Constraint Based Analysis

Question 1. Let edge be the input relation containing all edges in a directed graph. Let the relation path be defined as follows:

```
path(n1, n2) :- edge(n1, n2).
path(n1, n2) :- path(n1, n3), path(n3, n2).
```

a. Is the following Datalog relation path2 equivalent to the above relation path (do they always produce the same output given the same input edge relation)?

```
path2(n1, n2) :- edge(n1, n2).

path2(n1, n2) :- edge(n1, n3), path2(n3, n2).
```

b. Write a Datalog relation \mathbb{R} that outputs each node \mathbb{R} that has at least one incoming edge.

```
R(n) :- ?
```

c. Write a Datalog relation S that outputs each pair of nodes n1, n2 that occur in the same cycle. Your answer may use edge and/or path as necessary.

```
S(n1, n2) := ?
```

Question 2. State two benefits of writing a static analysis in Datalog instead of Java.