

Mathematics -2

1. LCM & GCD

- a. <https://www.geeksforgeeks.org/program-to-find-lcm-of-two-numbers/>
- b. <https://www.geeksforgeeks.org/steins-algorithm-for-finding-gcd/>

2. Permutation & Combination

- a. <https://www.geeksforgeeks.org/permutation-and-combination/>
- b. <https://www.tutorialspoint.com/permutation-and-combination-in-java>

3. Modular Arithmetic

a. Formulae:-

- i. $(a + b) \bmod M = ((a \bmod M) + (b \bmod M)) \bmod M$
- ii. $(a - b) \bmod M = ((a \bmod M) - (b \bmod M)) \bmod M$
- iii. $(a * b) \bmod M = ((a \bmod M) * (b \bmod M)) \bmod M$

- b. <https://www.hackerearth.com/practice/math/number-theory/basic-number-theory-1/tutorial/>

- c. <https://www.geeksforgeeks.org/modular-arithmetic/#:~:text=Modular%20Arithmetic,multiplication%2C%20division%20or%20any%20other.>

- d. The above three expressions are valid and can be performed as stated. But when it comes to modular division, there are some limitations. There isn't any formula to calculate: $(a / b) \bmod M$, Hence we have Modular Inverse.

4. Modular Inverse

- a. The modular inverse is an integer 'x' such that.
 - i. $a x \equiv 1 \pmod{M}$
- b. The value of x should be in $\{0, 1, 2, \dots, M-1\}$, i.e., in the ring of integer modulo M.
- c. The multiplicative inverse of "a modulo M" exists if and only if a and M are relatively prime (i.e., if $\gcd(a, M) = 1$).

Examples:

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Input:  a = 3, M = 11
Output: 4
Since (4*3) mod 11 = 1, 4 is modulo inverse of 3
One might think, 15 also as a valid output as "(15*3) mod 11"
is also 1, but 15 is not in ring {0, 1, 2, ..., 10}, so not
valid.

Input:  a = 10, M = 17
Output: 12
Since (10*12) mod 17 = 1, 12 is modulo inverse of 3
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- d. Euclidean algorithms : -<https://www.geeksforgeeks.org/euclidean-algorithms-basic-and-extended/>
 - e. Fermat Little Theorem :- <https://www.geeksforgeeks.org/fermats-little-theorem/>
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Sample Problems to Solve:-

1. <https://www.codechef.com/problems/FLOW016>
2. <https://www.hackerrank.com/challenges/picking-cards/problem>
3. <https://www.codechef.com/problems/IITK2P10>