

Advance DSA: Arrays 1

Q1 Given an integer array of size N.
Find the max. subarray sum.

Amazon
Microsoft
ZoomCar

Eg: A: { 1, -4, 5, 7, 11, 13, -5 }
Ans = 36

Soln 1) Brute force

⇒ For every subarray, calculate the sum & take max.

Code

```
int ans = INT_MIN;
```

```
for (i=0; i<N; i++) {
```

```
    sum = 0;
```

```
    for (j=i; j<N; j++) {
```

```
        // Subarray from i to j
```

$O(N) \leftarrow$ Iterate from i to j

2) Prefix Sum \Rightarrow T.C. = $O(1)$
S.C. = $O(N)$

3) Carry forward $\Rightarrow O(1)$

```
    sum = sum + A[j];
```

```
    ans = max(ans, sum);
```

```
}
```

```
}
```

T.C. = $O(N^2)$

↓

$O(N) ???$

2) Optimise ??

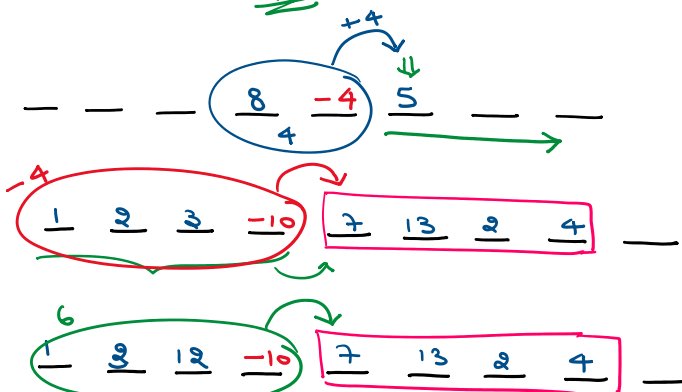
Q What will be the max subarray sum if:

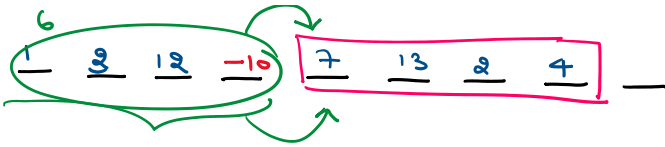
1) All elements are +ve ??
⇒ All elements.

2) All elements are -ve

A = { -3, -1, -5, -7, -20, -6 }

Ans





ans = INT_MIN

Kadane's Algorithm. (carry forward)

A: ~~0~~ 5, ~~1~~ 6, ~~2~~ 7, ~~3~~ -3, 2, ~~4~~ -10, ~~5~~ -12, ~~6~~ 7, 8, 12, 21
 Sum: 5, 11, 18, 15, 17, 7, -5, 8, 20, 41
 ans: 5, 11, 18, 18, 18, 18, 18, 18, 20, 41
 T.C. = $O(N)$
 S.C. = $O(1)$
 Ans

Code

```
ans = INT_MIN;
sum = 0;
for (i=0; i < N; i++) {
    sum = sum + A[i];
    ans = max(ans, sum);
    if (sum < 0) {
        sum = 0;
    }
}
```

Code_2 (Find Subarray)

```
ans = INT_MIN;
start = -1;
end = -1;
sum = 0;
s = 0;
for (e=0; e < N; e++) {
    sum = sum + A[e];
    if (sum > ans) {
        ans = sum;
        start = s;
        end = e;
    }
    if (sum < 0) {
        sum = 0;
        s = e+1;
    }
}
```

41
 ans = ~~7~~ 8 ~~20~~
 start = ~~0~~ 4 4 4
 end = ~~0~~ 4 5 6
 A = ~~0~~ 7, ~~1~~ -3, ~~2~~ -2, -

T.C. = $O(N)$

S.C. = $O(1)$

Beginners Outside Temple (Amazon, MS, Google)

Q Given an Array of size N.
 Initially $\forall i, A[i] = 0;$

$$\begin{array}{r}
 \text{sum} = \cancel{0} \cancel{0} \cancel{2} \cancel{4} \\
 \underline{S = 0}
 \end{array}
 \quad
 \begin{array}{r}
 0 \\
 -15 \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 \begin{array}{c} 3 \\ -10 \end{array} \bigg| \begin{array}{c} \cancel{4} \\ 8 \end{array} \begin{array}{c} 5 \\ 12 \end{array}, \begin{array}{c} 6 \\ 21 \end{array}, \begin{array}{c} 7 \\ -56 \end{array} \bigg| \begin{array}{c} \\ 0 \end{array} \\
 \cancel{0} \quad \cancel{0} \quad \cancel{0} \quad \cancel{0} \quad \cancel{0} \quad 0
 \end{array}
 \quad
 \begin{array}{r}
 S = 8 \\
 \cancel{0}
 \end{array}$$

$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$
 $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$

Initially $\forall i, A[i] = 0;$

Q queries \Rightarrow index, value

Queries		A:	0	1	2	3	4	5	6
			0	0	0	0	0	0	0
				+3	+3	+3	+3	+3	+3
<u>1</u>	<u>3</u>		0	3	3	3	3	3	3
							+2	+2	+2
<u>4</u>	<u>2</u>		0	3	3	3	5	5	5
					+1	+1	+1	+1	+1
<u>2</u>	<u>1</u>		0	3	4	4	6	6	6

Ans

Solⁿ 1) Brute force:

\Rightarrow \forall queries, iterate from index to end & add the value to each element.

Code

int ans[N] = {0};

for (i=0; i<Q; i++) { // O(Q)
 input (index, value);

for (j=index; j<N; j++) {
 ans[j] += value;
}

> Optimise??

return ans;

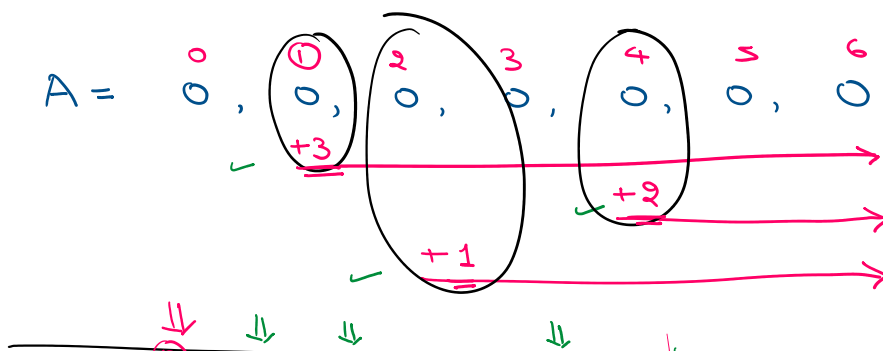
T.C. = $O(N \times Q)$

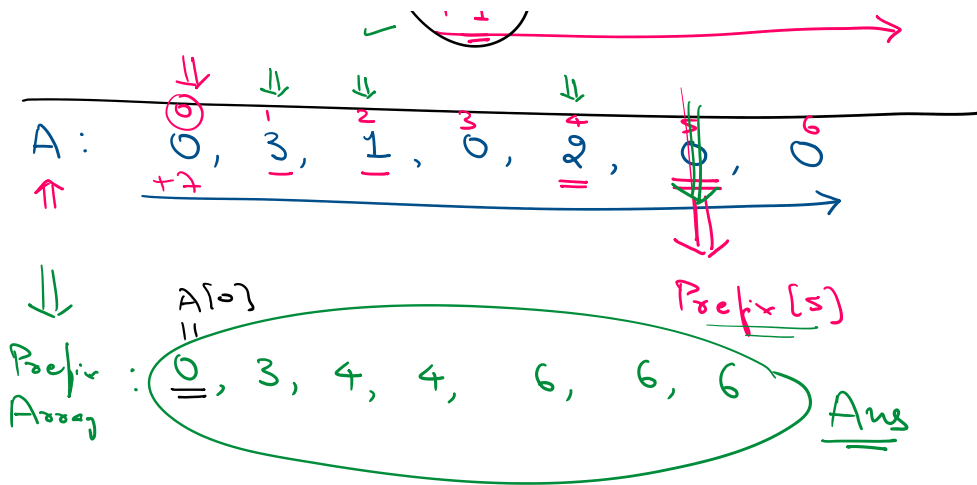
S.C. = $O(1)$

\uparrow (TLE)

$1 \leq N \leq 10^5, 1 \leq Q \leq 10^5$

2) Optimise





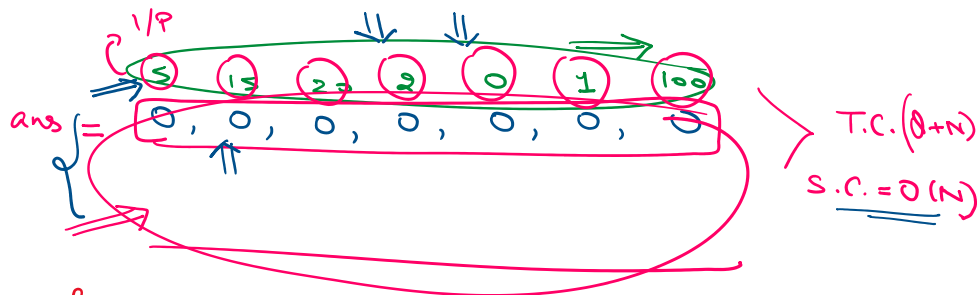
Code

```
int ans[N] = {0};
```

```
for (i=0; i<N; i++) {
    input(index, value);
    ans[index] += value;
}
```

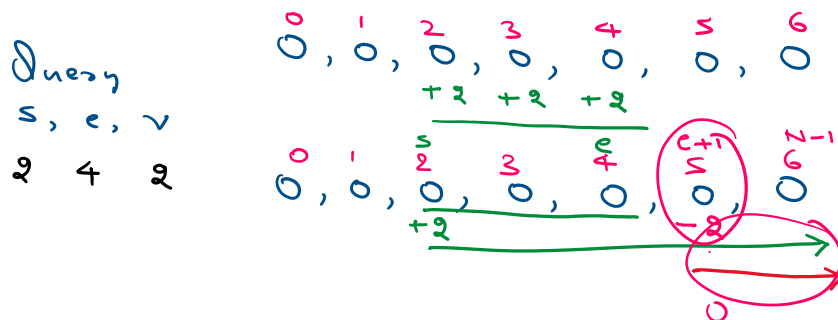
```
for (i=1; i<N; i++) {
    ans[i] = ans[i-1] + ans[i];
}
```

T.C. = $O(N+Q)$
S.C. = $O(1)$



google Variation

Query \Rightarrow start, end, value



Code

```
int ans[N] = {0};
```

```
for (int i=0; i<N; i++) & (10 times)
```

```
    (input(s, e, value));
```

```
    ans[s] += value;
```

```
    if (e < N-1 &
```

```
        ans[e+1] -= value; (if e == (N-1)??)
```

```
}
```

```
for (i=1; i<N; i++) &
```

```
    ans[i] = ans[i-1] + ans[i];
```

```
}
```

Doubt

```
i=0;
```

```
j=31;
```

```
while (i < j) & }
```

```
    swap(A, i, j);
```

```
    i++;
```

```
    j--;
```

```
}
```

```
swap(A, i, j) &
```

int \Rightarrow signed_int

unsigned_int

Implementation

(if $i < n$)

[1, 9A]

$2^5 = 32$

080 = 0

081 = 0

180 = 0

181 = 1

[1, 32]

(if $i < n$)

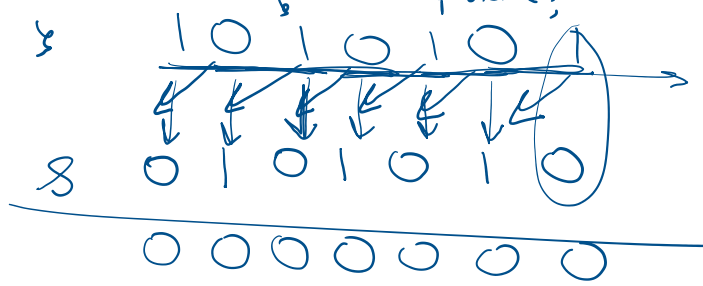
```
for (i=1; i <= 2^A; i++) &
```

```
    if (i & (i-1) == 0) &
```


$i \rightarrow$ for ($i=1$; $i \leq 2^n$; $i++$) {

if ($i \& (i-1) == 0$) {

print i ;



($i \& (i-1)$)

