Program Slicing

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Slicing: Program Dependent Graphs



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Learning Objectives

- Locate the set of statements that compose a program slice
- Construct a program dependent graph
- Assemble dynamic slices using a program dependency graph



What is Slicing?

 A Slice of variable v at statement s is the set of statements involved in computing the value of v at s. [Mark Weiser, 1982]

```
Control Dep.

Data Dep.
```

```
Slice(i @ 5) = {1 (or START), 3, 4, 5}
```

 A slice is a backwards traversal of the Program Dependence Graph!

```
1. void sumUp(int n) {
2.    int sum = 0;
3.    int i = 1;
4.    while ( i < n ) {
5.         i = i + 1;
6.         sum = sum + i;
7.    }
8.    printf("%d", sum);
9. }
```

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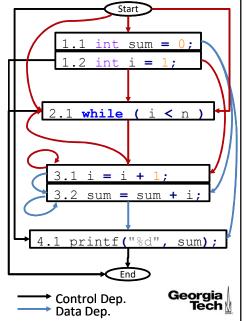
Remember the Program Dependence Graph?

- A program dependence graph PDG = (N, Ed, Ec)
 - A finite set N of nodes which represent statements, possibly within basic blocks "super-nodes"
 - A finite set Ed of edges (i, j) representing that node n_i is data dependent on node n_i
 - A finite set Ec of edges (i, j) representing that (super-)node n_j is control dependent on node n_i

```
Slice(i @ 3.1) =

{START, 1.2, 2.1, 3.1}

void sumUp(int n) {
    int sum = 0;
    int i = 1;
    while ( i < n ) {
        i = i + 1;
        sum = sum + i;
    }
    printf("%d", sum);
}
```



How To Compute A Slice Statically

- Build a PDG = (N, Ed, Ec)
 - A finite set N of nodes which represent statements, possibly within basic blocks "super-nodes"

```
void sumUp(int n) {
   int sum = 0;
   int i = 1;
   while ( i < n ) {
      i = i + 1;
      sum = sum + i;
   }
   printf("%d", sum);
}</pre>
```

```
1.1 int sum = 0;

1.2 int i = 1;

2.1 while (i < n)

3.1 i = i + 1;

3.2 sum = sum + i;

4.1 printf("%d", sum);

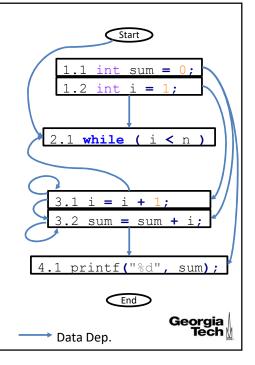
End

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```

5

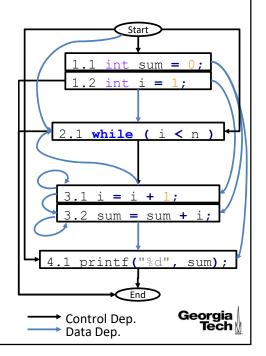
How To Compute A Slice Statically

- Build a PDG = (N, Ed, Ec)
 - A finite set N of nodes which represent statements, possibly within basic blocks "super-nodes"
 - A finite set Ed of edges (i, j) representing that node n_j is data dependent on node n_i
 - Recall: X is data dependent on Y iff
 - 1) There exists a variable v that is defined at Y and used at X
 - There exists a path of nonzero length from Y to X along which v is not re-defined



How To Compute A Slice Statically

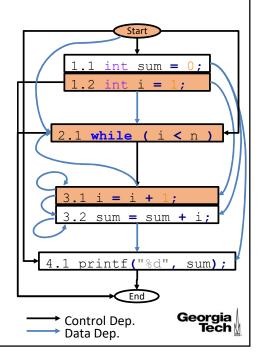
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 - A finite set Ed of edges (i, j) representing that node n_i is data dependent on node n_i
 - A finite set Ec of edges (i, j) representing that (super-)node n_i is control dependent on node n_i
 - Recall: Y is control-dependent on X iff
 X directly determines whether Y executes:
 - 1) X is not strictly post-dominated by Y
 - There exists a path from X to Y s.t. every node in the path other than X and Y is postdominated by Y



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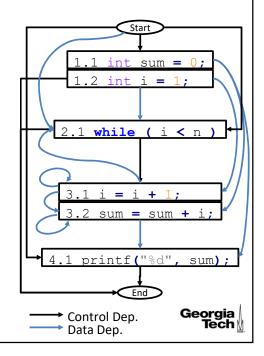
How To Compute A Slice Statically

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- Given a slice criterion, i.e., the starting point, a slice is computed by traversing the set of backward-reachable nodes in the program dependence graph
- Slice (I @ 3.1) = {START, 1.2, 2.1, 3.1}



How To Compute A Slice Statically

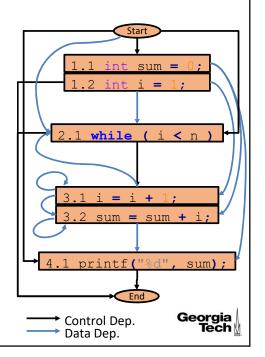
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- Given a slice criterion, i.e., the starting point, a slice is computed by traversing the set of backward-reachable nodes in the program dependence graph
- Slice (sum @ 4.1) = ?



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How To Compute A Slice Statically

- Build a PDG = (N, Ed, Ec)
 - A finite set N of nodes which represents statements, possibly within basic blocks "super-nodes"
 - A finite set Ed of edges (i, j) representing that node n_i is data dependent on node n_i
 - A finite set Ec of edges (i, j) representing that (super-)node n_i is control dependent on node n_i
- Given a slice criterion, i.e., the starting point, a slice is computed by traversing the set of backward-reachable nodes in the program dependence graph
- Slice (sum @ 4.1) = {START, 1.1, 1.2, 2.1, 3.1, 3.2, 4.1}



But I Thought We Were Done With Static Analysis??

- · We are!
- Static slices are extremely imprecise
 - Don't have dynamic control flow information
 - 2. Static alias analysis is very difficult (as you know)
- This makes the underlying Program Dependence Graph very imprecise
- So slicing is generally only performed dynamically

```
if (P)
x=f(...);
x=f(...);
else
x=g(...);
x=x;

x=f(...);
x=
```

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Dynamic Slicing



Static VS. Dynamic slicing Example

```
StaticSlice(sum @ 4.1) = {START, 1.1, 1.2, 2.1, 3.1, 3.2, 4.1}
```

Execution Trace (n = 0)

```
1.1 int sum = 0;

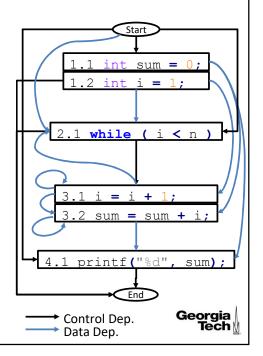
1.2 int i = 1;

2.1 while ( i < n )

4.1 printf("%d", sum);
```

DynamicSlice(sum @ 4.1) = {1.1, 4.1}

- · Much better right?
- Dynamic analysis concretizes many assumptions that restrict static analysis!



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Dynamic Slicing

- Korel and Laski, 1988
- Dynamic slicing makes use of all information about a particular execution of a program
- Dynamic slices are computed by constructing a Dynamic Program Dependence Graph
 - Each node is an **executed statement** (instruction)
 - · An edge is present between two nodes if there exists a data or control dependence
 - · A dynamic slice criterion is a triple <Variable, Execution Point, Input>
- The set of statements reachable in the DPDG from a criterion constitute the slice
- Dynamic slices are smaller, more precise, more helpful to the user (or malware analyst)



Computing Dynamic Slices

- · Data dependence
 - Do we still care about aliasing? No! ☺
 - · A backward linear scan over the trace is able to recover all data dependences
 - · We now only need to compute a dynamic Def/Use chain!
- Control Dependence
 - Recall that we need to find the predicate instance that a statement is control dependent on
 - · Can we simply traverse backwards and find the closest predicate?
 - No! ⊗
 - · Recall our execution trace from before:
 - Is 4.1 control dependent on 2.1? No!
 - We need to define the notion of dynamic control dependence!

```
Execution Trace (n = 0)

1.1 int sum = 0;

1.2 int i = 1;

2.1 while ( i < n )

4.1 printf("%d", sum);
```



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Dynamic Data Dependence



Dynamic Data Dependence

- Instrument the executable to log the Def/Use of each instruction
- At runtime, all memory locations will be resolved

```
.text:00 pow
                       proc near
.text:00
.text:00 var_ReturnVal = dword ptr -1Ch
.text:00 var_Y
                      = dword ptr -18h
.text:00 var_X
                      = dword ptr -14h
.text:00 var_X = dword ptr -1.

.text:00 var_Z = dword ptr -8

.text:00 var_Power = dword ptr -4
.text:00
.text:00 push rbp
                                 printf("00 D: rsp %d, U: rsp rbp", rsp-4)
[rbp+var_Power], eax printf("15 D: %d U: rbp eax", rbp+var_Power)
.text:15 mov
.text:18 jmp
             short loc_20
                                  printf("18 D: U:")
```

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Dynamic Data Dependence

 A backward linear scan over the trace is able to recover all data dependences

```
Trace Output (assume: RSP=0x460020)

00 D: rsp 0x46001c, U: rsp rbp

01 D: rbp, U: rsp

04 D: 0x460008, U: rbp edi

07 D: 0x460004, U: rbp esi

0A D: rflags, U: rbp 0x460004

0E D: U: rflags

10 D: eax, U: rbp 0x460004

13 D: eax, U: eax

15 D: 0x460018 U: rbp eax

18 D: U:

DD(01) = {00}
```

```
.text:00 pow
                        proc near
.text:00
.text:00 var_ReturnVal = dword ptr -1Ch
.text:00 var_Y = dword ptr -18h
                    = dword ptr -14h
.text:00 var_X
.text:00 var_Z
                     = dword ptr -8
.text:00 var_Power = dword ptr -4
.text:00
.text:00 push
                rbp
.text:01 mov
                rbp, rsp
                [rbp+var_X], edi
.text:04 mov
.text:07 mov
                [rbp+var Y], esi
                [rbp+var_Y], 0
.text:0A cmp
.text:OE jns
                short loc 1A
.text:10 mov
                eax, [rbp+var Y]
.text:13 neg
                eax
                [rbp+var_Power], eax
.text:15 mov
.text:18 jmp
                short loc 20
```

DD(07) = ? DD(10) = ? $DD(07) = {START, 01} DD(10) = {01, 07}$



Dynamic Control Dependence (DCD)

- Computing control dependence from only a dynamic trace is challenging
- Linear scan will not work
 - This is because an execution trace has no notion of the "curly bracket" i.e., { }

```
Execution Trace (n = 0)

1.1 int sum = 0;
1.2 int i = 1;
2.1 while (i < n)
4.1 printf("%d", sum);

Execution Trace (n = 0)

1.1 int sum = 0;
1.2 int i = 1;
2.1 while (i < n) {
}
4.1 printf("%d", sum);
```

- Can we just fall back to our previous static control dependence??
 - Maybe ...



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DCD - Offline TRACE Analysis

- 1. Assume there are no recursive functions
- 2. Assume we have already built a dictionary CD(i) = {cdi₁, cdi₂, ... cdi_n} which maps any instruction i to the set of static control dependencies for i, say cdi₁, cdi₂, ... cdi_n
- 3. Collect a dynamic control flow trace
- 4. To find the control dependence of any instruction **j** in that trace: Traverse backward starting from **j** & find the closest **x**, **s.t**. **x** is in **CD(j)**
- **5. j** is therefore dynamically control dependent on **x** (*Cont'd*)



DCD - Offline TRACE Analysis (Cont'd)

- **5. j** is therefore dynamically control dependent on **x**
 - VERY problematic in the presence of recursion
 - Notice that each instruction in the trace can only be dynamically control dependent on a single instruction!
 - Recall that one instruction could be statically control dependent on two!
 - This is because within a concrete trace you can only arrive at that instruction via a single path!



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Are We Done Yet?

- No
- The previously mentioned algorithms are essentially offline graph construction
 - This implies offline traversals of (extremely) long data reference and control flow traces
- · Can we do better?
- Yes
- · Efficient online algorithms:
 - · Online data dependence detection
 - Online control dependence detection
- The output of our dynamic dependence detection tool will only be the dependencies of each instruction and not a full trace



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Dynamic Data Dependence Detection

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Efficient Dynamic Data Dependence Detection

- Full Shadow Registers & Memory
- Basic idea: Store metadata in a structure which models every real data location
- This enables online def/use tracking!
- For each data location that an instruction can define, keep a "shadow" copy to mark the last instruction which defined it
- Implemented **via a dictionary** (or similar data structure) which maps data locations (i.e., registers or memory) to the last instruction which defined them

Efficient Dynamic Data Dependence Detection

- Update shadows before or after instruction executes?
 - E.g., shadow_mem[&[rsp]]="..." vs. shadow_mem[&[rsp]-4]="..."
- · Also, granularity considerations:
 - Shadow each flag? Shadow memory in 1,4,8 bytes?



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```
.text:00 var Y
                                      = dword ptr -18h
Efficient
                .text:00 var_X
                                       = dword ptr -14h
               .text:00 var Z
                                      = dword ptr -8
Dynamic Data
               .text:00 var_Power
                                      = dword ptr -4
Dependence
                .text:00
                               rbp printf("00 DD: %s, %s", shadow_regs[rsp], shadow regs[rbp]);
Detection
                .text:00 push
                                     shadow_regs[rsp]=".text:00"; shadow_mem[&[rsp]]=".text:00";
                .text:01 mov
                               rbp, rsp printf("01 DD: %s", shadow regs[rsp]);
                                         shadow_regs[rbp]=".text:01";
                .text:04 mov
                               [rbp+var_X], edi
                              printf("04 DD: %s, %s", shadow regs[rbp], shadow regs[edi]);
                              shadow_mem[&[rbp+var_X]]=".text:04";
                .text:07 mov
                               [rbp+var_Y], esi
                              printf("07 DD: %s, %s", shadow regs[rbp], shadow regs[esi]);
                              shadow_mem[&[rbp+var_Y]]=".text:07";
                .text:0A cmp
                               [rbp+var_Y],
                              printf("OA DD: %s, %s", shadow_regs[rbp], shadow_mem[&[rbp+var_Y]]);
                              shadow_regs[rflags]=".text:0A";
                .text: OE jns
                               short loc 1A
                                                printf("OE DD: %s", shadow regs[rflags]);
                .text:10 mov
                               eax, [rbp+var Y]
                              printf("10 DD: %s, %s", shadow_regs[rbp], shadow_mem[&[rbp+var_Y]]);
                              shadow regs[eax]=".text:10";
                .text:13 neg
                                         printf("13 DD: %s", shadow_regs[eax]);
                                         shadow_regs[eax]=".text:13";
                              .text:15 mov
                               short loc_20
                .text:18 jmp
```

Efficient Dynamic Data Dependence Detection

- Beware of space constraints!
 - You cannot pre-allocate 4 bytes of metadata for every byte of RAM!
- Implementation tradeoffs are everywhere!
 - · Time vs space, packed vs unpacked data, ...
- Read:
 - Nethercote, N. & Seward, J. (2007). How to shadow every byte of memory used by a program. *Proceedings of the 3rd International Conference on Virtual Execution Environments*. (yes, the valgrind author).
- Shadow data is also used to implement taint tracking
 - **Example**: Mark the initial input as "tainted" (1 bit shadow metadata) & taint everywhere the data flows during execution
 - Application: Can this program leak sensitive data?



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Efficient Dynamic Control Dependence Detection

- We can perform a similar online tracking of dynamic control dependence
- Recall our definition of control dependence:
- Y is control-dependent on X iff
 - 1. X is not strictly post-dominated by Y
 - 2. There exists a path from X to Y s.t. every node in the path other than X and Y is post-dominated by Y
- We can watch for these conditions at runtime & determine control dependence from

the final execution trace

- **Benefits**: 1) **May** not require ahead-of-time static control dependence analysis 2) Does not require logging the huge dynamic control flow trace
- Problems: Not as straightforward as the offline approach



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Dynamic "Regions"

- In order to monitor the execution for our control dependence conditions, we need to introduce the concept of an execution "region"
- Region: The set of executed statements between a predicate instance and its immediate post-dominator
- We can then say that each statement instance x_i is dynamically control dependent on the predicate instance leading x_i's nearest enclosing region
- Thanks to our definition of immediate post-dominated, regions are either nested or disjoint, but can never overlap!
- · Read:
 - Xin, B. & Zhang, X. (2007). Efficient online detection of dynamic control dependence. Proceedings of the 2007 International Symposium on Software Testing and Analysis.
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Region Examples

- Region: The set of executed statements between a predicate instance and its immediate postdominator
- We can then say that each statement instance x_i is dynamically control dependent on the predicate instance leading x_i's nearest enclosing region
- Regions are either nested or disjoint, but can never overlap!

1₁. for (i=0; i<N, i++) 2₁. if (i%2 == 0) 3₁. p = &a[i]; 4₁. foo (p); ... 1₂. for (i=0; i<N, i++) 2₂. if (i%2 == 0) 4₂. foo (p); ... 1₃. for (i=0; i<N, i++) 6₁. a = a+1;

Execution Trace

Program

```
1. for(i=0; i<N, i++) {
2. if(i%2 == 0)
3. p = &a[i];
4. foo(p);
5. }
6. a = a+1;
```

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Every node on this

path must be post-

Then x; is control-

dependent on pi

dominated by x_i

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Regions: Property One

Each statement instance x_i is dynamically control dependent on the predicate instance leading x_i 's nearest enclosing region

- Proof: Let the predicate instance be p_j and assume x_i is not control dependent on p_i
- · Therefore, either:
 - 1. No path exists from p_j to exit which that does not pass through x_i . This would indicate that x_i is a post-dominator of p_j , contradicting the condition that x_i is in the region delimited by p_j and its immediate post-dominator; OR

p_i is **not** strictly

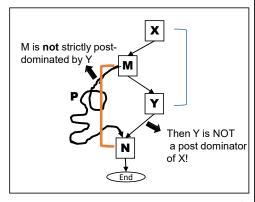
post-dominated by

2. There is a node x_k in between p_j and x_i such that x_k has a path to exit that does not pass x_i . Since p_j 's immediate post-dominator is also a post-dominator of x_k , x_k and p_j 's post-dominator form a smaller region that includes x_i , contradicting that p_j leads the enclosing region of x_i



Regions: Property Two

- Regions are either nested or disjoint, but can never overlap!
- Proof: Assume there are two regions (x, y) and (m, n) that overlap
- Let m reside in (x, y). Thus, y resides in (m, n)
- This implies there is a path P from m to exit without passing y
- Therefore, the path from x to m and P constitute a path from x to exit without passing y, contradicting the condition that y is a post-dominator of x





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Detecting Regions At Runtime

- **Observation**: During execution, Regions follow the LIFO pattern
 - · Otherwise, some regions must overlap
- **Implication**: The current sequence of nested regions for the current execution point can be maintained by a stack, called a control dependence stack (CDS)
- Each region is nested within the region immediately preceding it in the stack
- The enclosing region for the current execution point is always the top entry in the stack
 - Therefore any execution point is control dependent on the predicate that leads the top entry
- An entry is pushed onto CDS if a branching instruction (predicated jump) is executed
- The current entry is popped if the immediate post-dominator of the branching point is executed, denoting the end of the current region
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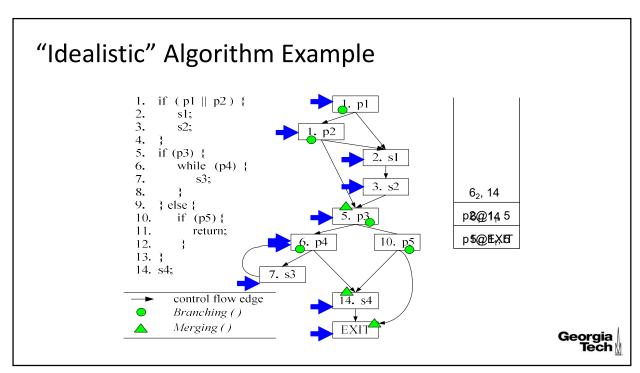
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"Idealistic" Algorithm

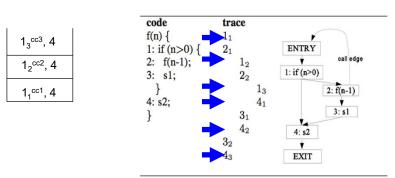
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Even Handles Recursion!

- · Annotate CDS entries with calling context
- · Consider this recursive code and execution trace

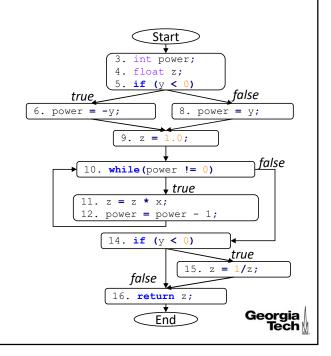


Source: B. Xin, X. Zhang. Efficient Online Detection of Dynamic Control Dependence, International Symposium on Software Testing and Analysis, 2007.

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Challenges in Practice

- 1. You may not know the immediate post-dominator ahead of time!
 - This requires first collecting the control flow trace, then computing the IPDs, then updating the control dependence



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Challenges in Practice

- 2. If you only have execution traces, then it is not clear what is a branch until you execute both paths!
 - In general, implementations use a hybrid of offline and online analyses to compute control dependence

Execution Trace (x=0, y=0)

```
3. int power;
4. float z;
5. if (y < 0)
8. power = y;
9. z = 1.0;
10. while(power != 0)
14. if (y < 0)
16. return z;</pre>
```

Execution Trace (x=1, y=1)

```
3. int power;
4. float z;
5. if (y < 0)
8. power = y;
9. z = 1.0;
10. while(power != 0)
11. z = z * x;
12. power = power - 1;
10. while(power != 0)
14. if (y < 0)
16. return z;</pre>
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```

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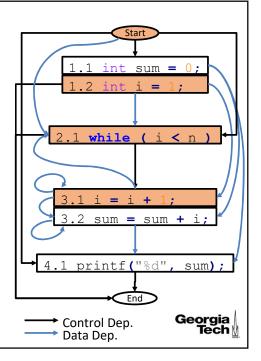
Dynamic Slice Concepts

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Wrap up of Dynamic Slice Concepts

- We have introduced the concept of slicing, slice criterions, and dynamic slicing
- We have seen two approaches to computing a dynamic slice:
 - Offline dynamic slicing algorithms based on backwards traversal over traces is not efficient
 - Online algorithms that detect dependences are efficient but control dependence can be complex/limited
- In fact, this form of slicing is called Backward Slicing
- Slice (I @ 3.1) = {START, 1.2, 2.1, 3.1}



Forward Dynamic Slice Computation

- The approaches we have discussed so far are for backward slicing
 - · Dependence graphs are traversed backwards from a slicing criterion
 - The space complexity is O(execution length)
- There is an orthogonal concept of Forward Slice Computation
- A forward slice of a program with respect to a program point p and variable v
 consists of all statements and predicates in the program that may be affected by
 the value of v at p
- Given a slice criterion, i.e., the starting point, a forward slice is computed by traversing the set of **forward-reachable** nodes in the program dependence graph

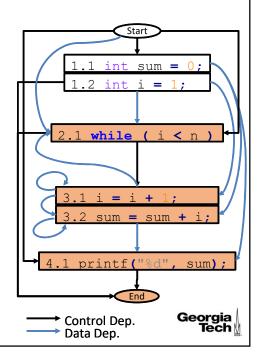


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Forward Slice Computation

- Step 1: Build a PDG (as discussed previously)
- Step 2: Traverse the forward-reachable nodes in the PDG from the slice criterion

ForwardStaticSlice (I @ 3.1) = {2.1, 3.1, 3.2, 4.1, END}

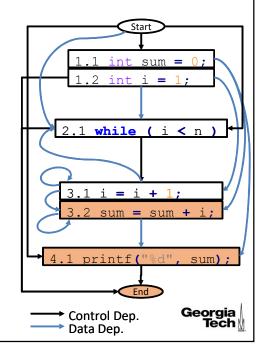


Forward Slice Computation

- Step 1: Build a PDG (as discussed previously)
- Step 2: Traverse the forward-reachable nodes in the PDG from the slice criterion

ForwardStaticSlice (I @ 3.1) = {2.1, 3.1, 3.2, 4.1, END}

ForwardStaticSlice (sum @ 3.2) = {3.2, 4.1, END}



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The Importance of Forward Slicing

- Slicing is by far the most commonly employed dynamic analysis
- Answer the question: "What program components might be affected by a particular computation?"
- Useful in determining which statements in a program can be affected by changes in the value of v at statement s



The Importance of Forward Slicing: Example 1

 As software is maintained, modifications to parts of the program can lead to unforeseen side effects.
 When part of a program is changed, the effect of the change "ripples" through the program. Forward slicing exposes these effects.



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The Importance of Forward Slicing: Example 2

 When analyzing malware, we want to focus on only the most important payloads (and not waste time on others). When the malware receives an input or checks a condition, that value will only affect some payloads. Forward slicing can give you foresight into what values will be important later in the execution.



Finally: Chopping

- Given a source criterion S and a target criterion T, determine what statements transmit the effects of S to T
- Simply the intersection of forward and backward slices
- Step 1: Compute a backward slice from the target criterion T
 - Recall: This is the set of all prior statements involved in computing the value of T.v at T.s
- Step 2: Compute a forward slice from the source criterion S
 - Recall: This is the set of all future statements affected by the value of S.v at S.s
- Step 3: Compute the intersection of the two graphs



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Lesson Summary

- Locate the set of statements that compose a program slice
- Construct a program dependent graph
- Assemble dynamic slices using a program dependency graph

