# Thermodynamik Formelsammlung

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$$\frac{d}{dt}\left\{U+m\left(\frac{c^2}{2}+gz\right)\right\} = \sum_{j}\left[\dot{m}_{j}\left(h+\frac{c^2}{2}+gz\right)_{i}\right] + \sum_{l}\left(\dot{Q}_{l}\right)_{l} + \sum_{i}\left(\dot{W}_{l}\right)_{i} - p\frac{dV}{dt}$$

#### 1 Nomenklatur

 $\mathbf{An} = \text{Anergie}[\mathbf{J}]$ 

 $c_s = Schallgeschwindigkeit[m/s]$ 

 $\mathbf{c_p} = \text{Spezifische Wärmekapazität dp} = 0 [J/kg*K]$ 

 $\mathbf{c_v} = \text{Spezifische Wärmekapazität dv} = 0 [J/kg*K]$ 

 $\mathbf{E} = \text{Energie}[\mathbf{J}]$ 

 $\mathbf{E}\mathbf{x} = -\mathbf{W}_{\mathbf{e}\mathbf{x}} = \mathrm{Exergie}[\mathbf{J}]$ 

 $\mathbf{F} = Kraft[N]$ 

 $\mathbf{F} = \mathbf{U} - \mathbf{TS} = \text{Freie Energie}[\mathbf{J}]$ 

 $\mathbf{f} = \mathbf{u} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Energie}[J/kg]$ 

 $\mathbf{f} = \text{Fugazität}[Pa]$ 

G = H - TS = Freie Enthalpie[J]

 $\mathbf{g} = \mathbf{h} - \mathbf{T}\mathbf{s} = \text{Spezifische freie Enthalpie}[J/kg]$ 

 $\mathbf{g} = \text{Erdbeschleunigung}[\text{m/s}^2]$ 

 $\mathbf{H} = \mathbf{U} + \mathbf{p}\mathbf{V} = \text{Enthalpie}[\mathbf{J}]$ 

 $\mathbf{h} = \mathbf{u} + \mathbf{p}\mathbf{v} = \text{Spezifische Enthalpie}[J/kg]$ 

 $\Delta$ **Hg** = Molare Reaktionsenthalpie

**K** = Konstante des Massenwirkungsgesetztes[-]

 $\mathbf{M} = \text{Molmasse[kg/mol]}$ 

 $\dot{\mathbf{m}} = \text{Massenstrom}[\text{kg/s}]$ 

 $\mathbf{m}' = \text{Masse in der flüssigen Phase[kg]}$ 

 $\mathbf{m}'' = \text{Masse in der gasförmigen Phase[kg]}$ 

 $Ma = c/c_s = Machzahl[-]$ 

 $\mathbf{n} = \mathbf{m}/\mathbf{M} = \text{Molzahl[mol]}$ 

**n** = Polytropenexponent[-]

 $\mathbf{P_t} = \text{technische Leistung}[\mathbf{W}]$ 

 $\mathbf{Q} = \text{W\"{a}rme}[J]$ 

 $\dot{\mathbf{Q}} = \text{Wärmestrom}[\mathbf{W}]$ 

q = Spezifische Wärme[J/kg]

 $\mathbf{r} = \text{Spezifische Verdampfungsenthalpie}[J/kg]$ 

 $\mathbf{R} = \text{Gaskonstante}[J/(\text{kg K})]$ 

 $\mathbf{R}_{\mathbf{m}} = \text{Universelle Gaskonstante}[J/(\text{mol } K)]$ 

S = Entropie[J/K]

s = Spezifische Entropie[J/(kg K)]

T = Temperatur[K]

 $\mathbf{t} = \text{Zeit}[s]$ 

 $\mathbf{t} = \text{Temperatur}[^{\circ}\text{C}]$ 

T = Sättigungstemperatur[K]

U = Innere Energie[J]

 $\mathbf{u} = \text{Spezifische innere Energie [J/kg]}$ 

 $V = Volumen[m^3]$ 

 $\mathbf{v} = \text{Spezifisches Volumen}[\text{m}^3/\text{kg}]$ 

 $V_m = Molares Volumen[m<sup>3</sup>/mol]$ 

 $\mathbf{W} = \text{Arbeit}[J]$ 

 $\mathbf{w} = \text{Spezifische Arbeit}[J/kg]$ 

 $\mathbf{W}_{\mathbf{V}} = \text{Volumen}$ änderungsarbeit[J]

 $\mathbf{W_{el}} = \text{Elektrische Arbeit[J]}$ 

 $\mathbf{W}_{\mathbf{w}} = \text{Wellenarbeit}[\mathbf{J}]$ 

 $W_{diss} = Dissipations arbeit[J]$ 

 $\mathbf{W_t} = \text{Technische Arbeit}[\mathbf{J}]$ 

 $\mathbf{W}_{Virrev} = \text{Arbeits verlust durch Irreversibilität}[J]$ 

 $\mathbf{x} = \frac{m''}{m' + m''} = \text{Dampfanteil[-]}$ 

 $\mathbf{x} = \frac{m_{H_2O}}{m_L} = \text{Wassergehalt}$ 

 $\mathbf{Z} = \text{Allgemeine extensive Zustandsgrößen}[\mathbf{Z}]$ 

z = Allgemeine

 $\beta$  = Isobarer Ausdehnungskoeffizient[1/K]

 $\gamma$  = Isochorer Spannungskoeffizient[1/K]

 $\delta_{\rm T} = {\rm Isothermer\ Drosselkoeffizient[m^3/kg]}$ 

 $\delta_{\mathbf{h}} = \text{Isenthalper Drosselkoeffizient}[\text{Ks}^2\text{m/kg}]$ 

 $\varepsilon$  = Leistungsziffer[-]

 $\varepsilon = \text{Verdichtungsverhältnis}[-]$ 

 $\eta_{\rm th} = \text{Thermischer Wirkungsgrad}[-]$ 

 $\eta_{\text{mech}} = \text{Mechanischer Wirkungsgrad[-]}$ 

 $\kappa = \text{Adiabaten- oder Isentropenexponent}[-]$ 

 $\lambda = \text{Reaktionslaufzahl}[-]$ 

 $\mu_i$  = Chemisches Potential[J/mol]

 $v_i$  = Stöchiometrische Koeffizienten[-]

 $\xi_{\mathbf{i}} = \text{Masseanteil}[-]$ 

 $\pi = \text{Druckverhältnis}[-]$ 

 $\rho = \text{Dichte}[\text{kg/m}^3]$ 

 $\tau =$  Temperaturverhältnis[-]

 $\phi$  = Relative Feuchte[-]

 $\phi = \text{Einspritzverhältnis}[-]$ 

 $\xi$  = Isothermer Kompressibilitätskoeffizient[m²/N]

 $\Psi = \text{Dissipationsenergie}[J]$ 

 $\psi = \text{Spezifische Dissipationsenergie}[J]$ 

 $\psi$  = Drucksteigerungsverhältnis[-]

 $\psi_i = Molanteil[-]$ 

# 2 Grundbegriffe

#### Systeme

- Abgeschlossenes System kein Stoff oder Energietransport
- Geschlossenes System kein Stofftransport
- Adiabates System kein  $\Delta q$ , aber Masse und Arbeit.
- Offenes System Stoff und Energietransport
- Stationäres System  $\rightarrow \Delta U = 0$

## Messgrößen

- Prozessgrößen sind wegabhängig (eg. Arbeit, Wärme)
- Zustandsgrößen sind wegunabhängig (eg. Volumen, Druck)
- Extensive Zustandsgrößen sind abhängig von der Masse des Systems (V, m, H, S, F, G, E)
- Intensive Zustandsgrößen sind unabhängig von der Masse des Systems (T, p)

#### Zustandsgleichungen

- Thermisch  $\rightarrow f(p, V, T) = 0$
- Kalorisch  $\rightarrow f(U, V, T) = 0$ , U = U(V, T), u = u(v, T)

#### Hauptsätze

- Temperatur existiert, ihre Gleichheit ist notwendige Voraussetzung für das thermische Gleichgewicht von zwei Systemen.
- 1: Energie existiert, sie ist für abgeschlossene Systeme konstant.
- 2: Entropie existiert, sie wird bei allen irreversiblen Prozessen erzeugt.  $dS = \frac{\delta Q_{rev}}{T}$
- 3: 0K existiert, bei dieser Temperatur ist die Entropie = 0

#### 3 Basisformeln

$$dS = \frac{Q_{rev}}{T} + S_{prod}$$

$$dS = \frac{Q_{rev}}{T}$$

$$dS = \frac{\delta Q_{rev}}{T}$$

$$F = U - TS$$

$$G = H - ST$$

$$W = -\int p \, dV$$

$$dU = mc_v dT$$

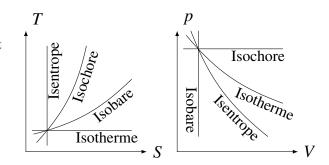
$$dS_{prod} = \frac{\Psi}{T}$$

$$\Psi = \int_1^2 T \, dS_{prod}$$

$$W_{ir} = \frac{T_u}{T} \Psi$$

$$p_1 = p_a + \frac{\varphi_1 - \varphi_a}{\varphi_b - \varphi_a} (p_b - p_a)$$

#### 4 Iso



### 5 Gibbs

$$dU = Tds - pdV + \sum_{k=1}^{K} \mu_k dn_k$$

$$dG = -SdT + Vdp + \sum_{k=1}^{K} \mu_k dn_k$$

$$dH = TdS + Vdp + \sum_{k=1}^{K} \mu_k dn_k$$

$$dF = -SdT - pdV + \sum_{k=1}^{K} \mu_k dn_k$$

$$dU = \left(\frac{\partial U}{\partial S}\right)_V dS + \left(\frac{\partial U}{\partial V}\right)_S dV + \sum_{k=1}^{K} \left(\frac{\partial U}{\partial n_k}\right)_S dn_k$$

# 6 Thermodynamische Beziehungen

$$T = \left(\frac{\partial U}{\partial S}\right)_{V} = T(S, V) \qquad -S = \left(\frac{\partial F}{\partial T}\right)_{V} = S(T, V)$$

$$T = \left(\frac{\partial H}{\partial S}\right)_{p} = T(S, p) \qquad -S = \left(\frac{\partial G}{\partial T}\right)_{p} = S(T, p)$$

$$p = -\left(\frac{\partial U}{\partial V}\right)_{S} = p(V, S) \qquad V = \left(\frac{\partial G}{\partial p}\right)_{T} = V(p, T)$$

$$-p = \left(\frac{\partial F}{\partial V}\right)_{T} = p(T, V) \qquad \mu = \left(\frac{\partial U}{\partial n}\right)_{S, V} = \mu(S, V, n)$$

# 7 Guggenheim

$$\underbrace{\frac{d}{dt} \left\{ U + m \left( \frac{c^2}{2} + gz \right) \right\}}_{j} = \underbrace{\sum_{j} \left[ \dot{m}_{j} \left( h + \frac{c^2}{2} + gz \right)_{j} \right]}_{Geschlossenes System -> 0} + \underbrace{\sum_{l} \left( \dot{Q}_{t} \right)_{l}}_{Keine Wärmestrom -> 0} + \underbrace{\sum_{l} \left( \dot{W}_{t} \right)_{i}}_{Keine Leistung -> 0} - \underbrace{\sum_{l} \left( \dot{W}_{t} \right)_{i}}_{Keine Volumenänderung -> 0} + \underbrace{\sum_{l} \left( \dot{W}_{t} \right)_{i}}_{Kein$$

#### 8 Maxwell

$$\left(\frac{\partial T}{\partial p}\right)_{S,n_j} = \left(\frac{\partial V}{\partial S}\right)_{p,n_j} \\
\left(\frac{\partial S}{\partial V}\right)_{T,n_j} = \left(\frac{\partial p}{\partial T}\right)_{V,n_j} \\
\left(\frac{\partial S}{\partial p}\right)_{T,n_j} = -\left(\frac{\partial V}{\partial T}\right)_{p,n_j} \\
\left(\frac{\partial \mu_i}{\partial T}\right)_{p,n_j} = -\left(\frac{\partial S}{\partial n_i}\right)_{T,p,n_j \neq n_i} \\
\left(\frac{\partial \mu_i}{\partial p}\right)_{T,n_i} = \left(\frac{\partial V}{\partial n_i}\right)_{T,p,n_i \neq n_j} \\$$

# 9 Ideales Gas

pV = mRT

$$pv = RT$$

$$pV = nR_mT$$

$$\beta = \frac{1}{T}$$

$$\gamma = \frac{1}{T}$$

$$\chi = \frac{1}{p}$$

$$\beta = p\gamma\chi$$

$$R_m = 8,3143 \left[ \frac{kJ}{kmolK} \right]$$

$$R = c_p - c_v$$

$$R = \frac{R_m}{M}$$

$$U - U_0 = mc_v(T - T_0) \quad \leftarrow \text{Für } c_p \text{ und } c_v \text{ const.}$$

$$s - s_0 = R \ln \left( \frac{v}{v_0} \right) \quad + c_v \ln \left( \frac{T}{T_0} \right)$$

$$= c_v \ln \left( \frac{p}{p_0} \right) \quad + c_p \ln \left( \frac{v}{v_0} \right)$$

$$= c_p \ln \left( \frac{T}{T_0} \right) \quad - R \ln \left( \frac{p}{p_0} \right)$$

$$\beta = \frac{1}{T} = \frac{1}{V} \left( \frac{\partial V}{\partial T} \right)_p = \frac{1}{V} \left( \frac{\partial v}{\partial T} \right)_p = -\frac{1}{\rho} \left( \frac{\partial \rho}{\partial T} \right)_p$$

$$\gamma = \frac{1}{T} = \frac{1}{p} \left( \frac{\partial p}{\partial T} \right)_V$$

$$\chi = \frac{1}{p} = -\frac{1}{V} \left( \frac{\partial V}{\partial p} \right)_T = -\frac{1}{V} \left( \frac{\partial V}{\partial p} \right)_T$$

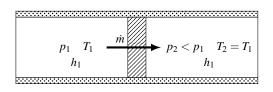
$$u_2 - u_1 = \int_{T_1}^{T_2} c_v(T) dT$$

$$U_2 - U_1 = Q_{12} + W_{V,12}$$

#### 10 Van-der-Waals

$$\begin{split} \left(p + \frac{a}{v^2}\right)(v - b) &= RT \\ \left(\overline{p} + \frac{3}{\overline{v^2}}\right)(3\overline{v} - 1) &= 8\overline{T} \\ \overline{p} &= \frac{p}{p_K}, \quad \overline{v} = \frac{v}{v_K}, \quad \overline{T} = \frac{T}{T_K} \\ p_K &= \frac{a}{27b^2}, \quad T_K = \frac{8}{27} \frac{a}{b} \frac{1}{R}, \\ a &= 3p_K v_K^2, \quad b = \frac{v_K}{3}, \quad \frac{p_K v_K}{RT_K} = \frac{3}{8} \\ \beta &= \frac{(v - b)Rv^2}{RTv^3 - 2a(v - b)^2} \\ \gamma &= \frac{Rv^2}{RTv^3 - 2a(v - b)^2} \\ \chi &= \frac{(v - b)^2 v^2}{RTv^3 - 2a(v - b)^2} \\ du &= \frac{a}{v^2} dv + c_v(T) dT \\ u - u_0 &= \left(\frac{a}{v_0} - \frac{a}{v}\right) + \int_{T_0}^T c_v(\tilde{T}) d\tilde{T} \\ u - u_0 &= \left(\frac{a}{v_0} - \frac{a}{v}\right) + c_v(T - T_0) \leftarrow \text{für } c_v = \text{const.} \\ c_p - c_v &= \frac{Tv\beta^2}{\chi} \\ s - s_0 &= c_v \ln\left(\frac{T}{T_0}\right) + R\ln\left(\frac{v - b}{v_0 - b}\right) \\ h_2 - h_1 &= \frac{1}{2}(p_2 - p_1)\left(\frac{1}{\rho_1} + \frac{1}{\rho_2}\right) \end{split}$$

# 11 Adiabate Drosselung



$$h + \frac{c^2}{2} + gz = \text{const.}$$

$$dh = 0, \quad T_1 = T_2$$

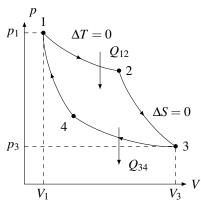
$$\delta_h = \left(\frac{\partial T}{\partial p}\right)_h = -\frac{v}{c_p}(1 - \beta T)$$

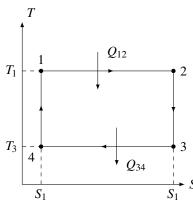
$$\delta_T = \left(\frac{\partial h}{\partial p}\right)_T$$

$$s_2 - s_1 = R \ln\left(\frac{v_2}{v_1}\right) = R \ln\left(\frac{p_1}{p_2}\right)$$

#### 12 Carnot

$$\begin{split} &\eta_{th} = 1 - \frac{-Q_{34}}{Q_{12}} = 1 - \frac{T_3(S_3 - S_4)}{T_1(S_2 - S_1)} = 1 - \frac{T_1}{T_3} \\ &\frac{Q_{12}}{T_1} + \frac{Q_{34}}{T_3} = 0 \\ &\Delta S_{ges} = -Q_{34} \left( \frac{1}{T_{KK}} - \frac{T_1}{T_3} \frac{1}{T_{HK}} \right) \end{split}$$





#### 13 Gemische Idealer Gase

$$\xi_{i} = \frac{m_{i}}{m}, \quad \psi_{i} = \frac{n_{i}}{n}, \quad p_{i} = \psi_{i}p$$

$$\xi_{i} = \frac{M_{i}n_{i}}{\sum_{k=1}^{K} M_{k}n_{k}} = \frac{M_{i}}{M_{G}} \Psi$$

$$p_{i}V = m_{i}R_{i}T, \quad p_{i}V = n_{i}R_{m}T, \quad pV = mR_{G}T$$

$$\sum_{k=1}^{K} p_{k} = p$$

$$R_{G} = \frac{1}{m} \sum_{k=1}^{K} m_{k}R_{k} = \sum_{k=1}^{K} \xi_{k}R_{k}$$

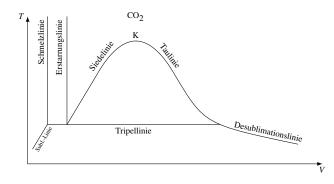
$$U_{G} = \sum_{k=1}^{K} U_{k} = \sum_{k=1}^{K} m_{k}u_{k} = \sum_{k=1}^{K} c_{vk}m_{k}T \leftarrow c_{v} = \text{const}$$

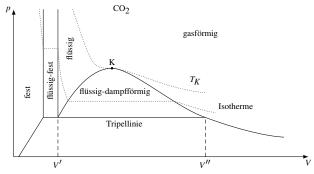
$$H_{G} = \sum_{k=1}^{K} H_{k} = \sum_{k=1}^{K} m_{k}h_{k} = \sum_{k=1}^{K} c_{pk}m_{k}T \leftarrow c_{p} = \text{const}.$$

$$c_{vG} = \sum_{k=1}^{K} c_{vk}\xi_{k}, \quad c_{pG} = \sum_{k=1}^{K} c_{pk}\xi_{k}$$

$$S_{2} - S_{1} = R_{m} \left( n \ln n - \sum_{k=1}^{K} n_{k} \ln n_{k} \right)$$

## 14 Nassdampf





$$v = (1 - x)v' + xv''$$

$$v = v' + (v'' - v')x$$

$$u = (1 - x)u' + xu''$$

$$u = u' + (u'' - u')x$$

$$h = (1 - x)h' + xh''$$

$$h = h' + (h'' - h')x$$

$$T' = T''$$

$$g' = g''$$

$$dg' = v'dp' - s'dT'$$

$$dg'' = v''dp'' - s''dT''$$

$$dg'' = dg''$$

$$dg' = dg''$$

$$dg' = dg''$$

$$dg' = dg''$$

$$df = \frac{s'' - s'}{v'' - v'}$$

$$\frac{dp}{dT} = \frac{1}{T} \frac{h'' - h'}{v'' - v'}$$

$$r = h'' - h' = T(s'' - s')$$

## 15 Realer Stoff im Nassdampfgebiet

Isobare Zustandsänderung

$$q_{12} = T(s_2 - s_1)$$

$$= T(s'' - s')(x_2 - x_1)$$

$$w_{V,12} = -\int_1^2 p \, dv$$

$$= -p(v_2 - v_1) = -p(v'' - v')(x_2 - x_1)$$

Isochore Zustandsänderung

$$q_{12} = u_2 - u_1 = u'_2 + x_2 \left( u''_2 - u'_2 \right) - u'_1 - x_1 \left( u''_1 - u'_1 \right)$$

Adiabate Zustandsänderung

$$w_{V,12} = u_2 - u_1 = u_2' + x_2 \left(u_2'' - u_2'\right) - u_1' - x_1 \left(u_1'' - u_1'\right)$$

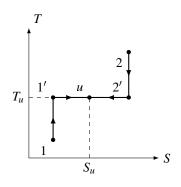
EntropieÄnderung während des Mischvorgangs

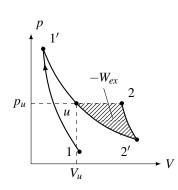
$$S_2 - S_2 = R_m \left( n \ln n - \sum_i n_i \ln n_i \right)$$

## 16 Maximale Arbeit und Exergie

Maximal nutzbare Arbeit → isentrop, reibungsfrei

 $1 \rightarrow 1'$ : isentrop auf  $T_u$  $1' \rightarrow u$ : isotherm auf u





$$-\dot{W}_{ex} = -(\dot{W}_{t})_{rev} = -\frac{d}{dt} \left( U + m \left( \frac{c^{2}}{2} + gz \right) + p_{u}V - T_{u}S \right) + \sum_{i=1}^{K} \left( \dot{m}_{j} \left( h + \frac{c^{2}}{2} + gz - T_{s} \right) \right) + \sum_{l=1}^{K} \left( 1 - \frac{T_{u}}{T} \right) \dot{Q}_{l}$$

Die Exergie der Enthalpie (offenes, stationäres System)

$$-\dot{W}_{ex,1u} = \dot{m}(h_1 - h_u - T_u(s_1 - s_u))$$

Die Exergie der inneren Energie (geschlossenes, instationäres System)

$$\begin{split} -\dot{W}_{ex} &= -\frac{d}{dt}(U + p_u V - T_u S) \\ -\dot{W}_{ex,1u} &= U_1 - U_u - p_u (V_1 - V_u) - T_u (S_1 - S_u) \\ -\dot{W}_{ex,1u} &= H_1 - (p_1 - p_u) V_1 - H_u - T_u (S_1 - S_u) \end{split}$$

Für Ideales Gas

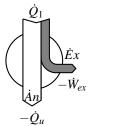
$$\begin{split} -W_{ex} &= mc_v(T_1 - T_u) + p_u(V_1 - V_u) - T_u m \left(c_p \ln\left(\frac{T_1}{T_u}\right) - R_i \ln\left(\frac{p_1}{p_u}\right)\right) \\ -W_{ex} &= m \left[c_p(T_1 - T_u) - T_u c_p \ln\left(\frac{T_1}{T_u}\right)\right] \leftarrow \text{isobar} \end{split}$$

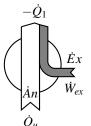
Dampf/Luftdruckkammer

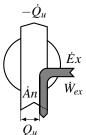
$$-W_{ex,1u} = m_1[u_1 - u_u + p_u(v_1 - v_u) - T_u(s_1 - s_u)]$$

Die Exergie der Wärme (geschlossenes, stationäres System)

$$-\dot{W}_{ex} = \left(1 - \frac{T_u}{T_1}\right)\dot{Q}_1 = \eta_{th,C}\dot{Q}_1$$



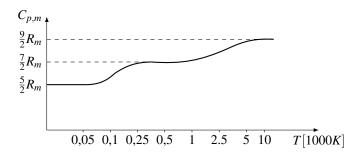




WärmekraftprozessWärmepumpenprozess

Kälteprozess

## 17 Wärmekapazität



$$C_{v,m} = \frac{1}{\kappa - 1} R_m \qquad C_{p,m} = \frac{\kappa}{\kappa - 1} r_m$$

$$c_v = \frac{1}{\kappa - 1} R_j \qquad c_p = \frac{\kappa}{\kappa - 1} R_j$$

$$\kappa = \frac{c_p}{c_v} \qquad R = c_p - c_v$$

$$R = \frac{R_m}{M} \qquad R_m = 8,3143 \left[ \frac{kJ}{kmolK} \right]$$

$$C_{v,m} = \underbrace{3 + \frac{R_m}{2}}_{\text{translatorisch}} + \underbrace{\frac{n_{\text{rot}}R_m}{2}}_{\text{rotatorisch}} + \underbrace{\frac{R_M(3n_{\text{Atome}} - 3 - n_{rot})}_{\text{vibratorisch}}}_{\text{Relevant ab: } T \approx 10^4 K}$$

## 18 Technische Anwendung

adiabat 
$$(c_p = const.)$$
  $W_{t,12} = mc_p(T_2 - T_1) = \frac{\kappa}{\kappa - 1}(p_2V_2 - p_1V_1)$   $Q_{12} = 0$ 

reversibel adiabat  $\kappa = const.$   $W_{t,12} = \frac{\kappa}{\kappa - 1}(p_1V_1) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{\kappa - 1}{\kappa}} - 1 \right]$   $Q_{12} = 0$ 

irreversibel adiabat als Polytrope  $n > \kappa; n, \kappa = const.$   $W_{t,12} = \frac{\kappa}{\kappa - 1}(p_1V_1) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{n - 1}{n}} - 1 \right]$   $Q_{12} = 0$ 
 $v_{t,12} = \frac{\kappa}{\kappa - 1}(p_1V_1) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{n - 1}{n}} - 1 \right]$   $Q_{12} = mc_n(T_2 - T_1)$ 
 $v_{t,12} = \frac{n}{n - 1}(p_2V_2 - p_1V_1)$   $v_{t,12} = \frac{n}{n - 1}(p_2V_2 - p_1V_1)$   $v_{t,12} = \frac{n}{n - 1}(p_1V_1) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{n - 1}{n}} - 1 \right]$   $v_{t,12} = \frac{n}{n - 1}(p_1V_1) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{n - 1}{n}} - 1 \right]$   $v_{t,12} = \frac{n - \kappa}{n - 1}cv$ 

isotherm  $v_{t,12} = (p_1V_1) \ln \left( \frac{p_2}{p_2} \right)$   $v_{t,12} = -v_{t,12}$ 

Thermischer Wirkungsgrad 
$$\eta_{th} = \frac{-w}{q_{2tt}} = \frac{\text{Nutzen}}{\text{Aufwand}} = 1 - \frac{|q_{ab}|}{q_{2tt}}$$

Isentroper Verdichterwirkungsgrad  $\eta_{tV} = \frac{w_{t,12,rer}}{w_{t,12}} = \frac{h_{2,rer} - h_1}{h_2 - h_1} = \frac{T_{2,rer} - T_1}{T_2 - T_1}$ 

idealer Fall

Isentroper Turbinenwirkungsgrad  $\eta_{tV} = \frac{w_{t,12,rer}}{w_{t,12,rer}} = \frac{h_1 - h_2}{h_1 - h_{2,rer}} = \frac{T_1 - T_2}{T_1 - T_2 - T_1}$ 

idealer Fall

Isentroper Turbinenwirkungsgrad  $\eta_{tV} = \frac{w_{t,12,rer}}{w_{t,12,rer}} = \frac{h_1 - h_2}{h_1 - h_{2,rer}} = \frac{T_1 - T_2}{T_1 - T_{2,rer}}$ 

Dampfkraftprozess Wirkungsgrad  $\eta_{th} = 1 - \frac{|q_{6t}|}{q_{23} + q_{34} + q_{45}} = 1 - \frac{h_6 - h_1}{h_5 - h_2}$ 

Leistungszahl Kältluftprozess  $\varepsilon_K = \frac{q_{2tt}}{w} = \frac{Q_0}{w}$ 

Leistungszahl Kaltdampfprozess  $\varepsilon_K = \frac{q_0}{|q| - q_0} = \frac{q_0}{w_t} = \frac{h_1 - h_0}{h_2 - h_1}$ 

Linkslaufender Carnotprozess  $\varepsilon_{cornot} = \frac{T_{1}}{T_{1} - T_{K}}$ 

Leistungszahl Wärmepumpe  $\varepsilon_{WP} = \frac{q}{|q| - q_0} = \frac{|q|}{w_t} = \frac{q_{2tt}}{w} = \frac{h_2 - h_3}{h_2 - h_1} = 1 + \varepsilon_{K(A)}$ 

Arbeit der Enthalpie  $W_t = Q = mdh = mcpdT$ 

Verdichtungsverhältnis  $\varepsilon = \frac{v_1}{v_2}$ 

Einspritzverhältniss  $\varphi = \frac{v_3}{v_3}$ 

Einspritzverhältniss  $\varphi = \frac{v_3}{v_3}$ 

Temperaturverhältnis  $\tau = \frac{T_1}{T_1}$ 

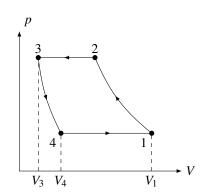
Verdrichtungsdruckverhältnis  $\tau = \frac{p_2}{p_1}$ 

 $= au^{rac{\kappa}{2(\kappa-1)}}$ 

 $\pi_{opt}$ 

für Joule-Prozess

#### Kolbenverdichter



V1 = Maximales Zylindervolumen

*V*2 = Volumen nach Verdichtung

V3 =

V4 = Schädlicher Raum

$$\mu = \frac{V_1 - V_4}{V_1 - V_3}, \qquad \varepsilon_S = \frac{V_3}{V_1 - V_3}$$

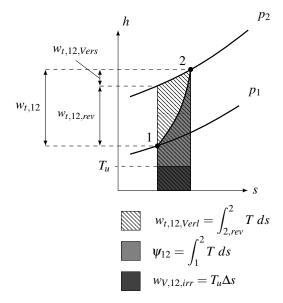
$$\mu = 1 - \varepsilon_S \left[ \left( \frac{p_2}{p_1} \right)^{\frac{1}{n}} - 1 \right]$$

$$W_{t,12} = \int_1^2 V \, dp$$

$$= \underbrace{p_2 V_2}_{Ausschiebearbeit} - \underbrace{p_1 V_1}_{Einschiebearbeit} - \int_1^2 p \, dV$$

$$= \frac{n}{n - 1} p_1 (V_1 - V_4) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{n - 1}{n}} - \right]$$

#### Turboverdichter



Verdichter Wirkungsgrad

$$\eta_{sV} = \frac{w_{t,12,rev}}{w_{t,12}} = \frac{h_{2,rev} - h_1}{h_2 - h_1}$$

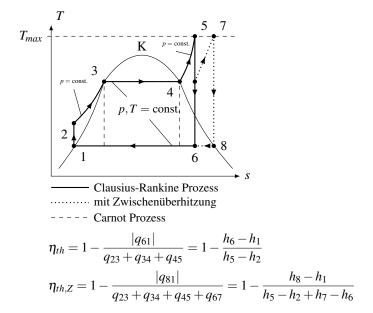
Verdichter wirkungsgrad (Ideales Gas,  $c_p = \text{const.}$ )

$$\eta_{sV} = \frac{T_{2,rev} - T_1}{T_2 - T_1}$$

Technische Verlustarbeit

$$w_{t,Verl,12} = w_{t,12} - w_{t,12,rev} = h_2 - h_{2,rev}$$
  
=  $\int_{2,rev}^{2} T|_{p_2 = const.} ds$ 

#### 19 Clausius-Rankine-Prozess



# 20 Eindimensionale Strömungsvorgänge

$$\chi = \frac{1}{p} = -\frac{1}{V} \left( \frac{\partial V}{\partial p} \right)_{T}$$

$$c_{S}^{2} = \left( \frac{\partial p}{\partial \rho} \right)_{S}$$

$$c_{S}^{2} = \left( \frac{R}{c_{v}} + 1 \right) \left( v^{2} \frac{RT}{(v - b)^{2}} \right) - \frac{2a}{v} \leftarrow VdW$$

$$c_{S}^{2} = \kappa RT \leftarrow ideal$$

$$Ma = \frac{c}{c_{S}}$$

$$\frac{T_{0}}{T} = 1 + \frac{\kappa - 1}{2} \frac{c^{2}}{\kappa RT} = 1 + \frac{\kappa - 1}{2} Ma^{2}$$

$$\frac{p_{0}}{p} = \left( \frac{T_{0}}{T} \right)^{\frac{\kappa}{\kappa - 1}} = \left( 1 + \frac{\kappa - 1}{2} Ma^{2} \right)^{\frac{\kappa}{\kappa - 1}}$$

$$\frac{\rho_{0}}{\rho} = \left( \frac{T_{0}}{T} \right)^{\frac{\kappa - 1}{\kappa}} = \left( 1 + \frac{\kappa - 1}{2} Ma^{2} \right)^{\frac{\kappa - 1}{\kappa}}$$

$$\left( \frac{A}{A^{*}} \right)^{2} = \frac{1}{Ma^{2}} \left[ \frac{2}{\kappa + 1} \left( 1 + \frac{\kappa - 1}{2} Ma^{2} \right) \right]^{\frac{\kappa + 1}{\kappa - 1}}$$

$$h_2 - h_1 = \frac{1}{2}(p_2 - p_1)\left(\frac{1}{\rho_1} + \frac{1}{\rho_2}\right) = (p_2 - p_1)\frac{1}{2}(v_1 + v_2)$$

Stoßbeziehungen für ein ideales Gas

$$\begin{split} \frac{p_2}{p_1} &= \frac{2\kappa Ma^2 - (\kappa - 1)}{\kappa + 1} \\ \frac{\rho_2}{\rho_1} &= \frac{(\kappa + 1)Ma^2}{2 + (\kappa - 1)Ma^2} \\ \frac{T_2}{T_1} &= \frac{\left[2\kappa Ma^2 - (\kappa - 1)\left[2 + (\kappa - 1)Ma^2\right]}{(\kappa + 1)^2}Ma^2 \\ Ma_2^2 &= \frac{(\kappa - 1)(Ma_1^2 - 1) + (\kappa + 1)}{2\kappa(Ma_1^2 - 1) + (\kappa + 1)} \end{split}$$

Entropie über den senkrechten Verdichtungsstoß

$$s_2 - s_1 = c_v \ln\left(\frac{T_2}{T_1}\right) + R \ln\left(\frac{v_2}{v_1}\right)$$
$$= c_p \ln\left(\frac{T_2}{T_1}\right) + R \ln\left(\frac{p_2}{p_1}\right)$$

#### 21 Feuchte Luft

$$x = \frac{m_{H_2O}}{m_L}$$

$$x = x_{D(ampf)} + x_{W(asser)} + x_{E(is)}$$

$$\varphi = \frac{p_D}{p_s}$$

$$x_D = \frac{m_d}{m_L} = \frac{R_L}{R_D} \frac{p_D}{p_L} = \frac{R_L}{R_D} \frac{p_D}{p - p_D} = 0.622 \frac{p_D}{p - p_D}$$

$$x_s = \frac{m_{D,max}}{m_L} = 0.622 \frac{p_s}{p - p_s} \to \text{für } \varphi = 1$$

$$\rho = \frac{p}{R_{gesT}} = \frac{1 + x}{R_L + xR_D} \frac{p}{T}$$

$$R_{ges} = \frac{R_L + xR_D}{1 + x}$$

$$h = c_{pL}t + x_D(c_{pD}t + r_D) + x_W c_W t + x_E(c_E t - r_E)$$

#### 22 Chemische Reaktionen

$$\frac{dn_1}{v_1} = \frac{dn_2}{v_2} = \dots = d\lambda = .const$$

$$\sum_{k=1}^K \mu_k dn_k = \sum_{k=1}^K \mu_k (v_k d\lambda) = \sum_{k=1}^K \mu_k v_k = 0$$

$$\mu_i = \left(\frac{\partial U}{\partial n_i}\right)_{S,V} = \left(\frac{\partial H}{\partial n_i}\right)_{S,p} = \left(\frac{\partial F}{\partial n_i}\right)_{T,V} = \left(\frac{\partial G}{\partial n_i}\right)_{T,p}$$

$$\mu(p,T) = \mu(p^+,T) + R_m T \ln\left(\frac{p}{p^+}\right)$$

Massenwirkungsgesetz

$$\prod_{k=1}^{K} \psi_{k}^{v_{k}} = exp - \frac{1}{R_{m}T} \sum_{k=1}^{K} v_{k} \mu_{0k}(p, T)$$
$$= exp - \frac{1}{R_{m}T} \sum_{k=1}^{K} v_{k} G_{m,k}(p, T)$$

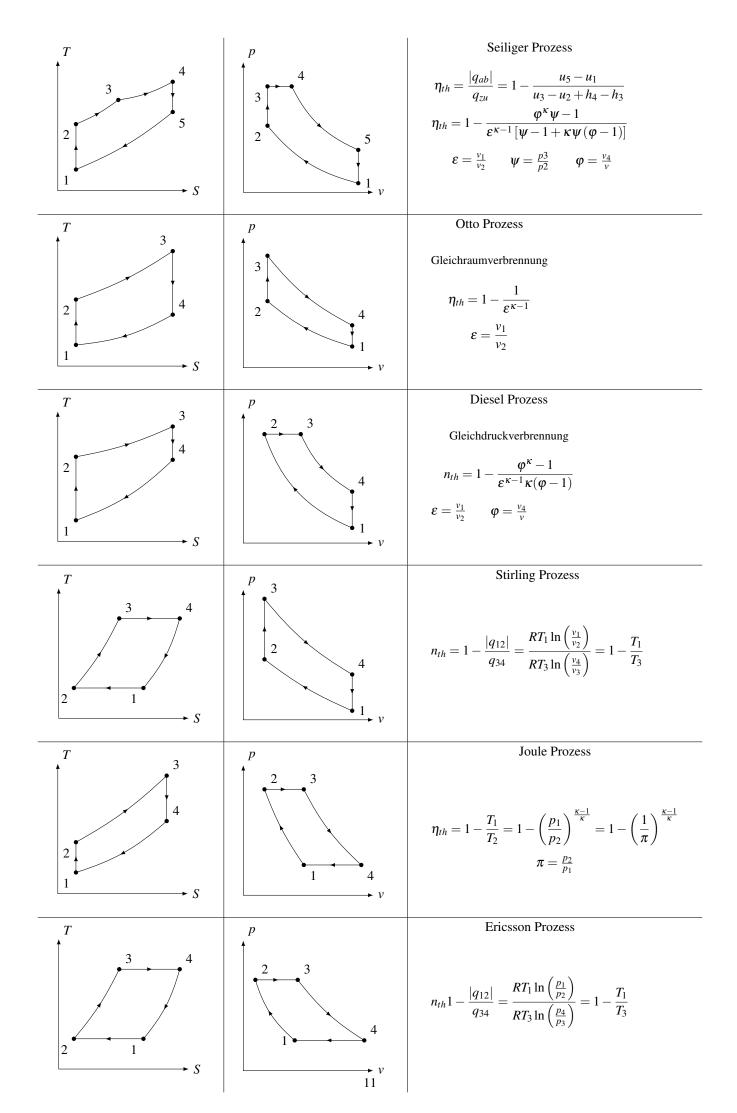
Gleichgewichtkonstante

$$K(p,T) = \prod_{k=1}^{K} \psi_k^{\nu_k}$$

$$K(p_2,T) = K(p_1,T) \left(\frac{p_1}{p_2}\right)^{\sum \nu_k}$$

$$\ln\left(\frac{K(p,T_2)}{K(p,T_1)}\right) = \frac{\Delta H_R}{R_m} \left(\frac{1}{T_1} - \frac{1}{T_2}\right) = \frac{\Delta H_R}{R_m} \frac{T_2 - T_1}{T_1 T_2}$$

$$\Delta H_R = \sum_{k=1}^{K} \nu_k H_{m,k}$$



Ideales Gas

	Isotherm	Isobare	Isochore	Isentrop	Polytrope
konstant:	T	d	Λ	$\delta q = 0$	$p_{V^n}$
	ı	ı	ı	$p_1 v_1^K = p_2 v_2^K$	$v_1^n = p_2 v_2^n$
	$p_1p_2=p_2v_2$	$\frac{v_1}{v_2} = \frac{T_1}{T_2}$	$\frac{p_1}{T_1} = \frac{p_2}{T_2}$	<u> </u>	
	ľ	ı	ı	$\frac{T_1^{\frac{K}{K-1}}}{p_1} = \frac{T_2^{\frac{K}{K-1}}}{p_2}$	$\frac{T_1^{\frac{n}{n-1}}}{p_1} = \frac{T_2^{\frac{n}{n-1}}}{p_2}$
$p, \nu$	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$\nu = \nu_1$	$p = \frac{p_1 v_1^K}{v^K}$	$p = \frac{p_1 v_1^n}{v^n}$
p,T	$p = \frac{p_1 v_1}{v}$	$p = p_1$	$p = \frac{p_1}{T_1}T$	$p = rac{p_1}{T_1^{K-1}} T^{rac{K}{K-1}}$	$p = rac{p_1}{T_1^{n-1}} T^{rac{n}{n-1}}$
u, T	$T = T_1$	$ u = rac{ u_1}{T_1} T $	$\nu = \nu_1$	$T = \frac{T_1 v_1^{K-1}}{v^{K-1}}$	$T = \frac{T_1 v_1^{n-1}}{v^{n-1}}$
<b>q</b> 12	$= p_1 v_1 \ln \frac{p_2}{p_1}$	$=c_p(T_2-T_1)$	$=c_{\nu}(T_2-T_1)$	0 =	$= c_{\nu} \frac{n - \kappa}{n - 1} (T_2 - T_1)$
WV,12	$=-q_{12}$	$=-p_1(\nu_2-\nu_1)$	0=	$= \frac{p_1 v_1}{k-1} \left[ \left( \frac{v_1}{v_1} \right)^{K-1} - 1 \right]$	$= \frac{p_1 v_1}{n-1} \left[ \left( \frac{v_1}{v_2} \right)^{n-1} - 1 \right]$
$s_2 - s_1$	$=R\ln\left(rac{p_2}{p_1} ight)$	$=c_p \ln \left(rac{T_2}{T_1} ight)$	$= c_ u \ln \left(rac{T_2}{T_1} ight) \; \; \; \; \; \; \; \; \; \; \; \; \; \; \; \; \; \; \;$	0 =	$= c_{\nu} \frac{n-\kappa}{n-1} \ln \left( \frac{T_2}{T_1} \right)$

Van-Der-Waals-Gas

	Isotherme	Isobare	Isochore	Isentrop
const.	T	d	Λ	$\delta = 0$
	$(p_1 + \frac{a}{v^2})(v_1 - b) = (p_2 + \frac{a}{v^2})(v_2 - b)$	$\frac{RT_1}{v_1 - b} - \frac{a}{v_1^2} = \frac{RT_2}{v - b} - \frac{a}{v_2^2}$	$\frac{p_1 + \frac{a}{\sqrt{1}}}{T_1} = \frac{p_2 + \frac{a}{\sqrt{2}}}{T_2}$	$ (p_1 + \frac{a}{v^2})(v_1 - b) \frac{c_v + R}{c_v} $ $= (p + \frac{a}{v^2})(v_2 - b) \frac{c_v + R}{c_v}, $ $T_1(v_1 - b)^{R/c_v} = T_2(v_2 - b)^{R/c_v} $
$p, \nu$	$p = (p + \frac{a}{v^2}) \frac{v_u}{v - b} - \frac{a}{v^2}$	$p = p_1$	$ u = \nu_1 $	$p = -\frac{a}{v^2} + \left(p_1 + \frac{a}{v^2}\right) \left(\frac{v_1 - b}{v_m}\right)^{\frac{v_v + R}{R}}$
p,T	$T=T_{ m l}$	$p = p_1$	$p = \frac{T}{T_1}(p_1 + \frac{a}{v^2}) - \frac{a}{v_1^2}$	$p = \frac{T}{T_1}(p_1 + \frac{a}{v^2}) - \frac{a}{v_1^2} \left  p = -\frac{a}{v^2} + (p_1 + \frac{a}{v^2}) \left( \frac{T}{T_1} \right)^{\frac{c_V + R}{R}} \right $
$\nu, T$	$T=T_{ m l}$	$T = T_1 \frac{\nu - b}{\nu_1 - b} + \frac{a}{R} (\nu - b) \left( \frac{1}{\nu^2} - \frac{1}{\nu_1^2} \right)$	$\nu = \nu_1$	$T=T_1\left(rac{ u_1-b}{ u-b} ight)^{rac{R}{c_ u}}$
<i>q</i> 12	$=RT_1\ln\left(\frac{v_2-b}{v_1-b}\right)$	$=rac{a}{ u_1}-rac{a}{ u_2}+c_ u(T_2-T_1)+p_1( u_2- u_1)\ =c_ u(T_2-T_1)$		0 =
WV,12	$=-RT_1 \ln \left(\frac{v_2-b}{v_1-b}\right) + \frac{a}{v_1} - \frac{a}{v_2}$	$=-p_1(\nu_2-\nu_1)$	0 =	$=rac{a}{v_1}-rac{a}{v_2}+c_{ u}(T_2-T_1)$
$s_2 - s_1$	$\left  s_2 - s_1 \right  = R \ln \left( rac{v_2 - b}{v_1 - b}  ight)$	$=c_ u \ln \left(rac{T_2}{T_1} ight) + R \ln \left(rac{ u_2 - b}{ u_1 - b} ight)$	$= c_{\nu} \ln \left( \frac{T_2}{T_1} \right)$	0 =

# 23 Stoffwerte einiger Gase

Bezeichnung	Symbol	Molmasse	Gaskonstante	Dichte	$c_p$	$c_v$	κ
		[kg/kmol]	[J/(kg K)]	$[kg/m^3]$	[J/(kg K)]	[J/(kg,K)]	
Acetylen	$C_2H_2$	26.038	319.3	1.16	1616	1278	1.26
Ammoniak	$NH_3$	17.031	488.2	0.76	2056	1526	1.35
Argon	Ar	39.948	208.1	1.76	519	309	1.68
Äthan	$C_2H_6$	30.070	276.5	1.34	1650	1355	1.22
Butan	$C_4H_10$	58.124	143.0	2.67	1599	1410	1.13
Chlor	$C_l2$	56.108	117.3	3.17	473	343	1.38
Chlorwasserstoff	HCl	70.906	228.0	1.62	795	556	1.43
Helium	He	4.003	2077.0	0.18	5200	3124	1.66
Kohlendioxid	$CO_2$	44.010	188.9	1.95	816	618	1.32
Kohlenmonoxid	CO	28.010	296.8	1.23	1038	739	1.40
Luft	<u> </u>	28.964	287.1	1.28	1006	718	1.40
Methan	$CH_4$	16.043	518.3	0.71	2165	1638	1.32
Propan	$C_3H_8$	44.097	188.5	1.99	1549	1331	1.16
Sauerstoff	$O_2$	31.999	259.8	1.41	909	647	1.40
Stickstoff	$N_2$	28.013	296.8	1.23	1038	739	1.40
Wasserstoff	$H_2$	2.016	4124.2	0.09	14050	9926	1.42
Xenon	Xe	131.300	63.3	5.82	159	93	1.71
Ideales Gas			8.3143				

# 24 Stoffdaten einiger Stoffe

Name	chemische	Molmasse	Normal-	kritische	kritischer
Name	Formel	[kg/kmol]	Siedepunkt [°C]	Temperatur [°C]	Druck [MPa]
Wasserstoff	$H_2$	2.02	-252.9	-240.0	1.32
Helium	He	4.00	-268.9	-268.0	0.23
Ammoniak	$NH_3$	17.03	-33.3	132.3	11.33
Wasser	$H_2O$	18.02	100.0	373.9	22.06
	78%				
Luft	$N_221\%$	28.96	-194.2	-140.4	3.84
	$O_2.1\%Ar.+$				
Kohlendioxid	$CO_2$	44.01	-78.4	31.0	7.38
Methan	$CH_4$	16.04	-161.5	-82.6	4.60
Äthan	$C_2H_6$	30.07	-88.6	32.2	4.87
Propan	$C_3H_8$	44.10	-42.1	96.7	4.25
R134a	$CH_2FCF_3$	102.03	-26.1	101.1	4.06

# 25 Zahlenwerte feuchte Luft

Bezeichnung	Formelzeichen	Zahlenwert	Dimension
Molmasse der Luft	ML	28,96	kg/ kmol
Molmasse des Wassers	MH2O	18,02	kg/ kmol
spezifische Gaskonstante der Luft	RL	0,287	kJ/ (kg K)
spezifische Gaskonstante des Dampfes	RD	0,461	kJ/ (kg K)
spezifische Wärmekapazität der Luft	cpL	1,006	kJ/ (kg K)
spezifische Wärmekapazität des Dampfes	cpD	1,92	kJ/ (kg K)
spezifische Wärmekapazität des Wassers	cW	4,182	kJ/ (kg K)
spezifische Wärmekapazität des Eises	cЕ	2,1	kJ/ (kg K)
Verdampfungsenthalpie des Wassers bei 0 °C	rD	2500	kJ/ kg
Schmelzenthalpie des Eises bei 0 °C	rE	334	kJ/ kg
	1		

#### 26 Obskure Zusammenhänge

$$dV = \left(\frac{\partial V}{\partial T}\right)_{p} dT + \left(\frac{\partial V}{\partial p}\right)_{T,n} + \sum_{k=1}^{K} \left(\frac{\partial V}{\partial n_{k}}\right)_{T,p} dkn_{k}$$

$$dS = \left(\frac{nC_{p,m}}{T}\right) dT - \left(\frac{\partial V}{\partial T}\right)_{p,n} dp + \sum_{k=1}^{K} \left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n} dn_{k}$$

$$dU = \left[nC_{p,m} - p\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dT - \left[p\left(\frac{\partial V}{\partial p}\right)_{T,n} + T\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dp + \sum_{k=1}^{K} \left[\mu_{k} - T\left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n} - p\left(\frac{\partial V}{\partial n_{k}}\right)_{T,p,n}\right] dn_{k}$$

$$dH = nC_{p,m} dT + \left[VT\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] + \sum_{k=1}^{K} \left[\mu_{k} - T\left(\frac{\partial \mu_{k}}{\partial T}\right)_{p,n}\right] dn_{k}$$

$$dF = -\left[S + p\left(\frac{\partial V}{\partial T}\right)_{p,n}\right] dT - p\left(\frac{\partial V}{\partial p}\right)_{T,n} dp + \sum_{k=1}^{K} \left[\mu_{k} - p\left(\frac{\partial V}{\partial n_{k}}\right)_{T,p}\right] dn_{k}$$

$$\left(\frac{\partial C_{p,m}}{\partial p}\right)_{T,\psi_{j}} = T\frac{\partial}{\partial p} \left[\left(\frac{\partial S_{m}}{\partial T}\right)_{p,\psi_{j}}\right]_{T,\psi_{j}} = T\frac{\partial}{\partial T} \left[\left(\frac{\partial S_{m}}{\partial p}\right)_{T,\psi_{j}}\right]_{p,\psi_{j}} = -T\left(\frac{\partial^{2}V_{m}}{\partial T}\right)_{p,\psi_{j}}$$

$$C_{p,m} = (C_{p,m})_{\text{ideales Gas}} - T\int_{0}^{p} \left(\frac{\partial^{2}V_{m}}{\partial T^{2}}\right)_{p,\psi_{j}} d\tilde{V}$$

1J = 1W = 1Nm

 $E_{kin} = \frac{1}{2}mc^2$ 

 $E_{rot} = \frac{1}{2}I\omega^2$ 

 $E_{Feder} = \frac{1}{2}kx^2$  $E_{pot} = mgz$ 

## 27 Dinge die man eigentlich wissen sollte

$$E_{Kondensator} = \frac{1}{2}C\left(\frac{Q_e}{C}\right)^2$$
 
$$E_{Spule} = \frac{1}{2}LI^2$$
 
$$E_{Elektrisch} = UA$$
 
$$10^1 = 1$$
 
$$10^1 = 10$$
 
$$10^{-1} = 0.1$$
 
$$10^2 = 100$$
 
$$10^{-2} = 0.01$$
 
$$m^2 dm^2 cm^2 mm^2$$
 
$$10^3 = 1000$$
 
$$10^{-4} = 0.001$$
 
$$1 10^2 10^4 10^6$$
 
$$10^4 = 10\,000$$
 
$$10^{-4} = 0.000\,1$$
 
$$10^{-2} 1 10^2 10^4$$
 
$$10^5 = 100\,000$$
 
$$10^{-5} = 0.000\,01$$
 
$$10^{-4} 10^{-2} 1 10^2 10^4$$
 
$$10^5 = 100\,000$$
 
$$10^{-5} = 0.000\,01$$
 
$$10^{-6} = 1000\,000$$
 
$$10^{-6} = 0.000\,001$$
 
$$10^{-6} = 1000\,000$$
 
$$10^{-7} = 0.000\,000\,1$$
 
$$10^{-6} = 1000\,000$$
 
$$10^{-9} = 0.000\,000\,1$$
 
$$10^{-8} = 0.000\,000\,1$$
 
$$10^{-8} = 0.000\,000\,01$$
 
$$10^{-9} = 1000\,000\,000$$
 
$$10^{-9} = 0.000\,000\,001$$
 
$$10^{-9} = 1000\,000\,000$$
 
$$10^{-10} = 0.000\,000\,000\,1$$
 
$$10^{-3} 1 10^3 10^6 10^9$$
 
$$10^10 = 10\,000\,000\,000$$
 
$$10^{-11} = 0.000\,000\,000\,01$$
 
$$10^{-3} 1 10^3 10^6$$
 
$$10^11 = 100\,000\,000\,000$$
 
$$10^{-11} = 0.000\,000\,000\,01$$
 
$$10^{-6} 10^{-3} 1 10^3 10^6$$
 
$$10^{-1} = 10^{-1} =$$