions	Part-A			
		Marks	BL	CO	PO
1	If $\phi(x, y, z)$ be a scalar point function, then	1	1	1	1,2
	(a) If $\phi(x, y, z) = 0$ (b) $\operatorname{div}(\operatorname{grad} \phi) = 0$ (c) $\operatorname{grad} \phi = 0$ (d) $\vec{F} = \operatorname{grad} \phi$	1	1	1	1,2
2	If \vec{r} be the position vector of any point (x, y, z) with respect to origin then	1	2	3	1,2
	(a) $\operatorname{curl} \vec{r} = 1$ (b) $\operatorname{div} \vec{r} = 1$ (c) $\operatorname{curl} \vec{r} = 3$ (d) $\operatorname{div} \vec{r} = 3$	1	2	3	1,2
3	$L[e^{-t} \sin 3t] =$	3	3	3	1,2
	(a) $\frac{3}{s^2+9}$ (b) $\frac{s}{s^2+9}$ (c) $\frac{3}{(s+1)^2+9}$ (d) $\frac{3}{(s-1)^2+9}$	1	2	3	1,2
4	$L^{-1}\left\{\frac{s}{s^2+16}\right\} =$	4	3	2	1,2
	(a) $\cos t$ (b) $\sin 4t$ (c) $\sin 2t$ (d) $\cos 4t$	4	3	2	1,2
	Part-B				
	Answer ANY TWO questions (2X8 = 16 Marks)				
	Answer of $f(x, y, z) = x^2yz + xy^2z + xyz^2$ at the point $(1, -1, 2)$ in the direction of the vector $2\vec{i} - 3\vec{j} + 2\vec{k}$.				
5	(i) Find the directional derivative of $f(x, y, z) = x^2yz + xy^2z + xyz^2$ at the point $(1, -1, 2)$ in the direction of the vector $2\vec{i} - 3\vec{j} + 2\vec{k}$. (ii) Prove that $\vec{F} = (2x + yz)\vec{i} + (4y + xz)\vec{j} + (-6z + xy)\vec{k}$ is solenoidal and irrotational.	4	3	2	1,2
6	(i) Find a unit vector normal to the surface $x^2 + y^2 - z = 10$ at $(1, 1, 1)$. (ii) Find the angle between the surfaces $x^2 + y^2 + z^2 = 9$ and $x^2 + y^2 - z = 3$ at the point $(2, -1, 2)$.	4	3	2	1,2

7	(i) Find $L\{t \sin 4t\}$.		4	3	3	1,2
	(ii) Find $L^{-1}\left\{\frac{s-3}{s^2+4s+13}\right\}$		4	3	3	1,2
Part-C						
	Answer ANY TWO questions (2X15 = 30 Marks)			15	4	2
8	Verify Stoke's theorem for $\vec{F} = (x^2 - y^2)\hat{i} + 2xy\hat{j}$ for the rectangular region in the xy plane bounded by the lines $x = 0, x = 2, y = 0$ and $y = 3$.		for	15	4	2
9	Verify Gauss divergence theorem over the rectangular parallelepiped $0 \leq x \leq 2, 0 \leq y \leq 4$, and $0 \leq z \leq 6$.			10	4	3
10	(i) Using convolution theorem evaluate $L^{-1}\left\{\frac{1}{s^2(s+3)}\right\}$. (ii) Verify the final value theorem for the function $f(t) = 1 + e^{-t}(\sin t + \cos t)$.			5	3	3

Course Outcome (CO) and Bloom's level (BL) Coverage in Questions



Approved by the Audit Professor/Course Coordinator

Evaluation Sheet

Q. No	CO	Mat. Marks	Marks Obtained	Total
1	2	1	1	
2	2	1	1	
3	3	1	1	

Name of the Student:

Register No.:

Part-A

Answer ALL the questions (4X1 = 4Marks)

Q. No	Questions	Marks	BL	CO	PO
-------	-----------	-------	----	----	----

1 If $\phi(x, y, z) = c$ be a scalar point function, then the unit normal to this surface is

- (a) $\nabla \phi$ (b) $\nabla \cdot \phi$ (c) $\nabla \times \phi$ (d) $\nabla \phi / |\nabla \phi|$

2 The angle between two surfaces $\phi_1(x, y, z) = c_1$ and $\phi_2(x, y, z) = c_2$ is

- (a) $\cos^{-1} \left(\frac{\nabla \phi_1 \cdot \nabla \phi_2}{|\nabla \phi_1| |\nabla \phi_2|} \right)$ (b) $\sin^{-1} \left(\frac{\nabla \phi_1 \cdot \nabla \phi_2}{|\nabla \phi_1| |\nabla \phi_2|} \right)$
 (c) $\tan^{-1} \left(\frac{\nabla \phi_1 \cdot \nabla \phi_2}{|\nabla \phi_1| |\nabla \phi_2|} \right)$ (d) $\cot^{-1} \left(\frac{\nabla \phi_1 \cdot \nabla \phi_2}{|\nabla \phi_1| |\nabla \phi_2|} \right)$

3 $L\{t^3 e^{-2t}\} =$

- (a) $\frac{6}{s^4}$ (b) $\frac{6}{s^4 + 2}$ (c) $\frac{6}{(s-2)^4}$ (d) $\frac{6}{(s+2)^4}$

4 $L^{-1} \left\{ \frac{1}{s^2 + 25} \right\} =$

- (a) $\cos 5t$ (b) $\sin 5t / 5$ (c) $\sin 5t$ (d) $\cos 5t / 5$

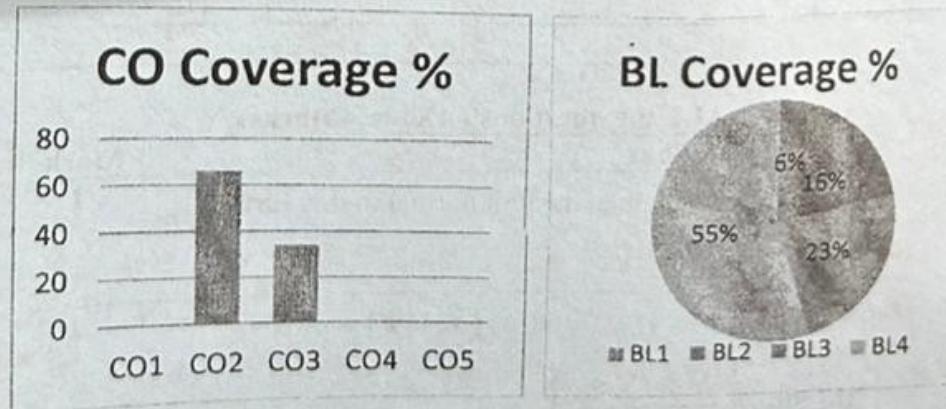
Part-B
Answer ANY TWO questions (2X8 = 16 Marks)

- 5 (i) Find the directional derivative of $f(x, y, z) = 3x^2y - 4xy^2z + 5yz^2$ at the point $(1, 1, 0)$ in the direction of the vector $\vec{i} + 3\vec{j} - 3\vec{k}$.
 (ii) Find the divergence and curl of the vector point function

4	3	2
---	---	---

	$\vec{F} = (x - x^2yz)\vec{i} + (y - xy^2z)\vec{j} + (z - xyz^2)\vec{k}$ at a point $(1, 1, 1)$.			
6	Show that $\vec{F} = (y+z)\vec{i} + (x+z)\vec{j} + (x+y)\vec{k}$ is irrotational such that $\vec{F} = \nabla\phi$ and hence calculate the scalar potential.	4 8	3 3	2 2
7	(i) Find $L\left\{\frac{\cos at - \cos bt}{t}\right\}$. (ii) Verify the initial value theorem for the function $f(t) = 3 - 2 \cos t$.	4 4	3 3	3 3
	Part-C Answer ANY TWO questions (2X15 = 30 Marks)			
8	Verify Green's theorem in the plane for $\oint_C [(3x^2 - 8y^3)dx + (4y - 6xy)dy]$, C is the closed curve of the region bounded by $x = 0, y = 0$, and $x + y = 1$.	15	4	2
9	Verify Gauss divergence theorem for $\vec{F} = 4xz\vec{i} - y^2\vec{j} + yz\vec{k}$ taken over the cube bounded by the planes $x = 0, x = 3, y = 0, y = 3, z = 0$ and $z = 3$.	15	4	2
10	(i) Using convolution theorem evaluate $L^{-1}\left\{\frac{1}{(s^2 + 1)^2}\right\}$. (ii) Find $L^{-1}\left\{\frac{1}{s(s+1)(s+2)}\right\}$.	10 5	4 3	3 3

Course Outcome (CO) and Bloom's level (BL) Coverage in Questions



Approved by the Audit Professor/Course Coordinator

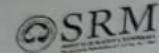
Evaluation Sheet

Q. No	CO	Max. Marks	Marks Obtained
1	2	1	
2	2	1	
3	3	1	
4	3	1	
5	2	8	

Name of the Student:

Register No.:

Consolidated Marks:



Internal Assessment: FT III
 Course Code & Title: 21MAB102T- Advanced Calculus and Complex Analysis
 Year & Sem: I & II

Date: 18.03.2024
 Duration: 2 periods
 Max. Marks: 50

Slot B1
 Set A

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
COS	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

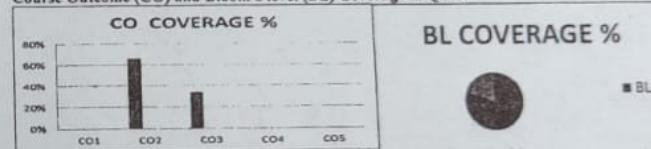
Part- A (4 * 1= 4 Marks)

Answer all the question

Q. No	Questions	Marks	BL	CO	PO
1	The value of $\nabla^2 u$ for $u = x^2 - y^2 + 4z$ is (a) 0 (b) 1 (c) 3 (d) 4	1	1	2	2
2	The value of $\nabla \cdot \vec{F}$ for $\vec{F} = (x+3y)\hat{i} + (y-3z)\hat{j} + (x-2z)\hat{k}$ is (a) 0 (b) 1 (c) 3 (d) 4	1	1	2	2
3	The value of $L[e^{st}]$ is (a) $4/s$ (b) $3/s$ (c) $1/s$ (d) s	1	1	3	2
4	The value of $L[r^n]$, when n is an integer is (a) $\frac{n!}{s^{n+1}}$ (b) $\frac{(n-1)!}{s^{n+1}}$ (c) $1/s$ (d) s	1	1	3	2
Part- B (2 * 8= 16 Marks) Answer any 2 questions					
5	Show that the vector field \vec{F} given by $\vec{F} = (x^2 - yz)\hat{i} + (y^2 - zx)\hat{j} + (z^2 - xy)\hat{k}$ is irrotational such that $\vec{F} = \nabla \phi$ and hence find the scalar potential ϕ	8	1	2	2
6	(i) Find the angle between the surfaces $z = x^2 + y^2 - 3$ and $x^2 + y^2 + z^2 = 9$ at the point $(2, -1, 2)$ (ii) Find the unit normal to the surface $x^2 + 2y^2 + z^2 = 7$ at the point $(1, -1, 2)$	4	1	2	2

7	(i) Find $L\left[\frac{e^{-st} - e^{-3t}}{t}\right]$	4	1	3	2
	(ii) Find $L^{-1}\left[\frac{1}{s(s^2 + 2s + 2)}\right]$	4	1	3	2
Part- C (2 * 15= 30 Marks) Answer any 2 questions					
8	Verify Stokes theorem for $\vec{F} = (y - z + 2)\hat{i} + (yz + 4)\hat{j} - (xz)\hat{k}$ where S is the surface of a cube $x=0, y=0, z=0, x=2, y=2, z=2$ above the Xoy plane	15	2	2	2
9	Verify Green's theorem in the plane for $\oint_C (xy + y^2)dx + x^2 dy$ where C is the closed curve of the region bounded by $y = x$ and $y = x^2$	15	2	2	2
10	(i) Find $L^{-1}\left[\frac{s}{(s^2 + 1)(s^2 + 4)}\right]$ using convolution theorem (ii) Verify initial value theorem for the function $f(t) = 1 + e^{-t}(\sin t + \cos t)$	10	1	3	2

Course Outcome (CO) and Bloom's level (BL) Coverage in Questions



Approved by the Audit Professor/Course Coordinator

Name of the Student:
 Register No.:

Evaluation Sheet

Part- A (4 * 1= 4 Marks)		
Q. No	CO	Marks Obtained
1	2	
2	2	
3	3	
4	3	

Part B (2 * 8=16)		
Q. No	CO	Marks Obtained
5	2	
6	2	
7	3	
	3	

Part B (2 * 15=30)		
Q. No	CO	Marks Obtained
8	2	
9	2	
10	3	
	3	

Consolidated Marks:

CO	Marks Scored
CO1	
CO2	
CO3	
Total	

Signature of the Course Teacher

Internal Assessment: FT3

Course Code & Title: 21MABJ02T- Advanced Calculus and Complex Analysis
 Year & Sem: I & II

Date: 18.03.2024
 Duration: 2 Periods
 Max. Marks: 50

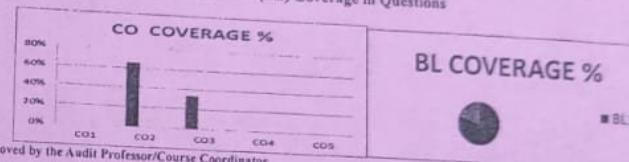
Course Articulation Matrix

At the end of this course, learners will be able to:		Program Outcomes (PO)												
		Learning Bloom's Level	1	2	3	4	5	6	7	8	9	10	11	12
CO1 Apply multiple integrals in solving problems in Science and Engineering		4	3	3										
CO2 Analyze vector differentiation and vector integration and related Theorems		4	3	3										
CO3 Apply Laplace Transforms techniques in solving Engineering problems		4	3	3										
CO4 Extend their knowledge in Fundamentals of analytic functions		4	3	3										
CO5 Utilize Complex integrals and Power series in solving Engineering problems		4	3	3										

Q. No.	Part A (4 * 1 = 4 Marks) Answer all Questions				Marks	BL	CO	PO
1	The value of $\text{curl } \vec{F}$ for $\vec{F} = xy\vec{i} + yz\vec{j} + zx\vec{k}$ is (a) $x\vec{i} + z\vec{j} + y\vec{k}$ (b) $y\vec{i} - z\vec{j} - x\vec{k}$ (c) $-y\vec{i} - z\vec{j} - x\vec{k}$ (d) $-x\vec{i} - y\vec{j} - z\vec{k}$	1	1	2	2			
2	If the vector $\vec{v} = (x+3y)\vec{i} + (y-2z)\vec{j} + (x+az)\vec{k}$ is solenoidal, then the value of the constant 'a' is (a) 2 (b) -2 (c) 1 (d) 4	1	1	2	2			
3	$L[5t^2] =$ (a) $\frac{z}{s^3}$ (b) $\frac{2}{s^2}$ (c) $\frac{10}{s^3}$ (d) $\frac{10}{s^2}$	1	1	3	2			
4	The value of $L^{-1}\left[\frac{3}{s-1}\right]$ is (a) $3e^t$ (b) $3e^{-t}$ (c) e^t (d) e^{-t}	1	1	3	2			
Part-B (2 * 8 = 16 Marks) Answer any two questions								
Q. No.	Questions	Marks	BL	CO	PO			
5	Find the total work done in moving a particle in a force field given by $\vec{F} = 3xy\vec{i} - 5z\vec{j} + 10x\vec{k}$ along the curve $x = t^2 + 1, y = 2t^2, z = t^3$ from $t = 1$ to $t = 2$.	8	1	2	2			
6	(i) Find the angle between the surfaces $x^2 + yz = 2$ and $x + 2y - z = 2$ at $(1,1,1)$. (ii) Find the unit normal vector to the level surface $x^2y + 2xz = 4$ at the point $(2, -2, 3)$	4	1	2	2			
7	(i) Find the Laplace transform of $\frac{\sin t}{t}$. (ii) Find $L^{-1}\left[\frac{s}{s^2+4s+5}\right]$	4	1	3	2			

Part-C (2 * 15= 30 Marks) Answer any two questions				
8	Verify Stoke's theorem for $\vec{F} = (x^2 + y^2)\vec{i} - 2xy\vec{j}$ taken around the rectangle bounded by the lines $x = \pm a, y = 0$ and $y = b$.	15	2	2
9	Verify Gauss Divergence theorem for the function $\vec{F} = 4xz\vec{i} - y^2\vec{j} + yz\vec{k}$ taken over the cube bounded by the planes $x = 0, x = 2, y = 0, y = 2, z = 0$ and $z = 2$.	15	2	2
10	(i) Find $L^{-1}\left[\frac{1}{(s^2+a^2)^2}\right]$ using convolution theorem. (ii) Evaluate $\int_0^\infty te^{-2t} \sin t dt$ using Laplace transform.	10	1	3

Course Outcome (CO) and Bloom's level (BL) Coverage in Questions



Approved by the Audit Professor/Course Coordinator

Name of the Student:
 Register No.:

Evaluation Sheet

Part-A (4 * 1= 4 Marks)			
Q. No	CO	Marks Obtained	Total
1	1		
2	1		
3	1		
4	1		

Part B(2 * 8=16)			
Q. No	CO	Marks Obtained	Total
5	2		
6	2		
7	3		
	3		

Part B(2 * 15=30)			
Q. No	CO	Marks Obtained	Total
8	2		
9	2		
10	3		
	3		

Consolidated Marks:

CO	Marks Scored
CO2	
CO3	
Total	

Signature of the Course Teacher

Answer any 2 questions
16 Marks)

Q. No	Questions	Marks	BL	CO	PO
1	Change the order of integration in $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} xy dy dx$ and hence evaluate it.	8	3	1	2
2	Evaluate $\iint r^3 dr d\theta$, over the area bounded between the circles $r = 2 \cos \theta$ and $r = 4 \cos \theta$.	8	3	1	2
3	Evaluate $\iint xy dx dy$ over the positive quadrant of the circle $x^2 + y^2 = 1$.	8	3	1	2
Part-B (1 * 14 = 14 Marks)					
4	(i) Evaluate $\int_0^1 \int_{y^2}^1 \int_0^{1-x} x dx dy dz$.	7	4	1	2

- (ii) Find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ using double integration.
- | | | | |
|---|---|---|---|
| 7 | 4 | 1 | 2 |
|---|---|---|---|



Date: 21.02.2024
Duration: 1 hour 10 minutes
Max. Marks: 30

Course Articulation Matrix

At the end of this course, learners will be able to:

Course Outcomes (CO)		Learning Bloom's Level	Program Outcomes (PO)											
CO1	CO2		1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

Part - A (2*8 = 16 Marks)
Answer any 2 questions

Q. No.	Questions	Marks	BL	CO	PO
1.	Change the order of integration in $\int_0^a \int_{a-y}^{\sqrt{a^2-y^2}} y dy dx$ and hence evaluate it.	8	3	1	2
2.	Evaluate $\iint_R xy dx dy$, where R is the region bounded by the parabola $y^2 = x$, the x -axis and the line $x + y = 2$, lying on the first quadrant.	8	3	1	2
3.	Evaluate $\iint_A r \sin \theta dr d\theta$ over the area of the cardioid $r = a(1 + \cos \theta)$ above the initial line.	8	3	1	2

PART - B (1*14 = 14 Marks)

4.	(i) Find the smaller of the area bounded by $y = 2 - x$ and $x^2 + y^2 = 4$ using double integral. (ii) Evaluate $\int_0^a \int_0^{b(1-\frac{x}{a})} \int_0^{c(1-\frac{x}{a}-\frac{y}{b})} dx dy dz$.	7	4	1	2
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SRM Institute of Science and Technology

College of Engineering and Technology

DEPARTMENT OF MATHEMATICS

SRM Nagar, Kattankulathur 603203, Chengalpattu District, Tamilnadu

Academic Year: 2023-2024 (EVEN)

Slot D2
Set B

Internal Assessment: CLA1 T1

Course Code & Title: 21MAB102T - Advanced Calculus and Complex Analysis

Year & Sem: I & II

Date: 21.02.2024

Duration: 1 hour 10 minutes

Max. Marks: 30

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

Part - A (2*8 = 16 Marks)

Answer any 2 questions

Q. No.	Questions	Marks	BL	CO	PO
1.	Change the order of integration in $\int_0^3 \int_1^{\sqrt{4-y}} (x+y) dx dy$ and hence evaluate it.	8	3	1	2
2.	Using double integral find the area enclosed by the curves $y = 2x^2$ and $y^2 = 4x$.	8	3	1	2
3.	Evaluate the double integral $\int_0^{\frac{\pi}{3}} \int_0^{a \sin 3\theta} r dr d\theta$.	8	3	1	2
PART - B (1*14 = 14 Marks)					
4.	(i) Evaluate $\int_0^1 \int_0^{\sqrt{1+x^2}} \frac{dy dx}{1+x^2+y^2}$. (ii) Evaluate $\int_0^a \int_0^{\sqrt{a^2-x^2}} \int_0^{\sqrt{a^2-x^2-y^2}} \frac{dz dy dx}{\sqrt{a^2-x^2-y^2-z^2}}$.	7	4	1	2
		7	4	1	2



**SRM Institute of Science and Technology
College of Engineering and Technology
DEPARTMENT OF MATHEMATICS**

SRM Nagar, Kattankulathur – 603203, Chengalpattu District, Tamilnadu

Academic Year: 2023-24 (EVEN)

Slot B2
Set B

Internal Assessment: CLA1 T1
Course Code & Title: 21MAB102T- Advanced Calculus and Complex Analysis
Year & Sem: I & II

Date: 19.02.2024
Duration: 1 hour 10 minutes
Max. Marks: 30

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

Part- A (2 * 8= 16 Marks) Answer any 2 questions					
Q. No	Questions	Marks	BL	CO	PO
1	Change the order of integration in $\int_0^a \int_x^a (x^2 + y^2) dy dx$ and hence evaluate it.	8	3	1	2
2	Find the area bounded by the circles $r = 2 \sin \theta$ and $r = 4 \sin \theta$.	8	3	1	2
3	Evaluate $\iint_R (4 - x^2 - y^2) dx dy$ where R is the region bounded by the lines $x = 0$, $x = 1$, $y = 0$ and $y = 3$.	8	3	1	2

Part- B (1 * 14= 14 Marks)					
4	(i) Evaluate $\int_0^1 \int_0^{1-x} \int_0^{x+y} e^z dz dy dx$. (ii) Using double integration find the area bounded by $y = x$ and $y = x^2$	7	4	1	2



Test: FT- IV **Date: 25.04.2024**
Course Code & Title: 21MAB102T- Advanced Calculus and Complex Analysis **Duration: 2 Periods**
Year & Sem: I & II **Max. Marks: 50**

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems.	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems.	4	3	3										
CO4	Extend their knowledge of the Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex Integrals and Power series in solving Engineering problems.	4	3	3										

Part-A

Answer ALL the questions (4X1 = 4 Marks)

Q. No	Questions	Marks	BL	CO	PO
1	The invariant points of the transformation $w = \frac{2z+4i}{iz+1}$ are (a) $z = 4i, -i$ (b) $z = -4i, i$ (c) $z = 2i, i$ (d) $z = -2i, i$	1	2	4	1,2
2	The necessary condition for $f(z)$ to be analytic is (a) $u_x = v_y, u_y = -v_x$ (b) $u_x = v_y, u_y = v_x$ (c) $u_x = v_y, u_y = -v_{xx}$ (d) $u_x = v_{yy}, u_y = v_x$	1	1	4	1,2
3	If $f(z)$ is analytic inside and on C , the value of $\int_C \frac{f(z)}{z-a} dz$, where C is the simple closed curve and 'a' is any point inside C is (a) $f(a)$ (b) $2\pi i f(a)$ (c) $\pi i f(a)$ (d) 0	1	1	5	1,2
4	The poles of $f(z) = \frac{1}{(z-5)^3}$ are (a) $z = 5$ is a pole of order 5 (b) $z = 5$ is a simple pole (c) $z = 3$ is a pole of order 3 (d) $z = 5$ is a pole of order 3	1	2	5	1,2

Part-B

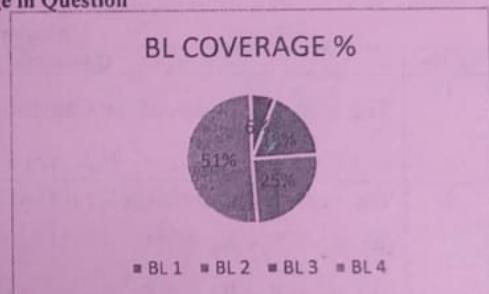
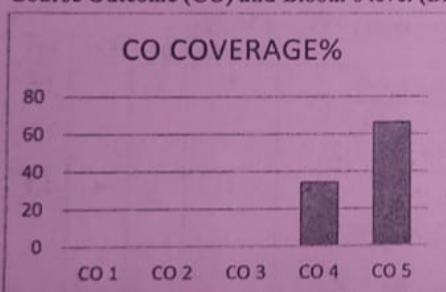
Answer ANY TWO questions (2 x 8 = 16 Marks)

5	Find the analytic function $f(z)$ whose real part is given by $u = x^3 - 3xy^2 + 3x^2 - 3y^2 + 1$ using Milne Thomson method.	8	4	4	1,2
6	Evaluate $\int_C \frac{4-3z}{z(z-1)(z-2)} dz$ where C is a circle $ z = \frac{3}{2}$ by using Cauchy's integral formula.	8	3	5	1,2
7	Expand $f(z) = \frac{1}{(z-1)(z-2)}$ in Laurent's series valid for the region (i) $1 < z < 2$ (ii) $ z > 2$	8	2	5	1,2



Part-C Answer ANY TWO questions (2 x 15 = 30 Marks)					
		10+5	3	4	1,2
8	(i) Find the bilinear transformation which maps the points $z = 1, i, -1$ into the points $w = 0, 1, \infty$. (ii) What is the region of the w-plane into which the rectangular region in the z-plane bounded by the lines $x = 0, y = 0, x = 1, y = 2$ is mapped under the transformation $w = z + 2 - i$.				
9	(i) Evaluate $\int_C \frac{\sin \pi z + \cos \pi z^2}{z(z+1)} dz$ where C is a circle $ z =2$ by using Cauchy's residue theorem. (ii) Expand $f(z) = \cos z$ about the point $z = \frac{\pi}{4}$ as a Taylor's series.	10+5	4	5	1,2
10	Evaluate $\int_0^{2\pi} \frac{d\theta}{5 - \sin \theta}$ using contour integration.	15	4	5	1,2

Course Outcome (CO) and Bloom's level (BL) Coverage in Question



Approved by the Audit Professor/Course Coordinator

Evaluation Sheet

Name of the Student:

Register No.:

Q. No	CO	Max. Marks	Marks Obtained	Total
1	4	1		
2	4	1		
3	5	1		
4	5	1		
5	4	8		
6	5	8		
7	5	8		
8	4	10+5		
9	5	10+5		
10	5	15		

Consolidated Marks:

CO	Marks Scored
CO4	
CO5	
Total	

Signature of Course teacher



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INSTITUTE OF SCIENCE & TECHNOLOGY
Dedicated to the memory of Sri S. V. R. I.

SRM Institute of Science and Technology

College of Engineering and Technology

DEPARTMENT OF MATHEMATICS

SRM Nagar, Kattankulathur – 603203, Chengalpattu District, Tamilnadu

Slot D1
Set B

Academic Year: 2023-2024 (EVEN)

Internal Assessment: FT IV

Date: 25.04.2024

Course Code & Title: 21MAB102T - Advanced Calculus and Complex Analysis

Duration: 2 Periods

Year & Sem: I & II

Max. Marks: 50

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

Part - A (4*1 = 4 Marks)

Answer all the questions

Q. No.	Questions	Marks	BL	CO	PO
1.	The image of the rectangular region in the z-plane bounded by the lines $x = 0, y = 0, x = 2$ and $y = 1$ under the transformation $w = 2z$ is (a) parabola (b) circle (c) straight line (d) rectangle is magnified twice	1	1	4	2
2.	The invariant point of the transformation $w = \frac{1}{z-2i}$ is (a) $z = i$ (b) $z = -i$ (c) $z = 1$ (d) $z = -1$	1	1	4	2
3.	The part $\sum_{n=1}^{\infty} b_n(z-a)^{-n}$ consisting of negative integral powers of $(z-a)$ is called as (a) The analytic part of the Laurent's series (b) The principal part of the Laurent's series (c) The real part of the Laurent's series (d) The imaginary part of the Laurent's series	1	1	5	2
4.	The value of $\oint_C \frac{1}{(3z+1)} dz$ where C is the circle $ z = 1$ is (a) 0 (b) πi (c) $\frac{2\pi}{3}i$ (d) 2	1	1	5	2

Part - B (2*8 = 16 Marks)

Answer any 2 questions

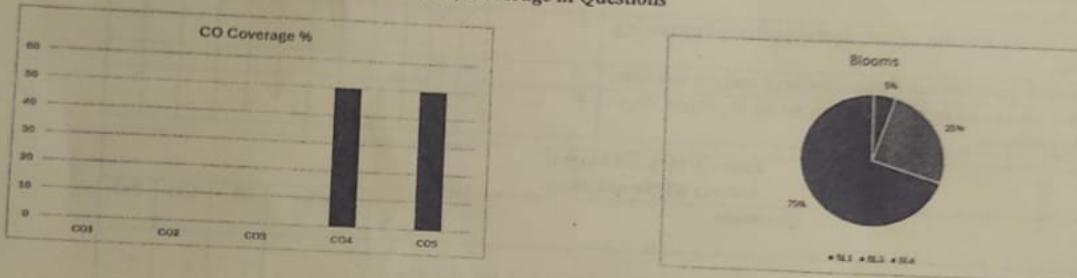
Q. No.	Questions	Marks	BL	CO	PO
5.	Find the analytic function $f(z)$ whose real part is $u = e^x(x \cos y - y \sin y)$, by Milne-Thompson method.	8	3	4	2
6.	Using Cauchy's integral formula, evaluate $\oint_C \frac{4-3z}{z(z-1)(z-2)} dz$, where $C : z = \frac{3}{2}$.	8	3	5	2
7.	Expand $f(z) = \frac{4z}{(z^2-1)(z-4)}$ in Laurent's series for the region $2 < z-1 < 3$.	8	3	5	2



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PART - C (2*15 = 30 Marks)						
8.	(a) Find the Bilinear transformation that maps $z = -1, 0, 1$ onto $w = 0, i, 3i$. (b) Prove that $f(z) = 2xy + i(x^2 - y^2)$ is analytic.	10	4	4	2	
9.	(a) Using Cauchy's Residue theorem, evaluate $\oint_C \frac{e^z}{(z+1)(z-1)} dz$, where $C : z = 3$. (b) Find the Taylor's series up to third degree for $f(z) = \sin z$ about $z = \frac{\pi}{4}$.	10	4	5	2	
10.	Evaluate $\int_0^{2\pi} \frac{d\theta}{5 + 3 \cos \theta}$, using contour integration.	15	4	5	2	

Course Outcome (CO) and Bloom's level (BL) Coverage in Questions



Approved by the Audit Professor/Course Coordinator

Name of the Student:

Register No.:

Q. No.	CO	PART - A (4*1 = 4 Marks)		PART - B (2*8 = 16 Marks)			
		Marks Obtained	Total	Q. No.	CO	Marks Obtained	Total
1	4			5	4		
2	4			6	5		
3	5			7	5		
4	5						
PART - C (2*15= 30 Marks)							
8.	4						
9.	5						
10.	5						

Consolidated Marks:

CO.	Marks Scored
CO4	
CO5	
Total	

Signature of the Course Teacher



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Test: FT- IV
Course Code & Title: 21MAB102T- Advanced Calculus and Complex Analysis
Year & Sem: I & II

Date: 25.04.2024
Duration: 2 Periods
Max. Marks: 50

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems.	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems.	4	3	3										
CO4	Extend their knowledge of the Fundamentals of analytic functions	4	3	3										
COS	Utilize Complex Integrals and Power series in solving Engineering problems.	4	3	3										

Part-A

Answer ALL the questions (4x1 = 4 Marks)

Q. No	Questions	Marks	BL	CO	PO	
			1	2	4	1,2
1	The invariant points of the transformation $w = \frac{1}{z-2i}$ are (a) $z = 0, 2i$ (b) $z = 0, -i$ (c) $z = 2i, 0$ (d) $z = -2i, 2i$	1				
2	The transformation $w = cz$ where c is real constant known as (a) rotation (b) reflection (c) magnification (d) magnification and rotation	1	1	4	1,2	
3	If $f(z)$ is analytic inside and on C , the value of $\int_C \frac{f(z)}{z-a} dz$, where C is the simple closed curve and 'a' is any point outside C is (a) $f(a)$ (b) $2\pi i f(a)$ (c) $\pi i f(a)$ (d) 0	1	1	5	1,2	
4	The poles of $f(z) = \frac{1}{(z-10)^5}$ are (a) $z = 10$ is a pole of order 10 (b) $z = 5$ is a simple pole (c) $z = 5$ is a pole of order 10 (d) $z = 10$ is a pole of order 5	1	2	5	1,2	

Part-B

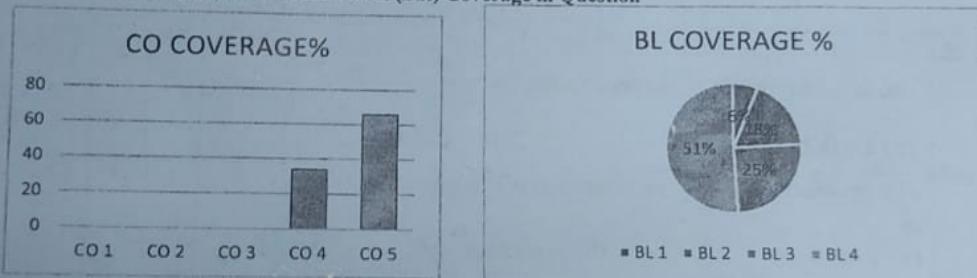
Answer ANY TWO questions (2x8 = 16 Marks)

5	Find the analytic function $f(z)$ whose imaginary part is given by $v = x^3 + 3x^2y - 3xy^2 - y^3 + 4x + 5$ using Milne Thomson method.	8	4	4	1,2
6	Evaluate $\int_C \frac{z}{(z-1)(z-2)^2} dz$ where C is a circle $ z-2 = \frac{1}{2}$ by using Cauchy's integral formula.	8	3	5	1,2
7	Expand $f(z) = \frac{z+3}{(z+1)(z-2)}$ in Laurent's series valid for the region (i) $1 < z < 2$ (ii) $ z > 2$	8	3	5	1,2



Part-C Answer ANY TWO questions (2x15 = 30 Marks)					
		10+5	3	4	1,2
8	(i) Find the bilinear transformation which maps the points $z=0, -1, i, \infty$ into $w=i, 0, \infty$. (ii) Prove that $u=\frac{1}{2} \log(x^2+y^2)$ is harmonic.				
9	(i) Evaluate $\int_C \frac{\cos \pi z^2}{(z-1)(z-2)} dz$ where C is a circle $ z =3$ by using Cauchy's residue theorem. (ii) Expand $f(z)=\frac{1}{z-2}$ about the point $z=1$ as a Taylor's series.		4	5	1,2
10	Evaluate $\int_0^{2\pi} \frac{d\theta}{2+\cos\theta}$ using contour integration.	15	4	5	1,2

Course Outcome (CO) and Bloom's level (BL) Coverage in Question



Anp. /ed by the Audit Profesor/Course Coordinator

Evaluation Sheet

Name of the Student:

Register No.:

Q. No	CO	Max. Marks	Marks Obtained	Total
1	4	1		
2	4	1		
3	5	1		
4	5	1		
5	4	8		
6	5	8		
7	5	8		
8	4	10+5		
9	5	10+5		
10	5	15		

Consolidated Marks:

CO	Marks Scored
CO4	
CO5	
Total	

Signature of Course teacher



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Academic Year: 2023-2024 (EVEN)

Internal Assessment: FT IV

Date: 25.04.2024

Course Code & Title: 21MAB102T - Advanced Calculus and Complex Analysis

Duration: 2 Periods

Year & Sem: I & II

Max. Marks: 50

Course Articulation Matrix

At the end of this course, learners will be able to:		Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems	4	3	3										
CO4	Extend their knowledge in Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex integrals and Power series in solving Engineering problems	4	3	3										

Part - A (4*1 = 4 Marks) - Answer ALL the questions

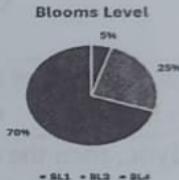
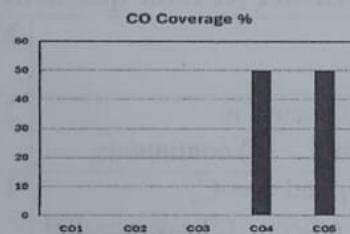
Q. No.	Questions	Marks	BL	CO	PO
1.	If a function $u(x, y)$ satisfies $u_{xx} + u_{yy} = 0$, then u is (a) analytic (b) harmonic (c) differentiable (d) continuous	1	1	4	1
2.	If $u + iv$ is analytic, then the curves $u = C_1$ and $v = C_2$ (a) cut orthogonally (b) intersect each other (c) are parallel (d) coincides	1	1	4	1
3.	The value of $\oint_C \frac{1}{2z+1} dz$, where $C : z = 1$ is (a) 0 (b) πi (c) $\frac{\pi}{2} i$ (d) 2	1	1	5	1
4.	The annular region for the function $f(z) = \frac{1}{z(z-1)}$ is (a) $0 < z < 1$ (b) $0 < z < 2$ (c) $ z > 1$ (d) $ z < 1$	1	1	5	1

Part - B (2*8 = 16 Marks) - Answer any TWO Questions

Q. No.	Questions	Marks	BL	CO	PO
5.	Using Milne's method, construct an analytic function $f(z) = u + iv$ if $v = (x - y)(x^2 + 4xy + y^2)$.	8	3	4	2
6.	Using Cauchy's integral formula, evaluate $\oint_C \frac{\cos \pi z^2 + \sin \pi z^2}{(z-1)(z-2)} dz$, where $C : z = 3$.	8	3	5	2
7.	Find the Laurent's expansion of $f(z) = \frac{7z-2}{z(z+1)(z-2)}$ in the region $1 < z+1 < 3$.	8	3	5	2

Part - C (2*15 = 30 Marks) - Answer any TWO Questions					
Q. No.	Questions			Marks	BL CO PO
8.	(a) Find the Bilinear transformation that maps $z = 1, i, -1$ onto $w = 2, i, -2$. (b) Determine the region D of the w-plane into which the triangular region D enclosed by the lines $x = 0, y = 0, x+y = 1$ is transformed under the transformation $w = 2z$	10	4	4	2
9.	(a) By Cauchy-Residue theorem, evaluate $\int_C \frac{2z-1}{z(z+1)(z-3)} dz$, where $C : z = 2$. (b) Find Taylor's series for $f(z) = \cos z$ about $z = \frac{\pi}{2}$, upto fourth degree.	5	4	4	2
10.	Evaluate $\int_0^{2\pi} \frac{d\theta}{13 + 5 \sin \theta}$, using contour integration.	15	4	5	2

Course Outcome (CO) and Blooms level (BL) Coverage in Questions



Name of the Student:

Register No.:

PART - A (4*1 = 4 Marks)				PART - B (2*8 = 16 Marks)			
Q. No.	CO	Marks Obtained	Total	Q. No.	CO	Marks Obtained	Total
1	4			5	4		
2	4			6	5		
3	5			7	5		
4	5						
PART - C (2*15= 30 Marks)							
8.	4						
9.	5						
10.	5						

Consolidated Marks:

CO.	Marks Scored
CO4	
CO5	
Total	

Signature of the Course Teacher



**SRM Institute of Science and Technology
College of Engineering and Technology
Department of Mathematics**

Department of Mathematics
SRM Nagar, Kattankulathur - 603203, Chengalpattu District, Tamilnadu

Academic Year: 2023-24 (EVEN)

Slot B2

Test: FT-IV

Course Code & Title: 21MAB102T- Advanced Calculus and Geometry

Year 5 Sem: I & II

Course Articulation Matrix

Date: 30.04.24

Duration: 2 Periods

Max. Marks: 50

Part-A

Answer ALL the questions (4X1 = 4 Marks)

Q. No	Questions	Marks	BL	CO	PO
1	The necessary condition for the function $f(z) = u + iv$ to be analytic is (a) $u_x = v_y, u_y = -v_x$ (b) $u_x = -v_y, u_y = v_x$ (c) $u_x = v_y, u_y = v_x$ (d) $u_y = v_y, u_x = v_x$	1	1	4	1,2
2	The real part u of an analytic function $f(z) = u + iv$ is (a) analytic (b) harmonic (c) discontinuous (d) not analytic	1	1	4	1,2
3	The value of $\int_C \frac{z}{(z-1)} dz$ where C is the circle $ z = 2$ is (a) πi (b) $2\pi i$ (c) $4\pi i$ (d) 0	1	2	5	1,2
4	In the Laurent's series, the part $\sum_1^{\infty} b_n(z-a)^{-n}$, consisting of negative integral powers of $(z-a)$, is called the (a) analytic part (b) principal part (c) harmonic (d) conjugate	1	1	5	1,2

Part-B

Answer ANY TWO questions (2X8 = 16 Marks)

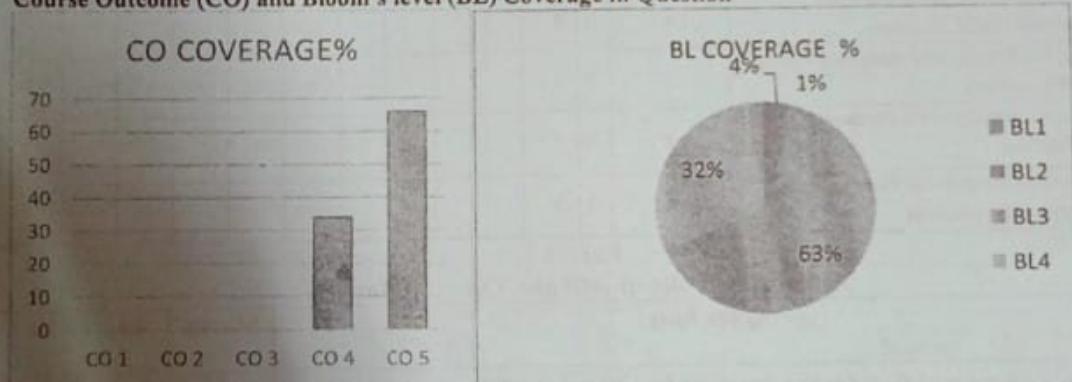
5	Obtain the analytic function $f(z) = u + iv$ if the imaginary part is given as $v = -2\sin x(e^y - e^{-y})$ using Milne Thomson Method.	8	3	4	1,2
6	Evaluate $\oint_C \frac{z-2}{z(z-1)} dz$ where C is $ z = 3$ using Cauchy Integral Formula.	8	3	5	1,2
7	Expand $f(z) = \frac{1}{(z+1)(z+2)}$ as a Laurent series in the region (i) $1 < z < 2$ (ii) $ z > 2$.	8	4	5	1,2

Part-C

Answer ANY TWO questions (2x15 = 30 Marks)

8 (i)	Find the bilinear transformation which maps the points $z_1 = 1$, $z_2 = i$ and $z_3 = -1$ into the points $w_1 = i$, $w_2 = 0$ and $w_3 = -i$.	10+5	3	4	1,2
(ii)	Find the image of the rectangular region in the z -plane bounded by the lines $x = 0, y = 0, x = 2$ and $y = 1$ under the transformation $w = 2z$.				
9(i)	Evaluate $\oint_C \frac{z^2}{(z-1)(z+1)} dz$ where C is a circle $ z = 2$ by using Cauchy's Residue theorem.	10+5	4	5	1,2
(ii)	Obtain the Taylor's series to represent the function $f(z) = \frac{1}{z}$ at the point $z = 2$ upto fourth degree term.				
10	Evaluate $\int_0^{2\pi} \frac{d\theta}{5+4\sin\theta}$ by using Contour Integration.	15	3	5	1,2

Course Outcome (CO) and Bloom's level (BL) Coverage in Question



Approved by the Audit Professor/Course Coordinator

Evaluation Sheet

Name of the Student:

Register No.:

Q. No	CO	Max. Marks	Marks Obtained	Total
1	4	1		
2	4	1		
3	5	1		
4	5	1		
5	4	8		
6	5	8		
7	5	8		
8	4	15		
9	5	15		
10	5	15		

Consolidated Marks:

CO	Marks Scored
CO4	
CO5	
Total	

Signature of Course teacher

Academic Year: 2023-24 (EVEN)

Test: FT- IV

Date : 30.04.2024

Course Code & Title: 21MAB102T- Advanced Calculus and Complex Analysis

Duration : 2 Periods

Year & Sem: I & II

Max. Marks : 50

Course Articulation Matrix

At the end of this course, learners will be able to:		Learning Bloom's Level	Program Outcomes (PO)											
Course Outcomes (CO)			1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply multiple integrals in solving problems in Science and Engineering.	4	3	3										
CO2	Analyze vector differentiation and vector integration and related Theorems.	4	3	3										
CO3	Apply Laplace Transforms techniques in solving Engineering problems.	4	3	3										
CO4	Extend their knowledge of the Fundamentals of analytic functions	4	3	3										
CO5	Utilize Complex Integrals and Power series in solving Engineering problems.	4	3	3										

Part-A

Answer ALL the questions (4X1 = 4 Marks)

Q. No	Questions	Marks	BL	CO	PO
1	The critical point of transformation $w = z^2$ is (a) $z = 2$ (b) $z = 0$ (c) $z = 1$ (d) $z = -2$	1	2	4	1,2
2	An analytic function with constant modulus is (a) zero (b) analytic (c) constant (d) harmonic	1	1	4	1,2
3	Let $C_1: z - a = R_1$ and $C_2: z - a = R_2$ be two concentric circles ($R_2 < R_1$), the annular region is defined as (a) within C_1 (b) within C_2 (c) within C_2 and outside C_1 (d) within C_1 and outside C_2	1	1	8	1,2
4	The part $\sum_{n=0}^{\infty} a_n(z - a)^n$ consisting of positive integral powers of $(z - a)$ is called as (a) the analytic part of the Laurent's series (b) the principal part of the Laurent's series (c) the real part of the Laurent's series (d) the imaginary part of the Laurent's series	1	1	8	1,2

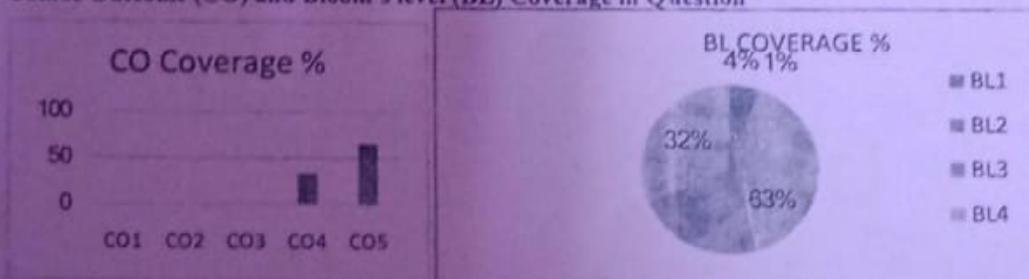
Part-B

Answer ANY TWO questions (2X8 = 16 Marks)

5	Find the analytic function $f(z) = u+iv$ if $u = e^x(x\cos 2y - y\sin 2y)$ using Milne Thomson method.	8	3	4	1,2
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6	Evaluate $\oint_C \frac{z^2+1}{(z-1)(z-2)} dz$, where C is a circle $ z =3$ using Cauchy Integral Formula.	8	3	5	1,2
7	Find the Laurent's series of $f(z) = \frac{z^2-1}{(z+2)(z+3)}$ valid in the region (i) $2 < z < 3$ (ii) $ z > 3$.	8	4	5	1,2
Part-C					
Answer ANY TWO questions (2X15 = 30 Marks)					
8	i) Find the bilinear transformation which maps the points $z_1 = 0$, $z_2 = -i$ and $z_3 = -1$ onto the points $w_1 = i$, $w_2 = 1$ and $w_3 = 0$. ii) Test whether the following function is analytic or not $f(z) = x^2 - y^2 + i2xy$.	10+5	3	4	1,2
9	i) Evaluate $\oint_C \frac{4-3z}{z(z-1)(z-2)} dz$, where C is a circle $ z = \frac{3}{2}$ by using Cauchy's Residue theorem. ii) Expand $f(z) = \frac{1}{z-3}$ at $z = 1$, in a Taylor's series upto fourth degree term.	10+5	4	5	1,2
10	Evaluate $\int_0^{2\pi} \frac{d\theta}{13+12\cos\theta}$, by using Contour Integration.	15	3	5	1,2

Course Outcome (CO) and Bloom's level (BL) Coverage in Question



Approved by the Audit Professor/Course Coordinator

Evaluation Sheet

Name of the Student:

Register No.:

Q. No	CO	Max. Marks	Marks Obtained	Total
1	4	1		
2	4	1		
3	5	1		
4	5	1		
5	4	8		
6	5	8		
7	5	8		
8	4	15		
9	5	15		
10	5	15		

Consolidated Marks:

CO	Marks Scored
CO4	
CO5	
Total	

Signature of Course Teacher