Questions and Exercises to work out and turn in:

Grading Guidelines:

* A right answer will get full credit when:

1. It is right (worth 25%)
2. It is right **AND** neatly presented making it easy and pleasant to read. (worth an **extra** 15%)
3. There is an **obvious and clear link** between 1) the information provided in the exercise and in class and 2) the final answer. A clear link is built by properly writing, justifying, and documenting an answer (worth an **extra** 60%).
4. Calculation mistakes will be minimally penalized (2 to 5% of full credit) while errors on units will be more heavily penalized.

You are welcome/encouraged to discuss exercises with other students or the instructor. But, ultimately, **personal** writing is expected.

* USE THIS FILE AS THE STARTING DOCUMENT YOU WILL TURN IN. **DO NOT DELETE ANYTHING FROM THIS FILE:** JUST **INSERT** YOUR ANSWERS.
* IF USING HAND WRITING (STRONGLY DISCOURAGED), **USE THIS FILE** BY CREATING SUFFICIENT SPACE AND WRITE IN YOUR ANSWERS.
* FAILING TO FOLLOW TURN IN DIRECTIONS /GUIDELINES WILL COST **A 30% PENALTY.**

Objectives of this assignment:

* to use and manipulate the concepts presented in this module
* to propose and write algorithms in pseudocode
* to analyze the time complexity of algorithms
* to analyze the space complexity of algorithms
* to learn autonomously new concepts

What you need to do:

Answer the questions and/or solve the exercises described below.

Questions (20 points):

The objective is to compare two data structures: a min-heap and a binary search tree*.* Determine the time complexity for *Search, Minimum, Maximum, Successor, Predecessor, Insert, and Delete* on a min-heap and a binary search tree, respectively. Use a table to present and to compare their time complexities. You do not need to show how you get/determine the time complexities. Just refer your sources.

|  |  |  |
| --- | --- | --- |
|  | Min-heap | Binary Search Tree |
| **Search** | **O(n)** | **O(h)** |
| **Minimum** | **O(1)** | **O(h)** |
| **Maximum** | **O(n)** | **O(h)** |
| **Successor** | **O(n)** | **O(h)** |
| **Predecessor** | **O(n)** | **O(h)** |
| **Insert** | **O(h)** | **O(h)** |
| **Delete** | **O(h)** | **O(h)** |

**https://stackoverflow.com/questions/6147242/heap-vs-binary-search-tree-bst#:~:text=Heap%20just%20guarantees%20that%20elements,sorted%20elements%2C%20go%20with%20BST.&text=Heap%20is%20better%20at%20findMin,(%20O(logN)%20).**

Exercise 1 (10 points)

Suppose that we have numbers between 1 and 1000 in a binary search tree, and we want to search for the number 393. Which of the following sequences could not be the sequence of nodes examined?

a. 32, 282, 431, 428, 360, 374, 427, 393.

b. 954, 250, 941, 274, 928, 288, 392, 393.

c. 955, 232, 941, 270, 942, 275, 393.

d. 32, 429, 417, 249, 296, 412, 411, 308, 393.

e. 965, 308, 377, 651, 329, 422, 388, 393.

C. cannot be the sequence of nodes examined. This is because of the property of binary search trees that all nodes on the left of a given node have a key less than that node. In this sequence, however, after 941 is visited, 270 is visited, meaning the left child of 941 was chosen. The right child of 270 is 942, but 942 > 941, which breaks the rule that all nodes in the left subtree must be less than the given node. Thus, c. cannot be the sequence of nodes examined.

Exercise 2 (35 points) A Recursive TREE-MAXIMUM(x)

1. Write a **recursive** version of TREE-MAXIMUM(s).
2. Analyze the **time** complexity of recursive version and compare it with the **iterative** version’s.
3. Analyze the **space** complexity of recursive version and compare it with the **iterative** version’s.

Exercise 3 (35 points) TREE-PREDECESSOR

1. Write the TREE-PREDECESSOR procedure
2. Analyze its time complexity.
3. Analyze its space complexity.

What you need to turn in:

* Electronic copy of this file (including your answers) (standalone). Submit the file as a Microsoft Word or PDF file.
* Recall that answers must be well written, documented, justified, and presented to get full credit.
* How this assignment will be graded:
* A right answer will get full credit when:
* It is right (worth 25%)
* It is right AND neatly presented making it easy and pleasant to read. (worth 15%)
* There is an obvious and clear link between 1) the information provided in the exercise and in class and 2) the final answer. A clear link is built by properly writing, justifying, and documenting an answer (worth 60%).
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* You are welcome/encouraged to discuss exercises with other students or the instructor. But, ultimately, personal writing is expected.