$$\frac{d}{dt}\left\{U+m\left(\frac{c^2}{2}+gz\right)\right\} = \sum_{j} \left[\dot{m}_{j}\left(h+\frac{c^2}{2}+gz\right)_{i}\right] + \sum_{l} \left(\dot{Q}_{l}\right)_{l} + \sum_{i} \left(\dot{W}_{l}\right)_{i} - p\frac{dV}{dt}$$

#### 1 Nomenklatur

 $\mathbf{An} = \text{Anergie}[\mathbf{J}]$ 

 $c_s = Schallgeschwindigkeit[m/s]$ 

 $\mathbf{c_p} = \text{Spezifische Wärmekapazität dp} = 0 [J/kg*K]$ 

 $\mathbf{c_v} = \text{Spezifische Wärmekapazität dv} = 0 \left[ \frac{J}{kg*K} \right]$ 

 $\mathbf{E} = \text{Energie}[\mathbf{J}]$ 

 $\mathbf{E}\mathbf{x} = -\mathbf{W}_{\mathbf{e}\mathbf{x}} = \mathrm{Exergie}[\mathbf{J}]$ 

 $\mathbf{F} = Kraft[N]$ 

 $\mathbf{F} = \mathbf{U} - \mathbf{TS} = \text{Freie Energie}[\mathbf{J}]$ 

 $\mathbf{f} = \mathbf{u} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Energie}[J/kg]$ 

 $\mathbf{f} = \text{Fugazität}[Pa]$ 

G = H - TS = Freie Enthalpie[J]

 $\mathbf{g} = \mathbf{h} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Enthalpie}[J/kg]$ 

 $\mathbf{g} = \text{Erdbeschleunigung}[\text{m/s}^2]$ 

 $\mathbf{H} = \mathbf{U} + \mathbf{p}\mathbf{V} = \text{Enthalpie}[\mathbf{J}]$ 

 $\mathbf{h} = \mathbf{u} + \mathbf{p}\mathbf{v} = \text{Spezifische Enthalpie}[\text{J/kg}]$ 

**■Hg** = Molare Reaktionsenthalpie

**K** = Konstante des Massenwirkungsgesetztes[-]

 $\mathbf{M} = \text{Molmasse[kg/mol]}$ 

 $\dot{\mathbf{m}} = \text{Massestrom}[\text{kg/s}]$ 

 $\mathbf{m}' = \text{Masse in der flüssigen Phase[kg]}$ 

 $\mathbf{m}'' = \text{Masse in der gasförmigen Phase[kg]}$ 

 $Ma = c/c_s = Machzahl[-]$ 

 $\mathbf{n} = \mathbf{m}/\mathbf{M} = \text{Molzahl[mol]}$ 

**n** = Polytropenexponent[-]

 $\mathbf{P_t} = \text{technische Leistung}[\mathbf{W}]$ 

 $\mathbf{Q} = \text{W\"{a}rme}[J]$ 

 $\dot{\mathbf{Q}} = \text{Wärmestrom}[W]$ 

q = Spezifische Wärme[J/kg]

 $\mathbf{r} = \text{Spezifische Verdampfungsenthalpie}[J/kg]$ 

 $\mathbf{R} = Gaskonstante[J/(kg\ K)]$ 

 $\mathbf{R}_{\mathbf{m}} = \text{Universelle Gaskonstante}[J/(\text{mol } K)]$ 

S = Entropie[J/K]

s = Spezifische Entropie[J/(kg K)]

T = Temperatur[K]

 $\mathbf{t} = \text{Zeit}[s]$ 

 $\mathbf{t} = \text{Temperatur}[^{\circ}\text{C}]$ 

T = Sättigungstemperatur[K]

U = Innere Energie[J]

 $\mathbf{u} = \text{Spezifische innere Energie [J/kg]}$ 

 $V = Volumen[m^3]$ 

 $\mathbf{v} = \text{Spezifisches Volumen}[\text{m}^3/\text{kg}]$ 

 $V_m = Molares Volumen[m<sup>3</sup>/mol]$ 

 $\mathbf{W} = \text{Arbeit}[J]$ 

 $\mathbf{w} = \text{Spezifische Arbeit}[J/kg]$ 

 $\mathbf{W}_{\mathbf{V}} = \text{Volumen}$ änderungsarbeit[J]

 $W_{el} = Elektrische Arbeit[J]$ 

 $\mathbf{W}_{\mathbf{w}} = \text{Wellenarbeit}[\mathbf{J}]$ 

 $\mathbf{W}_{\mathbf{diss}} = \mathrm{Dissipationsarbeit}[\mathrm{J}]$ 

 $\mathbf{W_t} = \text{Technische Arbeit}[\mathbf{J}]$ 

 $\mathbf{W}_{\mathbf{Virrev}} = \text{Arbeits verlust durch Irreversibilität}[\mathbf{J}]$ 

 $\mathbf{x} = \frac{m''}{m' + m''} = \text{Dampfanteil[-]}$ 

 $\mathbf{x} = \frac{m_{H_2O}}{m_L} = \text{Wassergehalt}$ 

 $\mathbf{Z} = \text{Allgemeine extensive Zustandsgrößen}[\mathbf{Z}]$ 

z = Allgemeine

 $\beta$  = Isobarer Ausdehnungskoeffizient[1/K]

 $\gamma$  = Isochorer Spannungskoeffizeint[1/K]

 $\delta_{\rm T} = {\rm Isothermer\ Drosselkoeffizient[m^3/kg]}$ 

 $\delta_{\rm h} = \text{Isenthalper Drosselkoeffizient}[\text{Ks}^2\text{m/kg}]$ 

 $\varepsilon = \text{Leistungsziffer}[-]$ 

 $\varepsilon$  = Verdichtungsverhältnis[-]

 $\eta_{\text{th}} = \text{Thermischer Wirkungsgrad[-]}$ 

 $\eta_{\rm mech} = {\rm Mechanischer\ Wirkungsgrad}[-]$ 

 $\kappa$  = Adiabaten- oder Isentropenexponent[-]

 $\lambda = \text{Reaktionslaufzahl}[-]$ 

 $\mu_i$  = Chemisches Potential[J/mol]

 $v_i$  = Stöchiometrische Koeffizienten[-]

 $\xi_{\mathbf{i}} = \text{Masseanteil[-]}$ 

 $\pi = \text{Druckverhältnis}[-]$ 

 $\rho = \text{Dichte}[\text{kg/m}^3]$ 

 $\tau =$  Temperaturverhältnis[-]

 $\phi$  = Relative Feuchte[-]

 $\phi = \text{Einspritzverhältnis}[-]$ 

 $\xi$  = Isothermer Kompressibilitätskoeffizient[m<sup>2</sup>/N]

 $\blacksquare$  = Dissipationsenergie[J]

 $\psi = \text{Spezifische Dissipationsenergie}[J]$ 

 $\psi$  = Drucksteigerungsverhältnis[-]

 $\psi_i = Molanteil[-]$ 

# Grundbegriffe

Systeme

- Abgeschlossenes System kein Stoff oder Energietransport
- Geschlossenes System kein Stofftransport
- · Offenes System Stoff und Energietransport

Messgrößen

- Prozessgrößen sind Wegabhängig (eg. Arbeit, Wärme)
- Zustandsgrößen sind Wegunabhängig (eg. Volumen, Druck)
- Intensive Zustandsgrößen sind unabhängig von der Größe des Systems (eg. Druck, Temperatur)
- Extensive Zustandsgrößen sind abhängig von der Größe des Systems (eg. Volumen, Masse)

Zustandsgleichungen

- Thermisch  $\rightarrow f(p, V, T) = 0$
- Kalorisch  $\rightarrow f(U, V, T) = 0$ , U = U(V, T), u = u(v, T)

## Maxwell

$$\left(\frac{\partial T}{\partial p}\right)_{S,n_i} = \left(\frac{\partial V}{\partial S}\right)_{p,n_i}$$

$$\left(\frac{\partial S}{\partial V}\right)_{T,n_j} = \left(\frac{\partial p}{\partial T}\right)_{V,n_j}$$

$$\left(\frac{\partial S}{\partial p}\right)_{T,n_j} = -\left(\frac{\partial V}{\partial T}\right)_{p,n_j}$$

$$\left(\frac{\partial \mu_i}{\partial T}\right)_{p,n_j} = -\left(\frac{\partial S}{\partial n_i}\right)_{T,p,n_j \neq n_i}$$

$$\left(\frac{\partial \mu_i}{\partial p}\right)_{T,n_j} = \left(\frac{\partial V}{\partial n_i}\right)_{T,p,n_j \neq n_i}$$

#### 3 **Basisformeln**

$$H = U + pV$$
$$dS = \frac{\delta Q_{rev}}{T}$$

$$F = U - TS$$

$$G = \underbrace{H - TS}_{2}$$

$$W_{V,12} = -\int_1^2 p \ dV$$

$$dS = \frac{Q_{rev}}{T} + S_{prod}$$

$$\Psi_{12} = \int_{1}^{2} T \, dS_{prod}$$

$$dU = Tds - pdV + \sum_{k=1}^{K} \mu_k dn_k \leftarrow \text{Gibbs}$$

$$dG = -SdT + Vdp + \sum_{k=1}^{K} \mu_k dn_k \qquad \leftarrow \text{Gibbs}$$

$$dH = TdS + Vdp + \sum_{k=1}^{K} \mu_k dn_k \leftarrow \text{Gibbs}$$

$$dF = -SdT - pdV + \sum_{k=1}^{K} \mu_k dn_k \qquad \leftarrow \text{Gibbs}$$

$$dU = \left(\frac{\partial U}{\partial S}\right)_{V,n_j} dS + \left(\frac{\partial U}{\partial V}\right)_{S,n_j} dV + \sum_{k=1}^K \left(\frac{\partial U}{\partial n_k}\right)_{S,V,n_j \neq n_k} dn_k$$

$$p_1 = p_a \frac{\varphi_1 - \varphi_a}{\varphi_b - \varphi_a} (p_b - p_a)$$

# Guggenheim

$$-S \quad U \quad V \qquad U = U(S,V)$$

$$H F H = H(S,p)$$

-p G T 
$$F = F(T,V)$$

$$G = G(T,p)$$

#### Thermodynamische Beziehungen 6

$$T = \left(\frac{\partial U}{\partial S}\right)_{V}$$

$$T = \left(\frac{\partial H}{\partial S}\right)_{p}$$

$$T = \left(\frac{\partial H}{\partial S}\right)_{p}$$

$$T = \left(\frac{\partial U}{\partial V}\right)_{S}$$

$$T = \left(\frac{\partial U}{\partial V}\right)_{S}$$

$$T = \left(\frac{\partial U}{\partial V}\right)_{T}$$

$$V = \left(\frac{\partial G}{\partial P}\right)_{T}$$

$$\underbrace{\frac{d}{dt} \left\{ U + m \left( \frac{c^2}{2} + gz \right) \right\} }_{\text{Stationäres System -> 0}} = \underbrace{\sum_{j} \left[ \dot{m}_{j} \left( h + \frac{c^2}{2} + gz \right)_{j} \right]}_{\text{Geschlossenes System -> 0}} + \underbrace{\sum_{l} \left( \dot{Q}_{l} \right)_{l}}_{\text{Keine Leistung -> 0}} + \underbrace{\sum_{l} \left( \dot{W}_{l} \right)_{i}}_{\text{Keine Volumenänderung -> 0}} + \underbrace{\sum_{l} \left( \dot{W}_{l} \right)_{i}}_{\text{Adv}} + \underbrace{\sum_{l}$$

#### 7 Ideales Gas

$$pV = mRT$$

$$pV = nR_mT$$

$$\beta = \frac{1}{T},$$

$$\gamma = \frac{1}{T}, \quad \chi = \frac{1}{p}, \quad \beta = p\gamma\chi,$$

$$R_m = 8,3143 \left[ \frac{kJ}{kmolK} \right], \quad R = c_p - c_v$$

$$U - U_0 = mc_v(T - T_0)$$

$$H - H_0 = mc_p(T - T_0) \quad \leftarrow \text{Für } c_p \text{ und } c_v \text{ const.}$$

$$s - s_0 = R \ln\left(\frac{v}{v_0}\right) + c_v \ln\left(\frac{T}{T_0}\right)$$

$$= c_v \ln\left(\frac{p}{p_0}\right) + c_p \ln\left(\frac{v}{v_0}\right)$$

$$= c_p \ln\left(\frac{T}{T_0}\right) - R \ln\left(\frac{p}{p_0}\right)$$

$$\beta = \frac{1}{T} = \frac{1}{V} \left(\frac{\partial V}{\partial T}\right)_p = \frac{1}{v} \left(\frac{\partial v}{\partial T}\right)_p = -\frac{1}{\rho} \left(\frac{\partial \rho}{\partial T}\right)_p$$

$$\gamma = \frac{1}{T} = \frac{1}{p} \left(\frac{\partial p}{\partial T}\right)_V$$

$$\chi = \frac{1}{p} = -\frac{1}{V} \left(\frac{\partial V}{\partial p}\right)_T = -\frac{1}{v} \left(\frac{\partial v}{\partial p}\right)_T$$

## 8 Van-der-Waals

$$\left(p + \frac{a}{v^2}\right)(v - b) = RT$$

$$\left(\overline{p} + \frac{3}{\overline{v}^2}\right)(3\overline{v} - 1) = 8\overline{T}$$

$$\overline{p} = \frac{p}{p_K}, \quad \overline{v} = \frac{v}{v_K}, \quad \overline{T} = \frac{T}{T_K}$$

$$p_K = \frac{a}{27b^2}, \quad T_K = \frac{8}{27}\frac{a}{b}\frac{1}{R}, \quad = 2$$

$$a = 3p_K v_K^2, \quad b = \frac{v_K}{3}, \quad \frac{p_K v_K}{RT_K} = \frac{3}{8}$$

$$\beta = \frac{(v - b)Rv^2}{RTv^3 - 2a(v - b)^2}$$

$$\gamma = \frac{Rv^2}{RTv^3 - 2a(v - b)^2}$$

$$\chi = \frac{(v - b)^2 v^2}{RTv^3 - 2a(v - b)^2}$$

$$du = \frac{a}{v^2}dv + c_v(T)dT$$

$$u - u_0 = \left(\frac{a}{v_0} - \frac{a}{v}\right) + \int_{T_0}^T c_v(\tilde{T}) d\tilde{T}$$

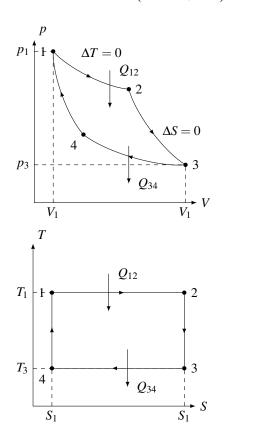
$$u - u_0 = \left(\frac{a}{v_0} - \frac{a}{v}\right) + c_v(T - T_0) \leftarrow \text{für } c_v = \text{const.}$$

$$c_p - c_v = \frac{Tv\beta^2}{\chi}$$

$$s - s_0 = c_v \ln\left(\frac{T}{T_0}\right) + R\ln\left(\frac{v - b}{v_0 - b}\right)$$

### 9 Carnot

$$\begin{split} &\eta_{th} = 1 - \frac{-Q_{34}}{Q_{12}} = 1 - \frac{T_3(S_3 - S_4)}{T_1(S_2 - S_1)} = 1 - \frac{T_3}{T_1} \\ &\frac{Q_{12}}{T_1} + \frac{Q_{34}}{T_3} = 0 \\ &\Delta S_{ges} = -Q_{34} \left( \frac{1}{T_{KK}} - \frac{T_1}{T_3} \frac{1}{T_{HK}} \right) \end{split}$$



#### 10 Gemische Idealer Gase

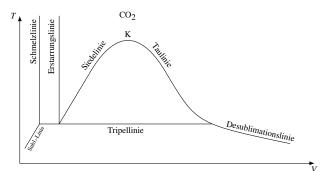
$$\begin{split} \xi_{i} &= \frac{m_{i}}{m}, \quad \psi_{i} = \frac{n_{i}}{n}, \quad p_{i} = \psi_{i}p \\ \xi_{i} &= \frac{M_{i}n_{i}}{\sum_{k=1}^{K}M_{k}n_{k}} = \frac{M_{i}}{M_{G}} \psi \\ p_{i}V &= m_{i}R_{i}T, \quad p_{i}V = n_{i}R_{m}T, \quad pV = mR_{G}T \\ \sum_{k=1}^{K}p_{k} &= p \\ R_{G} &= \frac{1}{m}\sum_{k=1}^{K}m_{k}R_{k} = \sum_{k=1}^{K}\xi_{k}R_{k} \\ U_{G} &= \sum_{k=1}^{K}U_{k} = \sum_{k=1}^{K}m_{k}u_{k} = \sum_{k=1}^{K}c_{vk}m_{k}T \leftarrow c_{v} = \text{const.} \\ H_{G} &= \sum_{k=1}^{K}H_{k} = \sum_{k=1}^{K}m_{k}h_{k} = \sum_{k=1}^{K}c_{pk}m_{k}T \leftarrow c_{p} = \text{const.} \\ c_{vG} &= \sum_{k=1}^{K}c_{vk}\xi_{k}, \quad c_{pG} &= \sum_{k=1}^{K}c_{pk}\xi_{k} \\ S_{2} - S_{1} &= R_{m}\left(n\ln n - \sum_{k=1}^{K}n_{k}\ln n_{k}\right) \end{split}$$

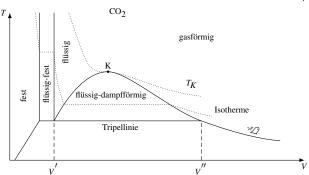
Adiabate Drosselung (ideal):  $h + \frac{c^2}{2} + gz = \text{const.}$ 

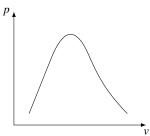
$$dh = 0$$

Adiabet Drosselung (real): 
$$\delta_h = \left(\frac{\partial T}{\partial p}\right)_h = -\frac{v}{c_p}(1 - \beta T)$$

# 11 Nassdampf







r = h'' - h' = T(s'' - s')

$$v = (1 - x)v' + xv''$$

$$v = v' + (v'' - v')x$$

$$u = (1 - x)u' + xu''$$

$$u = u' + (u'' - u')x$$

$$h = (1 - x)h' + xh''$$

$$h = h' + (h'' - h')x$$

$$r' = T''$$

$$g' = g''$$

$$dg' = v'dp' - s'dT'$$

$$dg'' = v''dp'' - s''dT''$$

$$dg' = dg''$$

$$dg' = dg''$$

$$dg' = dg''$$

$$df' = \frac{s'' - s'}{v'' - v'}$$

$$\frac{dp}{dT} = \frac{1}{T} \frac{h'' - h'}{v'' - v'}$$

$$s = s' + (s'' - s')x$$

$$\frac{dp}{dT} = \frac{1}{T} \frac{r}{v'' - v'}$$

# 12 Realer Stoff im Nassdampfgebiet

IsobareZustandsänderung

$$q_{12} = T(s_2 - s_1) = T(s'' - s')(x_2 - x_1)$$

$$w_{V,12} = -\int_1^2 p \, dv = -p(v_2 - v_1) = -p(v'' - v')(x_2 - x_1)$$

IsochoreZustandsänderung

$$q_{12} = u_2 - u_1 = u_2' + x_2 \left(u_2'' - u_2'\right) - u_1' - x_1 \left(u_1'' - u_1'\right)$$

AdiabateZustandsänderung

$$w_{V,12} = u_2 - u_1 = u_2' + x_2 \left(u_2'' - u_2'\right) - u_1' - x_1 \left(u_1'' - u_1'\right)$$

Entropieänderung wärend des Mischvorgangs

$$S_2 - S_2 = R_m \left( n \ln n - \sum_i n_i \ln n_i \right) \tag{1}$$

# 13 Maximale Arbeit und Exergie

$$-\dot{W}_{ex} = -(\dot{W}_{t})_{rev} = -\frac{d}{dt} \left( U + m \left( \frac{c^{2}}{2} + gz \right) + p_{u}V - T_{u}S \right) + \sum_{i=1}^{K} \left( \dot{m}_{j} \left( h + \frac{c^{2}}{2} + gz - T_{s} \right) \right) + \sum_{l=1}^{K} \left( 1 - \frac{T_{u}}{T} \right) \dot{Q}_{l}$$
 (2)

Die Exergie der Enthalpie (offens, stationäres System)

$$-\dot{W}_{ex\ 1u} = \dot{m}(h_1 - h_u - T_u(s_1 - s_u)) \tag{3}$$

Die Exergie der inneren Energie (geschlossenes, instationäres System)

$$-\dot{W}_{ex} = -\frac{d}{dt}(U + p_u V - T_u S) \tag{4}$$

$$-\dot{W}_{ex,1u} = U_1 - U_u - p_u(V_1 - V_u) - T_u(S_1 - S_u)$$
 (5)

Die Exergie der Wärme (geschlossenes, stationäres System)

$$-\dot{W}_{ex} = \left(1 - \frac{T_u}{T_1}\right)\dot{Q}_1 = \eta_{th,C}\dot{Q}_1 \tag{6}$$

# 14 Wärmekapazität

Translatorisch: 
$$C_v = \frac{3}{2}R_m$$

Rotatorisch: 
$$C_v = n \cdot \frac{1}{2} R_m$$

n = Anzahl der Rotatorischen Freiheitsgrade

Ideales Gas

	Isothermo	Isobare	Isochore	Isentrop	Polytrope
konstant:	T	ď	>	$\delta q = 0$	$pv^n$
	1	1	ı	$p_1 v_1^K = p_2 v_2^K$	$v_1^n = p_2 v_2^n$
	$p_1p_2=p_2v_2$	$\frac{v_1}{v_2} = \frac{T_1}{T_2}$	$\frac{p_1}{T_1} = \frac{p_2}{T_2}$	$T_1 \nu_1^{K-1} = T_2 \nu_2^{K-1}$	$T_1 \nu_1^{n-1} = T_2 \nu_2^{n-1}$
	•	•	thud ————————————————————————————————————	$\frac{T_1^{\frac{K}{K-1}}}{p_1} = \frac{T_2^{\frac{K}{K-1}}}{p_2}$	$\frac{T_1^{\frac{n}{n-1}}}{p_1} = \frac{T_2^{\frac{n}{n-1}}}{p_2}$
p,v	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$\nu = \nu_1$	$p = \frac{p_1 \nu_1^K}{\nu^K}$	$p = \frac{p_1 \nu_1^n}{\nu^n}$
p,T	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$p = \frac{p_1}{T_1}T$	$p = \frac{p_1}{T_1^{\frac{K}{K-1}}} T^{\frac{K}{K-1}}$	$p = \frac{p_1}{T_1^{\frac{n}{n-1}}} T^{\frac{n}{n-1}}$
v,T	$T=T_{ m l}$	$\nu = \frac{\nu_1}{T_1}T$	$\nu = \nu_1$	$T=rac{T_1  u_1^{K-1}}{ u^{K-1}}$	$T=rac{T_1  u_1^{n-1}}{ u^{n-1}}$
<i>q</i> 12	$q_{12} = p_1 v_1 \ln \frac{p_1}{p_2}$	$q_{12} = c_p(T_2 - T_1)$	$q_{12} = c_{\nu}(T_2 - T_1)$	$q_{12} = 0$	$q_{12} = c_{\nu} \frac{n-K}{n-1} (T_2 - T_1)$
WV,12	$w_{V,12} = -q_{12}$	$w_{V,12} = -p_1(v_2 - v_1)$	$w_{V,12} = 0$	$w_{V,12} = \frac{p_1 v_1}{k-1} \left( \left( \frac{v_1}{v_1} \right)^{K-1} - 1 \right)$	$w_{V,12} = \frac{p_1 v_1}{n-1} \left( \left( \frac{v_1}{v_2} \right)^{n-1} - 1 \right)$
$s_2 - s_1$	$s_2 - s_1 = R \ln \left( \frac{p_1}{p_2} \right)$	$s_2 - s_1 = c_p \ln\left(\frac{T_2}{T_1}\right)$	$s_2 - s_1 = c_{\nu} \ln \left( \frac{T_2}{T_1} \right)$	$s_2 - s_1 = 0$	$s_2 - s_1 = c_v \frac{n - \kappa}{n - 1} \ln \left( \frac{T_2}{T_1} \right)$

bM = M	$p_M = p + \frac{a}{v^2},  v_M = v - b,  k_M = (c_v + R)/c_v)$			
	Isotherme	Isobare	Isochore	Isentrop
konst.	T	d	Λ	$\delta = 0$
	$(p_1 + \frac{a}{v^2})(v_1 - b) = (p_2 + \frac{a}{v^2})(v_2 - b)$	$\frac{RT_1}{\nu_1 - b} - \frac{a}{\nu_1^2} = \frac{RT_2}{\nu - b} - \frac{a}{\nu_2^2}$	$\frac{p_1 + \frac{a}{v_1^2}}{T_1} = \frac{p_2 + \frac{a}{v_1^2}}{T_2}$	$(p_1+rac{a}{ u^2})( u_1-b)rac{c u+R}{ u}=(p+rac{a}{ u^2})( u_2-b)rac{c u+R}{ u}, \ T_1( u_1-b)^{R/c_ u}=T_2( u_2-b)^{R/c_ u}$
$p, \nu$	$p = (p + \frac{a}{v^2}) \frac{v_u}{v - b} - \frac{a}{v^2}$	$p = p_1$	$\nu = \nu_1$	$p = -\frac{a}{v^2} + \left(p_1 + \frac{a}{v^2}\right) \left(\frac{v_1 - b}{v_m}\right)^{\frac{v_v + R}{R}}$
p,T	$T=T_1$	$p = p_1$	$p = \frac{T}{T_1} (p_1 + \frac{a}{v^2}) - \frac{a}{v_1^2}$	
$\nu,T$	$T=T_1$	$T = T_1 rac{v-b}{v_1-b} + rac{a}{R}(v-b) \left(rac{1}{v^2} - rac{1}{v_1^2} ight)$	$\nu = \nu_1$	$T=T_1\left(rac{ u_1-b}{ u-b} ight)^{rac{R}{C_V}}$
<i>q</i> 12	$q_{12} = RT_1 \ln \left( \frac{v_2 - b}{v_1 - b} \right)$	$q_{12} = rac{a}{v_1} - rac{a}{v_2} + c_v(T_2 - T_1) + p_1(v_2 - v_1) \ \ q_{12} = c_v(T_2 - T_1)$	$q_{12} = c_{\nu} (T_2 - T_1)$	$q_{12} = 0$
WV,12	$w_{V,12} = -RT_1 \ln \left( \frac{v_2 - b}{v_1 - b} \right) + \frac{a}{v_1} - \frac{a}{v_2}$	$w_{V,12} = -p_1(v_2 - v_1)$	$w_{V,12}=0$	$w_{V,12} = rac{a}{v_1} - rac{a}{v_2} + c_{ u}(T_2 - T_1)$
$s_2 - s_1$	$s_2 - s_1 = R \ln \left( \frac{v_2 - b}{v_1 - b} \right)$	$s_2 - s_1 = c_{\nu} \ln \left( \frac{T_2}{T_1} \right) + R \ln \left( \frac{v_2 - b}{v_1 - b} \right)$	$s_2 - s_1 = c_v \ln \left( \frac{T_2}{T_1} \right)$	$s_2 - s_1 = 0$