

Task 3: kakuroDecode (5 %)

Write a Prolog predicate `kakuroDecode(Map,Solution)` with mode `kakuroDecode(+,-)`, which decodes the Map of variables generated by `kakuroEncode/3` to a Kakuro solution.

Task 4: kakuroSolve (10 %)

Write a Prolog predicate `kakuroSolve(Instance,Solution)`, with mode `kakuroSolve(+,-)` that takes a Kakuro instance, solves it using BEE. When solving you must encode the instance to BEE constraints, decode the solution and verify it. We recommend you use the BEE framework to implement `kakuroSolve`

Killer Sudoku with BEE

A *Killer Sudoku* is a 9×9 Sudoku puzzle. In this type of puzzle one must fill the values of cells according to the following constraints

1. Each row, column and box consist of all-different values (between 1 and 9).
2. Any two cells separated by a Knight's move (the chess-piece) must be different.
3. Any two cells separated by a King's move (the chess-piece) must be different.
4. The values of any two cells which appear next to each other in a row, or column must have absolute difference of at least 2.

For example, the following are a Killer Sudoku puzzle and its solution.

[_, _, _, _, _, _, _, _, _],	[4, 8, 3, 7, 2, 6, 1, 5, 9],
[_, _, _, _, _, _, _, _, _],	[7, 2, 6, 1, 5, 9, 4, 8, 3],
[_, _, _, _, _, _, _, _, _],	[1, 5, 9, 4, 8, 3, 7, 2, 6],
[_, _, _, _, 6, _, _, _, _],	[8, 3, 7, 2, 6, 1, 5, 9, 4],
[_, _, 1, _, _, _, _, _, _],	[2, 6, 1, 5, 9, 4, 8, 3, 7],
[_, _, _, _, _, _, 2, _, _],	[5, 9, 4, 8, 3, 7, 2, 6, 1],
[_, _, _, _, _, _, _, _, 8],	[3, 7, 2, 6, 1, 5, 9, 4, 8],
[_, _, _, _, _, _, _, _, _],	[6, 1, 5, 9, 4, 8, 3, 7, 2],
[_, _, _, _, _, _, _, _, _]	[9, 4, 8, 3, 7, 2, 6, 1, 5]

A Killer Sudoku puzzle is represented by a list of assignment constraints (hints). The above puzzle is represented by the term:

```
Instance = killer([cell(5,3) = 1, cell(6,7) = 2, cell(4,5) = 6, cell(7,9) = 8])
```

A solution is represented as a list of assignment constraints:

```
Solution = [cell(1,1) = 4, cell(1,2) = 8, cell(1,3) = 3, ..., cell(9,9) = 5]
```

Notice that (like a normal Sudoku puzzle) a Killer Sudoku puzzle is *legal* only in case it has exactly one solution.

Task 5: Killer Sudoku Verifier (10%)

Write a Prolog predicate `verify_killer(Instance, Solution)` with mode `verify_killer(+, +)` which succeeds if and only if its second argument `Solution` represents a legal Killer Sudoku solution for the instance `Instance` in its first argument. Otherwise, `verify_killer` should fail. The instance is represented as a term `Instance=killer(Hints)` where `Hints` is a list of assignment constraints (hints) and the solution is represented as a list with 81 assignment constraints, one for each cell of the 9×9 board. This predicate does not verify the uniqueness of the `Solution`, only that it assigns valid values to the `Instance` cells. This predicate must also be deterministic. In this task you should assume that the given `Instance` is a legal Killer Sudoku instance. For example,

```
?- Instance = killer([cell(5,3) = 1, cell(6,7) = 2, cell(4,5) = 6, cell(7,9) = 8]),
   Solution = [cell(1,1) = 4, cell(1,2) = 8, ..., cell(9,9) = 5], % full solution above
   verify_killer(Instance, Solution).
true.

?- Instance = killer([cell(5,3) = 1, cell(6,7) = 2, cell(4,5) = 6, cell(7,9) = 8]),
   Solution = [cell(1,1) = 8, ..., cell(2,3) = 8, ...],
   verify_killer(Instance, Solution).
false.

?- Instance = killer([cell(5,3) = 1, cell(6,7) = 2, cell(4,5) = 6, cell(7,9) = 8]),
   Solution = [cell(1,1) = 8, ..., cell(2,1) = 9, ...],
   verify_killer(Instance, Solution).
false.
```

Task 6: Killer Sudoku Encoder (20%)

Write a Prolog predicate `encode_killer(Instance, Map, Constraints)` with mode `encode_killer(+, -, -)` which given a Killer Sudoku instance which is represented by a list of hints (assignment constraints) `Instance = killer(Hints)` unifies `Map` with a representation of the instance as a list of 81 terms of the form `cell(I,J) = Value`, where `I` and `J` are Prolog integers representing the index of the cell, and `Value` represents a BEE integer between 1 and 9 encoded in `Constraints`. A call to the predicate instantiates `Constraints` with a set of BEE constraints such that the satisfying assignments for `Constraints` correspond to solutions of the Killer Sudoku instance `Instance` and bind the variables in `Map` to represent the corresponding integer values. In this task you should assume that the given `Instance` is a legal Killer Sudoku instance.

Task 7: Killer Sudoku Decoder (10%)

Consider the following predicate to solve Killer Sudoku puzzles using a sat solver.

```
solve_killer(Instance, Solution) :-
    runExpr(Instance, Map, encode_killer, decode_killer, verify_killer).
```

The call to `runExpr/5` should succeed and bind the variables in `Map` to a representation of integer values (using the representation of BEE).

Write the predicate `decode_killer(Map,Solution)` with mode `decode_killer(+, -)` which creates from the given `Map` a corresponding solution in the format which is a list of (81) assignment constraints.

Task 8: Legal Killer Sudoku Instance (10%)

Write a Prolog predicate `all_killer(Instance, Solutions)` with mode `all_killer(+, -)` which given an instance of a Killer Sudoku puzzle unifies `Solutions` with a list of all possible solutions to `Instance`. This predicate must be deterministic. If `Instance` is a legal Killer Sudoku instance then `Solutions` will contain exactly one solution.

Grading & Procedures

After Solving :

When grading your work, an emphasis will be given on code efficiency and readability. We appreciate effective code writing. The easier it is to read your code — the more we appreciate it! Even if you submit a partial answer. So please indent your code, add good comments.

Procedure

Submit a single file called `ex3.pl` with the assignment's solution. Please include a header with following statement:

```
/* I, Name (ID number) assert that the work I submitted is entirely my
own. I have not received any part from any other student in the class (or other
source), nor did I give parts of it for use to others. I have clearly marked in
the comments of my program any code taken from an external source. */
```

Submission is solo, i.e., you may *not* work in pairs. If you take any parts of your solution from an external source you must acknowledge this source in the comments. Please note that we test your work using a Linux installed SWI-Prolog (as in the CS Labs) – so please make sure your assignment runs on such a configuration.