

# Simulating Turbulent Flow with Synthetic Eddy: System Verification and Validation Plan for SynthEddy

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## Revision History

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# 1 Symbols, Abbreviations, and Acronyms

Please refer to the Software Requirements Specification (SRS) [Du \(2024\)](#) of this project. Section 1 contains Symbols, Abbreviations, and Acronyms. If you are not familiar with fluids and CFD, Section 4.1.1 of the SRS contains a list of Terminology and Definitions.

The following symbols and operators are used in this document:

---

| symbol | description   |
|--------|---|
| tol    | Tolerance, a small value used when testing differences, see <a href="#">6.1</a> |
| std()  | Standard deviation of multiple values.  |
| div()  | Divergence of a velocity field.   |

---

This document lays the plan for the verification and validation of the software SynthEddy. It provides an overview of what the tests aim to achieve, and then details the plan for each test. It also serves as a communication aid between the software development team and the domain experts on the theoretical side, so that it can be ensured that the correct aspect of the software is being tested with valid expectations.

## 2 General Information

### 2.1 Summary

The software being tested is a program that generates approximated turbulent flow field with synthetic eddies. It is intended to provide initial and boundary conditions (IC and BC) to CFD solvers for turbulent flow simulations, which would cut down simulation time and save computational resources. An illustration of the flow field that the software is intended to generate is shown in Figure 1.

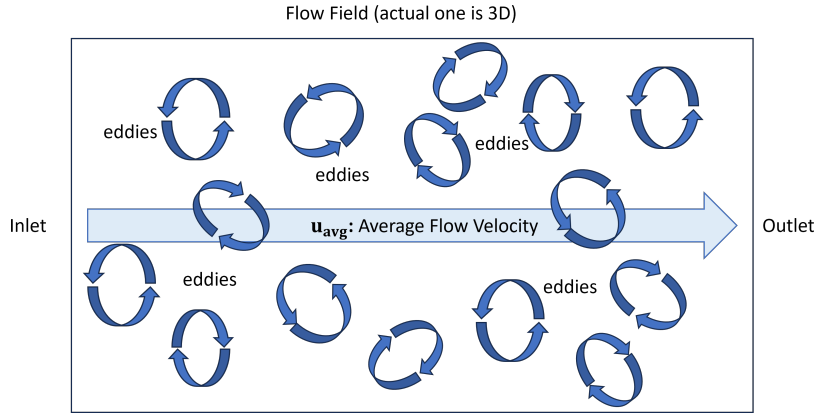


Figure 1: System Context

### 2.2 Objectives

The most crucial objective here is to build confidence that this software can correctly generate turbulent flow fields according to the synthetic eddy

method proposed by [Poletto et al. \(2013\)](#). As no suitable pseudo-oracle exists to allow for direct comparison of the results, the focus is to test for characteristics that a flow field generated with such method should exhibit. In the future with more theoretical background given, this will expand to making sure the generated flow fields are physically realistic in terms of turbulent properties.

Another objective is to demonstrate the this software can interface with CFD solvers and provide in order to IC and BC for turbulent flow simulations (future development).

Furthermore, maintainability, namely the ability for user to easily modify the software to fit their specific needs should also be demonstrated.

## 2.3 Relevant Documentation

- Software Requirements Specification (SRS) [Du \(2024\)](#) is the most important guideline for this VnV plan. It contains the requirements of the software, and the theoretical Modules of the synthetic eddy method.
- Design Documents will be used to guide the unit testing and the design verification.

# 3 Plan

This section lays out how the VnV will be carried out in aspect and by whom. It also includes the tools that will be used for the VnV.

## 3.1 Verification and Validation Team

- Phil Du - Developer: Writing test scripts according to VnV and implementing automated tests with continuous integration (CI). Ensuring coding standards are respected with linters.
- Nikita Holyev - Theorist: Reviewing the VnV plan to ensure that the tests are relevant to the theoretical models.
- Cynthia Liu - Subject Matter Expert: Reviewing the VnV plan and design documents to make sure the SRS is met.
- Morteza Mirzaei - Secondary reviewer of the VnV plan.

- Dr. Spencer Smith - Supervisor.
- Several volunteers as subjects for usability (future) and maintainability testing.

### 3.2 SRS Verification Plan

Most of the Functional Requirements in the SRS [Du \(2024\)](#), namely R1-R4 are derived from the synthetic eddy method by [Poletto et al. \(2013\)](#), and can be represented mathematically. Thus, they are covered by automated testing detailed in Section [4.1](#). R5, the interface with CFD software, need to be verified with manual testing by actually conducting CFD simulations with the generated IC and BC.

The Nonfunctional Requirements in the SRS, including Accuracy, Usability, Maintainability and Portability, will be verified by manual testing. All of these other than Maintainability involves running the software in conjecture with CFD solvers, and will be performed when the CFD integration is implemented in the future. Maintainability will be verified by persons other than the developer attempting to modify the software, and is detailed in Section [4.2](#).

The Functional and Nonfunctional Requirements in the SRS serve as a checklist.

### 3.3 Design Verification Plan

*Pending design documents.*

- [\[Plans for design verification —SS\]](#)
- [\[The review will include reviews by your classmates —SS\]](#)
- [\[Create a checklists? —SS\]](#)

### 3.4 Verification and Validation Plan Verification Plan

The VnV plan itself is verified by review. The developer and reviewers will ensure that all the requirements in the SRS are covered by the plan. The theorist will specifically review the flow field tests to ensure that they represent the theoretical characteristics of the synthetic eddy method.



### 3.5 Implementation Verification Plan

Successful implementation of the synthetic eddy method can be verified by automated tests detailed in Section [4.1](#).

### 3.6 Automated Testing and Verification Tools

- Continuous Integration (CI): GitHub Actions for automated tests.
- Memory Usage Monitoring: pytest.
- Code Coverage: pytest.
- Linters: flake8.

### 3.7 Software Validation Plan

As there is no suitable external data or pseudo-oracle to directly compare with the results of this software, the validation will be done by comparing the generated flow fields with the expected theoretical characteristics of the synthetic eddy method. Several aspects of the flow field will be tested, as detailed in Section [4.1](#). The test scripts will be run automatically with GitHub Actions.

## 4 System Test Description

### 4.1 Tests for Functional Requirements

These tests are traced to R1-R5 (Section 5.1) of the SRS [Du \(2024\)](#). With R5 being the only Function Requirement that needs to be tested manually, the rest will be automated.

Areas of testing are structured with respect to the list of Function Requirements.

#### 4.1.1 Input Test

##### Check Query Point within Flow Field [R1]

1. test-query-coordinate

Control: Automatic

Initial State: Empty flow field with size (1m, 1m, 1m)

Input:  $\mathbf{x} = (2, 2, 2)$

Output: Throw exception: Queried point outside of flow field!

Test Case Derivation: Execution should be halted as results outside of the flow field are not meaningful.

How test will be performed: Automated test script, GitHub Actions.

### 4.1.2 Eddy Generation Test

#### Generation of a Single Eddy [R2]

1. test-eddy-shape

Control: Automatic

Initial State: Empty flow field, zero  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: 1 eddy with predetermined center location  
 $\mathbf{x} = (0, 0, 0)$   $\sigma = 1$  (length-scale, i.e. radius)
- Query: Pairs of points relative to center:  
 $\mathbf{x}_1 = (0.5, 0.5, 0.5)$   $\mathbf{x}_2 = (-0.5, -0.5, -0.5)$   
 $\mathbf{x}_3 = (2, 2, 2)$   $\mathbf{x}_4 = (-2, -2, -2)$

Output: Velocity vectors at each point:  $\mathbf{u}_1, \mathbf{u}_2, \mathbf{u}_3, \mathbf{u}_4$

Expected behavior:

- $|\mathbf{u}_1 - \mathbf{u}_2| < \text{tol}|\mathbf{u}_1|$   $|\mathbf{u}_3| = |\mathbf{u}_4| = 0$

Test Case Derivation: Points should have equal and opposite velocities inside the eddy, and zero velocity outside. We can also make the script query more points inside the eddy to test if the magnitude follows shape function

How test will be performed: Automated test script, GitHub Actions.

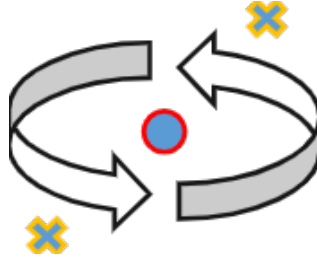


Figure 2: Query Pair of Points

## 2. test-eddy-std

Control: Automatic

Initial State: Empty flow field, zero  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: 1 eddy with predetermined orientation  
 $\mathbf{x} = (0, 0, 0)$   $\sigma = 1$   
 $\alpha = (0, 0, 1)$  (intensity = 1, orientation along z-axis)
- Query: Mesh grid of points covering the eddy

Output: Velocity vectors at each point  $\mathbf{u}$

Expected behavior:

- $\text{std}(\mathbf{u}_z) < \text{tol}$

Test Case Derivation: Flow of an eddy should be around its orientation axis. Thus, velocity standard deviation along the eddy orientation should be zero.

How test will be performed: Automated test script, GitHub Actions.

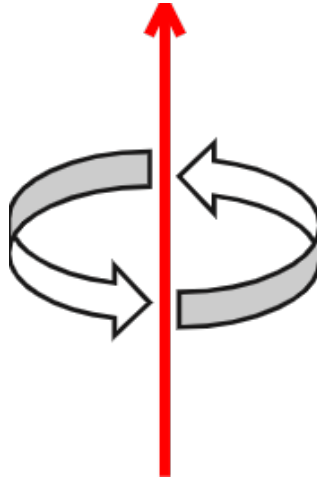


Figure 3: Eddy Orientation

### 4.1.3 Field Generation Test

#### Generation of Flow Field [R2]

1. test-field-sum

Control: Automatic

Initial State: Empty flow field,  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: Any number of eddies, random orientations
- Query: Mesh grid of points of the entire flow field at any  $t$

Output: Velocity vectors at each point:  $\mathbf{u}$

Expected behavior:

- $|\sum \mathbf{u} - \mathbf{u}_{\text{avg}}| < \text{tol}$

Test Case Derivation: The vector sum of all velocity fluctuations caused by the eddies should be zero.

How test will be performed: Automated test script, GitHub Actions.

2. test-field-std-time

Control: Automatic

Initial State: Empty flow field,  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: Any number of eddies, random orientations
- Query: Mesh grid of points of the entire flow field  
 $t_0 = 0$   $t_1 = 10$

Output: Velocity vectors at each point:  $\mathbf{u}$

Expected behavior:

- $\text{std}(\mathbf{u})|_{t_0} - \text{std}(\mathbf{u})|_{t_1} < \text{tol}$

Test Case Derivation: Velocity standard deviation should stay the same regardless of time.

How test will be performed: Automated test script, GitHub Actions.

### 3. test-field-std-intensity

Control: Automatic

Initial State: Empty flow field,  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: Any number of eddies, random orientations  
Increasing eddy intensity  $|\alpha|$
- Query: Mesh grid of points of the entire flow field

Output: Velocity vectors at each point:  $\mathbf{u}$

Expected behavior:

- if  $|\alpha|_1 > |\alpha|_2$  then  $\text{std}(\mathbf{u})_1 > \text{std}(\mathbf{u})_2$

Test Case Derivation: Velocity standard deviation should increase with eddy intensity  $|\alpha|$ .

How test will be performed: Automated test script, GitHub Actions.

#### 4.1.4 Divergence Test

##### Divergence Free Condition [R4]

### 1. test-field-divergence

Control: Automatic

Initial State: Empty flow field,  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: Any number of eddies, random orientations
- Query: Mesh grid of points of the entire flow field

Output: Velocity vectors at each point:  $\mathbf{u}$

Expected behavior:

- $\text{div}(\mathbf{u}) < \text{tol}$

Test Case Derivation: The flow field should be divergence-free.

How test will be performed: Automated test script, GitHub Actions.

#### 4.1.5 Eddy Profile

##### **Provide Realistic Profile Before Generation [R3]**

Test case for this requirement will be added in the future given more theoretical background.

#### 4.1.6 CFD Interface

##### **Feed IC and BC to CFD Software [R5]**

###### 1. test-cfd-interface

Type: Manual.

Initial State: Empty flow field,  $\mathbf{u}_{\text{avg}}$

Input:

- Profile: Any number of eddies, random orientations
- Query: CFD software should query points in the flow field

Output: Velocity vectors at each point:  $\mathbf{u}$

Expected behavior:

- They should be feed into the CFD software

Test Case Derivation: The CFD software should be able get the flow field generated by SynthEddy as IC and BC.

How test will be performed: Manually perform a CFD simulation in conjecture with SynthEddy.

## 4.2 Tests for Nonfunctional Requirements

NFR1, NFR2 and NFR4 is already covered by functional test of CFD interface (4.1.6). NFR3 (maintainability) will be verified by a separate test detailed below.

### 4.2.1 Maintainability

#### Modifying Shape Function

In terms of maintainability, users who looks to modify SynthEddy would most likely want to change the shape functions of the eddies to fit their specific needs. If the software is well structured and documented, they should be able to do so with ease, even without systematic programming knowledge.

1. test-modify-shape-func

Type: Static

Initial State: Reviewer is provided with documentation and source code, and no other help.

Input/Condition: Reviewer is given a mathematical equation for a new shape function.

Output/Result: Reviewer should be able to modify the source code to implement the new shape function.

How test will be performed: Performed by volunteers or potential users of the software. Time taken will be recorded. Check if the modified software still passes the automated functional tests.



### 4.3 Traceability Between Test Cases and Requirements

|                            | R1 | R2 | R3 | R4 | R5 | NFR1 | NFR2 | NFR3 | NFR4 |
|----------------------------|----|----|----|----|----|------|------|------|------|
| Test <a href="#">4.1.1</a> | X  |    |    |    |    |      |      |      |      |
| Test <a href="#">4.1.2</a> |    | X  |    |    |    |      |      |      |      |
| Test <a href="#">4.1.3</a> |    | X  |    |    |    |      |      |      |      |
| Test <a href="#">4.1.4</a> |    |    |    | X  |    |      |      |      |      |
| Test <a href="#">4.1.5</a> |    |    | X  |    |    |      |      |      |      |
| Test <a href="#">4.1.6</a> |    |    |    |    | X  | X    | X    |      | X    |
| Test <a href="#">4.2.1</a> |    |    |    |    |    |      |      | X    |      |

Table 1: Traceability Between Test Cases and Requirements

## 5 Unit Test Description

[This section should not be filled in until after the MIS (detailed design document) has been completed. —SS]

[Reference your MIS (detailed design document) and explain your overall philosophy for test case selection. —SS]

[To save space and time, it may be an option to provide less detail in this section. For the unit tests you can potentially layout your testing strategy here. That is, you can explain how tests will be selected for each module. For instance, your test building approach could be test cases for each access program, including one test for normal behaviour and as many tests as needed for edge cases. Rather than create the details of the input and output here, you could point to the unit testing code. For this to work, your code needs to be well-documented, with meaningful names for all of the tests. —SS]

### 5.1 Unit Testing Scope

[What modules are outside of the scope. If there are modules that are developed by someone else, then you would say here if you aren't planning on verifying them. There may also be modules that are part of your software, but have a lower priority for verification than others. If this is the case, explain your rationale for the ranking of module importance. —SS]

## 5.2 Tests for Functional Requirements

[Most of the verification will be through automated unit testing. If appropriate specific modules can be verified by a non-testing based technique. That can also be documented in this section. —SS]

### 5.2.1 Module 1

[Include a blurb here to explain why the subsections below cover the module. References to the MIS would be good. You will want tests from a black box perspective and from a white box perspective. Explain to the reader how the tests were selected. —SS]

#### 1. test-id1

Type: [Functional, Dynamic, Manual, Automatic, Static etc. Most will be automatic —SS]

Initial State:

Input:

Output: [The expected result for the given inputs —SS]

Test Case Derivation: [Justify the expected value given in the Output field —SS]

How test will be performed:

#### 2. test-id2

Type: [Functional, Dynamic, Manual, Automatic, Static etc. Most will be automatic —SS]

Initial State:

Input:

Output: [The expected result for the given inputs —SS]

Test Case Derivation: [Justify the expected value given in the Output field —SS]

How test will be performed:

#### 3. ...

### 5.2.2 Module 2

...

## 5.3 Tests for Nonfunctional Requirements

[If there is a module that needs to be independently assessed for performance, those test cases can go here. In some projects, planning for nonfunctional tests of units will not be that relevant. —SS]

[These tests may involve collecting performance data from previously mentioned functional tests. —SS]

### 5.3.1 Module ?

1. test-id1

Type: [Functional, Dynamic, Manual, Automatic, Static etc. Most will be automatic —SS]

Initial State:

Input/Condition:

Output/Result:

How test will be performed:

2. test-id2

Type: Functional, Dynamic, Manual, Static etc.

Initial State:

Input:

Output:

How test will be performed:

### 5.3.2 Module ?

...

## 5.4 Traceability Between Test Cases and Modules

[Provide evidence that all of the modules have been considered. —SS]

## References

- Phil Du. System requirements specification. <https://github.com/omltcat/turbulent-flow/blob/main/docs/SRS/SRS.pdf>, 2024.
- Ruggero Poletto, T. Craft, and Alistair Revell. A new divergence free synthetic eddy method for the reproduction of inlet flow conditions for les. *Flow, Turbulence and Combustion*, 91:1–21, 10 2013. doi: 10.1007/s10494-013-9488-2.

## 6 Appendix

### 6.1 Symbolic Parameters

The definition of the test cases will call for `SYMBOLIC_CONSTANTS`. Their values are defined in this section for easy maintenance.

- Tolerance: some small value, e.g.  $\text{tol} = 0.0001$
- Average velocity: along x-axis (1D flow), e.g.  $\mathbf{u}_{\text{avg}} = (5, 0, 0)$