

1D array $\Rightarrow A[i] \rightarrow$ One index req.

2D array $\Rightarrow A[i][j]$

2 Dimensional array.

	0	1	2	3	4
0					
1			X		
2					
3					
4					

$M[5][5]$

(# of Rows) (# of columns)

$M[1][2]$

\rightarrow Rows
 $\text{int mat}[N][M]$

\rightarrow M cols.

	0	1	2	...	$j^{\text{th}} \text{ col}$		$M-1$
0					$0, j$		
1					$1, j$		
2					$2, j$		
...					...		
$i^{\text{th}} \text{ row}$	$(i, 0)$	$(i, 1)$	$(i, 2)$	$(i, 3)$	(i, j)	$(i, M-1)$	
...					...		
$N-1$					$N-1, j$		

$[0][0]$ $[0][M-1]$ $[N-1][0]$ $[N-1][M-1]$

$\rightarrow \text{mat}[i][j]$

j

Q Iterate on the i th row from left \rightarrow right. ($N \times M$)

Solⁿ

```
for (j = 0; j < M; j++) {  
    print (M[i][j]);  
}
```

Q

Iterate over the entire matrix of size $N \times M$

row by row (Top to Bottom)
(left to right)

Code

```
for (i = 0; i < N; i++) {
```

```
    for (j = 0; j < M; j++) {
```

```
        print (M[i][j]);
```

```
    }
```

```
}
```

S.C. = $O(1)$

T.C. = $O(N \times M)$

Q Iterate over the matrix ($N \times M$)
from top to Bottom
left to right

Q Print the row wise sum of the entire matrix.

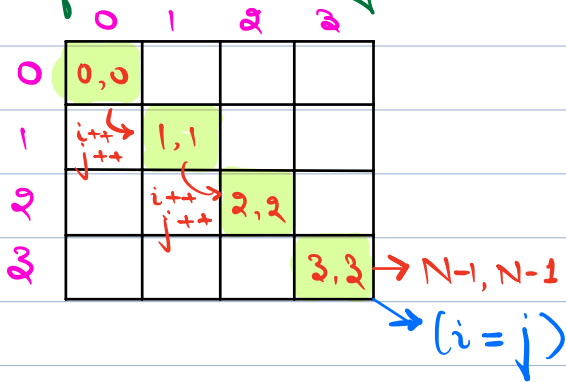
Solⁿ Code

```
for (i=0; i<N; i++) {  
    sum = 0;  
    for (j=0; j<M; j++) {  
        sum += M[i][j];  
    }  
    print (sum);  
}
```

T.C. = $O(N \times M)$

Q Given a square matrix $M[N][N]$
Print the diagonal.

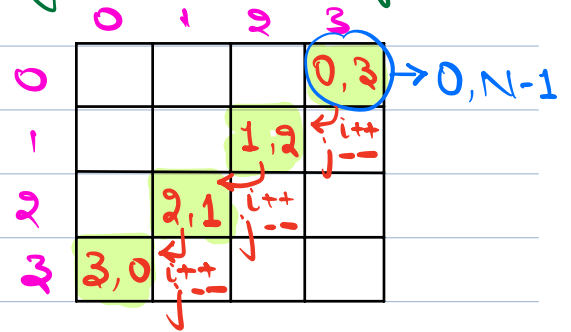
Left to Right



$i = 0, j = 0;$

```
while (i < N && j < N) {
    print (M[i][j]);
    i++;
    j++;
}
```

Right to Left



$i = 0, j = N - 1;$

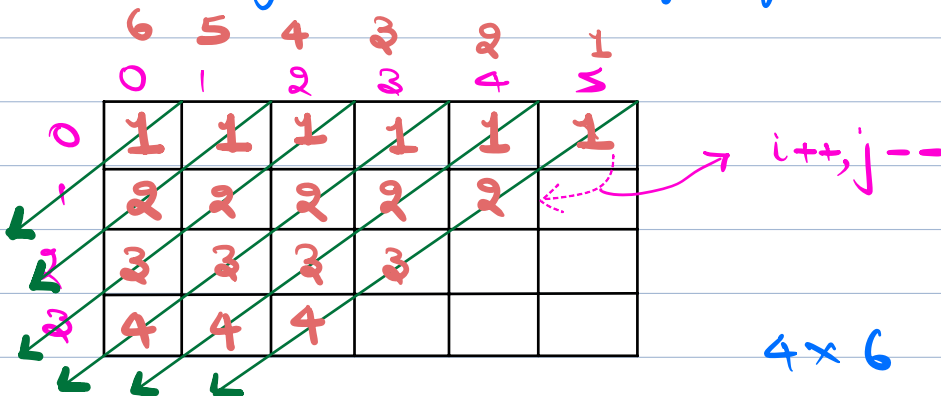
```
while (i < N && j >= 0) {
    print (M[i][j]);
    i++;
    j--;
}
```

T.C. = $O(N)$



Given a matrix of size $N \times M$
Print all diagonals ($R \rightarrow L$)

Diagonals starting from row 0.



4x6

Code

i, j

```
for (col = M-1; col >= 0; col--) {
```

```
    i = 0, j = col;
```

```
    while ((i < N) && (j >= 0)) {
```

```
        print (M[i][j]);
```

```
        i++;
```

```
        j--;
```

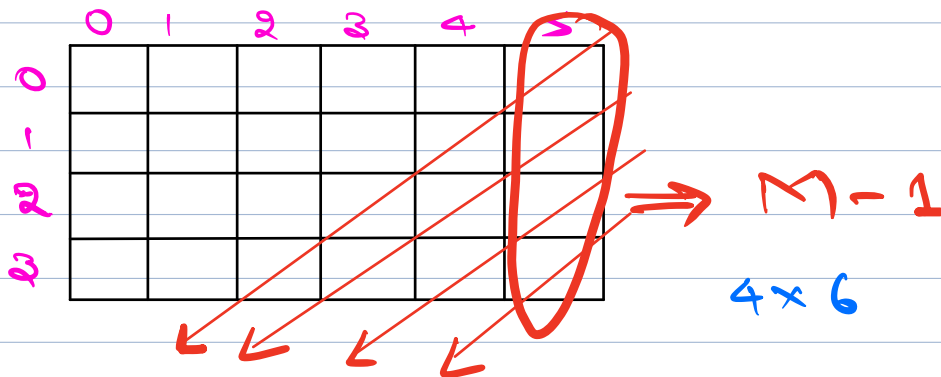
```
    }
```

```
}
```

T.C. = $O(N \times M)$

H.W.

Print diagonals starting on last column



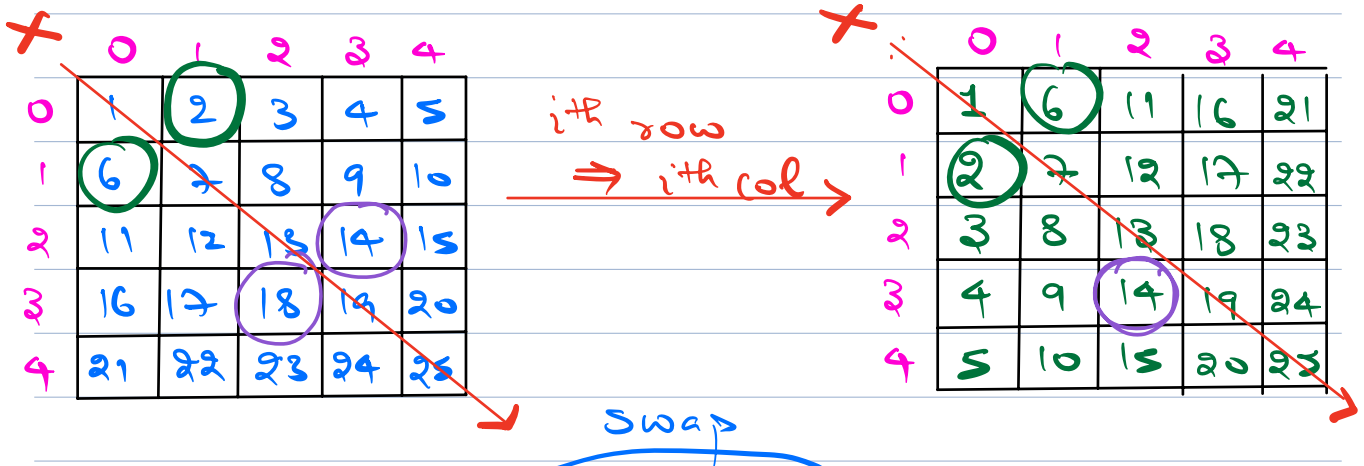
Q
H.W.

Print all diagonals of a square matrix

{ left → Right
Right → Left

Q

Given a square matrix $M[N][N]$
Convert the matrix to its transpose.
S.C. = $O(1)$



$(M[0][1] \rightarrow M[1][0]) \quad (M[1][0] \rightarrow M[0][1])$

$(M[2][3] \rightarrow M[3][2]) \quad (M[3][2] \rightarrow M[2][3])$

swap $(M[i][j] \text{ \& } M[j][i])$.

Code

```
for (i = 0; i < N; i++) {
```

```
    for (j = i+1; j < N; j++) {
```

```
        temp = M[i][j];
```

```
        M[i][j] = M[j][i];
```

```
        M[j][i] = temp;
```

```
    }
```

```
}
```

T.C. = $O(N^2)$

S.C. = $O(1)$

Q Is it possible to convert a rectangular matrix of size $N \times M$ ($N \neq M$) to its transpose w/o using extra space.

Ans

$A[2][5]$

0 $\begin{bmatrix} 1, 2, 3, 4, 5 \end{bmatrix}$
1 $\begin{bmatrix} 6, 7, 8, 9, 10 \end{bmatrix}$

($N \times M$)

2×5



$\begin{bmatrix} 1, 6 \\ 2, 7 \\ 3, 8 \\ 4, 9 \\ 5, 10 \end{bmatrix}$
($M \times N$) 5×2

H.W. Try to fill the new Transpose matrix.

Given a matrix of size $N \times M$
 Rotate the matrix 90° clockwise
 from Top-Right corner.
 S.C. = $O(1)$

	0	1	2	3	4			0	1	2	3	4
0	1	2	3	4	5	$R0 \rightarrow C4$	0	21	16	11	6	1
1	6	7	8	9	10	$R1 \rightarrow C3$	1	22	17	12	7	2
2	11	12	13	14	15	$R2 \rightarrow C2$	2	23	18	13	8	3
3	16	17	18	19	20	$R3 \rightarrow C1$	3	24	19	14	9	4
4	21	22	23	24	25	$R4 \rightarrow C0$	4	25	20	15	10	5

Transpose

0	1	2	3	4
2	7	12	17	22

Reverse even row

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

90° Rotated Matrix = Transpose + Reverse Each Row.

\downarrow

$O(N^2)$

\downarrow

$O(N^2)$

$$T.C. = O(N^2)$$

$$S.C. = O(1)$$

Q Is it possible to rotate a rectangular matrix in const space

$$\begin{bmatrix} 1, & 2, & 3 \\ 4, & 5, & 6 \end{bmatrix} \longrightarrow \begin{bmatrix} 4, & 1 \\ 5, & 2 \\ 6, & 3 \end{bmatrix}$$

Not poss. since dimensions change.

ArrayList < ArrayList < > >

vector <vector<>>

list <list<>>

Dynamic Array is

↑
language of your
choice.