Task 3: Histogram Equalization

Given the following 5x5 image, apply histogram equalization to it.

```
[5,3,1,0,1,0,2,1,0,5,1,5,0,1,2,4,2,6,2,1,6,2,0,1,5]
```

Solution

Step 1: Define the image

```
In [1]: import numpy as np

imgArr = np.array([5,3,1,0,1,0,2,1,0,5,1,5,0,1,2,4,2,6,2,1,6,2,0,1,5])
imgArr = imgArr.reshape(5,5)

maxVal = np.max(imgArr)

print(f'Image Bits: \n{imgArr}')
print(f'Image Shape: {imgArr.shape}')
print(f'Max Value: {maxVal}')

Image Bits:
[[5 3 1 0 1]
    [0 2 1 0 5]
    [1 5 0 1 2]
    [4 2 6 2 1]
    [6 2 0 1 5]]
Image Shape: (5, 5)
Max Value: 6
```

Step 2: Find Histogram and Cumulative Distribution Function (CDF)

From the above, we can see that the maximum value of this image is $\bf 6$. So, our histogram will have a size of $\bf 8$ (0 to 7 / 2^3)

```
In [2]: hist, _ = np.histogram(imgArr, bins=8, range=(0,7))
    prob = hist / imgArr.size

    cdf = np.cumsum(prob)

    print(f'Histogram: {hist}')
    print(f'Probability of each intensity: {prob}')
    print(f'CDF: {cdf}')

Histogram: [5 7 5 1 1 4 2 0]
    Probability of each intensity: [0.2 0.28 0.2 0.04 0.04 0.16 0.08 0. ]
    CDF: [0.2 0.48 0.68 0.72 0.76 0.92 1. 1. ]
```

Step 3: Find the Transfer Function

After finding the CDF, we will find the transfer function by multiplying each value of CDF with the maximum value of the image (6).

```
In [3]: S = np.floor(maxVal * cdf).astype(int)
    print(f'Transfer Function: {S}')

Transfer Function: [1 2 4 4 4 5 6 6]
```

Step 4: Apply the Transfer Function

```
In [4]: newimg = S[imgArr]
    print(f'Original Image: \n{imgArr}')
    print(f'New Image: \n{newimg}')

Original Image:
    [[5 3 1 0 1]
    [0 2 1 0 5]
    [1 5 0 1 2]
    [4 2 6 2 1]
    [6 2 0 1 5]]
    New Image:
    [[5 4 2 1 2]
    [1 4 2 1 5]
    [2 5 1 2 4]
    [4 4 6 4 2]
    [6 4 1 2 5]]
```