

Computer Vision

Jacobs University Bremen

Fall 2020

Homework 5

This notebook includes both coding and written questions. Please hand in this notebook file with all the outputs and your answers to the written questions.

This assignment covers K-Means and HAC methods for clustering and image segmentation.

In [1]:

```
# Setup
from __future__ import print_function
from time import time
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import rc
from skimage import io

%matplotlib inline
plt.rcParams['figure.figsize'] = (15.0, 12.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
%load_ext autoreload
%autoreload 2
```

Introduction

In this assignment, you will use clustering algorithms to segment images. You will then use these segmentations to identify foreground and background objects.

Your assignment will involve the following subtasks:

- **Clustering algorithms:** Implement K-Means clustering and Hierarchical Agglomerative Clustering.
- **Pixel-level features:** Implement a feature vector that combines color and position information and implement feature normalization.
- **Quantitative Evaluation:** Evaluate segmentation algorithms with a variety of parameter settings by comparing your computed segmentations against a dataset of ground-truth segmentations.

1 Clustering Algorithms (40 points)

In [2]:

```
# Generate random data points for clustering

# Set seed for consistency
np.random.seed(0)

# Cluster 1
mean1 = [-1, 0]
cov1 = [[0.1, 0], [0, 0.1]]
X1 = np.random.multivariate_normal(mean1, cov1, 100)

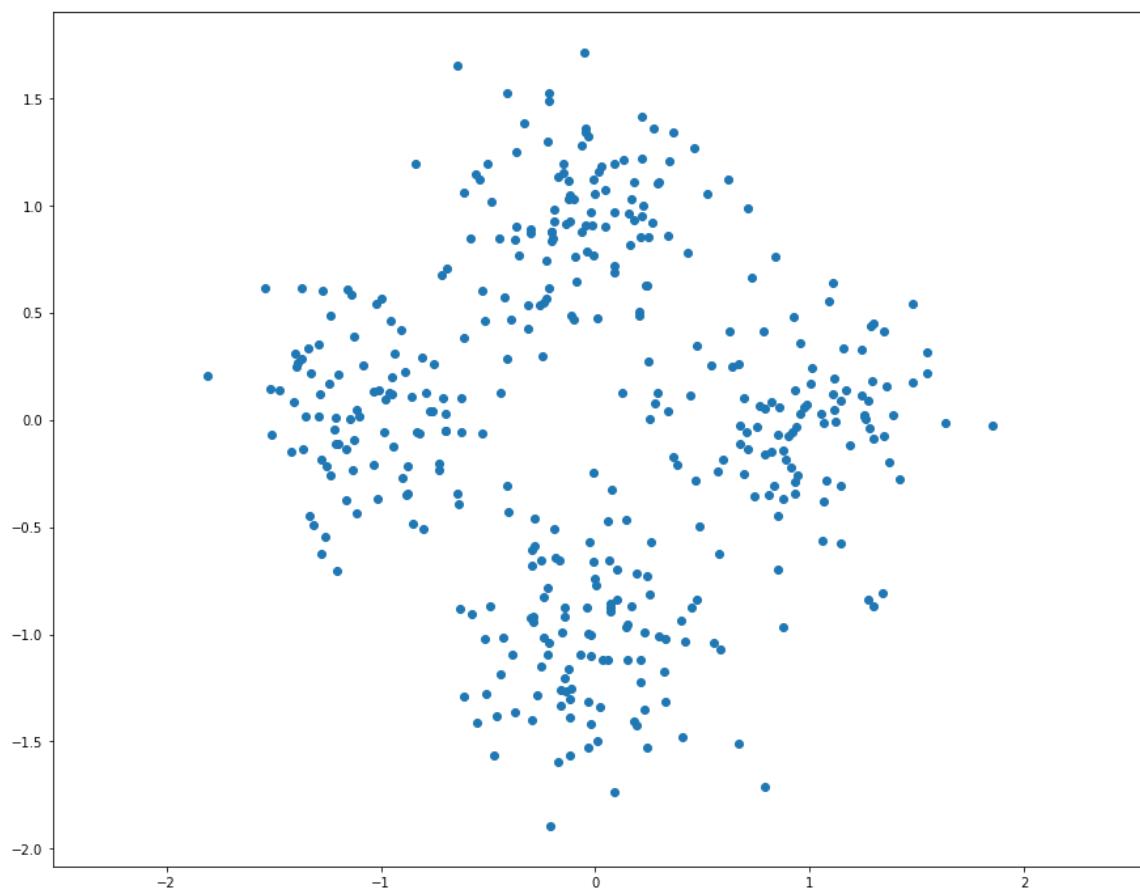
# Cluster 2
mean2 = [0, 1]
cov2 = [[0.1, 0], [0, 0.1]]
X2 = np.random.multivariate_normal(mean2, cov2, 100)

# Cluster 3
mean3 = [1, 0]
cov3 = [[0.1, 0], [0, 0.1]]
X3 = np.random.multivariate_normal(mean3, cov3, 100)

# Cluster 4
mean4 = [0, -1]
cov4 = [[0.1, 0], [0, 0.1]]
X4 = np.random.multivariate_normal(mean4, cov4, 100)

# Merge two sets of data points
X = np.concatenate((X1, X2, X3, X4))

# Plot data points
plt.scatter(X[:, 0], X[:, 1])
plt.axis('equal')
plt.show()
```



1.1 K-Means Clustering (20 points)

As discussed in class, K-Means is one of the most popular clustering algorithms. We have provided skeleton code for K-Means clustering in the file `segmentation.py`. Your first task is to finish implementing `kmeans` in `segmentation.py`. This version uses nested for loops to assign points to the closest centroid and compute a new mean for each cluster.

In [3]:

```
from segmentation import kmeans

np.random.seed(0)
start = time()
assignments = kmeans(X, 4)
end = time()

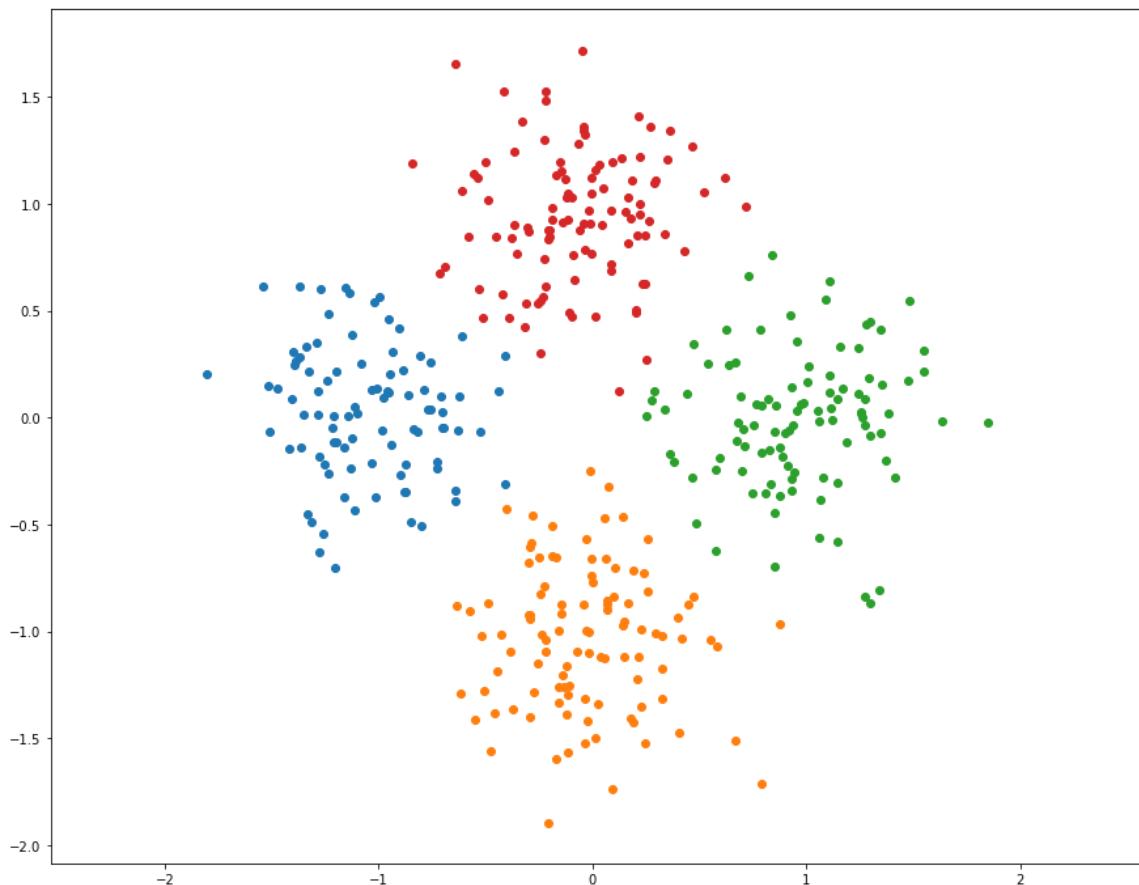
kmeans_runtime = end - start

print("kmeans running time: %f seconds." % kmeans_runtime)

for i in range(4):
    cluster_i = X[assignments==i]
    plt.scatter(cluster_i[:, 0], cluster_i[:, 1])

plt.axis('equal')
plt.show()
```

kmeans running time: 0.046903 seconds.



We can use numpy functions and broadcasting to make K-Means faster. Implement `kmeans_fast` in `segmentation.py`. This should run at least 10 times faster than the previous implementation.

In [5]:

```
from segmentation import kmeans_fast

np.random.seed(0)
start = time()
assignments = kmeans_fast(X, 4)
end = time()

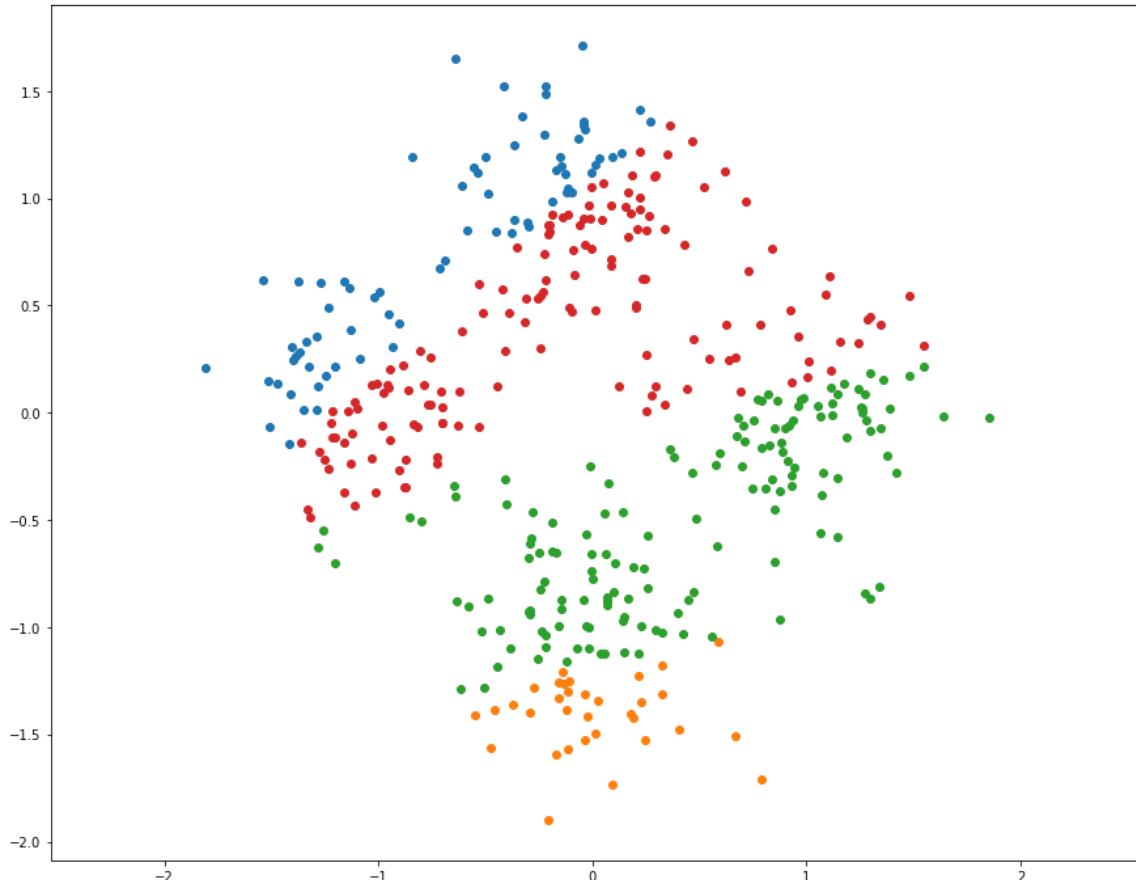
kmeans_fast_runtime = end - start
print("kmeans running time: %f seconds." % kmeans_fast_runtime)
print("%f times faster!" % (kmeans_runtime / kmeans_fast_runtime))

for i in range(4):
    cluster_i = X[assignments==i]
    plt.scatter(cluster_i[:, 0], cluster_i[:, 1])

plt.axis('equal')
plt.show()
```

kmeans running time: 0.001180 seconds.

39.742828 times faster!



1.2 K-Means Convergence (10 points)

Implementations of the K-Means algorithm will often have the parameter `num_iters` to define the maximum number of iterations the algorithm should run for. Consider that we opt to not include this upper bound on the number of iterations, and that we define the termination criterion of the algorithm to be when the cost L stops changing.

Recall that L is defined as the sum of squared distance between all points x and their nearest cluster center c :

$$L = \sum_{i \in \text{clusters}} \sum_{x \in \text{cluster}_i} (x - c_i)^2$$

Show that for any set of points D and any number of clusters k , the K-Means algorithm will terminate in a finite number of iterations.

Your answer here:

1.2 Hierarchical Agglomerative Clustering (10 points)

Another simple clustering algorithm is Hierarchical Agglomerative Clustering, which is sometimes abbreviated as HAC. In this algorithm, each point is initially assigned to its own cluster. Then cluster pairs are merged until we are left with the desired number of predetermined clusters (see Algorithm 1).

Implement `hierarchical_clustering` in `segmentation.py`.

Algorithm 1 Hierarchical Agglomerative Clustering

Require: Points $x_1, \dots, x_m \in \mathbb{R}^n$, desired number of clusters $k \in \mathbb{Z}$

Assign each point to its own cluster

while There are more than k clusters **do**

 Compute the distance between all pairs of clusters

 Merge the two closest clusters

end while

In [12]:

```
from segmentation import hierarchical_clustering

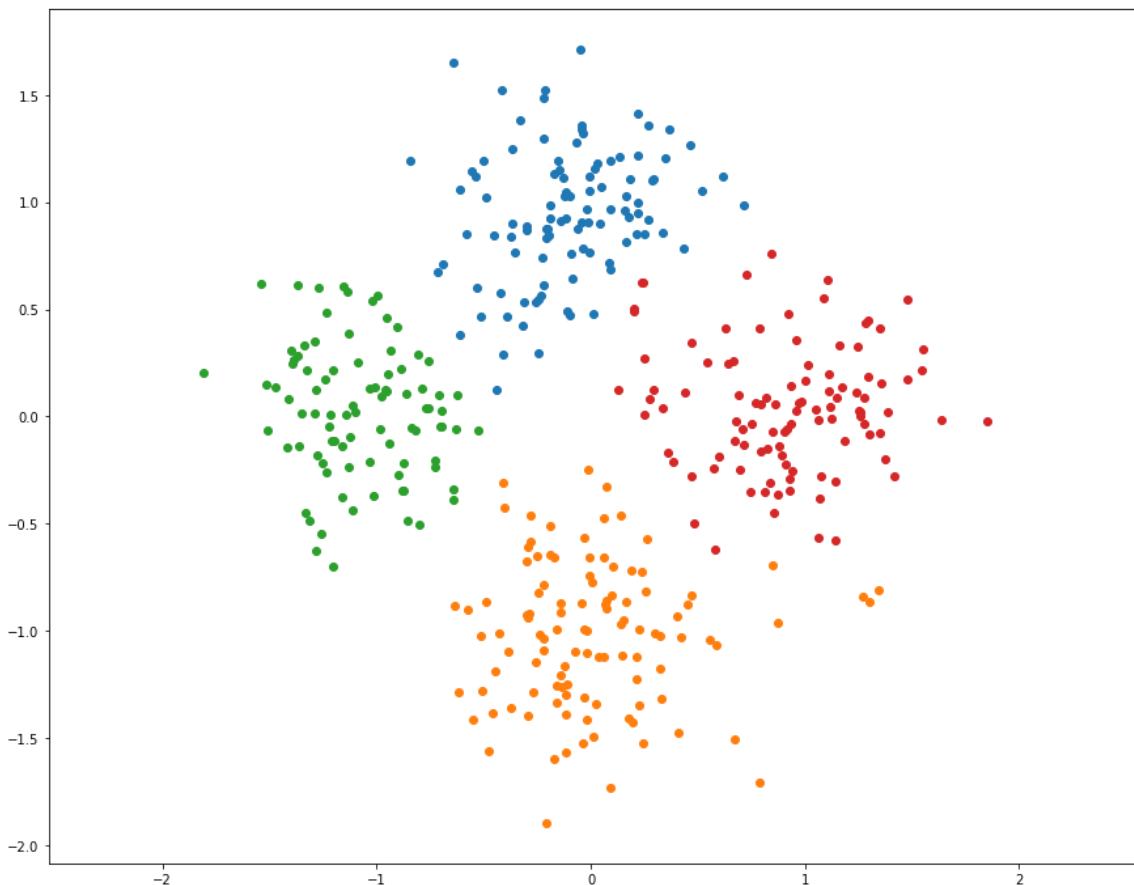
start = time()
assignments = hierarchical_clustering(X, 4)
end = time()

print("hierarchical_clustering running time: %f seconds." % (end - start))

for i in range(4):
    cluster_i = X[assignments==i]
    plt.scatter(cluster_i[:, 0], cluster_i[:, 1])

plt.axis('equal')
plt.show()
```

hierarchical_clustering running time: 0.754283 seconds.



2 Pixel-Level Features (30 points)

Before we can use a clustering algorithm to segment an image, we must compute some *feature vector* for each pixel. The feature vector for each pixel should encode the qualities that we care about in a good segmentation. More concretely, for a pair of pixels p_i and p_j with corresponding feature vectors f_i and f_j , the distance between f_i and f_j should be small if we believe that p_i and p_j should be placed in the same segment and large otherwise.

In [13]:

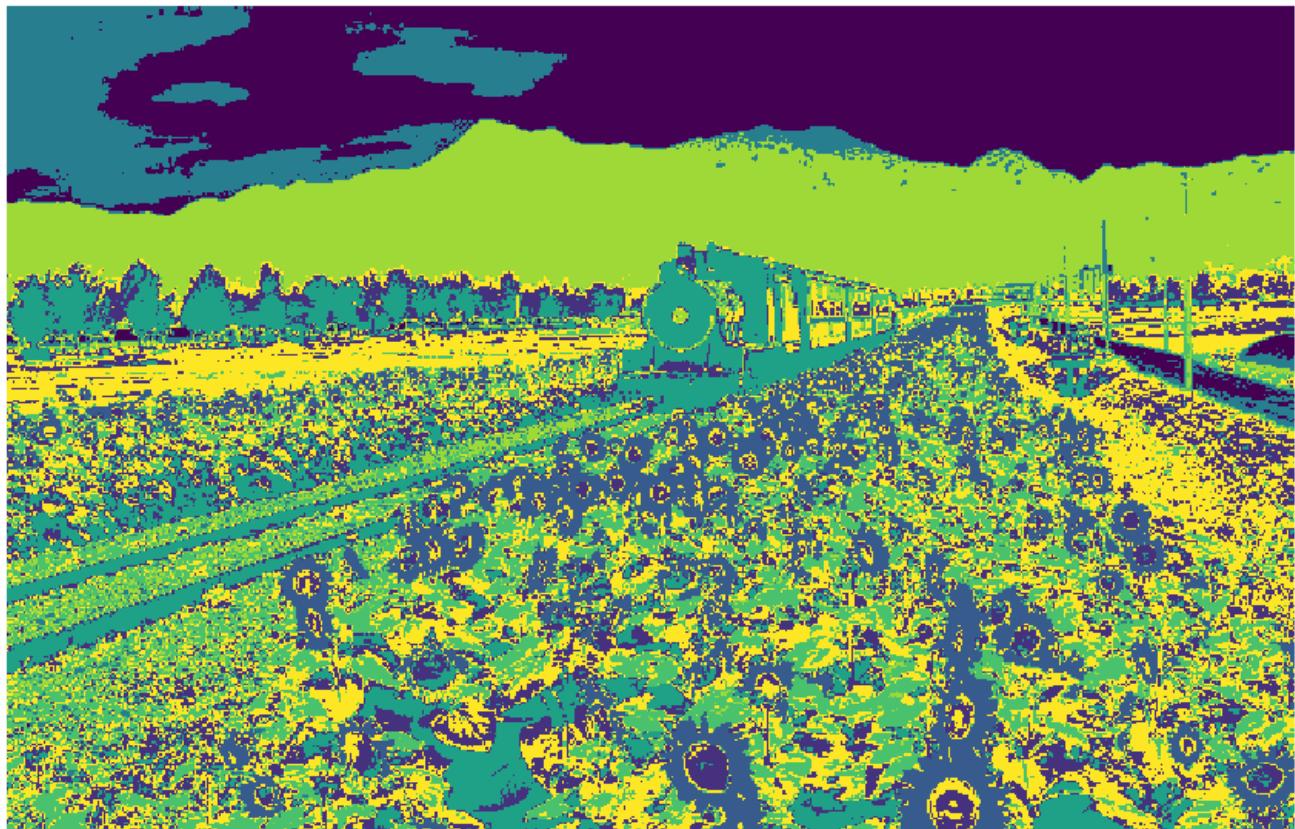
```
# Load and display image
img = io.imread('train.jpg')
H, W, C = img.shape

plt.imshow(img)
plt.axis('off')
plt.show()
```



2.1 Color Features (15 points)

One of the simplest possible feature vectors for a pixel is simply the vector of colors for that pixel. Implement `color_features` in `segmentation.py`. Output should look like the following:



In [14]:

```
from segmentation import color_features
np.random.seed(0)

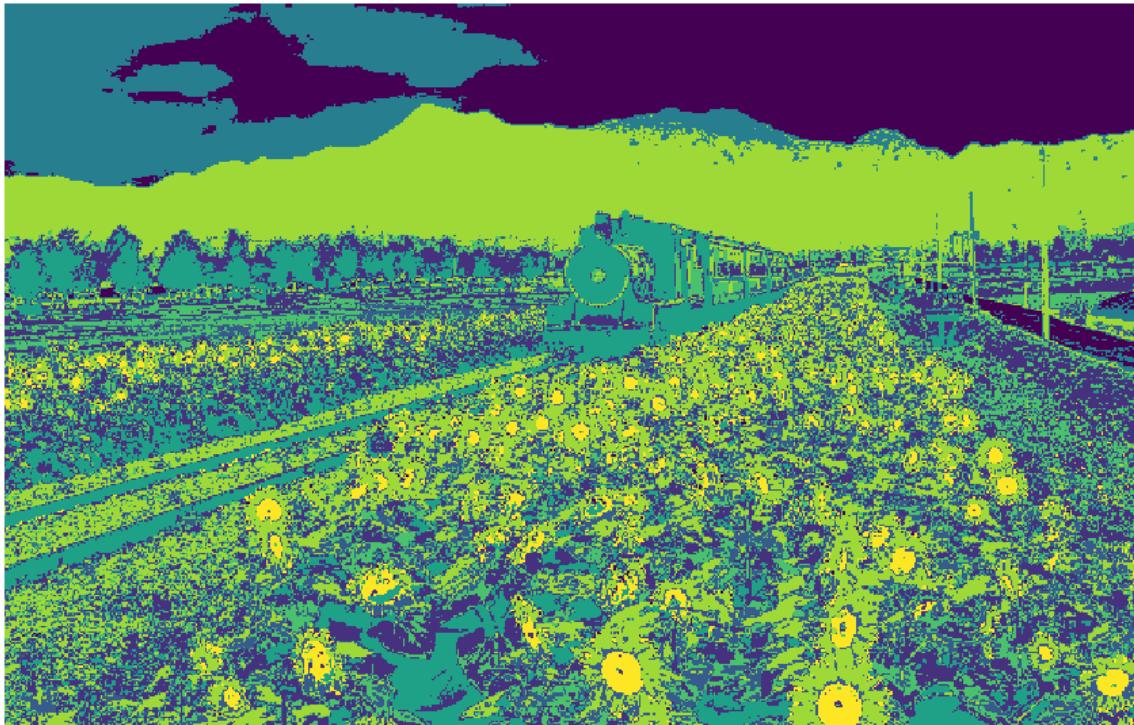
features = color_features(img)

# Sanity checks
assert features.shape == (H * W, C), \
    "Incorrect shape! Check your implementation."

assert features.dtype == np.float,\n    "dtype of color_features should be float."

assignments = kmeans_fast(features, 8)
segments = assignments.reshape((H, W))

# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
```



In the cell below, we visualize each segment as the mean color of pixels in the segment.

In [16]:

```
from utils import visualize_mean_color_image
visualize_mean_color_image(img, segments)
```



2.2 Color and Position Features (15 points)

Another simple feature vector for a pixel is to concatenate its color and position within the image. In other words, for a pixel of color (r, g, b) located at position (x, y) in the image, its feature vector would be (r, g, b, x, y) . However, the color and position features may have drastically different ranges; for example each color channel of an image may be in the range $[0, 1]$, while the position of each pixel may have a much wider range. Uneven scaling between different features in the feature vector may cause clustering algorithms to behave poorly.

One way to correct for uneven scaling between different features is to apply some sort of normalization to the feature vector. One of the simplest types of normalization is to force each feature to have zero mean and unit variance.

Implement `color_position_features` in `segmentation.py`.

Output segmentation should look like the following:



In [17]:

```
from segmentation import color_position_features
np.random.seed(0)

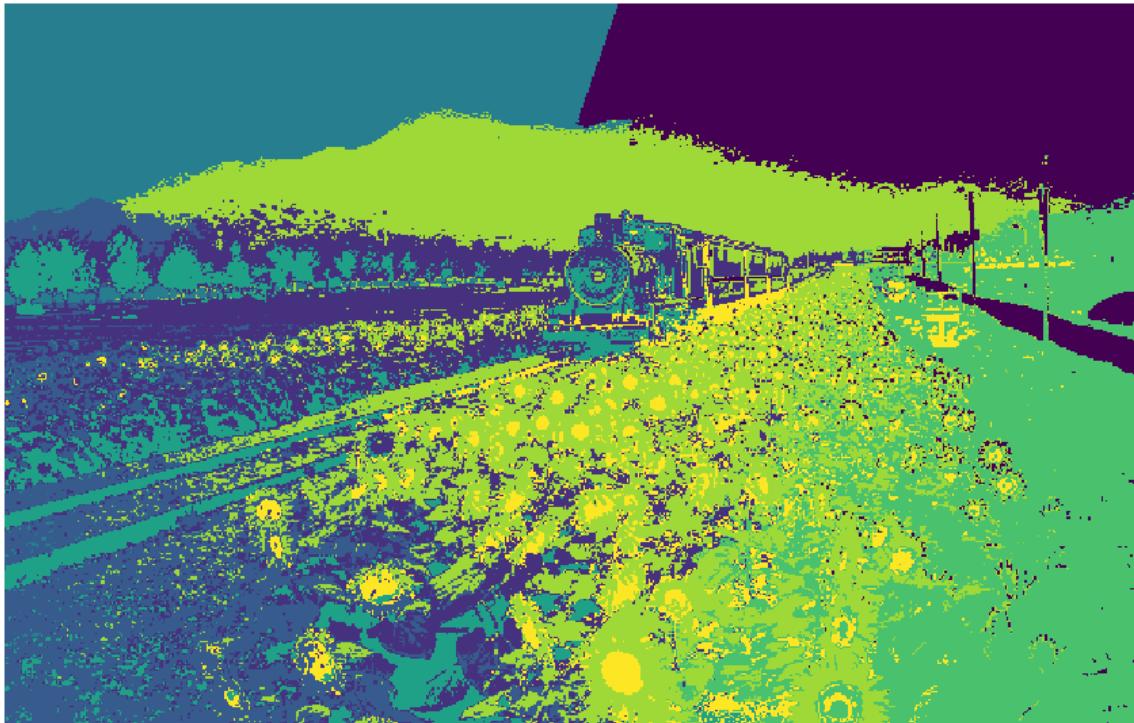
features = color_position_features(img)

# Sanity checks
assert features.shape == (H * W, C + 2), \
    "Incorrect shape! Check your implementation."

assert features.dtype == np.float, \
    "dtype of color_features should be float."

assignments = kmeans_fast(features, 8)
segments = assignments.reshape((H, W))

# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
```



In [18]:

```
visualize_mean_color_image(img, segments)
```



Extra Credit: Implement Your Own Feature

For this programming assignment we have asked you to implement a very simple feature transform for each pixel. While it is not required, you should feel free to experiment with other feature transforms. Could your final segmentations be improved by adding gradients, edges, SIFT descriptors, or other information to your feature vectors? Could a different type of normalization give better results?

Implement your feature extractor `my_features` in `segmentation.py`

Depending on the creativity of your approach and the quality of your writeup, implementing extra feature vectors can be worth extra credit (up to 1 point).

Describe your approach: (YOUR APPROACH)

In [54]:

```
from segmentation import my_features

# Feel free to experiment with different images
# and varying number of segments
img = io.imread('train.jpg')
num_segments = 8

H, W, C = img.shape

# Extract pixel-level features
features = my_features(img)

# Run clustering algorithm
assignments = kmeans_fast(features, num_segments)

segments = assignments.reshape((H, W))

# Display segmentation
plt.imshow(segments, cmap='viridis')
plt.axis('off')
plt.show()
```

```
-----
-
AttributeError                                Traceback (most recent call last)
t)
<ipython-input-54-9db26f306439> in <module>
    12
    13 # Run clustering algorithm
--> 14 assignments = kmeans_fast(features, num_segments)
    15
    16 segments = assignments.reshape((H, W))

~\Desktop\Computer Vision\Assignments\Assignment 5\segmentation.py in kmeans_fast(features, k, num_iters)
    75     """
    76
--> 77     N, D = features.shape
    78
    79     assert N >= k, 'Number of clusters cannot be greater than number of points'

AttributeError: 'NoneType' object has no attribute 'shape'
```

3 Quantitative Evaluation (30 points)

Looking at images is a good way to get an idea for how well an algorithm is working, but the best way to evaluate an algorithm is to have some quantitative measure of its performance.

For this project we have supplied a small dataset of cat images and ground truth segmentations of these images into foreground (cats) and background (everything else). We will quantitatively evaluate different segmentation methods (features and clustering methods) on this dataset.

We can cast the segmentation task into a binary classification problem, where we need to classify each pixel in an image into either foreground (positive) or background (negative). Given the ground-truth labels, the accuracy of a segmentation is $(TP + TN)/(P + N)$.

Implement `compute_accuracy` in `segmentation.py`.

In [19]:

```
from segmentation import compute_accuracy

mask_gt = np.zeros((100, 100))
mask = np.zeros((100, 100))

# Test compute_accuracy function
mask_gt[20:50, 30:60] = 1
mask[30:50, 30:60] = 1

accuracy = compute_accuracy(mask_gt, mask)

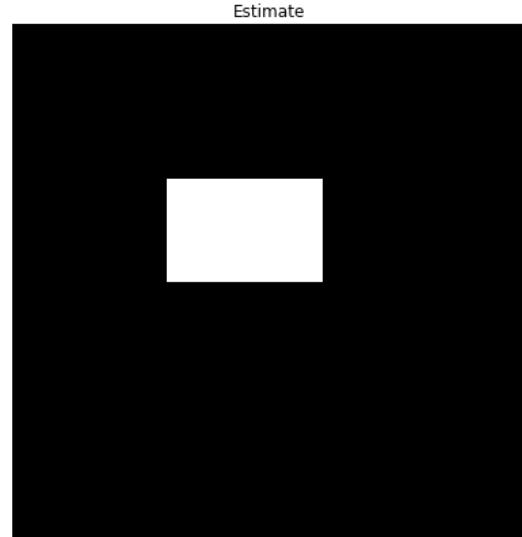
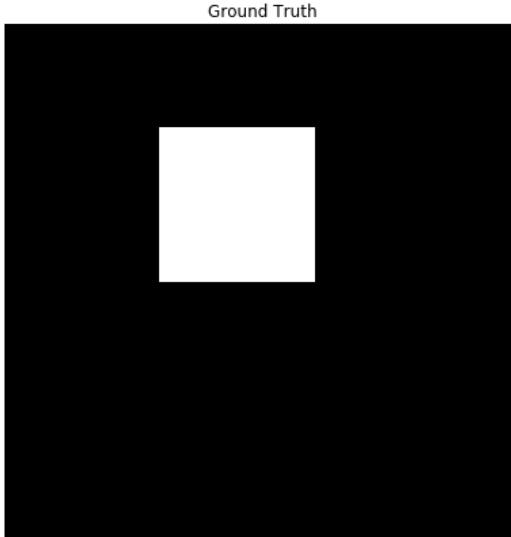
print('Accuracy: %0.2f' % (accuracy))
if accuracy != 0.97:
    print('Check your implementation!')

plt.subplot(121)
plt.imshow(mask_gt)
plt.title('Ground Truth')
plt.axis('off')

plt.subplot(122)
plt.imshow(mask)
plt.title('Estimate')
plt.axis('off')

plt.show()
```

Accuracy: 0.97



You can use the script below to evaluate a segmentation method's ability to separate foreground from background on the entire provided dataset. Use this script as a starting point to evaluate a variety of segmentation parameters.

In [38]:

```
from utils import load_dataset, compute_segmentation
from segmentation import evaluate_segmentation

# Load a small segmentation dataset
imgs, gt_masks = load_dataset('./data')

# Set the parameters for segmentation.
num_segments = 2
clustering_fn = kmeans_fast
feature_fn = color_features #color_position_features#
scale = 1

mean_accuracy = 0.0

segmentations = []

for i, (img, gt_mask) in enumerate(zip(imgs, gt_masks)):
    # Compute a segmentation for this image
    segments = compute_segmentation(img, num_segments,
                                    clustering_fn=clustering_fn,
                                    feature_fn=feature_fn,
                                    scale=scale)

    segmentations.append(segments)

# Evaluate segmentation
accuracy = evaluate_segmentation(gt_mask, segments)

print('Accuracy for image %d: %0.4f' %(i, accuracy))
mean_accuracy += accuracy

mean_accuracy = mean_accuracy / len(imgs)
print('Mean accuracy: %0.4f' % mean_accuracy)
```

```
Accuracy for image 0: 0.5784
Accuracy for image 1: 0.6224
Accuracy for image 2: 0.9837
Accuracy for image 3: 0.9273
Accuracy for image 4: 0.5035
Accuracy for image 5: 0.8053
Accuracy for image 6: 0.5677
Accuracy for image 7: 0.7468
Accuracy for image 8: 0.7405
Accuracy for image 9: 0.7819
Accuracy for image 10: 0.8751
Accuracy for image 11: 0.5866
Accuracy for image 12: 0.7646
Accuracy for image 13: 0.5821
Accuracy for image 14: 0.7842
Accuracy for image 15: 0.5355
Mean accuracy: 0.7116
```

In [39]:

```
# Visualize segmentation results

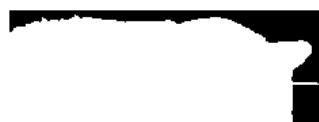
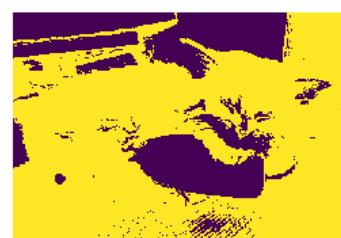
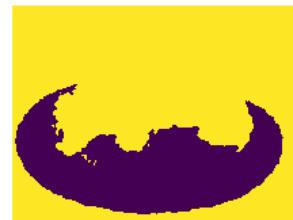
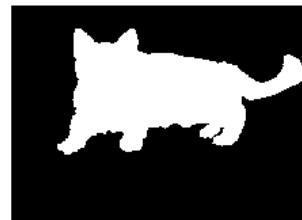
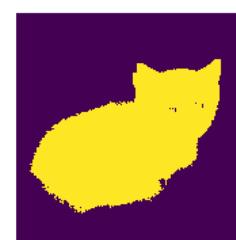
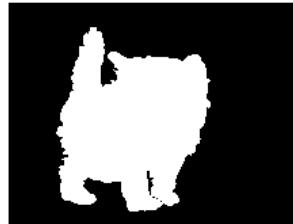
N = len(imgs)
plt.figure(figsize=(15,60))
for i in range(N):

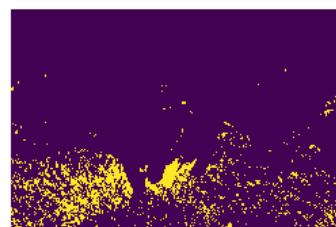
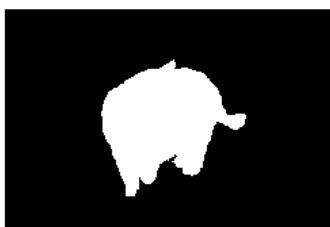
    plt.subplot(N, 3, (i * 3) + 1)
    plt.imshow(imgs[i])
    plt.axis('off')

    plt.subplot(N, 3, (i * 3) + 2)
    plt.imshow(gt_masks[i])
    plt.axis('off')

    plt.subplot(N, 3, (i * 3) + 3)
    plt.imshow(segmentations[i], cmap='viridis')
    plt.axis('off')

plt.show()
```







Include a detailed evaluation of the effect of varying segmentation parameters (feature transform, clustering method, number of clusters, resize) on the mean accuracy of foreground-background segmentations on the provided dataset. You should test a minimum of 10 combinations of parameters. To present your results, add rows to the table below (you may delete the first row).

Feature Transform	Clustering Method	Number of segments	Scale	Mean Accuracy
Color	K-Means	3	0.5	0.7550
Color	K-means	3	1	0.7979
Color	K-means	4	1	0.7607
Color	K-means	4	0.8	0.7503
Color	K-means	2	0.8	0.6977
Color	K-means	3	0.4	0.8020
Color-position	K-means	3	0.5	0.6773
Color-position	K-means	3	1	0.7229
Color-position	K-means	4	1	0.7362
Color-position	K-means	2	1	0.7116

Observe your results carefully and try to answer the following question:

1. Based on your quantitative experiments, how do each of the segmentation parameters affect the quality of the final foreground-background segmentation?
2. Are some images simply more difficult to segment correctly than others? If so, what are the qualities of these images that cause the segmentation algorithms to perform poorly?
3. Also feel free to point out or discuss any other interesting observations that you made.

Write your analysis in the cell below.

Your answer here:

1. In terms of the number of segments, 3 is the most optimum. Increasing the number decreases the quality and decreasing the number of segments worsens the quality further. In terms of the scale, the higher it is(approaching 1) the better the quality of the final foreground-background segmentation. Clustering based on colour-position features is less effective than clustering based on colour features.
2. Yes, some images are more difficult to segment correctly than others. For example, the dark spots or some colours of the objects/foreground may look similar to the background hence causing poor segmentation.
3. I noticed that the higher the colour contrast between the foreground and the background, the better the segmentation(with 3 number of segments).

In []: