

```

1 /**
2 adding a ? to a: array?<int> means that a can be null.
3 */
4 method {:verify false} searchArray(a: array<int>, key: int) returns (found: bool, i:
nat)
5 // requires a≠null such a precondition is no longer needed in our version of Dagny
6 ensures key in a[..]  $\iff$  found //a[..] is a as a sequence of integers. operator "in"
is only on sequence
7 ensures found  $\implies$  i < a.Length && a[i] = key
8 {
9     i := a.Length;
10    if a.Length = 0
11    {
12        found := false; //found and i are originally initialized with "garbage" value.
because we didn't specify i's value if found is false
13        // so we don't need to initialize i.
14    }
15    else
16    {
17        i,found := a.Length, false;
18        while Guard(a,key,found,i)
19            invariant Inv(a[..],key,found,i)
20            decreases i
21            {
22                ProofOfLoopBody(a,key,found,i);
23                i,found := i -1,UpdateFound(a,key,found,i);
24            }
25        StrengthenPostcondition(a[..],key,found,i);
26    }
27 }
28 predicate method UpdateFound (a: array<int>,key: int, found: bool, i: nat)
29 {
30
31 }
32
33
34 lemma {:verify true} StrengthenPostcondition (a: array<int>, key: int, found: bool, i:
nat)
35     requires Inv(a[..],key,found,i) //sometimes order of preconds is important
36     requires !Guard(a,key,found,i)
37     ensures key in a[..]  $\iff$  found
38     ensures found  $\implies$  i < a.Length && a[i] = key
39     {
40         //all this is probably not really needed, it was for our own convincing of the
design - guard/inv.
41         assert key in a[..]  $\iff$  found by {
42             assert key in a[i..]  $\iff$  found; // from invraiant
43             assert found || i = 0; // the negation of the guard
44             if i = 0
45             {
46                 assert a[i..] = a[0..] = a[..];
47                 assert key in a[..]  $\iff$  key in a[i..];

```

```

48     }
49     else
50     {
51         assert found;
52         assert key in a[..] by {
53             assert key in a[i..]; //from Inv (when found is true)
54             assert forall k :: k in a[i..] => k in a[i..];
55         }
56     }
57 }
58 }
59 assert found => i < a.Length && a[i] = key by {
60     if found
61     {
62         assert i < a.Length && a[i] = key; //from Inv when found is true
63     }
64     else
65     {
66         assert false => i < a.Length && a[i] = key; // false implies
everything
67     }
68 }
69 }
70 }
71
72 predicate method Guard(a: array<int>, key: int, found: bool, i: nat)
73 {
74     // !found && i ≥ 0 this guard is problematic since if the key isn't in the array, we
then do i = i-1 in the loop body and this is a type error
75     //since i is a natural number. so the guard isn't sufficient.
76     !found && i > 0
77 }
78 // not a method since it's called in specification (invariant of the loop).
79
80 predicate Inv(q: seq<int>, key: int, found: bool, i: nat)
81 {
82     |q| > 0 && i ≤ |q| &&
83     (key in q[i..] <=> found) && (found => i < |q| && q[i] = key)
84
85 }

```