Thermodynamik Formelsammlung

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$$\frac{d}{dt}\left\{U+m\left(\frac{c^2}{2}+gz\right)\right\} = \sum_{j}\left[\dot{m}_{j}\left(h+\frac{c^2}{2}+gz\right)_{i}\right] + \sum_{l}\left(\dot{Q}_{l}\right)_{l} + \sum_{i}\left(\dot{W}_{l}\right)_{i} - p\frac{dV}{dt}$$

1 Nomenklatur

 $\mathbf{An} = \text{Anergie}[\mathbf{J}]$

 $c_s = Schallgeschwindigkeit[m/s]$

 $c_{\rm p} = {\rm Spezifische\ W\"{a}rmekapazit\"{a}t\ dp} = 0\ [{\rm J/kg*K}]$

 $\mathbf{c_v} = \text{Spezifische Wärmekapazität dv} = 0 [J/kg*K]$

 $\mathbf{E} = \text{Energie}[\mathbf{J}]$

 $\mathbf{E}\mathbf{x} = -\mathbf{W}_{\mathbf{e}\mathbf{x}} = \mathrm{Exergie}[\mathbf{J}]$

 $\mathbf{F} = Kraft[N]$

 $\mathbf{F} = \mathbf{U} - \mathbf{TS} = \text{Freie Energie}[\mathbf{J}]$

 $\mathbf{f} = \mathbf{u} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Energie}[J/kg]$

 $\mathbf{f} = \text{Fugazität}[Pa]$

G = H - TS = Freie Enthalpie[J]

 $\mathbf{g} = \mathbf{h} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Enthalpie}[J/kg]$

 $\mathbf{g} = \text{Erdbeschleunigung}[\text{m/s}^2]$

 $\mathbf{H} = \mathbf{U} + \mathbf{pV} = \text{Enthalpie}[\mathbf{J}]$

 $\mathbf{h} = \mathbf{u} + \mathbf{p}\mathbf{v} = \text{Spezifische Enthalpie}[\text{J/kg}]$

■**Hg** = Molare Reaktionsenthalpie

K = Konstante des Massenwirkungsgesetztes[-]

 $\mathbf{M} = \text{Molmasse[kg/mol]}$

 $\dot{\mathbf{m}} = \text{Massestrom}[\text{kg/s}]$

 $\mathbf{m}' = \text{Masse in der flüssigen Phase[kg]}$

 $\mathbf{m}'' = \text{Masse in der gasförmigen Phase[kg]}$

 $Ma = c/c_s = Machzahl[-]$

 $\mathbf{n} = \mathbf{m}/\mathbf{M} = \text{Molzahl[mol]}$

n = Polytropenexponent[-]

 $\mathbf{P_t} = \text{technische Leistung}[\mathbf{W}]$

 $\mathbf{Q} = \text{W\"{a}rme}[J]$

 $\dot{\mathbf{Q}} = \text{Wärmestrom}[\mathbf{W}]$

q = Spezifische Wärme[J/kg]

 $\mathbf{r} = \text{Spezifische Verdampfungsenthalpie}[J/kg]$

 $\mathbf{R} = \text{Gaskonstante}[J/(\text{kg K})]$

 $\mathbf{R}_{\mathbf{m}} = \text{Universelle Gaskonstante}[J/(\text{mol } K)]$

S = Entropie[J/K]

s = Spezifische Entropie[J/(kg K)]

T = Temperatur[K]

 $\mathbf{t} = \text{Zeit}[s]$

 $\mathbf{t} = \text{Temperatur}[^{\circ}\text{C}]$

T = Sättigungstemperatur[K]

U = Innere Energie[J]

 $\mathbf{u} = \text{Spezifische innere Energie [J/kg]}$

 $V = Volumen[m^3]$

 $\mathbf{v} = \text{Spezifisches Volumen}[\text{m}^3/\text{kg}]$

 $V_m = Molares Volumen[m³/mol]$

 $\mathbf{W} = \text{Arbeit}[J]$

 $\mathbf{w} = \text{Spezifische Arbeit}[J/kg]$

 $\mathbf{W}_{\mathbf{V}} = \text{Volumen}$ änderungsarbeit[J]

 $W_{el} = Elektrische Arbeit[J]$

 $\mathbf{W}_{\mathbf{w}} = \text{Wellenarbeit}[\mathbf{J}]$

 $W_{diss} = Dissipations arbeit[J]$

 $W_t = \text{Technische Arbeit}[J]$

 $\mathbf{W}_{Virrev} = \text{Arbeits verlust durch Irreversibilität}[J]$

 $\mathbf{x} = \frac{m''}{m' + m''} = \text{Dampfanteil[-]}$

 $\mathbf{x} = \frac{m_{H_2O}}{m_L} = \text{Wassergehalt}$

 $\mathbf{Z} = \text{Allgemeine extensive Zustandsgrößen}[\mathbf{Z}]$

z = Allgemeine

 β = Isobarer Ausdehnungskoeffizient[1/K]

 γ = Isochorer Spannungskoeffizeint[1/K]

 $\delta_{\rm T} = {\rm Isothermer\ Drosselkoeffizient[m^3/kg]}$

 $\delta_{\mathbf{h}}$ = Isenthalper Drosselkoeffizient[Ks²m/kg]

 ε = Leistungsziffer[-]

 $\varepsilon = \text{Verdichtungsverhältnis}[-]$

 $\eta_{\rm th} = \text{Thermischer Wirkungsgrad}[-]$

 $\eta_{\text{mech}} = \text{Mechanischer Wirkungsgrad[-]}$

 $\kappa = \text{Adiabaten- oder Isentropenexponent}[-]$

 $\lambda = \text{Reaktionslaufzahl}[-]$

 μ_i = Chemisches Potential[J/mol]

 v_i = Stöchiometrische Koeffizienten[-]

 $\xi_{\mathbf{i}} = \text{Masseanteil}[-]$

 $\pi = \text{Druckverhältnis}[-]$

 $\rho = \text{Dichte}[\text{kg/m}^3]$

 $\tau = \text{Temperaturverhältnis}[-]$

 ϕ = Relative Feuchte[-]

 $\phi = \text{Einspritzverhältnis}[-]$

 ξ = Isothermer Kompressibilitätskoeffizient[m²/N]

 \blacksquare = Dissipationsenergie[J]

 $\psi = \text{Spezifische Dissipationsenergie}[J]$

 ψ = Drucksteigerungsverhältnis[-]

 $\psi_i = Molanteil[-]$

2 Grundbegriffe

Systeme

- Abgeschlossenes System kein Stoff oder Energietransport
- Geschlossenes System kein Stofftransport
- Adiabates System kein Δq , aber Masse und Arbeit.
- Offenes System Stoff und Energietransport
- Stationäres System $\rightarrow \Delta U = 0$

Messgrößen

- Prozessgrößen sind Wegabhängig (eg. Arbeit, Wärme)
- Zustandsgrößen sind Wegunabhängig (eg. Volumen, Druck)
- Extensive Zustandsgrößen sind abhängig von der Masse des Systems (V, m, H, S, F, G, E)
- Intensive Zustandsgrößen sind unabhängig von der Masse des Systems (T, p)

Zustandsgleichungen

- Thermisch $\rightarrow f(p, V, T) = 0$
- Kalorisch $\rightarrow f(U, V, T) = 0$, U = U(V, T), u = u(v, T)

Hauptsätze

- Temperatur existiert, ihre gleichheit ist notwendige Vorraussetzung für das thermische Gleichgewicht von zwei Systemen.
- 1: Energie existiert, sie ist für abgeschlossene Systeme konstant.
- 2: Entropie existiert, sie wird bei allen irreversiblen Prozessen erzeugt. $dS = \frac{\delta Q_{rev}}{T}$
- 3: 0K existert, bei dieser Temperatur ist die Entropie = 0

4 Gibbs

$$dU = Tds - pdV + \sum_{k=1}^{K} \mu_k dn_k$$

$$dG = -SdT + Vdp + \sum_{k=1}^{K} \mu_k dn_k$$

$$dH = TdS + Vdp + \sum_{k=1}^{K} \mu_k dn_k$$

$$dF = -SdT - pdV + \sum_{k=1}^{K} \mu_k dn_k$$

$$dU = \left(\frac{\partial U}{\partial S}\right)_V dS + \left(\frac{\partial U}{\partial V}\right)_S dV + \sum_{k=1}^{K} \left(\frac{\partial U}{\partial n_k}\right)_S dn_k$$

5 Thermodynamische Beziehungen

$$\begin{split} T &= \quad \left(\frac{\partial U}{\partial S}\right)_V = T(S,V) & \quad -S &= \left(\frac{\partial F}{\partial T}\right)_V = S(T,V) \\ T &= \quad \left(\frac{\partial H}{\partial S}\right)_p = T(S,p) & \quad -S &= \left(\frac{\partial G}{\partial T}\right)_p = S(T,p) \\ p &= -\left(\frac{\partial U}{\partial V}\right)_S = p(V,S) & \quad V &= \left(\frac{\partial G}{\partial p}\right)_T = V(p,T) \\ -p &= \quad \left(\frac{\partial F}{\partial V}\right)_T = p(T,V) & \quad \mu &= \left(\frac{\partial U}{\partial n}\right)_{S,V} = \mu(S,V,n) \end{split}$$

3 Basisformeln

$$dS = \frac{Q_{rev}}{T} + S_{prod}$$

$$H = U + pV$$

$$dS = \frac{\delta Q_{rev}}{T}$$

$$F = U - TS$$

$$G = \underbrace{H - ST}_{====2}$$

$$W = -\int p \, dV$$

$$dS_{prod} = \frac{\Psi}{T}$$

$$\Psi = \int_{1}^{2} T \, dS_{prod}$$

$$W_{ir} = \frac{T_{u}}{T} \Psi$$

$$p_{1} = p_{a} + \frac{\varphi_{1} - \varphi_{a}}{\varphi_{b} - \varphi_{a}} (p_{b} - p_{a})$$

6 Guggenheim

$$\underbrace{\frac{d}{dt} \left\{ U + m \left(\frac{c^2}{2} + gz \right) \right\}}_{\text{Stationäres System -> 0}} = \underbrace{\sum_{j} \left[\dot{m}_{j} \left(h + \frac{c^2}{2} + gz \right)_{j} \right]}_{\text{Geschlossenes System -> 0}} + \underbrace{\sum_{l} \left(\dot{Q}_{t} \right)_{l}}_{\text{Keine Leistung -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{Keine Volumenänderung -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}} + \underbrace{\sum_{i} \left(\dot{W}_{t} \right)_{i}}_{\text{At Matter System -> 0}}$$

7 Maxwell

$$\left(\frac{\partial T}{\partial p}\right)_{S,n_j} = \left(\frac{\partial V}{\partial S}\right)_{p,n_j} \\
\left(\frac{\partial S}{\partial V}\right)_{T,n_j} = \left(\frac{\partial p}{\partial T}\right)_{V,n_j} \\
\left(\frac{\partial S}{\partial p}\right)_{T,n_j} = -\left(\frac{\partial V}{\partial T}\right)_{p,n_j} \\
\left(\frac{\partial \mu_i}{\partial T}\right)_{p,n_j} = -\left(\frac{\partial S}{\partial n_i}\right)_{T,p,n_j \neq n_i} \\
\left(\frac{\partial \mu_i}{\partial p}\right)_{T,n_i} = \left(\frac{\partial V}{\partial n_i}\right)_{T,p,n_i \neq n_i} \\$$

8 Ideales Gas

$$pV = mRT$$

$$pV = nR_mT$$

$$\beta = \frac{1}{T}$$

$$\gamma = \frac{1}{T}$$

$$\chi = \frac{1}{p}$$

$$\beta = p\gamma\chi$$

$$R_m = 8,3143 \left[\frac{kJ}{kmolK} \right]$$

$$R = c_p - c_v$$

$$R = \frac{R_m}{M}$$

$$U - U_0 = mc_v(T - T_0)$$

$$H - H_0 = mc_p(T - T_0) \leftarrow \text{Für } c_p \text{ und } c_v \text{ const.}$$

$$s - s_0 = R \ln \left(\frac{v}{v_0} \right) + c_v \ln \left(\frac{T}{T_0} \right)$$

$$= c_v \ln \left(\frac{p}{p_0} \right) + c_p \ln \left(\frac{v}{v_0} \right)$$

$$= c_p \ln \left(\frac{T}{T_0} \right) - R \ln \left(\frac{p}{p_0} \right)$$

$$\beta = \frac{1}{T} = \frac{1}{V} \left(\frac{\partial V}{\partial T} \right)_p = \frac{1}{V} \left(\frac{\partial v}{\partial T} \right)_p = -\frac{1}{\rho} \left(\frac{\partial \rho}{\partial T} \right)_p$$

$$\gamma = \frac{1}{T} = \frac{1}{p} \left(\frac{\partial P}{\partial T} \right)_v$$

$$\chi = \frac{1}{p} = -\frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_T = -\frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_T$$

$$u_2 - u_1 = \int_{T_1}^{T_2} c_v(T) dT$$

9 Van-der-Waals

$$\left(p + \frac{a}{v^2}\right)(v - b) = RT$$

$$\left(\overline{p} + \frac{3}{\overline{v}^2}\right)(3\overline{v} - 1) = 8\overline{T}$$

$$\overline{p} = \frac{p}{p_K}, \quad \overline{v} = \frac{v}{v_K}, \quad \overline{T} = \frac{T}{T_K}$$

$$p_K = \frac{a}{27b^2}, \quad T_K = \frac{8}{27}\frac{a}{b}\frac{1}{R}, \quad \overline{z}_{\mathcal{Q}}$$

$$a = 3p_K v_K^2, \quad b = \frac{v_K}{3}, \quad \frac{p_K v_K}{RT_K} = \frac{3}{8}$$

$$\beta = \frac{(v - b)Rv^2}{RTv^3 - 2a(v - b)^2}$$

$$\gamma = \frac{Rv^2}{RTv^3 - 2a(v - b)^2}$$

$$\chi = \frac{(v - b)^2 v^2}{RTv^3 - 2a(v - b)^2}$$

$$du = \frac{a}{v^2} dv + c_v(T) dT$$

$$u - u_0 = \left(\frac{a}{v_0} - \frac{a}{v}\right) + \int_{T_0}^T c_v(\tilde{T}) d\tilde{T}$$

$$u - u_0 = \left(\frac{a}{v_0} - \frac{a}{v}\right) + c_v(T - T_0) \leftarrow \text{für } c_v = \text{const.}$$

$$c_p - c_v = \frac{Tv\beta^2}{\chi}$$

$$s - s_0 = c_v \ln\left(\frac{T}{T_0}\right) + R\ln\left(\frac{v - b}{v_0 - b}\right)$$

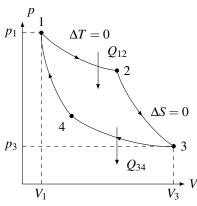
$$h_2 - h_1 = \frac{1}{2}(p_2 - p_1)\left(\frac{1}{Q_1} + \frac{1}{Q_2}\right)$$

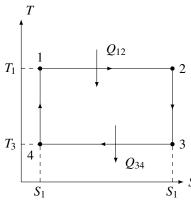
10 Carnot

$$\eta_{th} = 1 - \frac{-Q_{34}}{Q_{12}} = 1 - \frac{T_3(S_3 - S_4)}{T_1(S_2 - S_1)} = 1 - \frac{T_1}{T_3}$$

$$\frac{Q_{12}}{T_1} + \frac{Q_{34}}{T_3} = 0$$

$$\Delta S_{ges} = -Q_{34} \left(\frac{1}{T_{KK}} - \frac{T_1}{T_3} \frac{1}{T_{HK}} \right)$$





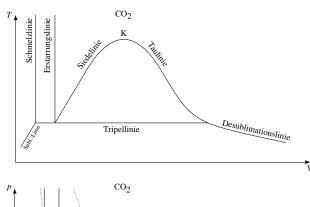
11 Gemische Idealer Gase

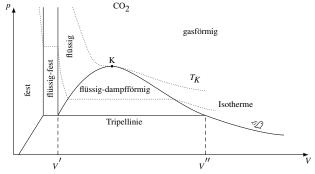
$$\begin{split} \xi_i &= \frac{m_i}{m}, \quad \psi_i = \frac{n_i}{n}, \quad p_i = \psi_i p \\ \xi_i &= \frac{M_i n_i}{\sum_{k=1}^K M_k n_k} = \frac{M_i}{M_G} \psi \\ p_i V &= m_i R_i T, \quad p_i V = n_i R_m T, \quad p V = m R_G T \\ \sum_{k=1}^K p_k &= p \\ R_G &= \frac{1}{m} \sum_{k=1}^K m_k R_k = \sum_{k=1}^K \xi_k R_k \\ U_G &= \sum_{k=1}^K U_k = \sum_{k=1}^K m_k u_k = \sum_{k=1}^K c_{vk} m_k T \leftarrow c_v = \text{const} \\ H_G &= \sum_{k=1}^K H_k = \sum_{k=1}^K m_k h_k = \sum_{k=1}^K c_{pk} m_k T \leftarrow c_p = \text{const.} \\ c_{vG} &= \sum_{k=1}^K c_{vk} \xi_k, \quad c_{pG} &= \sum_{k=1}^K c_{pk} \xi_k \\ S_2 - S_1 &= R_m \left(n \ln n - \sum_{k=1}^K n_k \ln n_k \right) \end{split}$$

Adiabate Drosselung (ideal): $h + \frac{c^2}{2} + gz = \text{const.}$ dh = 0Adiabet Drosselung (real):

$$\delta_h = \left(\frac{\partial T}{\partial p}\right)_h = -\frac{v}{c_p}(1 - \beta T)$$

12 Nassdampf





$$v = (1-x)v' + xv''$$

$$v = v' + (v'' - v')x$$

$$T' = T''$$

$$p' = p''$$

$$g' = g''$$

$$dg' = v'dp' - s'dT'$$

$$dg'' = v''dp'' - s''dT''$$

$$dg'' = dg''$$

$$dg' = dg''$$

$$df = \frac{1}{T} \frac{h'' - h'}{v'' - v'}$$

$$s = s' + (s'' - s')x$$

$$\frac{dp}{dT} = \frac{1}{T} \frac{r}{v'' - v'}$$

$$r = h'' - h' = T(s'' - s')$$

13 Realer Stoff im Nassdampfgebiet

Isobare Zustandsänderung

$$q_{12} = T(s_2 - s_1)$$

$$= T(s'' - s')(x_2 - x_1)$$

$$w_{V,12} = -\int_1^2 p \, dv$$

$$= -p(v_2 - v_1) = -p(v'' - v')(x_2 - x_1)$$

Isochore Zustandsänderung

$$q_{12} = u_2 - u_1 = u_2' + x_2 \left(u_2'' - u_2'\right) - u_1' - x_1 \left(u_1'' - u_1'\right)$$

Adiabate Zustandsänderung

$$w_{V,12} = u_2 - u_1 = u'_2 + x_2 \left(u''_2 - u'_2\right) - u'_1 - x_1 \left(u''_1 - u'_1\right)$$

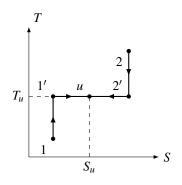
Entropieänderung wärend des Mischvorgangs

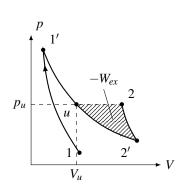
$$S_2 - S_2 = R_m \left(n \ln n - \sum_i n_i \ln n_i \right)$$

14 Maximale Arbeit und Exergie

Maxiaml nutzbare Arbeit → isentrop, reibungsfrei

 $1 \rightarrow 1'$: isentrop auf T_u $1' \rightarrow u$: isotherm auf u





$$-\dot{W}_{ex} = -(\dot{W}_{t})_{rev} = -\frac{d}{dt} \left(U + m \left(\frac{c^{2}}{2} + gz \right) + p_{u}V - T_{u}S \right) + \sum_{i=1}^{K} \left(\dot{m}_{j} \left(h + \frac{c^{2}}{2} + gz - T_{s} \right) \right) + \sum_{l=1}^{K} \left(1 - \frac{T_{u}}{T} \right) \dot{Q}_{l}$$

Die Exergie der Enthalpie (offens, stationäres System)

$$-\dot{W}_{ex,1u} = \dot{m}(h_1 - h_u - T_u(s_1 - s_u))$$

Die Exergie der inneren Energie (geschlossenes, instationäres System)

$$\begin{split} -\dot{W}_{ex} &= -\frac{d}{dt}(U + p_u V - T_u S) \\ -\dot{W}_{ex,1u} &= U_1 - U_u - p_u (V_1 - V_u) - T_u (S_1 - S_u) \\ -\dot{W}_{ex,1u} &= H_1 - (p_1 - p_u) V_1 - H_u - T_u (S_1 - S_u) \end{split}$$

Für Ideales Gas

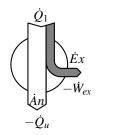
$$\begin{split} -W_{ex} &= mc_v(T_1 - T_u) + p_u(V_1 - V_u) - T_u m \left(c_p \ln\left(\frac{T_1}{T_u}\right) - R_i \ln\left(\frac{p_1}{p_u}\right)\right) \\ -W_{ex} &= m \left[c_p(T_1 - T_u) - T_u c_p \ln\left(\frac{T_1}{T_u}\right)\right] \leftarrow \text{isobar} \end{split}$$

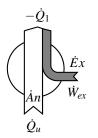
Dampf/Luftdruckkammer

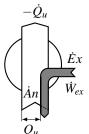
$$-W_{ex,1u} = m_1[u_1 - u_u + p_u(v_1 - v_u) - T_u(s_1 - s_u)]$$

Die Exergie der Wärme (geschlossenes, stationäres System)

$$-\dot{W}_{ex} = \left(1 - \frac{T_u}{T_1}\right)\dot{Q}_1 = \eta_{th,C}\dot{Q}_1$$



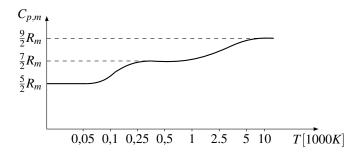




WärmekraftprozessWärmepumpenprozess

Kälteprozess

15 Wärmekapazität



$$C_{v,m} = \frac{1}{\kappa - 1} R_m \qquad C_{p,m} = \frac{\kappa}{\kappa - 1} r_m$$

$$c_v = \frac{1}{\kappa - 1} R_j \qquad c_p = \frac{\kappa}{\kappa - 1} R_j$$

$$\kappa = \frac{c_p}{c_v} \qquad R = c_p - c_v$$

$$R = \frac{R_m}{M} \qquad R_m = 8,3143 \left[\frac{kJ}{kmolK} \right]$$

$$C_{v,m} = \underbrace{3 + \frac{R_m}{2}}_{\text{Translatorisch}} + \underbrace{\frac{n_{\text{rot}}R_m}{2}}_{\text{Rotatorisch}} + \underbrace{\frac{R_M(3n_{\text{Atome}} - 3 - n_{rot})}{\text{Vibratorisch}}}_{\text{Relevant ab: } T \approx 10^4 K}$$

16 Technische Anwendung

adiabat
$$(c_p = const.)$$
 $W_{t,12} = mc_p(T_2 - T_1) = \frac{\kappa}{\kappa - 1}(p_2V_2 - p_1V_1)$ $Q_{12} = 0$

reversibel adiabat $\kappa = const.$ $W_{t,12} = \frac{\kappa}{\kappa - 1}(p_1V_1) \left[\left(\frac{p_2}{p_1} \right)^{\frac{\kappa - 1}{\kappa}} - 1 \right]$ $Q_{12} = 0$

irreversibel adiabat als Polytrope $n > \kappa; n, \kappa = const.$ $W_{t,12} = \frac{\kappa}{\kappa - 1}(p_1V_1) \left[\left(\frac{p_2}{p_1} \right)^{\frac{n-1}{n}} - 1 \right]$ $Q_{12} = 0$

reversibel polytrop $n, \kappa = const.$ $W_{t,12} = \frac{n}{n-1}(p_2V_2 - p_1V_1)$ $Q_{12} = mc_n(T_2 - T_1)$

$$= \frac{n}{n-1}mR(T_2 - T_1)$$

$$= \frac{n-\kappa}{(n-1)(\kappa - 1)}(p_1V_1) \left[\left(\frac{p_2}{p_1} \right)^{\frac{n-1}{n}} - 1 \right]$$

$$= \frac{n}{n-1}(p_1V_1) \left[\left(\frac{p_2}{p_1} \right)^{\frac{n-1}{n}} - 1 \right]$$
 $c_n = \frac{n-\kappa}{n-1}cv$

isotherm $W_{t,12} = (p_1V_1) \ln \left(\frac{p_2}{p_2} \right)$ $Q_{12} = -W_{t,12}$

Thermischer Wirkungsgrad
$$\eta_{th} = \frac{-w}{q_{cu}} = \frac{\text{Nutzen}}{\text{Aufwand}} = 1 - \frac{|q_{ab}|}{q_{cu}}$$

Isentroper Verdichterwirkungsgrad $\eta_{tV} = \frac{w_{t,12,rev}}{w_{t,12}} = \frac{h_{2,rev} - h_1}{h_2 - h_1} = \frac{T_{2,rev} - T_1}{T_2 - T_1}$

idealer Fall

Isentroper Turbinenwirkungsgrad $\eta_{tT} = \frac{w_{t,12}}{W_{t,12,rev}} = \frac{h_1 - h_2}{h_1 - h_{2,rev}} = \frac{T_1 - T_2}{T_1 - T_2, rev}$

Dampfkraftprozess Wirkungsgrad $n_{th} = 1 - \frac{|q_{ab}|}{q_{23} + q_{34} + q_{45}} = 1 - \frac{h_6 - h_1}{h_5 - h_2}$

Leistungszahl Kältemaschine $\varepsilon_{K(A)} = \frac{q_{cu}}{w} = \frac{Q_0}{w}$

Leistungszahl Kaltluftprozess $\varepsilon_{K} = \frac{q_0}{|q| - q_0} = \frac{q_0}{w_t} = \frac{h_1 - h_6}{h_2 - h_1}$

Linkslaufender Carnotprozess $\varepsilon_{curnot} = \frac{T}{T_h}$

Linkslaufender Carnotprozess $\varepsilon_{WP} = \frac{q}{|q| - q_0} = \frac{|q|}{w_t} = \frac{q_{2w}}{w} = \frac{h_2 - h_5}{h_2 - h_1} = 1 + \varepsilon_{K(A)}$

Verdichtungsverhältnis $\varepsilon = \frac{v_1}{v_2}$

Einspriztverhältniss $\varphi = \frac{v_4}{v_3}$

Temperaturverhältnis $\tau = \frac{T_3}{T_1}$

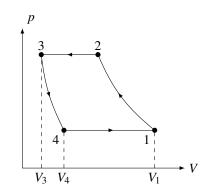
Verdrichtungsdruckverhältnis $\tau = \frac{P_2}{T_1}$

 $= au^{rac{\kappa}{2(\kappa-1)}}$

 π_{opt}

für Joule-Prozess

Kolbenverdichter



V1 = Maximales Zylindervolumen

V2 = Volumen nach Verdichtung

V3 =

V4 = Schädlicher Raum

$$\mu = \frac{V_1 - V_4}{V_1 - V_3}, \qquad \varepsilon_S = \frac{V_3}{V_1 - V_3}$$

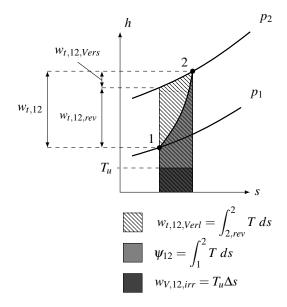
$$\mu = 1 - \varepsilon_S \left[\left(\frac{p_2}{p_1} \right)^{\frac{1}{n}} - 1 \right]$$

$$W_{t,12} = \int_1^2 V \, dp$$

$$= \underbrace{p_2 V_2}_{Ausschiebearbeit} - \underbrace{p_1 V_1}_{Einschiebearbeit} - \int_1^2 p \, dV$$

$$= \frac{n}{n-1} p_1 (V_1 - V_4) \left[\left(\frac{p_2}{p_1} \right)^{\frac{n-1}{n}} - \right]$$

Turboverdichter



Verdichter Wirkungsgrad

$$\eta_{sV} = \frac{w_{t,12,rev}}{w_{t,12}} = \frac{h_{2,rev} - h_1}{h_2 - h_1}$$

Verdichter wirkungsgrad (Ideales Gas, $c_p = \text{const.}$)

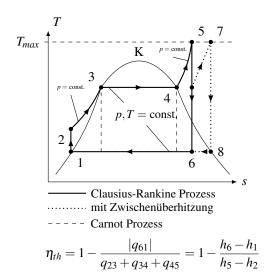
$$\eta_{sV} = \frac{T_{2,rev} - T_1}{T_2 - T_1}$$

Technische Verlustarbeit

$$w_{t,Verl,12} = w_{t,12} - w_{t,12,rev} = h_2 - h_{2,rev}$$

= $\int_{2,rev}^{2} T|_{p_2 = const.} ds$

17 Clausius-Rankine-Prozess



18 Eindimensionale Strömungsvorgänge

$$\chi = \frac{1}{p} = -\frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_{T}$$

$$c_{S}^{2} = \left(\frac{\partial p}{\partial \rho} \right)_{S}$$

$$c_{S}^{2} = \left(\frac{R}{c_{v}} + 1 \right) \left(v^{2} \frac{RT}{(v - b)^{2}} \right) - \frac{2a}{v} \leftarrow VdW$$

$$c_{S}^{2} = \kappa RT \leftarrow ideal$$

$$Ma = \frac{c}{c_{S}}$$

$$\frac{T_{0}}{T} = 1 + \frac{\kappa - 1}{2} \frac{c^{2}}{\kappa RT} = 1 + \frac{\kappa - 1}{2} Ma^{2}$$

$$\frac{p_{0}}{p} = \left(\frac{T_{0}}{T} \right)^{\frac{\kappa}{\kappa - 1}} = \left(1 + \frac{\kappa - 1}{2} Ma^{2} \right)^{\frac{\kappa}{\kappa - 1}}$$

$$\frac{\rho_{0}}{\rho} = \left(\frac{T_{0}}{T} \right)^{\frac{\kappa - 1}{\kappa}} = \left(1 + \frac{\kappa - 1}{2} Ma^{2} \right)^{\frac{\kappa - 1}{\kappa}}$$

$$\left(\frac{A}{A^{*}} \right)^{2} = \frac{1}{Ma^{2}} \left[\frac{2}{\kappa + 1} \left(1 + \frac{\kappa - 1}{2} Ma^{2} \right) \right]^{\frac{\kappa + 1}{\kappa - 1}}$$

$$h_2 - h_1 = \frac{1}{2}(p_2 - p_1)\left(\frac{1}{\rho_1} + \frac{1}{\rho_2}\right) = (p_2 - p_1)\frac{1}{2}(v_1 + v_2)$$

Stoßbeziehungen für ein ideales Gas

$$\begin{split} \frac{p_2}{p_1} &= \frac{2\kappa Ma^2 - (\kappa - 1)}{\kappa + 1} \\ \frac{\rho_2}{\rho_1} &= \frac{(\kappa + 1)Ma^2}{2 + (\kappa - 1)Ma^2} \\ \frac{T_2}{T_1} &= \frac{\left[2\kappa Ma^2 - (\kappa - 1)\left[2 + (\kappa - 1)Ma^2\right]}{(\kappa + 1)^2}Ma^2 \\ Ma_2^2 &= \frac{(\kappa - 1)(Ma_1^2 - 1) + (\kappa + 1)}{2\kappa(Ma_1^2 - 1) + (\kappa + 1)} \end{split}$$

Entropie über den senkrechten Verdichtungsstoß

$$s_2 - s_1 = c_v \ln\left(\frac{T_2}{T_1}\right) + R \ln\left(\frac{v_2}{v_1}\right)$$
$$= c_p \ln\left(\frac{T_2}{T_1}\right) + R \ln\left(\frac{p_2}{p_1}\right)$$

19 Feuchte Luft

$$x = \frac{m_{H_2O}}{m_L}$$

$$x = x_{D(ampf)} + x_{W(asser)} + x_{E(is)}$$

$$\varphi = \frac{p_D}{p_s}$$

$$x_D = \frac{m_d}{m_L} = \frac{R_L}{R_D} \frac{p_D}{p_L} = \frac{R_L}{R_D} \frac{p_D}{p - p_D} = 0.622 \frac{p_D}{p - p_D}$$

$$x_s = \frac{m_{D,max}}{m_L} = 0.622 \frac{p_s}{p - p_s} \rightarrow \text{für } \varphi = 1$$

$$\rho = \frac{p}{R_{ges}T} = \frac{1 + x}{R_L + xR_D} \frac{p}{T}$$

$$R_{ges} = \frac{R_L + xR_D}{1 + x}$$

$$h = c_{pL}t + x_D(c_{pD}t + r_D) + x_W c_W t + x_E(c_E t - r_E)$$

20 Chemische Reaktionen

$$\frac{dn_1}{v_1} = \frac{dn_2}{v_2} = \dots = d\lambda = .const$$

$$\sum_{k=1}^K \mu_k dn_k = \sum_{k=1}^K \mu_k (v_k d\lambda) = \sum_{k=1}^K \mu_k v_k = 0$$

$$\mu_i = \left(\frac{\partial U}{\partial n_i}\right)_{S,V} = \left(\frac{\partial H}{\partial n_i}\right)_{S,p} = \left(\frac{\partial F}{\partial n_i}\right)_{T,V} = \left(\frac{\partial G}{\partial n_i}\right)_{T,p}$$

$$\mu(p,T) = \mu(p^+,T) + R_m T \ln\left(\frac{p}{p^+}\right)$$

Massenwirkungsgesetz

$$\prod_{k=1}^{K} \psi_{k}^{v_{k}} = exp - \frac{1}{R_{m}T} \sum_{k=1}^{K} v_{k} \mu_{0k}(p, T)$$
$$= exp - \frac{1}{R_{m}T} \sum_{k=1}^{K} v_{k} G_{m,k}(p, T)$$

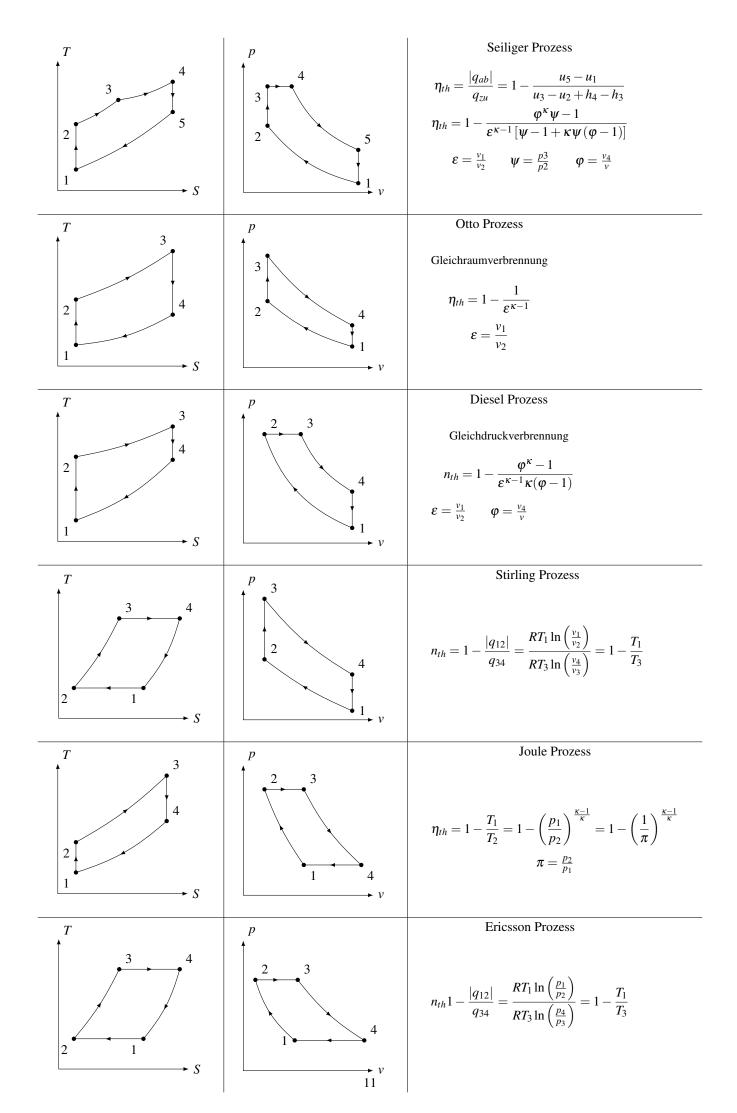
Gleichgewichtkonstante

$$K(p,T) = \prod_{k=1}^{K} \psi_k^{\nu_k}$$

$$K(p_2,T) = K(p_1,T) \left(\frac{p_1}{p_2}\right)^{\sum \nu_k}$$

$$\ln\left(\frac{K(p,T_2)}{K(p,T_1)}\right) = \frac{\Delta H_R}{R_m} \left(\frac{1}{T_1} - \frac{1}{T_2}\right) = \frac{\Delta H_R}{R_m} \frac{T_2 - T_1}{T_1 T_2}$$

$$\Delta H_R = \sum_{k=1}^{K} \nu_k H_{m,k}$$



Ideales Gas

	Isothermo	Isobare	Isochore	Isentrop	Polytrope
konstant:	${ m T}$	d	Λ	$\delta q = 0$	pv^n
	ı	ı	ı	$p_1 v_1^K = p_2 v_2^K$	$v_1^n = p_2 v_2^n$
	$p_1p_2=p_2v_2$	$\frac{v_1}{v_2} = \frac{T_1}{T_2}$	$\frac{p_1}{T_1} = \frac{p_2}{T_2}$	<u> </u>	$T_1 v_1^{n-1} = T_2 v_2^{n-1}$
	ı	ľ	$\mathcal{O}_{\mathbb{H}^n}$	$\frac{\frac{\kappa}{T_1^{\kappa-1}}}{p_1} = \frac{T_2^{\frac{\kappa}{\kappa-1}}}{p_2}$	$\frac{T_1^{n-1}}{p_1} = \frac{T_2^{n-1}}{p_2}$
p, ν	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$\nu = \nu_1$	$p = rac{p_1 v_1^K}{v^K}$	$p = \frac{p_1 v_1^n}{v^n}$
p,T	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$p = \frac{p_1}{T_1}T$	$p = rac{p_1}{T_1^{K-1}} T^{rac{K}{K-1}}$	$p = rac{p_1}{T_1^{n-1}} T^{rac{n}{n-1}}$
u, T	$T = T_1$	$ u = rac{ u_1}{T_1} T $	$\nu= u_1$	-1	$T = \frac{T_1 v_1^{n-1}}{v^{n-1}}$
q 12	$= p_1 v_1 \ln \frac{p_1}{p_2}$	$=c_p(T_2-T_1)$	$=c_{\nu}(T_2-T_1)$	0 =	$=c_{\nu}\frac{n-\kappa}{n-1}(T_2-T_1)$
WV,12	$=-q_{12}$	$=-p_1(\nu_2-\nu_1)$	0 =	$= \frac{p_1 v_1}{k-1} \left[\left(\frac{v_1}{v_1} \right)^{K-1} - 1 \right]$	$= \frac{p_1 v_1}{n-1} \left[\left(\frac{v_1}{v_2} \right)^{n-1} - 1 \right]$
$s_2 - s_1$	$= R \ln \left(\frac{p_1}{p_2} \right)$	$=c_p \ln \left(rac{T_2}{T_1} ight)$	$=c_{ u}\ln\left(rac{T_{2}}{T_{1}} ight)$	0 =	$= c_{\nu} \frac{n-\kappa}{n-1} \ln \left(\frac{T_2}{T_1} \right)$

Van-Der-Waals-Gas

	Isotherme	Isobare	Isochore	Isentrop
konst.	T	d	Λ	$\delta = 0$
	$(p_1 + \frac{a}{v^2})(v_1 - b) = (p_2 + \frac{a}{v^2})(v_2 - b)$	$\frac{RT_1}{v_1 - b} - \frac{a}{v_1^2} = \frac{RT_2}{v - b} - \frac{a}{v_2^2}$	$\frac{p_1 + \frac{a}{\sqrt{1}}}{T_1} = \frac{p_2 + \frac{a}{\sqrt{2}}}{T_2}$	$ (p_1 + \frac{a}{v^2})(v_1 - b) \frac{c_v + R}{c_v} $ $= (p + \frac{a}{v^2})(v_2 - b) \frac{c_v + R}{c_v}, $ $T_1(v_1 - b)^{R/c_v} = T_2(v_2 - b)^{R/c_v} $
p, ν	$p = (p + \frac{a}{v^2}) \frac{v_u}{v - b} - \frac{a}{v^2}$	$p = p_1$	$\nu = \nu_1$	$p = -\frac{a}{v^2} + \left(p_1 + \frac{a}{v^2}\right) \left(\frac{v_1 - b}{v_m}\right)^{\frac{v_v + R}{R}}$
p,T	$T=T_1$	$p = p_1$	$p=rac{T}{T_1}(p_1+rac{a}{v^2})-rac{a}{v_1^2}$	$p = \frac{T}{T_1}(p_1 + \frac{a}{v^2}) - \frac{a}{v_1^2} \left p = -\frac{a}{v^2} + (p_1 + \frac{a}{v^2}) \left(\frac{T}{T_1} \right)^{\frac{c_V + R}{R}} \right $
ν, T	$T=T_1$	$T = T_1 \frac{\nu - b}{\nu_1 - b} + \frac{a}{R} (\nu - b) \left(\frac{1}{\nu^2} - \frac{1}{\nu_1^2} \right)$	$v = v_1$	$T=T_1\left(rac{ u_1-b}{ u-b} ight)^{rac{R}{c u}}$
q 12	$=RT_1\ln\left(rac{ u_2-b}{ u_1-b} ight)$	$=rac{a}{ u_1}-rac{a}{ u_2}+c_ u(T_2-T_1)+p_1(u_2- u_1)\ =c_ u(T_2-T_1)$		0 =
WV,12	$=-RT_1\ln\left(rac{ u_2-b}{ u_1-b} ight)+rac{a}{ u_1}-rac{a}{ u_2}$	$=-p_1(\nu_2-\nu_1)$	0 =	$=rac{a}{v_1}-rac{a}{v_2}+c_{ u}(T_2-T_1)$
$s_2 - s_1$	$\left s_2 - s_1 \right = R \ln \left(\frac{v_2 - b}{v_1 - b} \right)$	$=c_ u \ln \left(rac{T_2}{T_1} ight) + R \ln \left(rac{ u_2 - b}{ u_1 - b} ight)$	$=c_ u \ln\left(rac{T_2}{T_1} ight)$	0 =

21 Stoffwerte einiger Gase

Bezeichnung	Symbol	Molmasse	Gaskonstante	Dichte	c_p	c_v	κ
		[kg/kmol]	[J/(kg K)]	[kg/m3]	[J/(kg K)]	[J/(kg,K)]	
Acetylen	C_2H_2	26.038	319.3	1.16	1616	1278	1.26
Ammoniak	NH_3	17.031	488.2	0.76	2056	1526	1.35
Argon	Ar	39.948	208.1	1.76	519	309	1.68
Äthan	C_2H_6	30.070	276.5	1.34	1650	1355	1.22
Butan	C_4H_10	58.124	143.0	2.67	1599	1410	1.13
Chlor	C_l2	56.108	117.3	3.17	473	343	1.38
Chlorwasserstoff	HCl	70.906	228.0	1.62	795	556	1.43
Helium	He	4.003	2077.0	0.18	5200	3124	1.66
Kohlendioxid	CO_2	44.010	188.9	1.95	816	618	1.32
Kohlenmonoxid	CO	28.010	296.8	1.23	1038	739	1.40
Luft	<u> </u>	28.964	287.1	1.28	1006	718	1.40
Methan	CH_4	16.043	518.3	0.71	2165	1638	1.32
Propan	C_3H_8	44.097	188.5	1.99	1549	1331	1.16
Sauerstoff	O_2	31.999	259.8	1.41	909	647	1.40
Stickstoff	N_2	28.013	296.8	1.23	1038	739	1.40
Wasserstoff	H_2	2.016	4124.2	0.09	14050	9926	1.42
Xenon	Xe	131.300	63.3	5.82	159	93	1.71

22 Stoffdaten einiger Stoffe

Name	chemische	Molmasse	Normal-	kritische	kritischer
Name	Formel	[kg/kmol]	siedepunkt [°C]	Temperatur [°C]	Druck [MPa]
Wasserstoff	H_2	2.02	-252.9	-240.0	1.32
Helium	Не	4.00	-268.9	-268.0	0.23
Ammoniak	NH_3	17.03	-33.3	132.3	11.33
Wasser	H_2O	18.02	100.0	373.9	22.06
	78%				
Luft	N ₂ 21%	28.96	-194.2	-140.4	3.84
	$O_2.1\%Ar.+$				
Kohlendioxid	CO_2	44.01	-78.4	31.0	7.38
Methan	CH_4	16.04	-161.5	-82.6	4.60
Äthan	C_2H_6	30.07	-88.6	32.2	4.87
Propan	C_3H_8	44.10	-42.1	96.7	4.25
R134a	CH_2FCF_3	102.03	-26.1	101.1	4.06

23 Zahlenwerte feuchte Luft

Bezeichnung	Formelzeichen	Zahlenwert	Dimension
Molmasse der Luft	ML	28,96	kg/ kmol
Molmasse des Wassers	MH2O	18,02	kg/ kmol
spezifische Gaskonstante der Luft	RL	0,287	kJ/ (kg K)
spezifische Gaskonstante des Dampfes	RD	0,461	kJ/ (kg K)
spezifische Wärmekapazität der Luft	cpL	1,006	kJ/ (kg K)
spezifische Wärmekapazität des Dampfes	cpD	1,92	kJ/ (kg K)
spezifische Wärmekapazität des Wassers	cW	4,182	kJ/ (kg K)
spezifische Wärmekapazität des Eises	cЕ	2,1	kJ/ (kg K)
Verdampfungsenthalpie des Wassers bei 0 °C	rD	2500	kJ/ kg
Schmelzenthalpie des Eises bei 0 °C	rE	334	kJ/ kg

24 Obskure Zusammenhänge

$$dV = \left(\frac{\partial V}{\partial T}\right)_{p} dT + \left(\frac{\partial V}{\partial p}\right)_{T,n} + \sum_{k=1}^{K} \left(\frac{\partial V}{\partial n_{k}}\right)_{T,p} dkn_{k}$$

$$dS = \left(\frac{nC_{p,m}}{T}\right) dT - \left(\frac{\partial V}{\partial T}\right)_{p,n} dp + \sum_{k=1}^{K} \left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n} dn_{k}$$

$$dU = \left[nC_{p,m} - p\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dT - \left[p\left(\frac{\partial V}{\partial p}\right)_{T,n} + T\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dp + \sum_{k=1}^{K} \left[\mu_{k} - T\left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n} - p\left(\frac{\partial V}{\partial n_{k}}\right)_{T,p,n}\right] dn_{k}$$

$$dH = nC_{p,m}dT + \left[VT\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] + \sum_{k=1}^{K} \left[\mu_{k} - T\left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n}\right] dn_{k}$$

$$dF = -\left[S + p\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dT - p\left(\frac{\partial V}{\partial p}\right)_{T,n} dp + \sum_{k=1}^{K} \left[\mu_{k} - p\left(\frac{\partial V}{\partial n_{k}}\right)_{T,p}\right] dn_{k}$$

$$\left(\frac{\partial C_{p,m}}{\partial p}\right)_{T,\psi_{j}} = T\frac{\partial}{\partial p} \left[\left(\frac{\partial S_{m}}{\partial T}\right)_{p,\psi_{j}}\right]_{T,\psi_{j}} = T\frac{\partial}{\partial T} \left[\left(\frac{\partial S_{m}}{\partial p}\right)_{T,\psi_{j}}\right]_{p,\psi_{j}} = -T\left(\frac{\partial^{2}V_{m}}{\partial T}\right)_{p,\psi_{j}}$$

$$C_{p,m} = (C_{p,m})_{\text{ideales Gas}} - T\int_{0}^{p} \left(\frac{\partial^{2}V_{m}}{\partial T^{2}}\right)_{p,\psi_{j}} d\tilde{v}$$

$$C_{v,m} = (C_{v,m})_{\text{ideales Gas}} - T\int_{0}^{V_{m}} \left(\frac{\partial^{2}P}{\partial T^{2}}\right)_{p,\psi_{j}} d\tilde{v}$$

25 Dinge die man eigentlich wissen sollte

$$1J = 1W = 1Nm$$
 $E_{kin} = \frac{1}{2}mc^2$
 $E_{rot} = \frac{1}{2}I\omega^2$
 $E_{Feder} = \frac{1}{2}kx^2$
 $E_{pot} = mgz$
 $E_{Kondensator} = \frac{1}{2}C\left(\frac{Q_e}{C}\right)^2$
 $E_{Spule} = \frac{1}{2}LI^2$
 $E_{Elelektrisch} = UA$

		L .	Etetektrisch	- 07 1	
$10^1 = 1$					
$10^1 = 10$	$10^{-1} = 0.1$				
$10^2 = 100$	$10^{-2} = 0.01$	m^2	dm^2	cm^2	mm^2
$10^3 = 1000$	$10^{-4} = 0.001$	1	10^{2}	10^{4}	10^{6}
$10^4 = 10000$ $10^4 = 10000$	$10^{-4} = 0.0001$	10^{-2}	1	10^{2}	10^{4}
$10^5 = 100000$ $10^5 = 100000$	$10^{-5} = 0.0001$ $10^{-5} = 0.00001$	10^{-4}	10^{-2}	1	10^{2}
$10^6 = 1000000$	$10^{-6} = 0.00001$	10^{-6}	10^{-4}	10^{2}	1
$10^7 = 10000s000$	$10^{-7} = 0.0000001$				
$10^8 = 100000000$	$10^{-8} = 0.00000001$	m^3	dm^3	cm^3	mm^3
$10^9 = 1000000000$	$10^{-9} = 0.000000001$	1	10^{3}	10^{6}	10^{9}
$10^10 = 10000000000$	$10^{-10} = 0.0000000001$	10^{-3}	1	10^{3}	10^{6}
$10^11 = 100000000000$	$10^{-11} = 0.00000000001$	10^{-6}	10^{-3}	1	10^{3}
$10^12 = 1000\ 000\ 000\ 000$	$10^{-12} = 0.000000000001$	10^{-9}	10^{-6}	10^{3}	1
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