

Nonclassicality and Higher-Order Nonlinearity in Levitated Optomechanics

Andrey A. Rakhubovsky, Darren W. Moore, Radim Filip

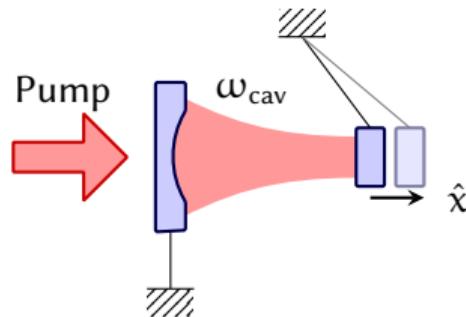
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Quant. Sci. Technol. **4**, 024006 (2019),
arXiv:1904.00772, 1904.00773 [quant-ph]

ICQOQI Minsk

15.05.2019

Cavity Optomechanics



- ★ Radiation pressure drives mechanical motion
- ★ Mechanical displacement changes optical length of the cavity

Experimental Realizations

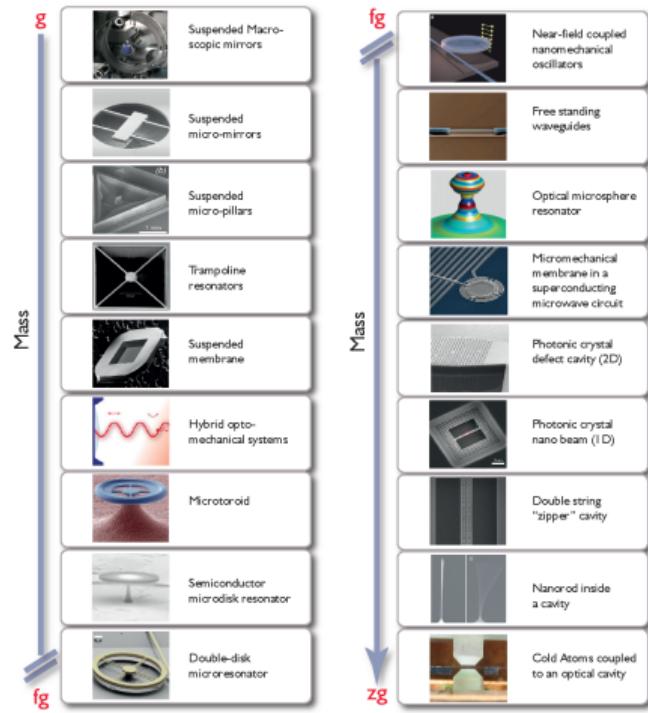


Figure source: ¹

¹ Aspelmeyer, Kippenberg and Marquardt, RMP **86**, 1391 (2014)

² Kashkanova *et al.*, Nat. Phys. **13**, 74 (2017)

Experimental Realizations

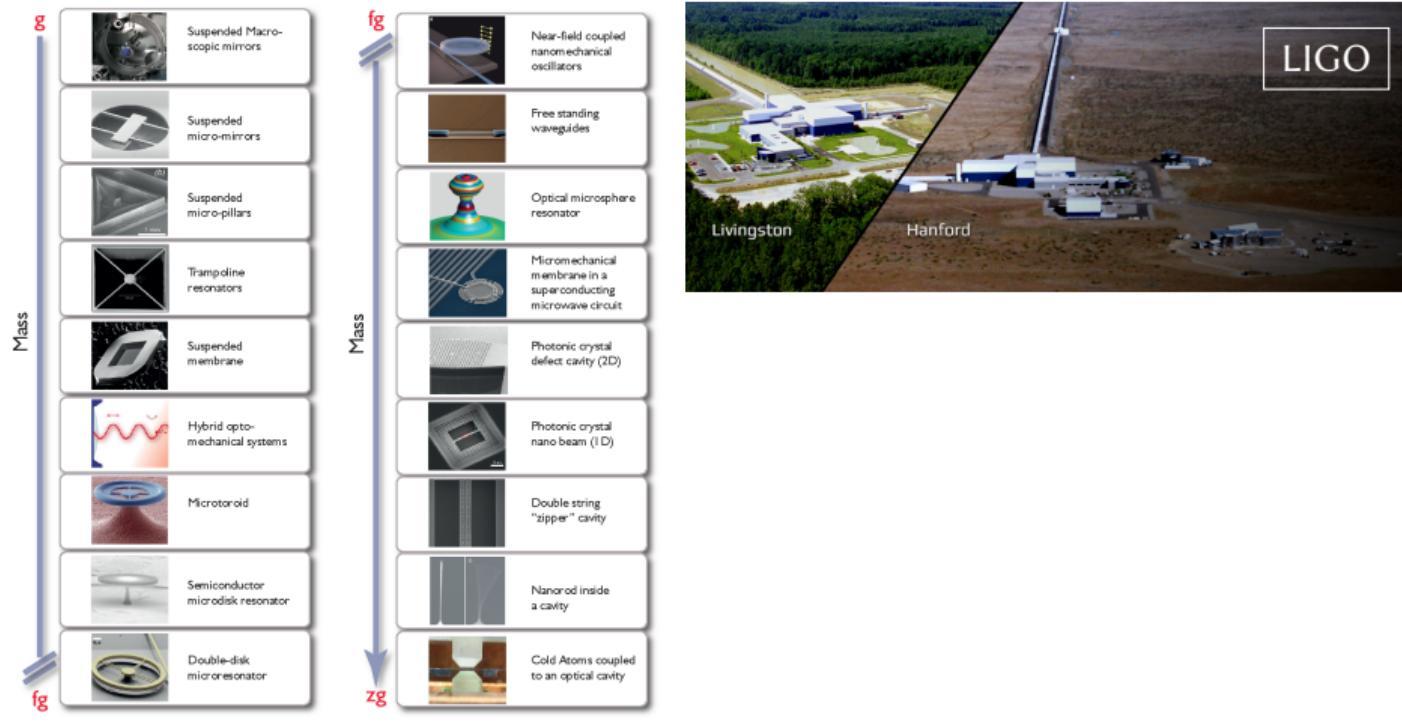


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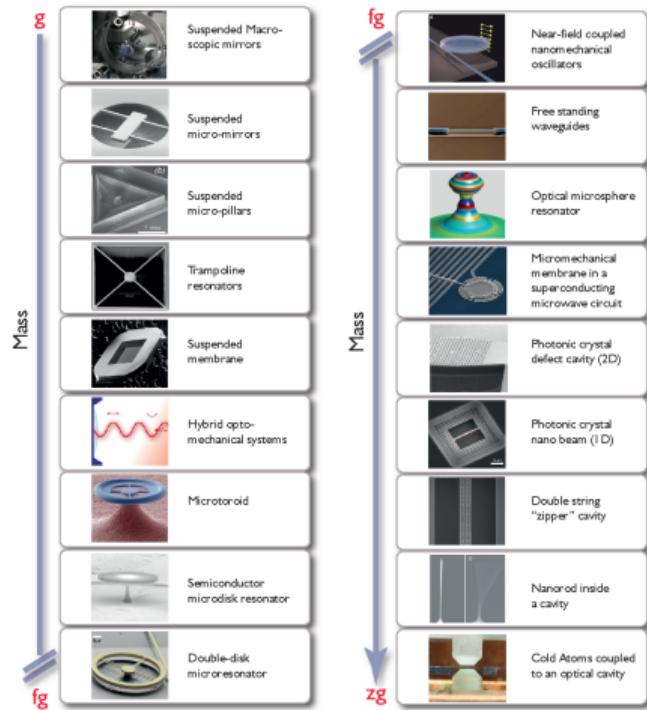


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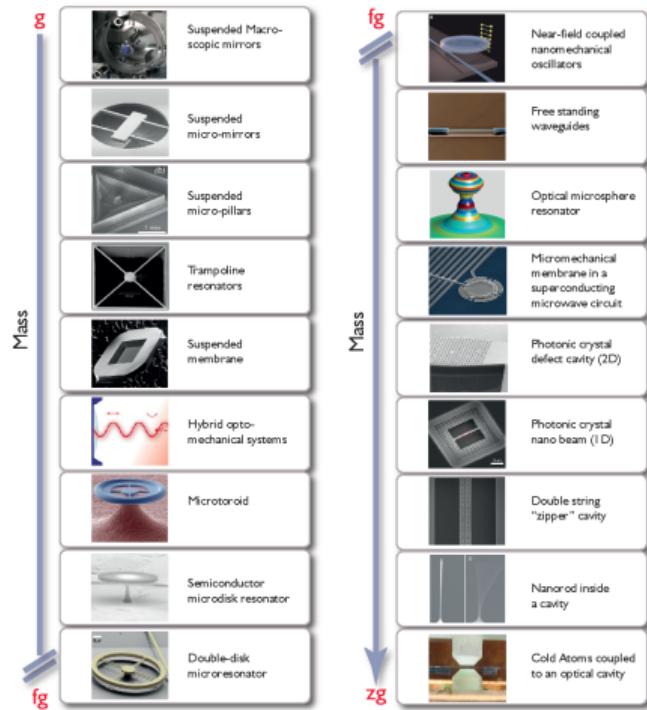


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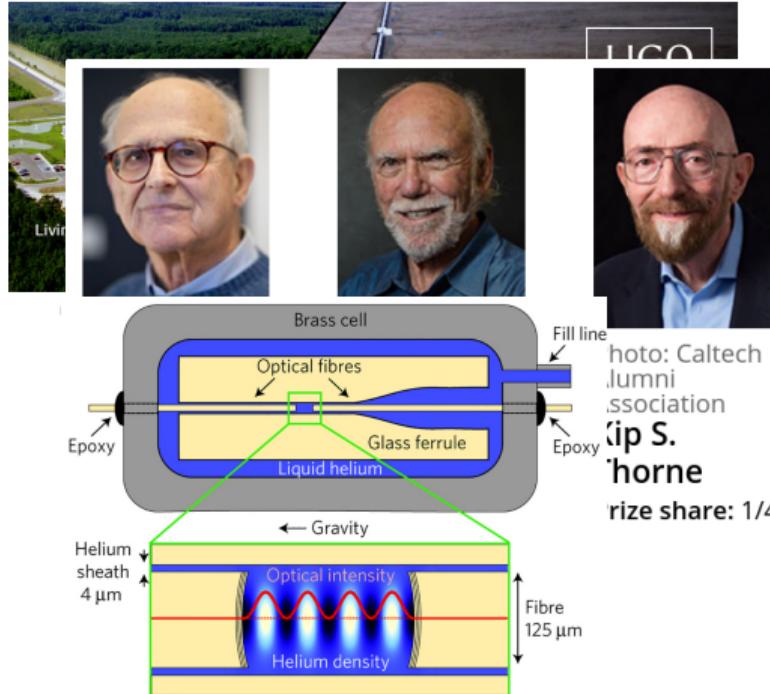
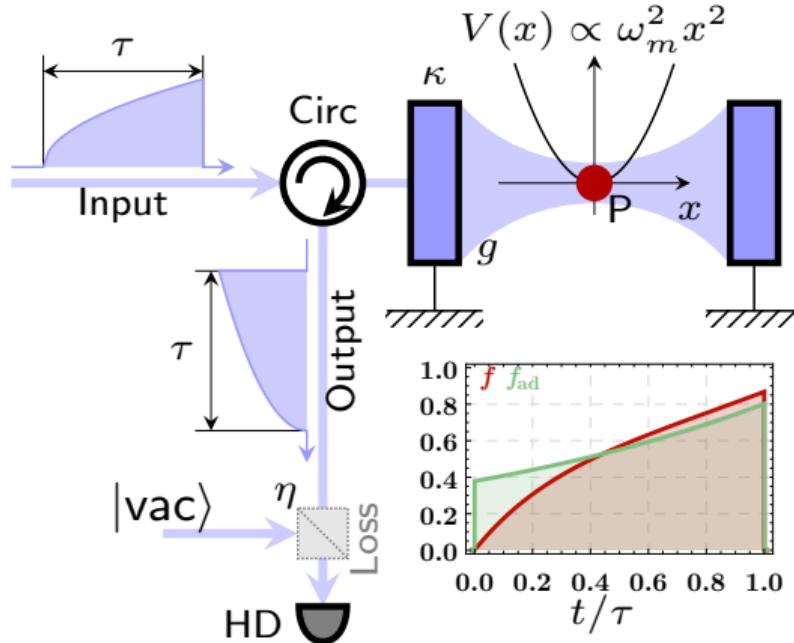


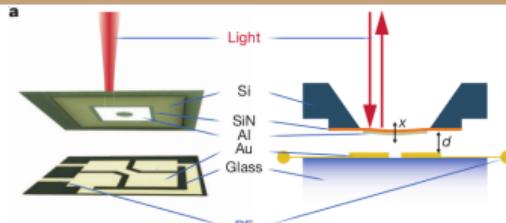
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Levitated Optomechanics



Advantages of Optomechanics for Quantum Technology

Quantum Communication

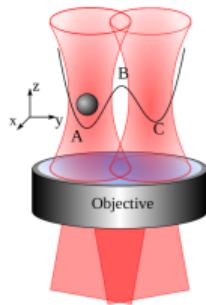


Bagci *et al.*, Nature 507, 81 (2014)

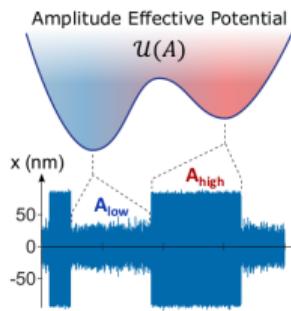
Quantum Metrology

- ★ High-Q oscillators
- ★ Squeezed states

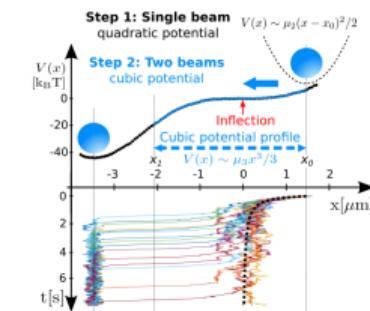
Quantum Computation and Simulation: Nonlinear Potentials



Rondin *et al.*, Nat. Nano 12, 1130 (2017)



Ricci *et al.*, Nat. Comms 8, 15141 (2017)



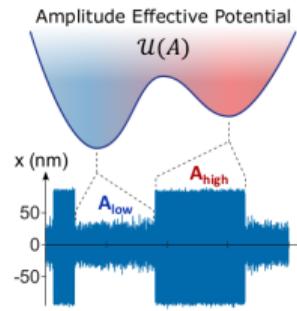
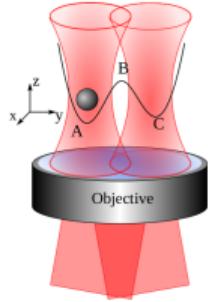
Siler *et al.*, Sci Rep 7, 1697 (2017)

Advantages of Optomechanics for Quantum Technology

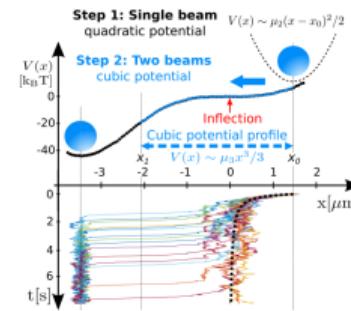
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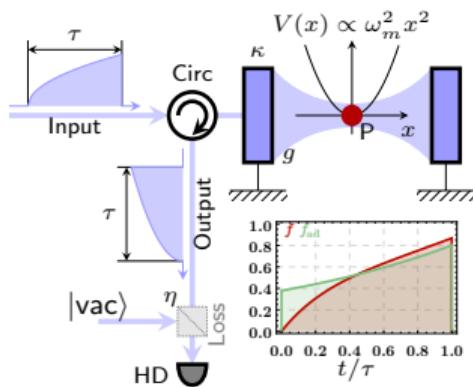
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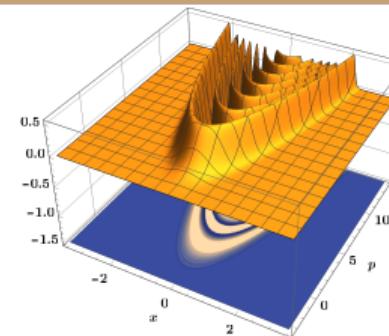
Siler *et al.*, Sci Rep 7, 1697 (2017)

Main Results

Squeezing Mechanical Motion



Approximate Cubic Phase State



$$|\gamma\rangle = e^{i\gamma x^3} |p\rangle \approx e^{i\gamma x^3} \hat{S} |0\rangle$$

A soft-focus, monochromatic image of a city skyline. In the center-right, a large cathedral with two prominent spires is visible, partially obscured by trees and other buildings. To the left, there are several modern, low-rise buildings. The sky is filled with scattered clouds.

Introduction

Linear Optomechanics

Quantum Squeezing and Entanglement

Pulsed Optomechanics

Mechanical Squeezing

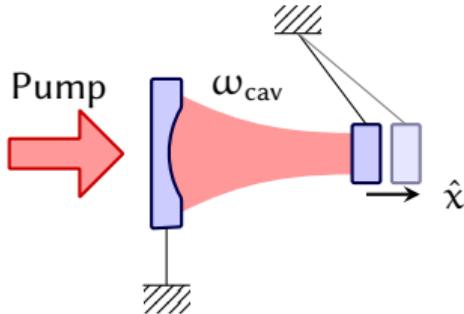
Cubic Phase State in Levitated Optomechanics

Introduction to Cubic Phase States

CPS Preparation

CPS Evaluation

The Optomechanical systems



Radiation

Standard quantization of the cavity field

$$\hat{E}(\mathbf{r}, t) = \sum_p \sum_k e_p u_k(\mathbf{r}) \hat{a}_k(t)$$

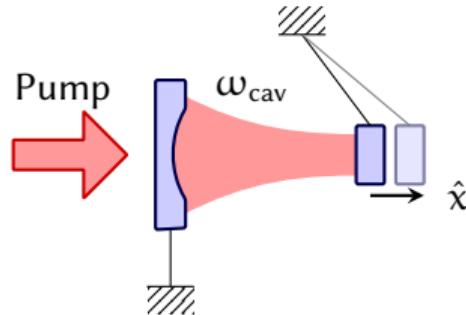
Mechanics

Displacement field

$$\hat{v}(\mathbf{r}, t) = \sum_n v_n(\mathbf{r}) \hat{x}_n(t)$$

Only one field mode a and one mechanical x are considered.

The Optomechanical interaction

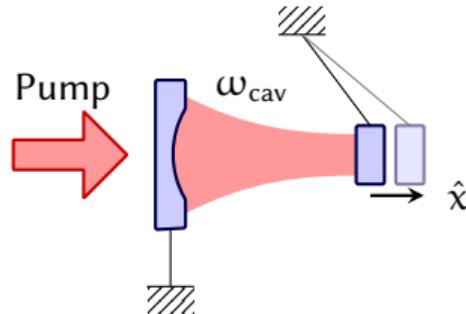


The single-mode cavity Hamiltonian

$$H_{\text{tot}} = \hbar\omega_{\text{cav}}[x] a^\dagger a + H_m$$

g_0 – single-photon optomechanical coupling, typically small

The Optomechanical interaction

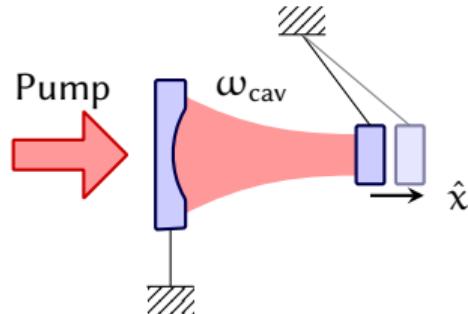


The single-mode cavity Hamiltonian

$$H_{\text{tot}} = \hbar \omega_{\text{cav}}[x] a^\dagger a + H_m = \hbar \left[\omega_{\text{cav}} + \frac{\partial \omega_{\text{cav}}}{\partial x} \Big|_{x=0} \cdot x \right] a^\dagger a + H_m$$

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The Optomechanical interaction

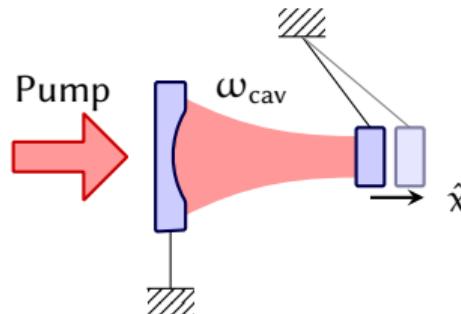


The single-mode cavity Hamiltonian

$$H_{\text{tot}} = \hbar \omega_{\text{cav}}[x] a^\dagger a + H_m = \hbar \left[\omega_{\text{cav}} + \frac{\partial \omega_{\text{cav}}}{\partial x} \Big|_{x=0} \cdot x \right] a^\dagger a + H_m \equiv \hbar \omega_{\text{cav}} a^\dagger a - \hbar g_0 a^\dagger a x + H_m.$$

g_0 – single-photon optomechanical coupling, typically small

The Optomechanical interaction



The single-mode cavity Hamiltonian

$$H_{\text{tot}} = \hbar\omega_{\text{cav}}[x]a^\dagger a + H_m = \hbar \left[\omega_{\text{cav}} + \frac{\partial \omega_{\text{cav}}}{\partial x} \Big|_{x=0} \cdot x \right] a^\dagger a + H_m \equiv \hbar\omega_{\text{cav}}a^\dagger a - \hbar g_0 a^\dagger a x + H_m.$$

g_0 — single-photon optomechanical coupling, typically small

In presence of strong classical pump the interaction is linearized

$$H = \hbar\omega_{\text{cav}}a^\dagger a - \hbar g(a^\dagger + a)(b_m^\dagger + b_m) + \hbar\omega_m b_m^\dagger b_m.$$

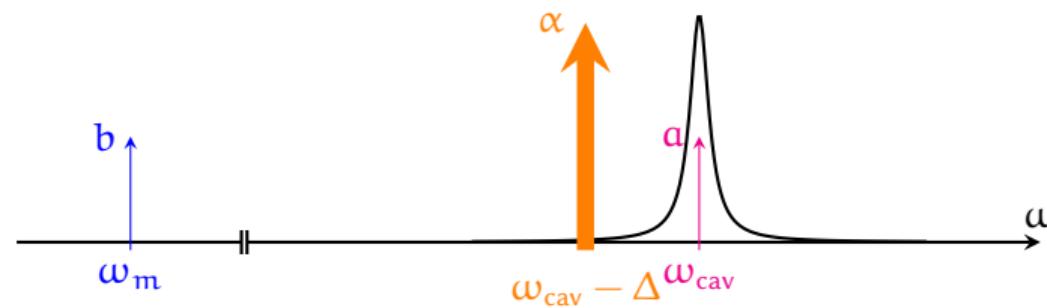
Linearized Optomechanics

The Hamiltonian

$$H = \hbar\Delta a^\dagger a + \hbar\omega_m b^\dagger b - \hbar g(a^\dagger + a)(b^\dagger + b)$$

The main participants

- a quantum optical mode at ω_{cav}
- α strong classical pump at $\omega_{\text{cav}} - \Delta$
- b quantized mechanical motion at ω_m

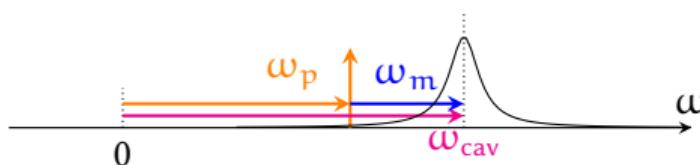


Resolved-sideband optomechanics

Lower Mechanical Sideband

Pump at the difference frequency

$$\omega_p = \omega_{\text{cav}} - \omega_m$$



$$H \propto ab^\dagger + a^\dagger b$$

- ★ Parametric Converter / Beam-splitter
- ★ State swap / Cooling

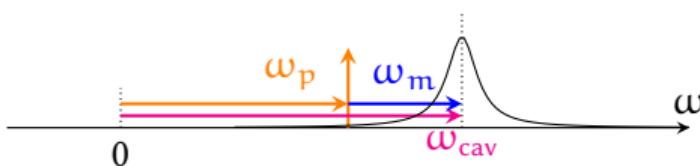
Required: resolved sideband $\kappa \ll \omega_m$

Resolved-sideband optomechanics

Lower Mechanical Sideband

Pump at the difference frequency

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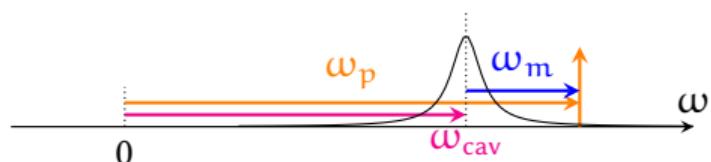
$$H \propto ab^\dagger + a^\dagger b$$

- ★ Parametric Converter / Beam-splitter
- ★ State swap / Cooling

Upper Mechanical Sideband

Pump at the sum frequency

$$\omega_p = \omega_{\text{cav}} + \omega_m,$$



$$H = ab + a^\dagger b^\dagger$$

- ★ Parametric Amp / Two-mode squeezing
- ★ Entanglement

Required: resolved sideband $\kappa \ll \omega_m$

Digression: Optical Spring

Radiation Pressure Force

$$\begin{aligned} F_{RP}(t) &\propto P(x) = -Kx \\ &= -Kx(t - \tau_*) \\ &\approx -Kx(x - \tau_* \dot{x}) = -Kx + \Gamma \dot{x} \end{aligned}$$

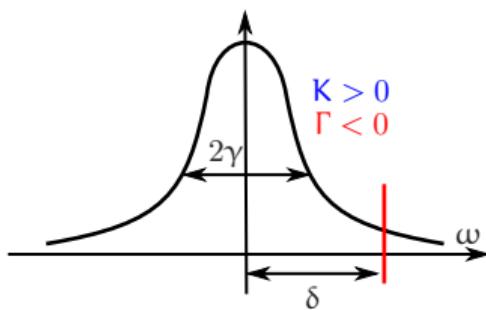
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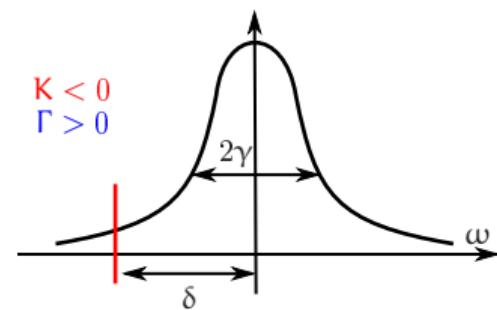
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Электромагнитная жесткость впервые наблюдалась В. Б. Брагинским ³

Настройка на правый склон



Настройка на левый склон



Положительная жесткость и
отрицательное затухание

Отрицательная жесткость и
положительное затухание

▶ Назад

³V.B. Braginsky, I.I. Minakova Bull. MSU III 1, 83 (1964)
А. Рахубовский (физфак МГУ)

A soft-focus photograph of a city skyline, likely Cologne, featuring the prominent twin towers of the Cologne Cathedral. In the foreground, there are several modern, low-rise buildings and trees. The sky is filled with large, white, billowing clouds.

Introduction

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CPS Preparation

CPS Evaluation

Environment

Optical Environment



κ_{ext} detection channel, κ_L losses

Interacts with the modes of travelling light,
(almost) each in vacuum. Collective operator a_i

$$[a_i(t), a_i^\dagger(t')] = \delta(t - t');$$

$$\frac{1}{2} \left\langle a_i(t)a_i^\dagger(t') + a_i^\dagger(t')a_i(t) \right\rangle = \delta(t - t').$$

Typically the cavity is overcoupled with

$$\kappa_{\text{ext}} \gg \kappa_L$$

Environment

Optical Environment



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Mechanical Environment

Q-factor:

$$Q_{\text{tot}}^{-1} = Q_{\text{clamp}}^{-1} + Q_{\text{mat}}^{-1} + Q_{\text{air}}^{-1} + Q_{\text{scat}}^{-1} + \dots$$

At rate $\gamma = \omega_m/Q$ coupled to a thermal bath with bosonic operator b^{th} :

$$\begin{aligned} [b^{\text{th}}(t), b^{\text{th}\dagger}(t')] &= \delta(t - t'), \\ \frac{1}{2} \left\langle \{b^{\text{th}}(t), b^{\text{th}\dagger}(t')\} \right\rangle &= (2n_{\text{th}} + 1)\delta(t - t'). \end{aligned}$$

$$n_{\text{th}} = \frac{1}{\exp[\hbar\omega_m/k_B t] - 1} \approx k_B T/\hbar\omega_m$$

Equations of motion

Assume blue detuning $\omega_p = \omega_{\text{cav}} + \omega_m$, therefore $H = -\hbar g(a^\dagger b^\dagger + ab)$.

$$\dot{a} = igb^\dagger - \kappa a + \sqrt{2\kappa}a^{\text{in}},$$

$$\dot{b} = iga^\dagger - \frac{\gamma}{2}b + \sqrt{\gamma}b^{\text{th}}$$

Input-output relation for optics $a^{\text{out}} = -a^{\text{in}} + \sqrt{2\kappa}a$

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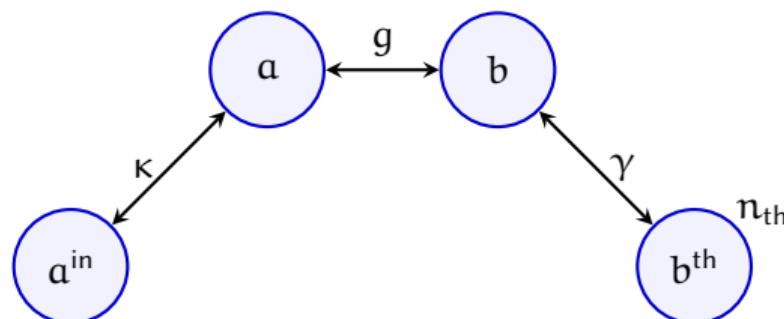
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Parameters:

- ★ Resolved sideband $\kappa \ll \omega_m$
- ★ Weak coupling $g \sim 10^{-3} \div -1 \kappa$
- ★ Slow mechanical decay $\gamma \sim 10^{-7} \div -4 \kappa$
- ★ Not too hot bath $\gamma n_{\text{th}} \leq \{g, \kappa\}$



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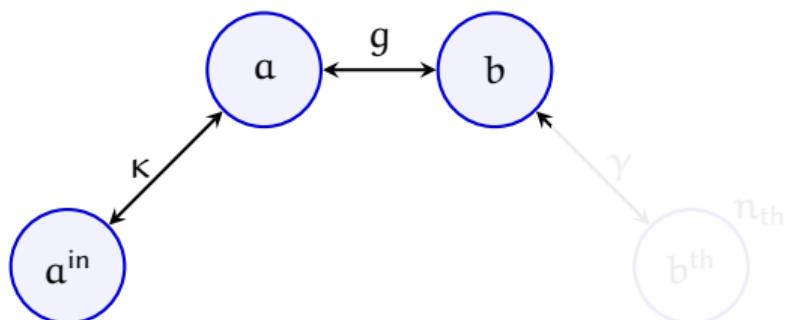
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That is,

- ★ mechanical decay can be approximately ignored



Equations of motion

Assume blue detuning $\omega_p = \omega_{\text{cav}} + \omega_m$, therefore $H = -\hbar g(a^\dagger b^\dagger + ab)$.

$$0 = igb^\dagger - \kappa a + \sqrt{2\kappa}a^{\text{in}},$$

$$\dot{b} = iga^\dagger$$

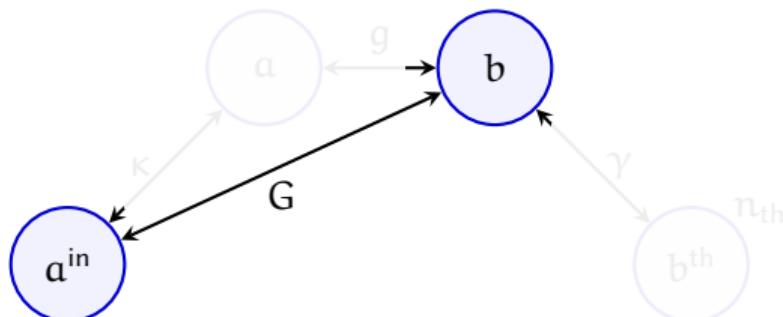
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- ★ cavity mode can be adiabatically eliminated



Equations of motion

Assume blue detuning $\omega_p = \omega_{\text{cav}} + \omega_m$, therefore $H = -\hbar g(a^\dagger b^\dagger + ab)$.

$$0 = igb^\dagger - \kappa a + \sqrt{2\kappa}a^{\text{in}},$$

$$\dot{b} = iga^\dagger$$

Input-output relation for optics $a^{\text{out}} = -a^{\text{in}} + \sqrt{2\kappa}a$

$$A^{\text{out}} = \sqrt{\mathfrak{G}}A^{\text{in}} + \sqrt{\mathfrak{G}-1}b^\dagger(0),$$

$$b(\tau) = \sqrt{\mathfrak{G}}b(0) + \sqrt{\mathfrak{G}-1}A^{\text{in},\dagger}.$$

$$A^{\text{in}} \propto \int_0^\tau dt a^{\text{in}}(t)e^{Gt}, \quad A^{\text{out}} \propto \int_0^\tau dt a^{\text{out}}(t)e^{-Gt}.$$

$$[a^k(t), a^{k',\dagger}(t')] = \delta(t-t')\delta_{kk'}.$$

Parameters:

- ★ Resolved sideband $\kappa \ll \omega_m$
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That is,

- ★ mechanical decay can be approximately ignored
- ★ cavity mode can be adiabatically eliminated

Two-mode squeezing

In general case (when adiabatic model does not hold, $g \propto \kappa$)

Define $\mathbf{a} = (a, b)$, $\mathbb{A}, \mathbf{f} = (\sqrt{2\kappa}a^{\text{in}}, \sqrt{\gamma}b^{\text{th}})$, then

$$\dot{\mathbf{a}} = \mathbb{A} \cdot \mathbf{a} + \mathbf{f}$$

Formal solution (with $\mathbb{M}(s) = \exp[-\mathbb{A}s]$)

$$\mathbf{a}(t) = \mathbb{M}(t)\mathbf{a}(0) + \int_0^t ds \mathbb{M}(t-s).\mathbf{f}(s).$$

Input-output transformations

$$A^{\text{out}} = \sqrt{\mathfrak{G}} A^{\text{in}} + \sqrt{\mathfrak{G} - 1} b^\dagger(0) + \text{Noise},$$

$$b(\tau) = \sqrt{\mathfrak{G}} b(0) + \sqrt{\mathfrak{G} - 1} A^{\text{in},\dagger} + \text{Noise}.$$

Two-mode squeezing gain

$$\mathfrak{G} = \mathfrak{G}(\kappa, g, \gamma_m, \tau),$$

Input-output pulse bosonic operators

$$A^{\text{in}} = \int_0^\tau dt a^{\text{in}}(t) f^{\text{in}}(\tau - t),$$

$$A^{\text{out}} = \int_0^\tau dt a^{\text{out}}(t) f^{\text{out}}(\tau - t).$$

$$[a^k(t), a^{k',\dagger}(t')] = \delta(t-t')\delta_{kk'}.$$

A soft-focus, monochromatic image of a city skyline. In the center-right, a large cathedral with two prominent spires is visible. To its left are several smaller buildings, some with red roofs. In the foreground, there are more modern, low-rise buildings and trees. The sky is filled with wispy clouds.

Introduction

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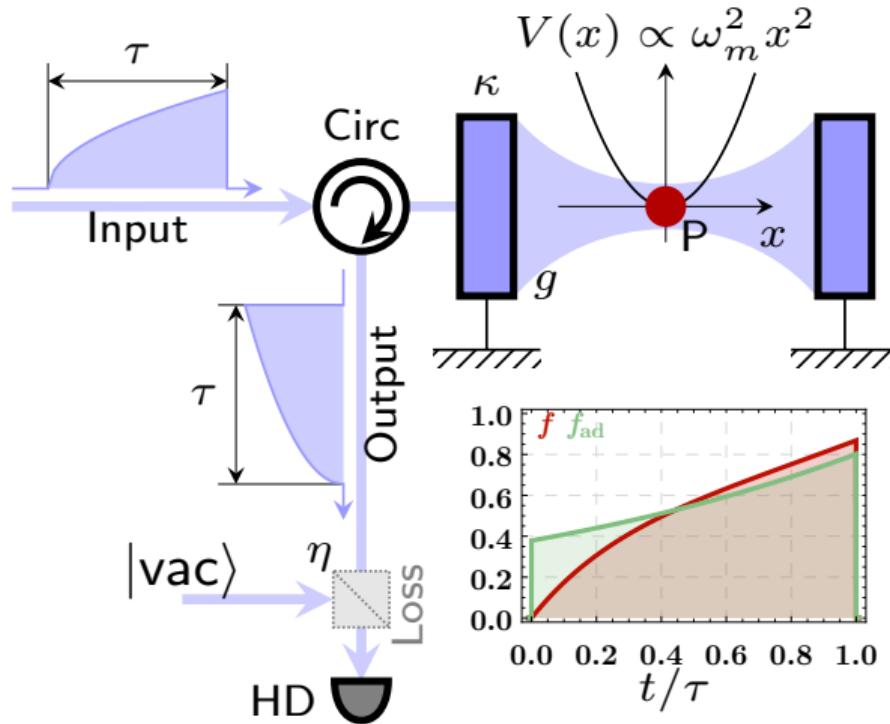
Cubic Phase State in Levitated Optomechanics

Introduction to Cubic Phase States

CPS Preparation

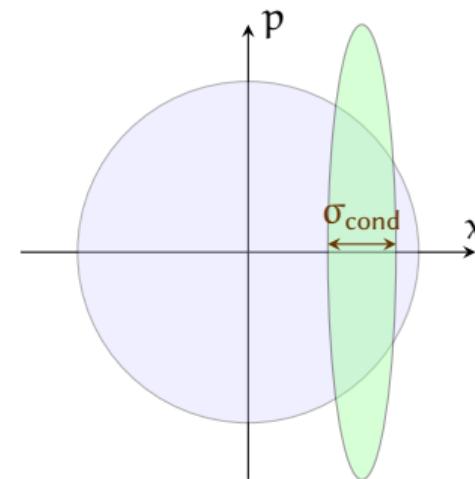
CPS Evaluation

The Protocol for Squeezing [Quant. Sci. Technol. 4, 024006 (2019)]

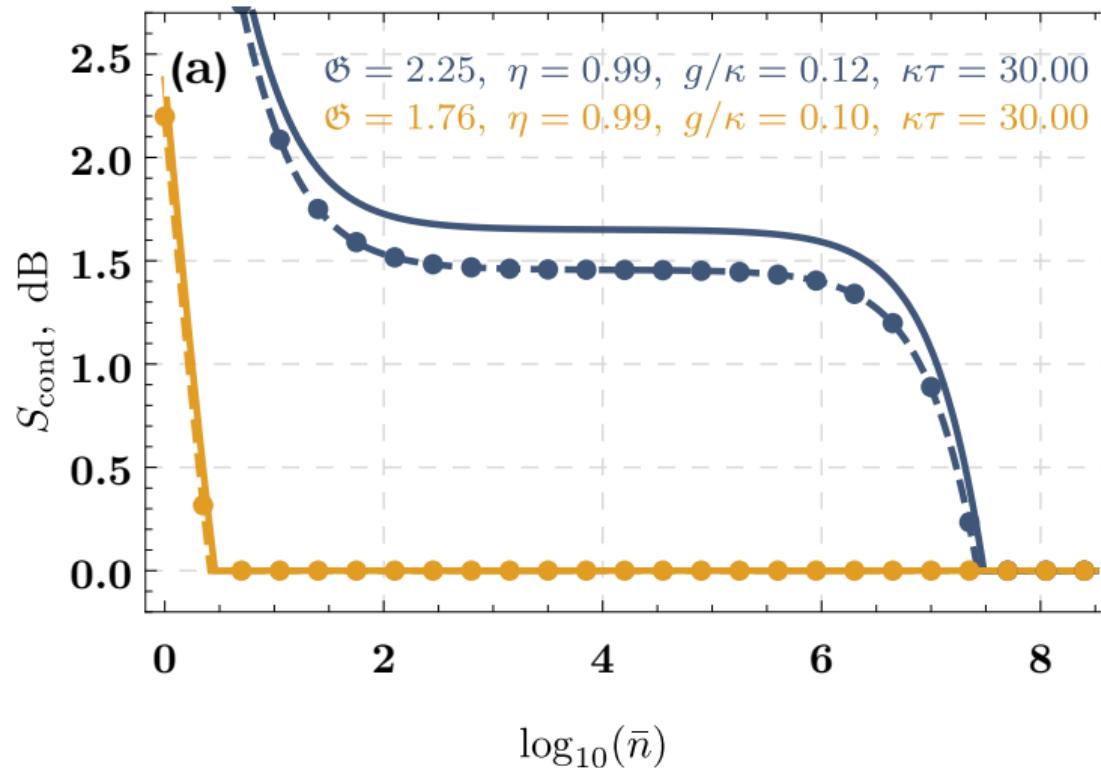


$$A^{\text{out}} = \int_0^\tau dt a^{\text{out}}(\tau - t) f^{\text{out}}(t).$$

$f^{\text{out}}(t)$ depends on the interaction type.
Detecting proper A^{out} projects
mechanical mode on a displaced
squeezed state.

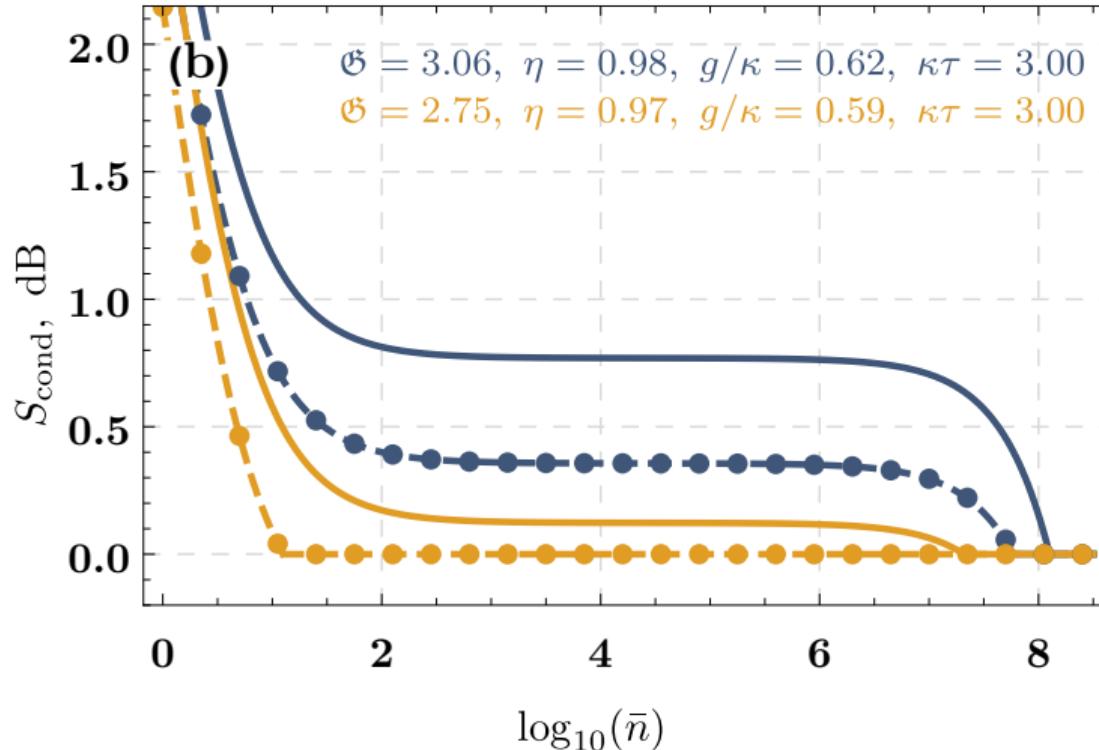


Squeezing in Adiabatic Regime



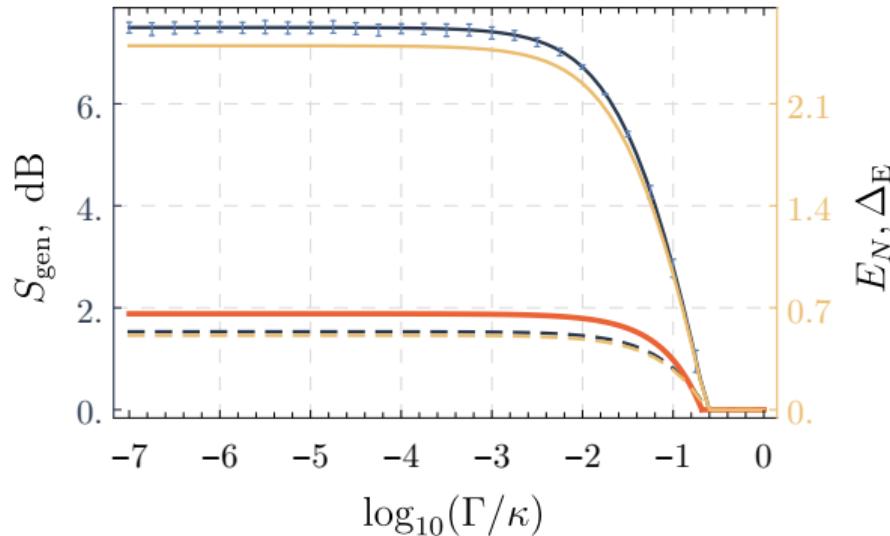
$$S_{\text{cond}} = -10 \log_{10} \sigma_{\text{cond}}$$

Squeezing in Non-adiabatic Regime



$$S_{\text{cond}} = -10 \log_{10} \sigma_{\text{cond}}.$$

Generalized Squeezing and Entanglement



$$S_{\text{gen}} = -10 \log_{10} \min \text{EigenVal}[V_{\text{cov}}].$$

Δ_E – Duan’s variance criterion violation.

A soft-focus, monochromatic image of a city skyline. In the center-right, a large cathedral with two prominent spires is visible, surrounded by other historical and modern buildings. The sky is filled with large, white, billowing clouds.

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CPS state

Devised by Gottesman, Kitaev and Preskill³

$$|\gamma_{\text{GKP}}\rangle \propto \int dx e^{i\gamma x^3} |x\rangle = e^{i\gamma x^3} |p=0\rangle,$$

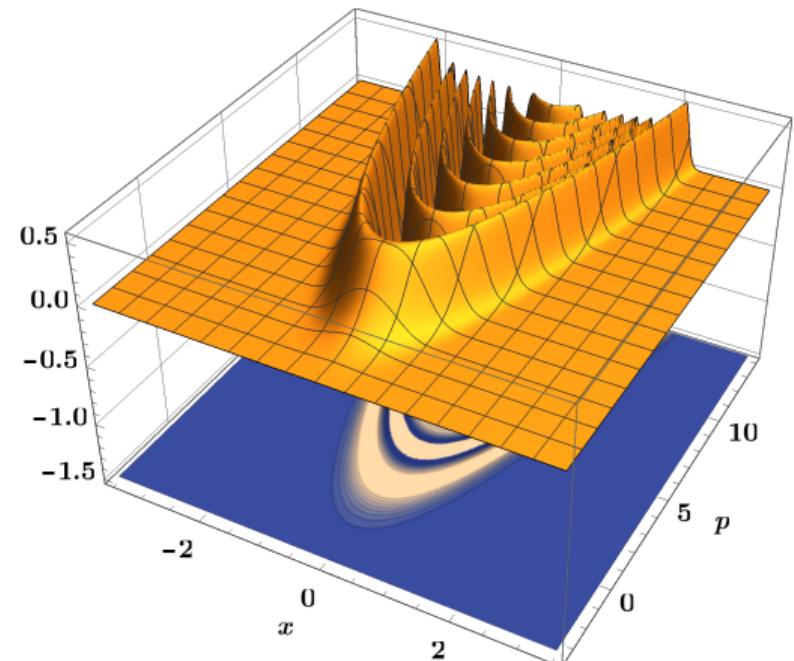
Wigner Function

$$W_{\text{GKP}}(x, p) \propto \text{Ai}\left[\left(\frac{4}{3\gamma}\right)^{1/3} (3\gamma x^2 - p)\right].$$

Nonlinear variance

$$(x, p) \rightarrow (x, p + \gamma x^2) \Rightarrow \langle \delta(p - \lambda x^2)^2 \rangle \rightarrow 0.$$

Required for (in particular) the
measurement-based quantum computing.



³Gottesman, Kitaev, Preskill, PRA **64**, 012310 (2001)

Measurement-based computing

PHYSICAL REVIEW A **97**, 022329 (2018)

General implementation of arbitrary nonlinear quadrature phase gates

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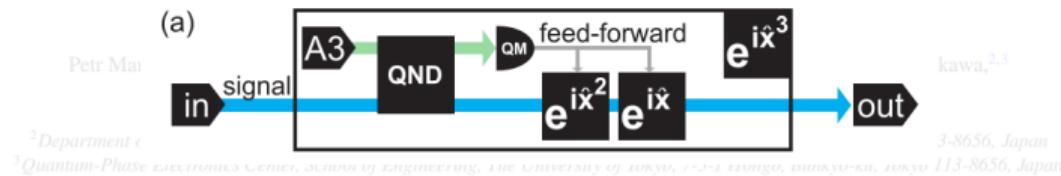
(Received 10 August 2017; published 20 February 2018)

We propose general methodology of deterministic single-mode quantum interaction nonlinearly modifying single quadrature variable of a continuous-variable system. The methodology is based on linear coupling of the system to ancillary systems subsequently measured by quadrature detectors. The nonlinear interaction is obtained by using the data from the quadrature detection for dynamical manipulation of the coupling parameters. This measurement-induced methodology enables direct realization of arbitrary nonlinear quadrature interactions without the need to construct them from the lowest-order gates. Such nonlinear interactions are crucial for more practical and efficient manipulation of continuous quadrature variables as well as qubits encoded in continuous-variable systems.

DOI: [10.1103/PhysRevA.97.022329](https://doi.org/10.1103/PhysRevA.97.022329)

Measurement-based computing

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FIG. 1. Schematic circuits for various implementations of nonlinear gates. QND: quantum nondemolition interaction; QM: quadrature measurement; A_k : ancillary state of the k th order squeezed in $\hat{p} - N \chi_N \hat{x}^{N-1}$. $e^{i\hat{x}^k}$: unitary realization of k th-order nonlinear gate with arbitrary strength. (a) Cubic gate with $N = 3$; (b) $(N + 1)$ th-

DOI: 10.1103/PhysRevA.97.022329
arXiv:1708.03120 [quant-ph]

$$\text{Required } \text{Var}(p - \lambda x^2) \rightarrow 0$$

A soft-focus, monochromatic image of a city skyline. In the center-right, a large cathedral with two prominent spires is visible. To its left are several smaller buildings, some with red roofs. In the foreground, there are more modern, low-rise buildings and trees. The sky is filled with wispy clouds.

Introduction

Linear Optomechanics

Quantum Squeezing and Entanglement

Pulsed Optomechanics

Mechanical Squeezing

Cubic Phase State in Levitated Optomechanics

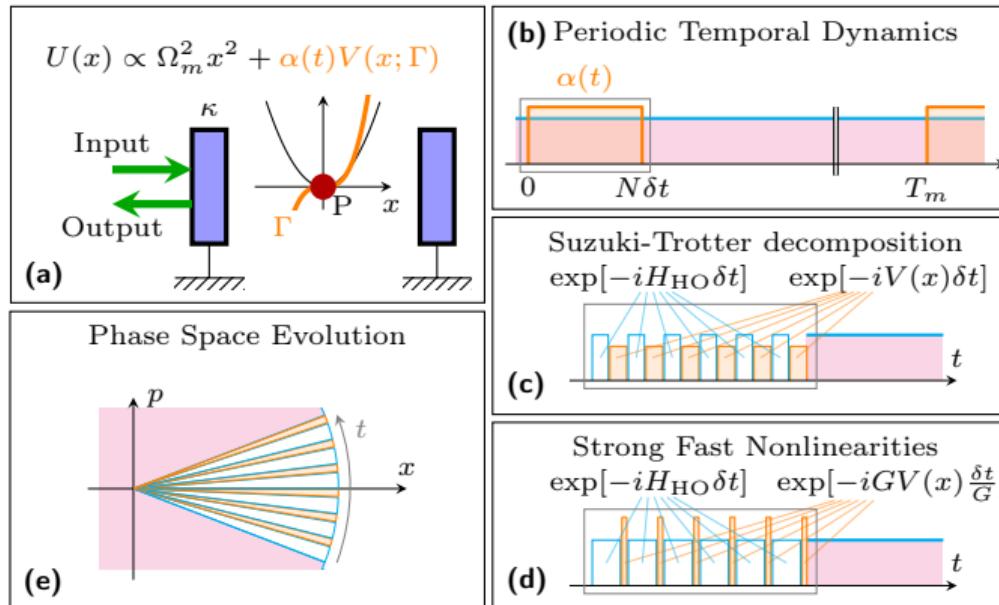
Introduction to Cubic Phase States

CPS Preparation

CPS Evaluation

The Model

Rakhubovsky and Filip [arxiv:1904.00773]



$$\left[\exp[-i(H_{HO} + V(x))\delta t] \right]^N \approx \left[\mathcal{U}_{HO}(\delta t) \mathcal{U}_{NL}(\delta t) + O(\delta t^2) \right]^N,$$

Numerical evaluation

Cubic evolution

In coordinate basis

$$\rho(x, x') \rightarrow \rho(x, x') e^{-i\gamma(x^3 - x'^3)}.$$

Harmonic evolution

Rotation in phase space

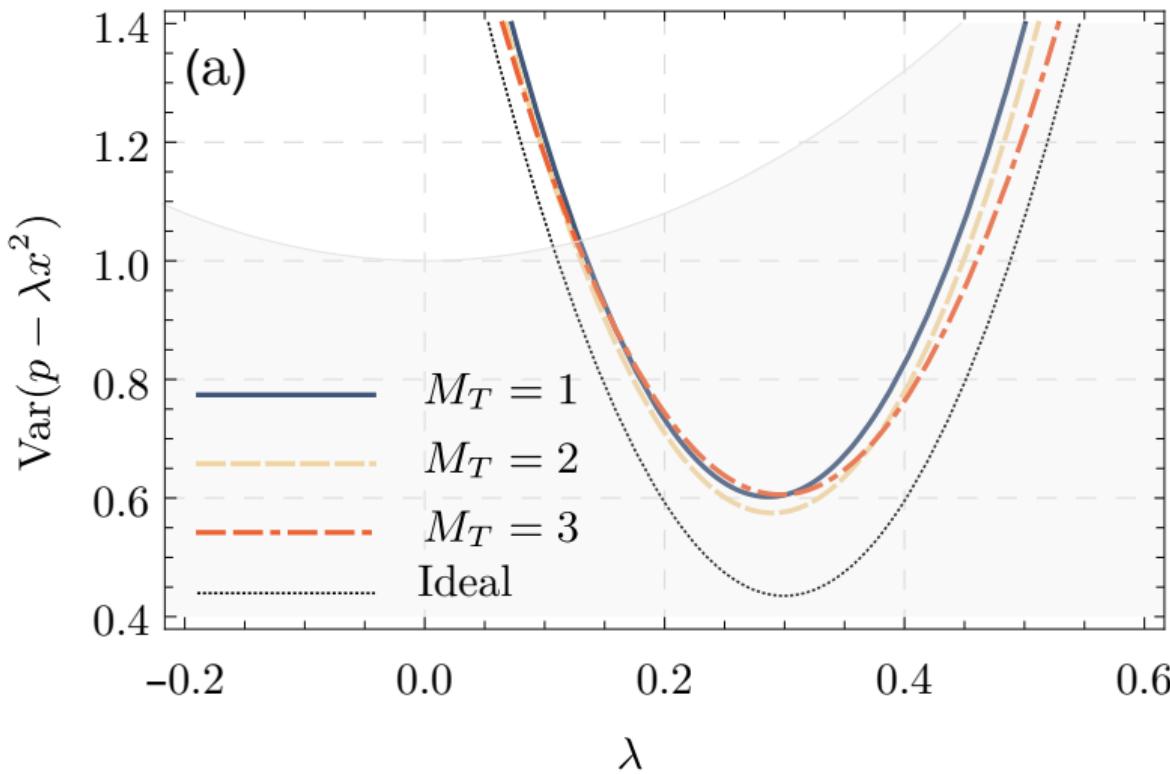
$$W(x, y) \rightarrow W(x \cos \delta + y \sin \delta, x \sin \delta + y \cos \delta).$$

Decoherence

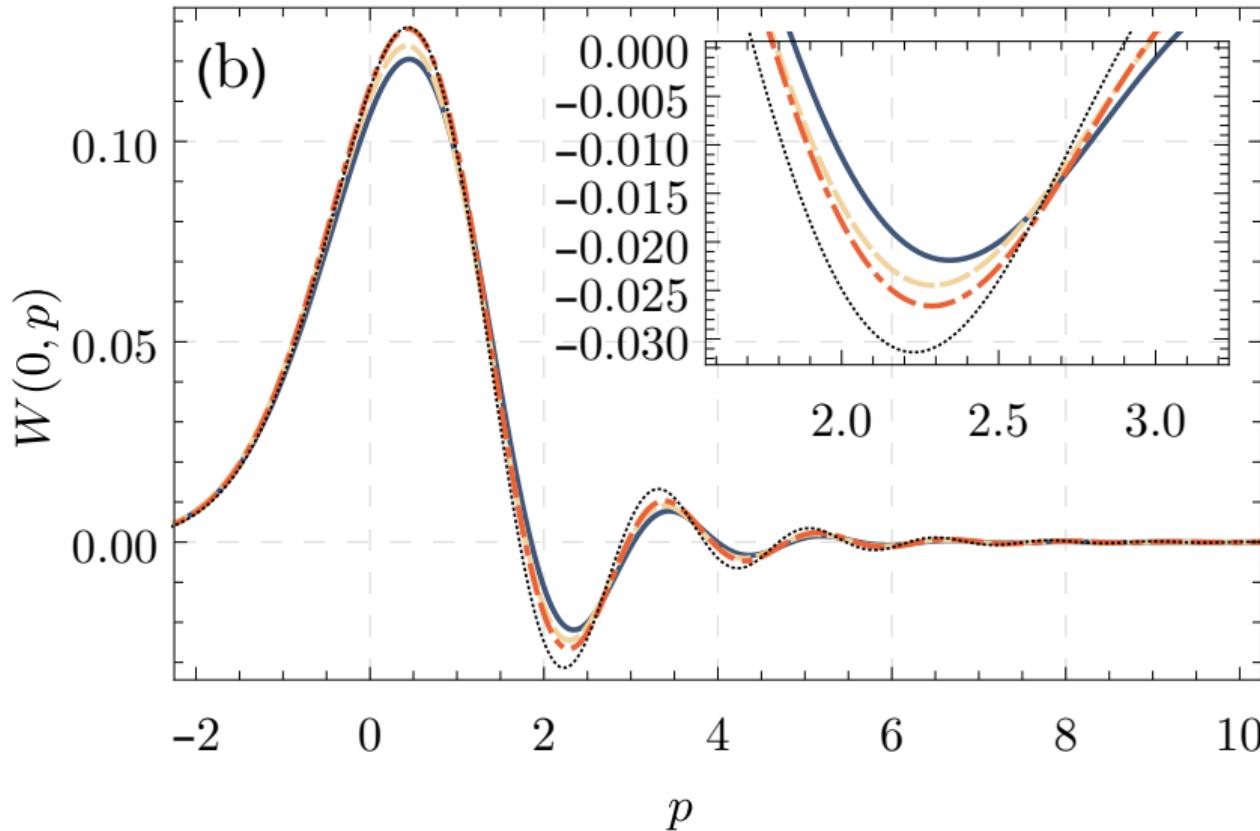
Convolution in phase space with a Gaussian kernel

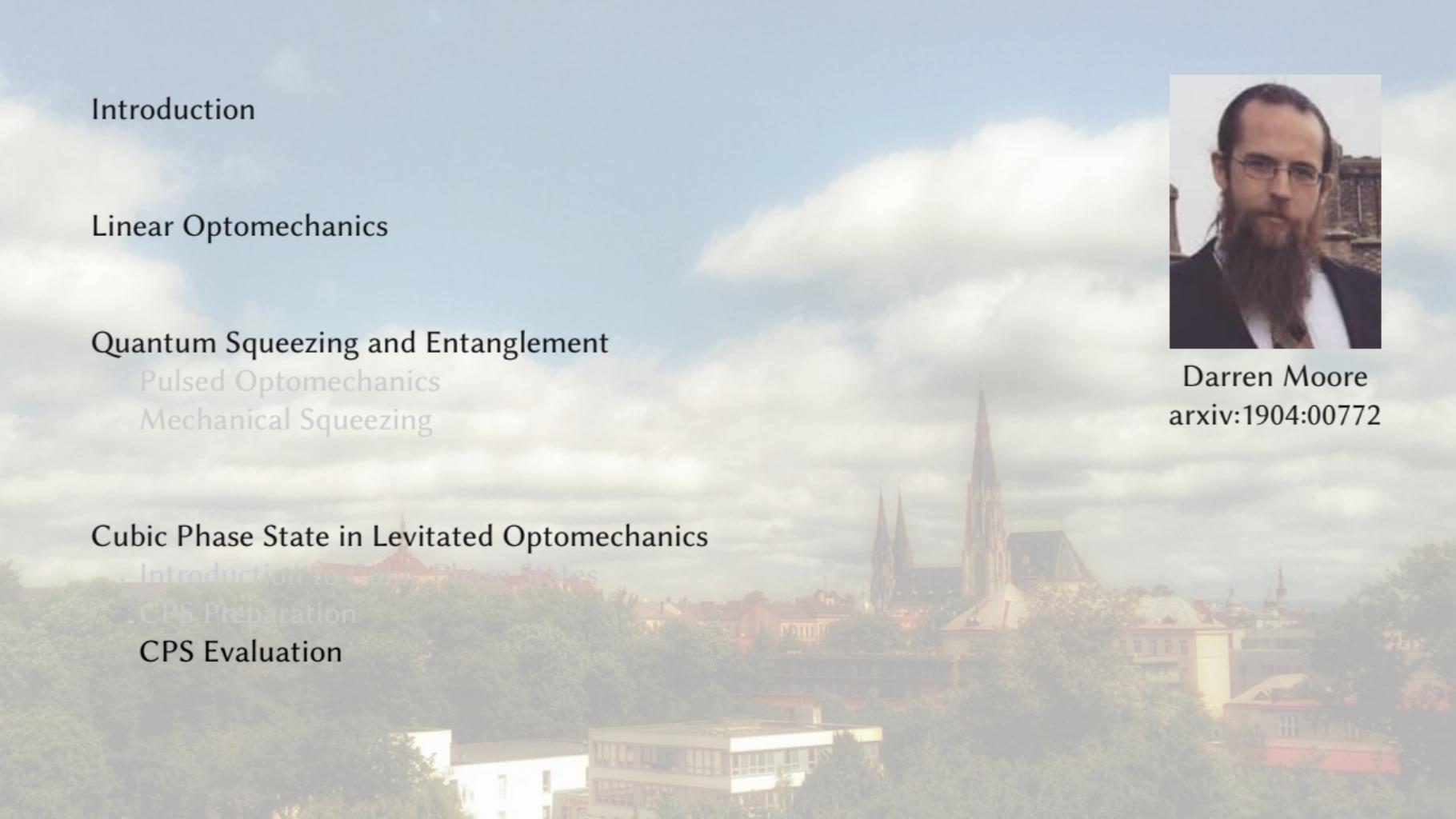
$$W(x, y) \rightarrow \iint d\xi d\eta W(x - \xi, y - \eta) W_{\text{th}}(\xi, \eta).$$

Nonlinear Variance



Wigner Function Cuts





Introduction

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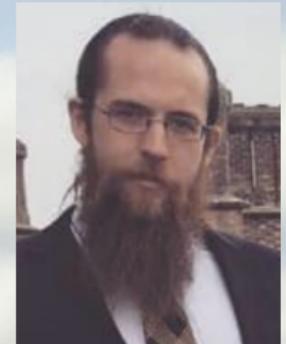
Mechanical Squeezing

Cubic Phase State in Levitated Optomechanics

Introduction to Cubic Phase States

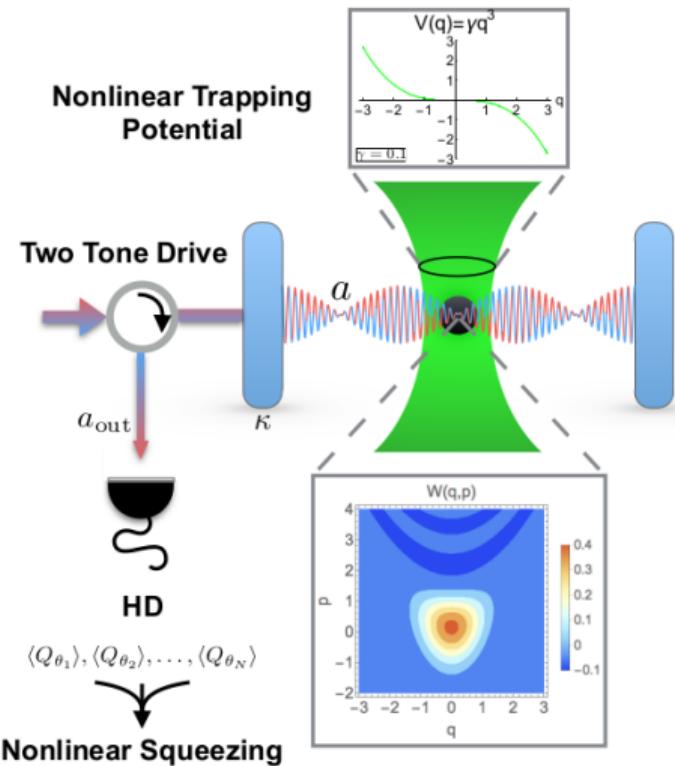
CPS Preparation

CPS Evaluation



Darren Moore
arxiv:1904:00772

The Model



Approximate cubic phase state in mechanics

$$e^{i\gamma q^3} |p=0\rangle.$$

Pulsed QND interaction

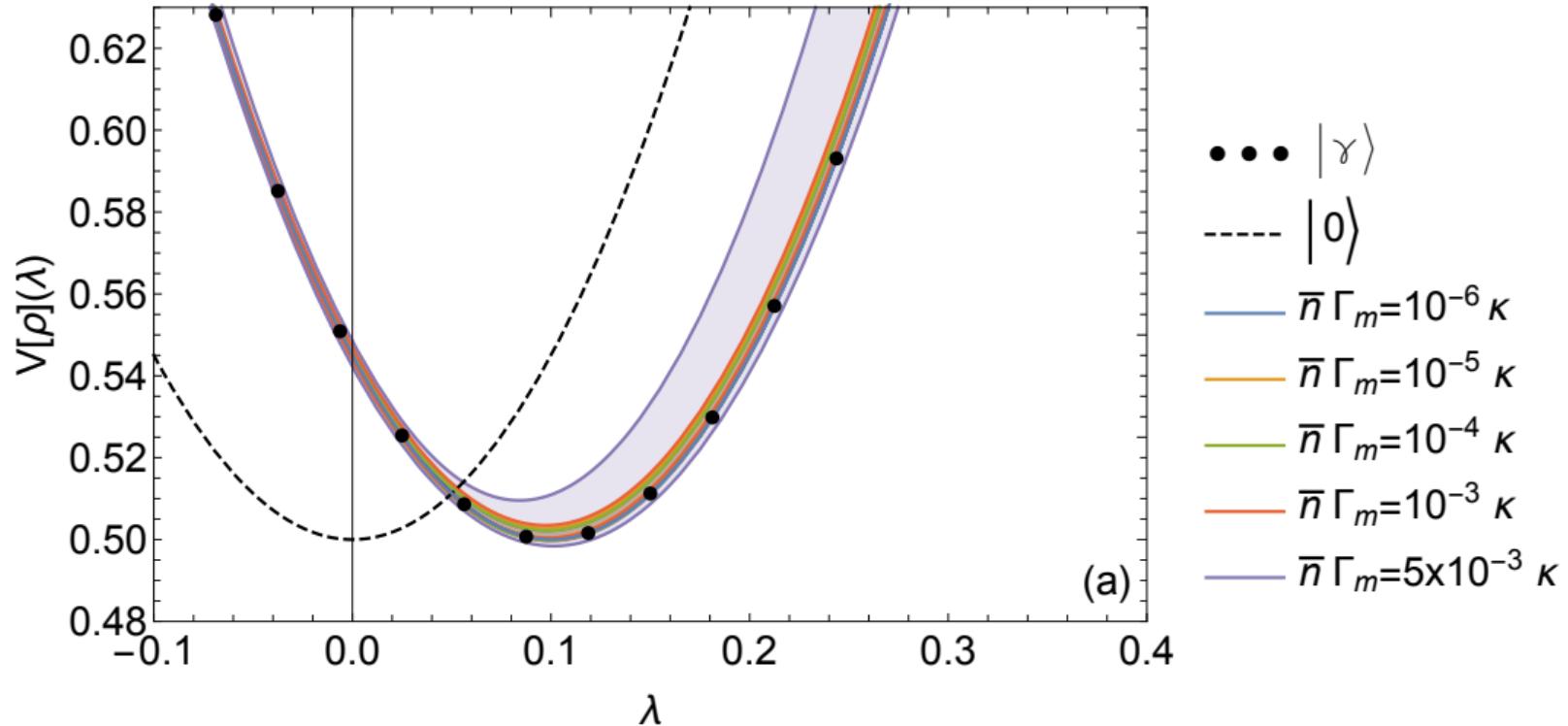
$$H_{int} \propto x_{light}(q \cos \phi + p \sin \phi).$$

Detect leaking light

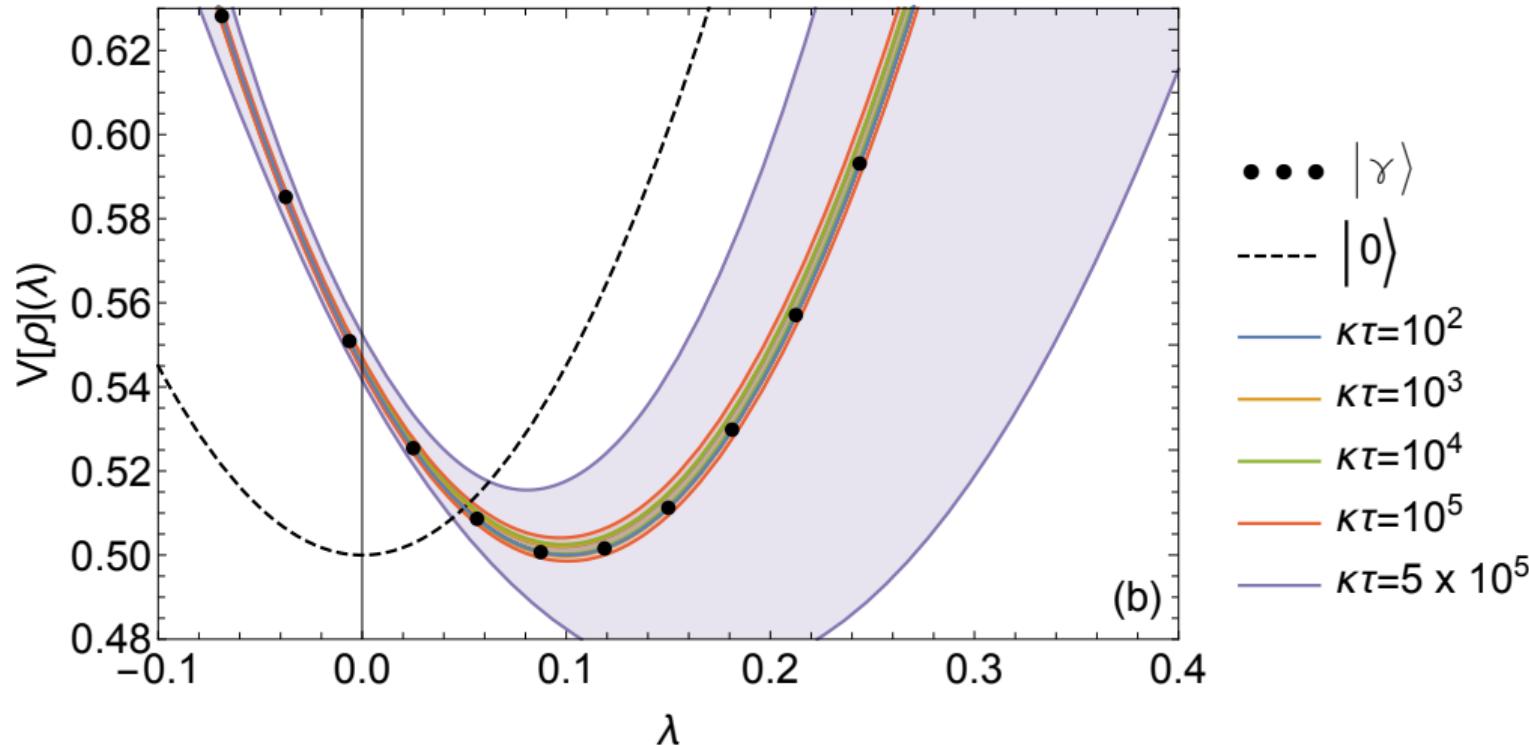
Estimate nonlinear variance

$$q_{NL} = p - \lambda x^2 \Rightarrow \text{Var}[q_{NL}]$$

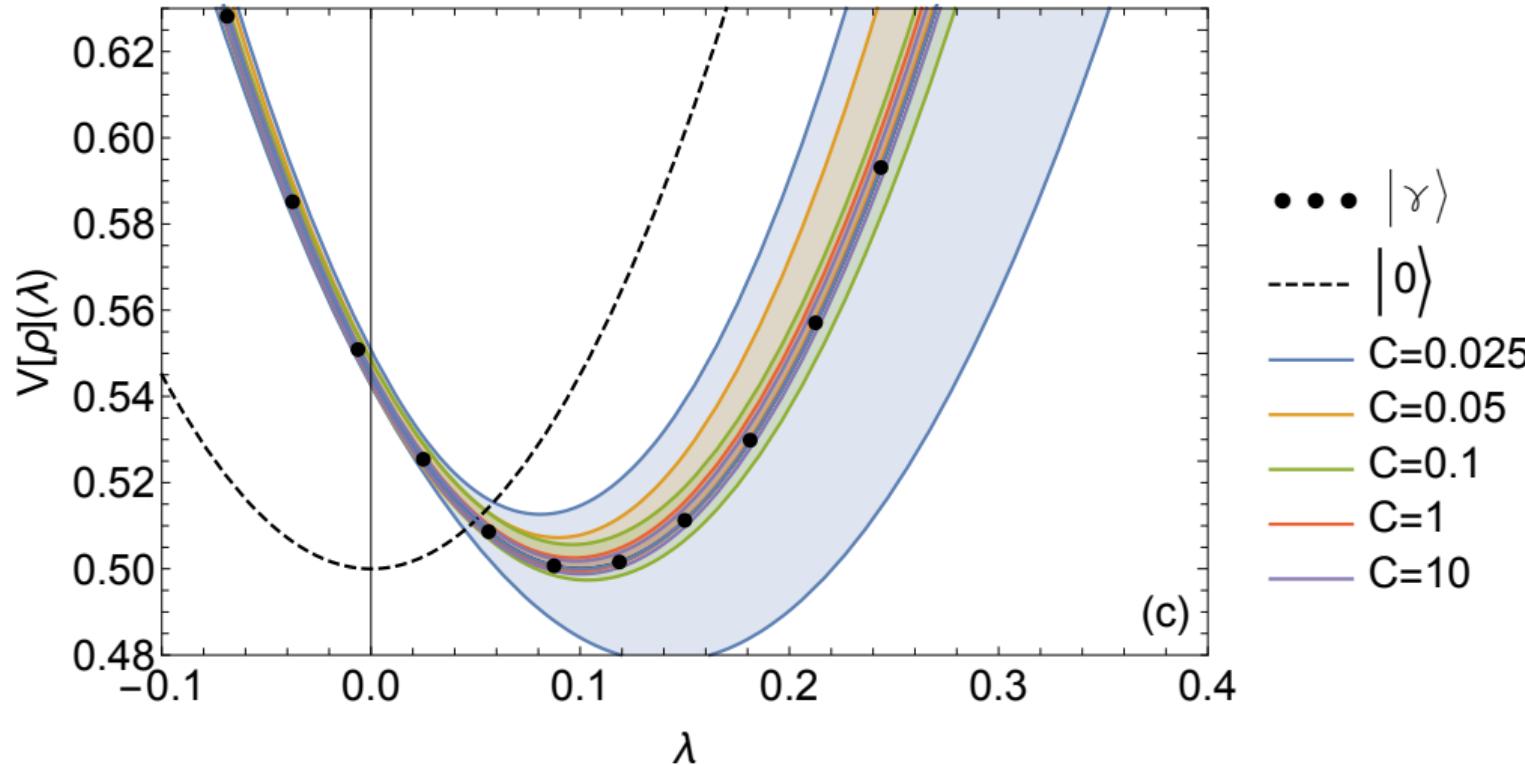
$$\text{Evaluation } V[\rho](\lambda) = \text{Tr}(\rho[\Delta(p - \lambda x^2)]^2)$$



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Conclusion

- ★ Levitated optomechanics allows production of mechanical squeezed states in the linearized blue-detuned regime
- ★ Optomechanical entanglement is possible and can be witnessed
- ★ Approximate Cubic Phase State can be prepared and verified with optomechanics

Thank You!

These slides: <http://bit.ly/ar-minsk-2019>

Phd positions available