



Beijing University of Technology
JSOL Corporation
ANSCOS Technology
MSC Corporation

Multiscale Mechanics in Polymer Composite

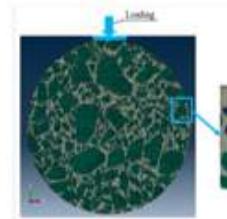
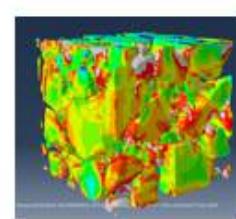
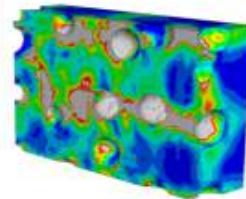
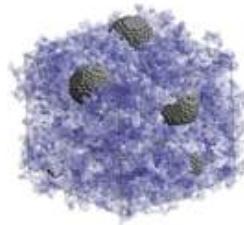
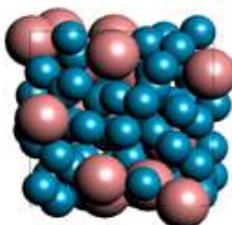
Speaker: Cao Peng

Associate Researcher

株式会社 JSOL



MSC Software®



Nanoscale

Microscale

Mesoscale

Macroscale

10^{-10} 10^{-9} 10^{-8} 10^{-7} 10^{-6} 10^{-5} 10^{-4} 10^{-3} 10^{-2} 10^{-1} 10^0 10^1

Unit: m

Some Challenges for Polymer composite



■ Electrification

- Battery, Motor, Inverter, etc.
 - Electrode (Active materials, Binder), Separator, Elect
 - Magnet
 - Power devices (SiC, etc), Sealing
 - Heat resistance, Thermal conductivity, Low thermal e
 - Adhesiveness

■ Lightweight

- Fiber Reinforced Plastics (CFRP, GFRP)
- Thermoplastic elastomer
 - Stiffness, Fracture

■ Low rolling resistance tire

- Rubber composite (Carbon black, Silica)
 - Viscoelasticity

■ High speed communication

- 5G
 - Low dielectric constant & $\tan\delta$, Heat resistance, Moisture resistance

2020 美国 500 强 (化工行业榜)		
今年排名	公司名称	收入 (百万美元)
78	陶氏	42951
103	3M	32136
152	杜邦	21512
180	宣伟 (Sherwin-Williams)	17900
209	PPG 工业公司	15146
213	艺康 (Ecolab)	14906
343	伊士曼化学公司 (Eastman Chemical)	9273
355	空气化工产品公司 (Air Products & Chemicals)	8919
356	美盛 (Mosaic)	8906
382	亨斯迈 (Huntsman)	8342
391	西湖化学 (Westlake Chemical)	8118
470	塞拉尼斯公司 (Celanese)	6297
481	奥林 (Olin)	6110

Cost-
Effective



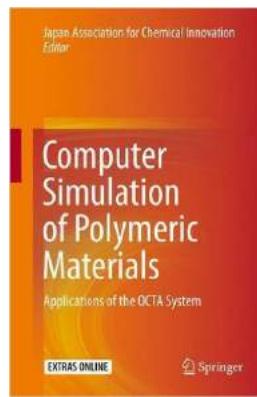
Basic material properties are targets.

OCTA and J-OCTA



Open Computational Tool for Advanced material technology

OCTA



Source :
<http://link.springer.com>

J-OCTA®

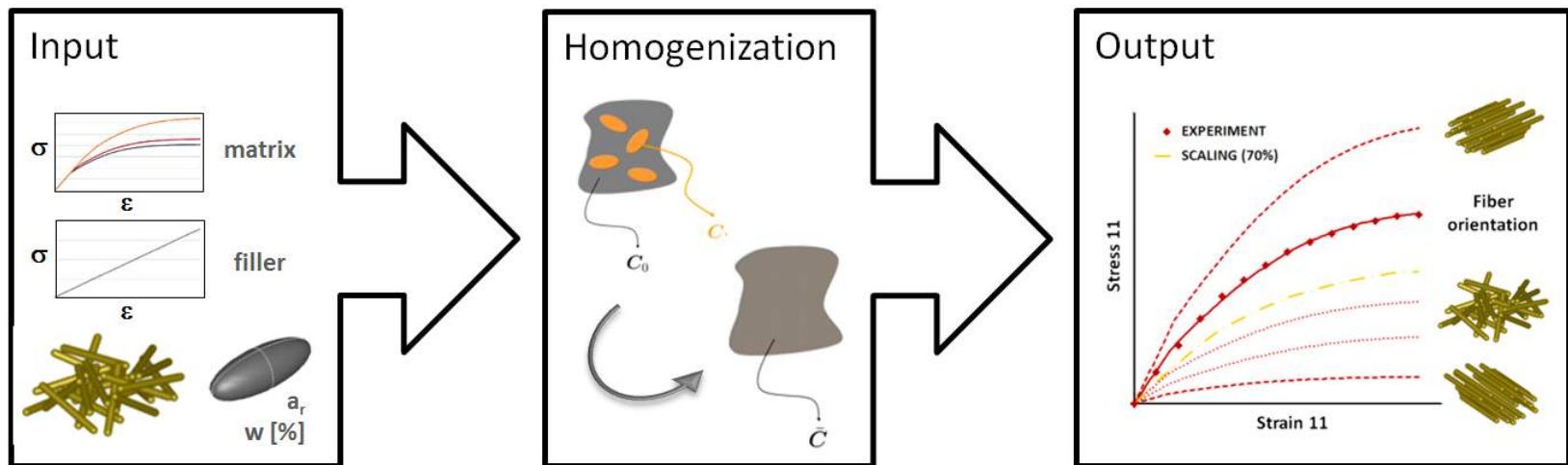
- Since 2002
- National project in Japan
- Open source
- Engines, Simple GUI, Python
- Current distributor = AIST
- BBS users > 3000

- Since 2005
- Developed by JSOL
- Commercial version
- Modelers for OCTA Engines
- Parallel MD engine
- Industrial users > 100 sites

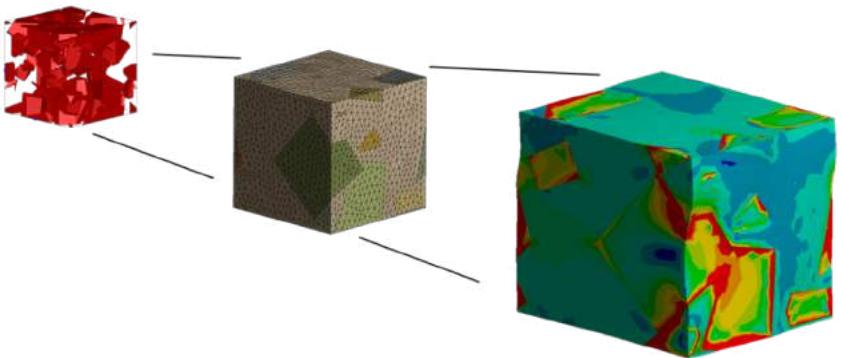
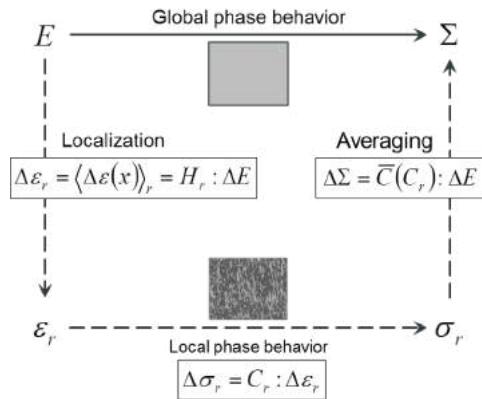
<http://octa.jp/references/publications/>



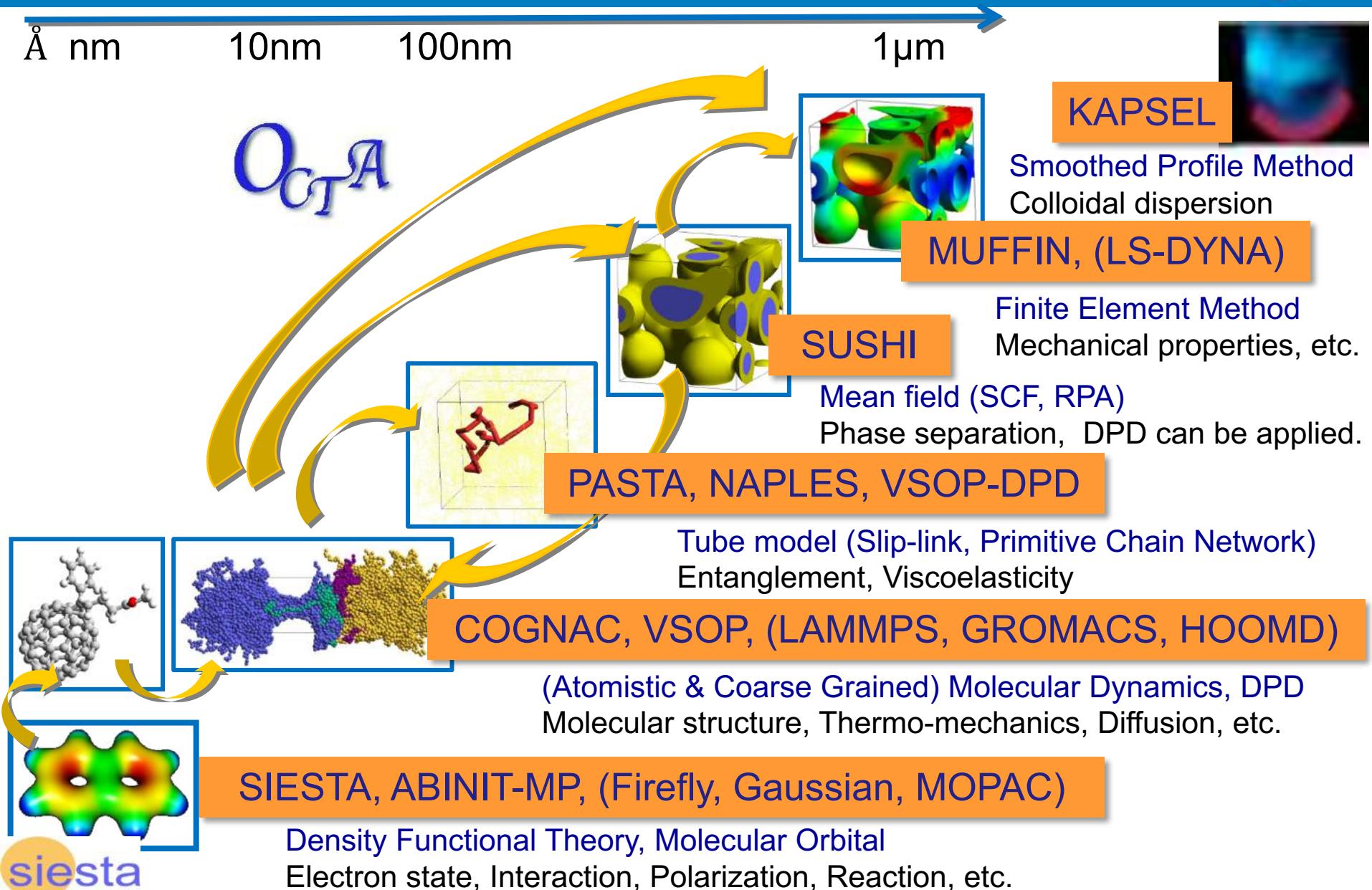
MFH and FEM



Mean-Field Homogenization



Simulation Engines





Case studies

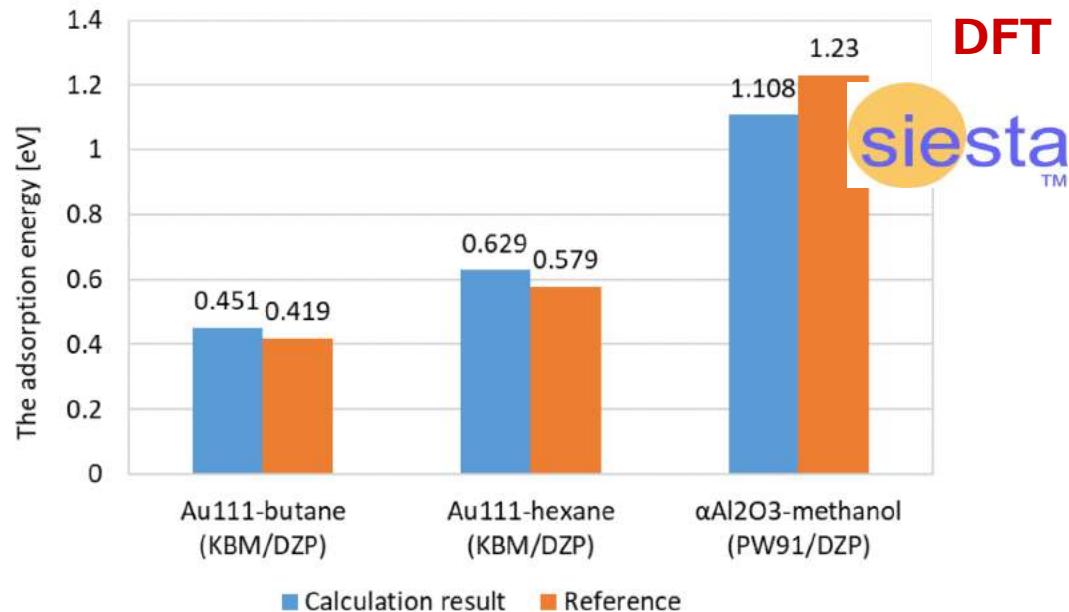
Adhesion (Intermolecular force)



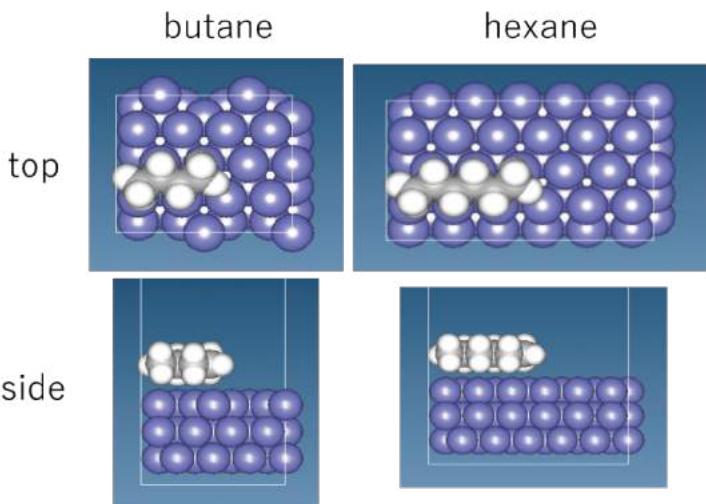
DFT

siesta™

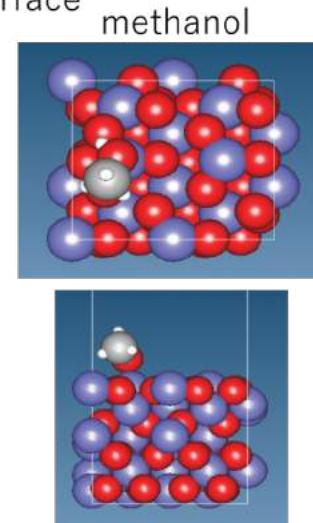
- ✓ Adhesion of molecules on Au/Alumina surfaces
- ✓ Density Functional Theory(DFT) calculation
- ✓ Structure optimization and the evaluation of the adsorption energy



Molecular adsorption on Au (111) surface



Molecular adsorption on α -alumina surface



APPLICATION:
Aeronautics and Astronautics

joint Sealing equipment

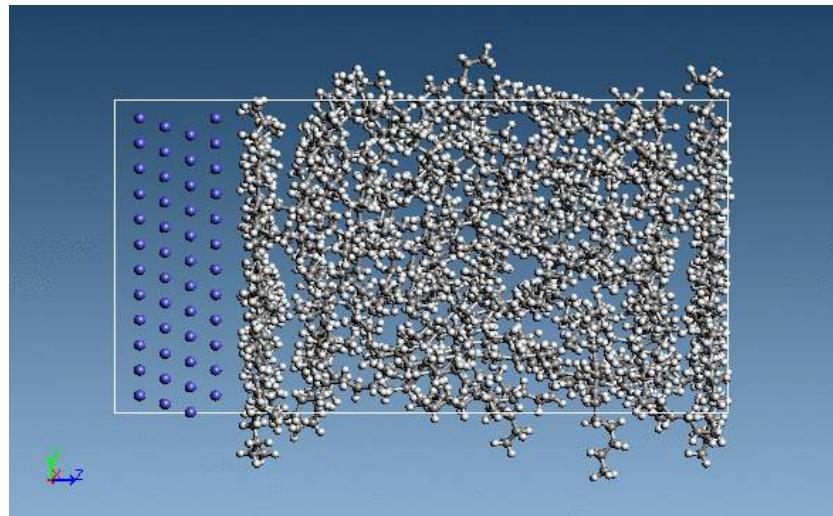
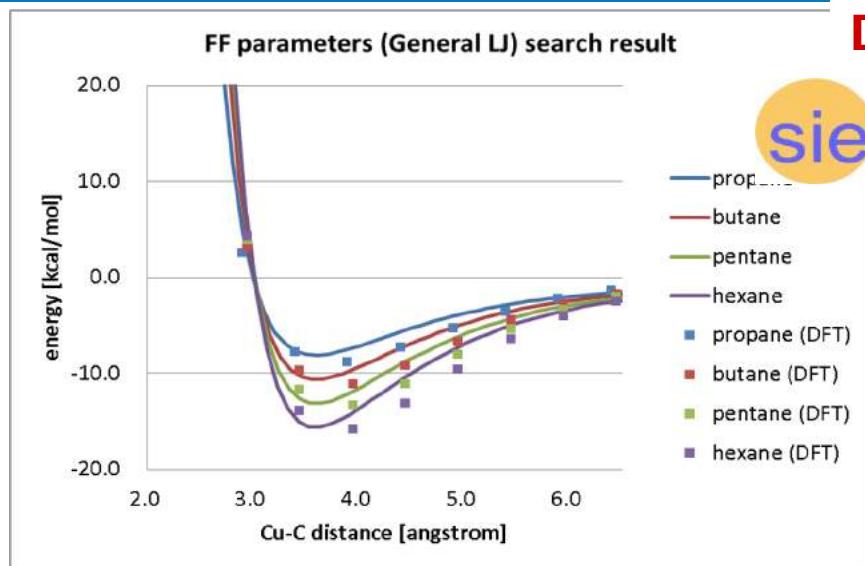
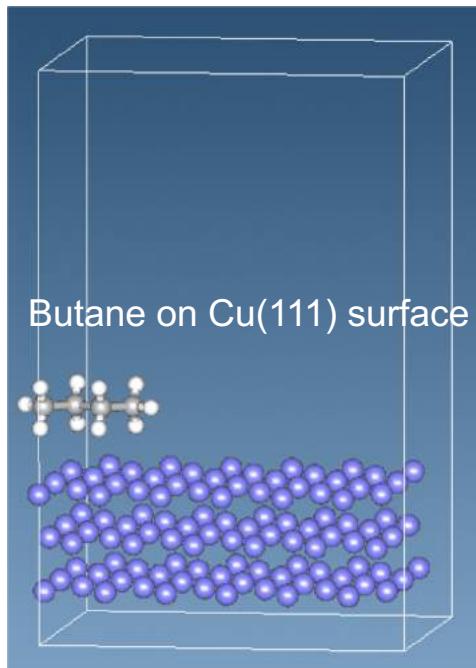
Adhesion (Intermolecular force)



DFT



- Siesta Interfacial Energy Tool
- Adsorption of Alkane molecules onto Cu surface
- Results of DFT was fitted to the Generalized Lennard Jones potential
- Obtained LJ potential was used in the classical MD calculation
- Composite materials, Adhesive, Electrode, etc.



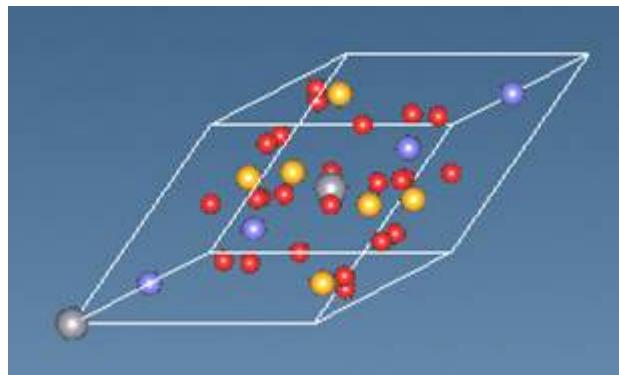
Thermal expansion of ceramics



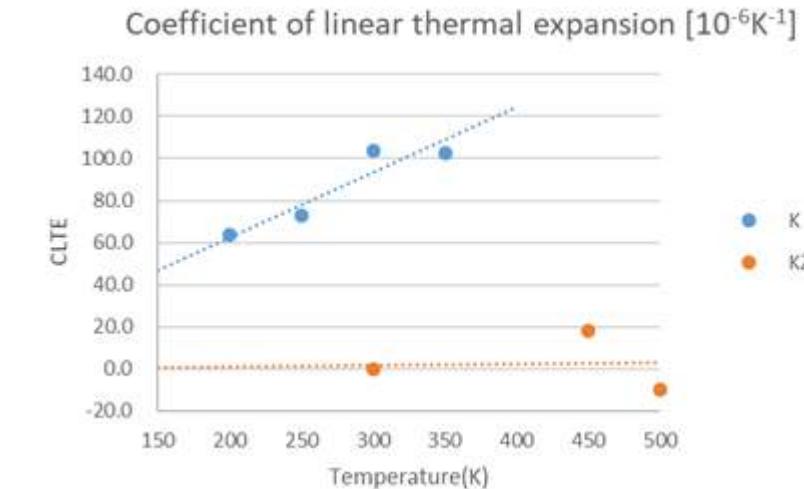
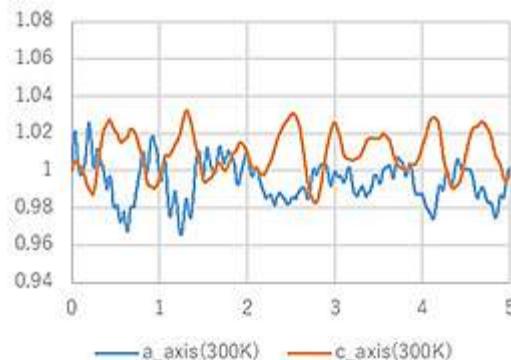
DFT



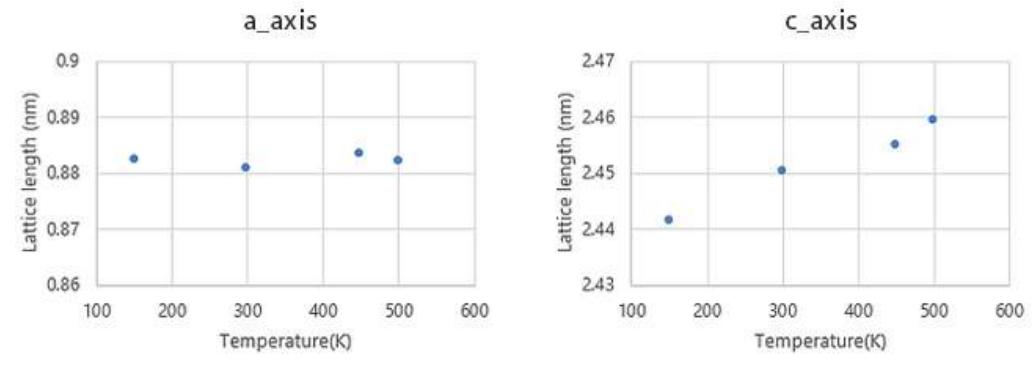
- The temperature variation in the crystal cell volumes of K and KZP ($\text{KZr}_2(\text{PO}_4)_3$) were studied with SIESTA.
- KZP shows low expansion.
- Anisotropic expansion is shown.



Cell volume changes



Anisotropy of thermal expansion of KZP

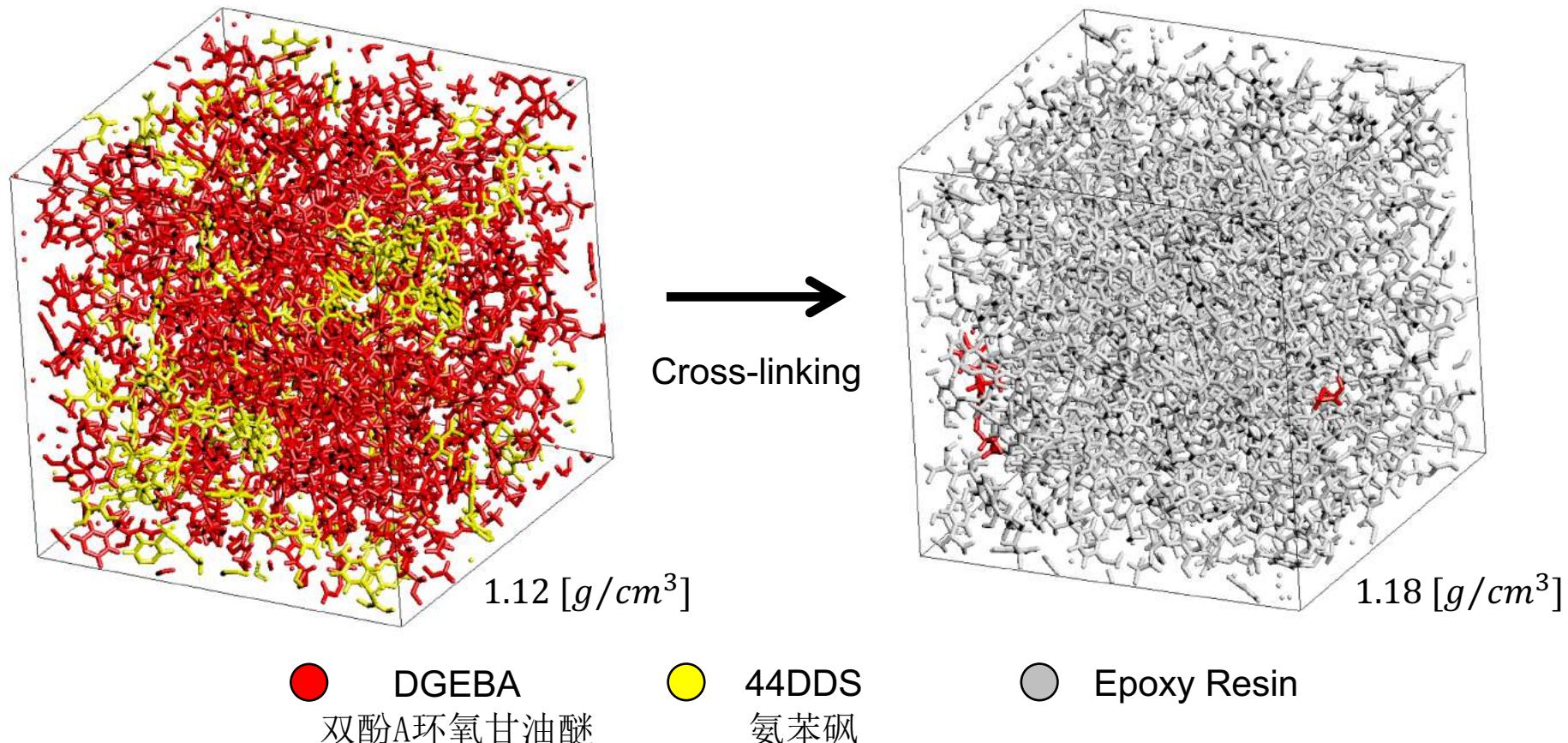


Cross-Linked Epoxy Resin



Full Atomistic Molecular Dynamics

■ Modeling of Epoxy Resin



Cross-linking of DGEBA and 44DDS simulated by J-OCTA / VSOP [1]

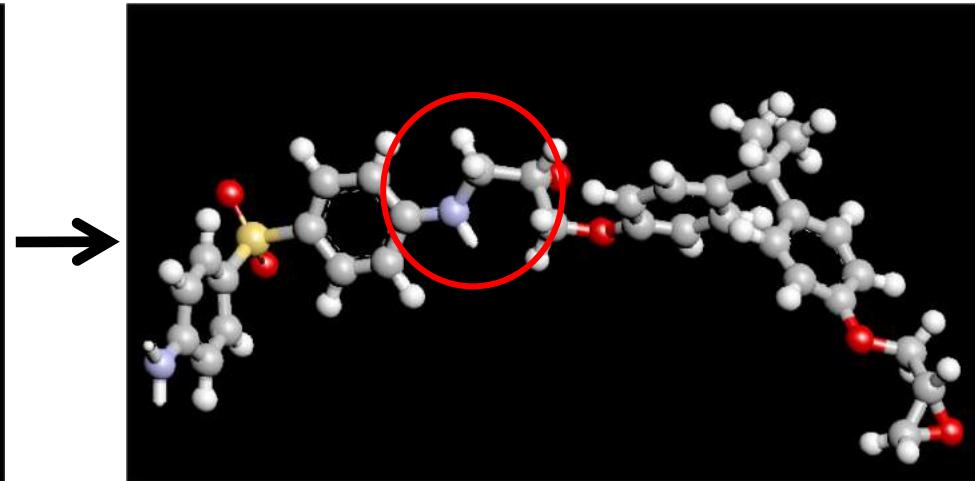
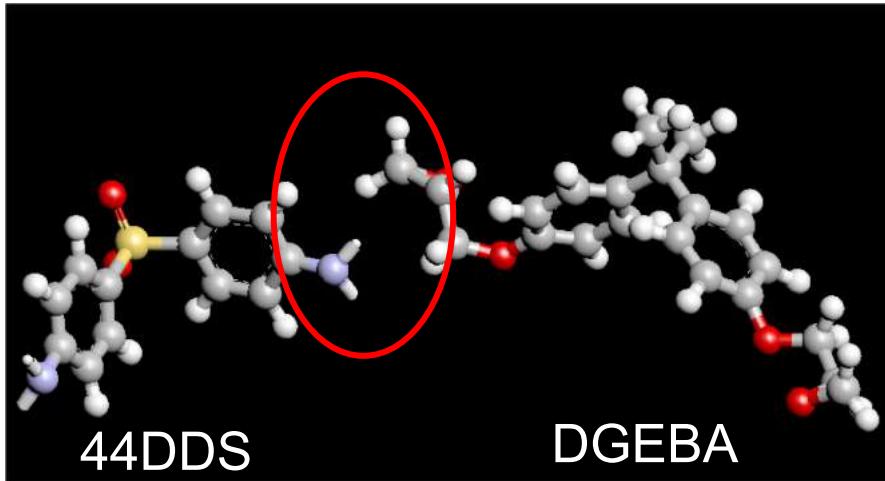
[1] T. Okabe, "Atomistic simulation of curing and mechanical properties of Epoxy resin", J-OCTA Users Conference 2014

Cross-Linked Epoxy Resin



Full Atomistic Molecular Dynamics

- Process of Cross-Linking Reactions



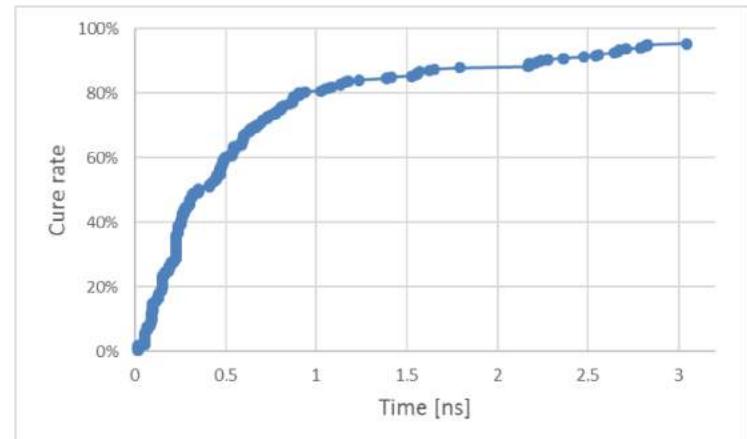
Distance Criterion of reactive atoms



Judge of reaction occurrences
by Monte Carlo using activation energy



Accelerations by heat of formation

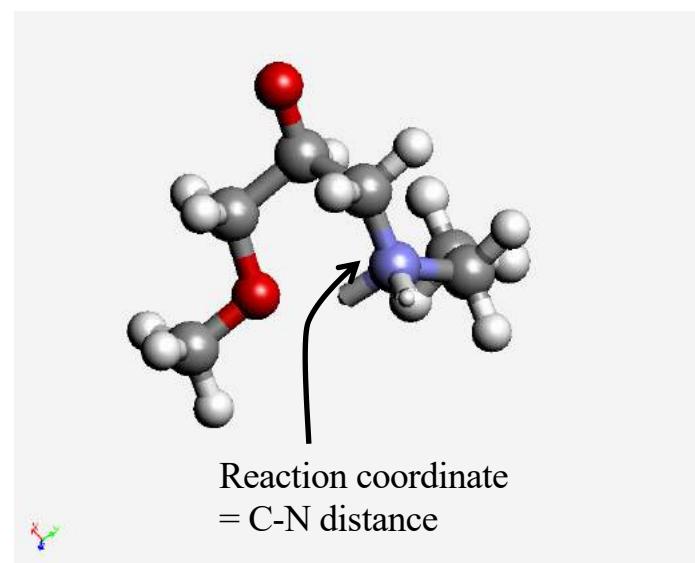
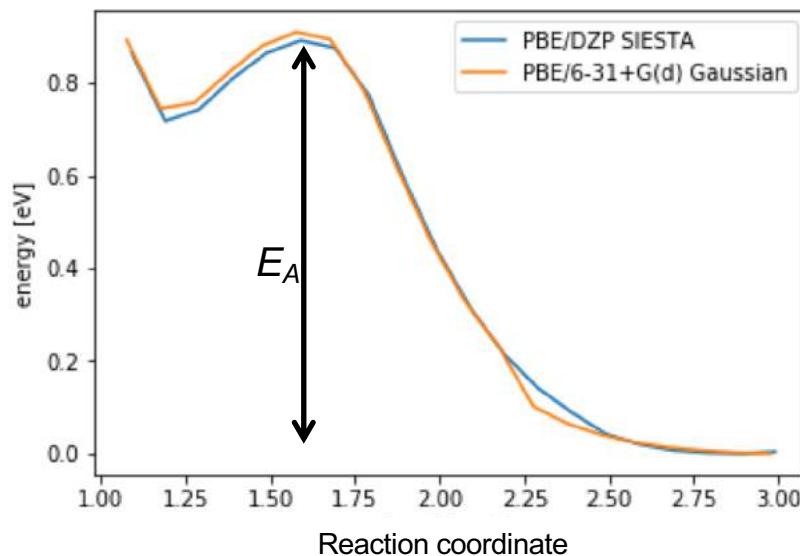


Curing curve

Reaction path analysis



- Relaxed Potential Energy Surface
 - Bond formation between epoxy and amine

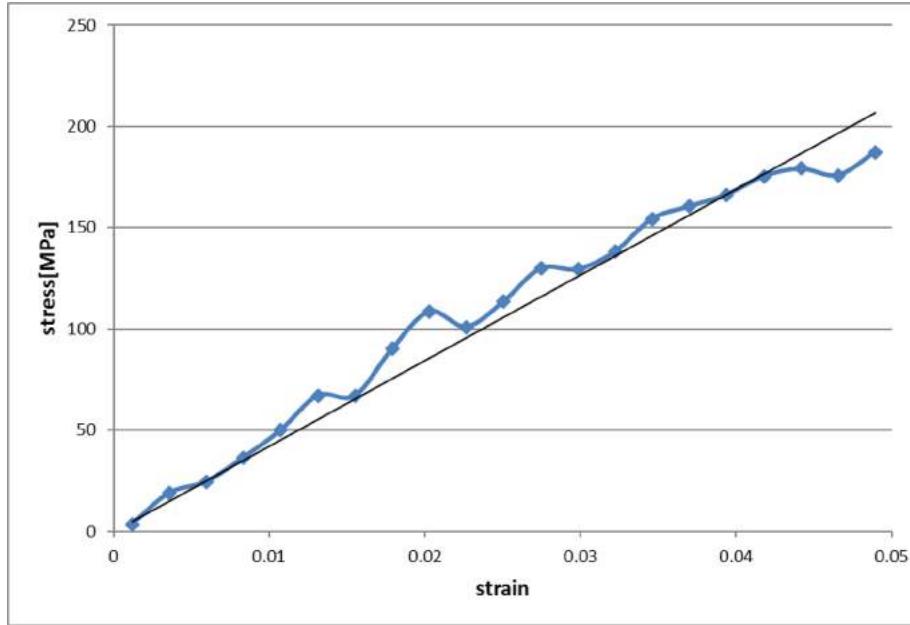


Cross-Linked Epoxy Resin



Full Atomistic Molecular Dynamics

Evaluation of Elastic Modulus



- Cell deformation with elongation rate 10.22 [m/s] under NPT ensemble.
- Young's modulus is evaluated with SS curve fitting of 5% strain.
- Evaluated Young's modulus : **4.22** [GPa] (Experiment [2] : 3.76 [GPa])

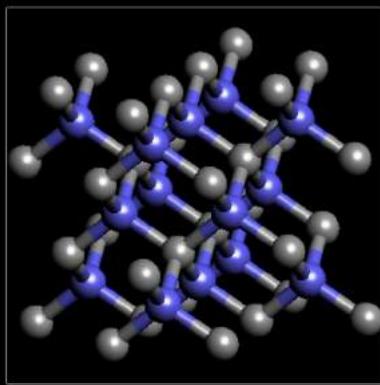
[2] V. Sundararaghavan, A. Kumar, International Journal of Plasticity, 47, 111 (2013)

Complex MD Calculation

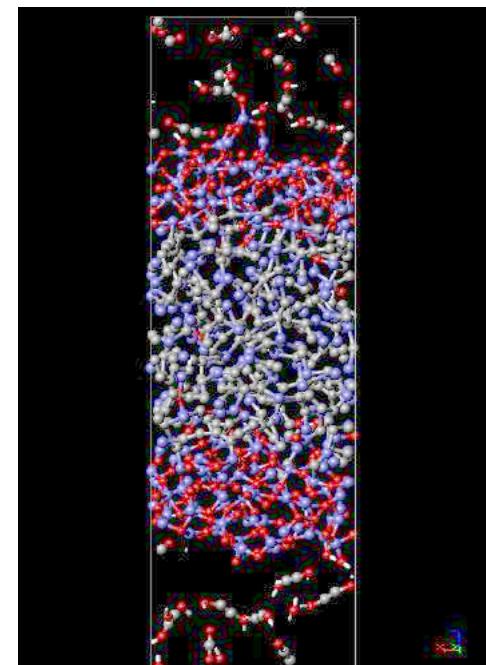
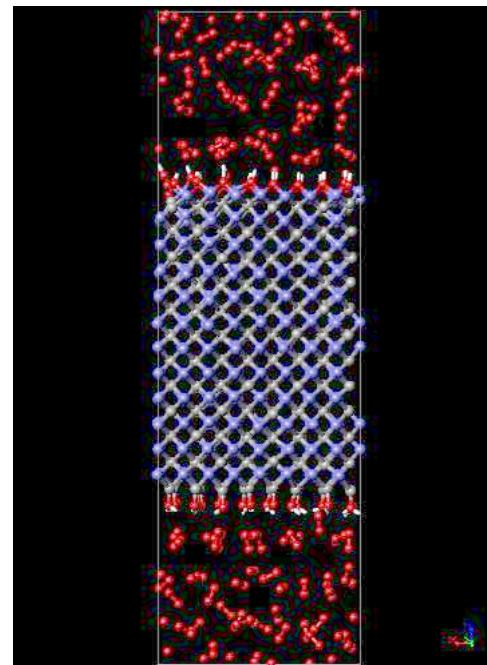


- Example of ReaxFF, I/F with LAMMPS
 - Example : Oxidation of SiC

Silicon Carbide crystal (modeled by J-OCTA)



J-OCTA



D. Newsome, D. Sengupta, H. Foroutan, M. F. Russo and Adrianus C van Duin, 2012, "Oxidation of silicon carbide by O₂ and H₂O: A ReaxFF reactive molecular dynamics study: Part I", Journal of Physical Chemistry, **116**, pp. 16111-16121

Cross-Linked Phenolic Resins

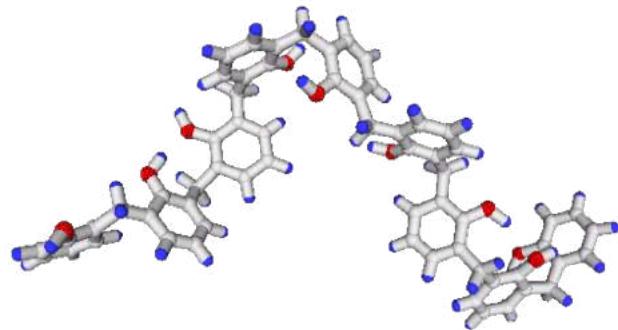


Full Atomistic Molecular Dynamics

- Modeling of Cross-Linked Phenolic Resins

courtesy of

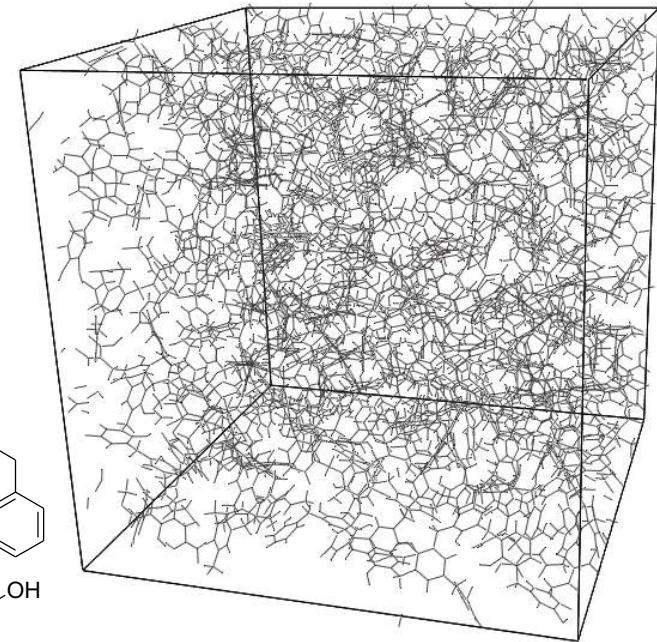
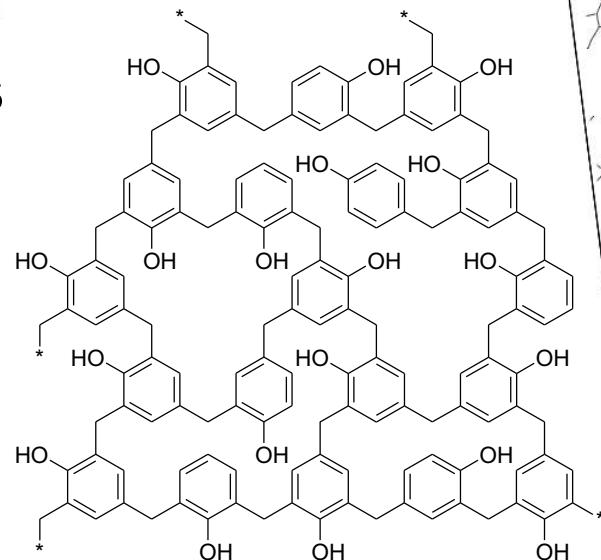
 SUMITOMO BAKELITE CO., LTD.



9-mer x 50 molecules



Cross-Linking Reactions



Cross-linking reactions were repeated until the degrees of cross-linking (D) reached 70%, 82%, and 92%, where D is given by $(2N_{\text{CH}_2})/(3N_{\text{PhOH}}) \times 100$.

Soft Matter, 8, 5283 (2012)

Cross-Linked Phenolic Resins

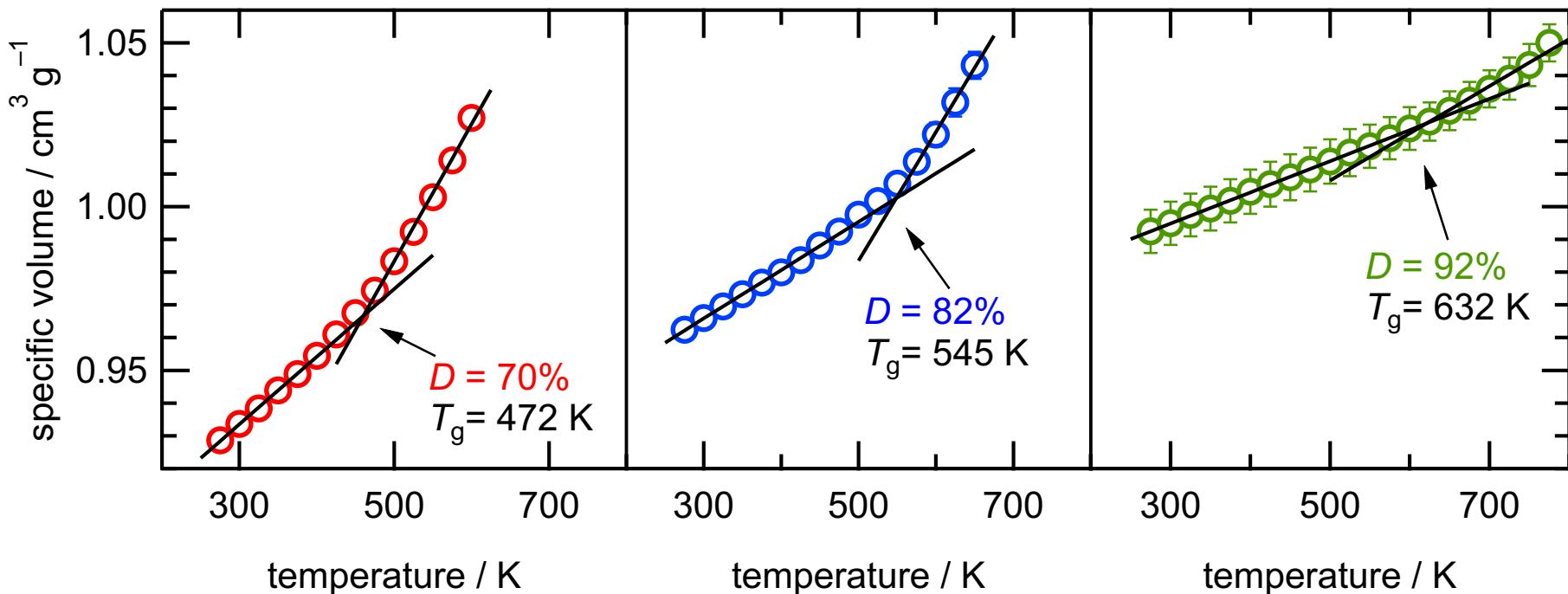


Full Atomistic Molecular Dynamics

- Glass Transition Temperature (T_g)

courtesy of

 SUMITOMO BAKELITE CO., LTD.



Cross-Linked Phenolic Resins

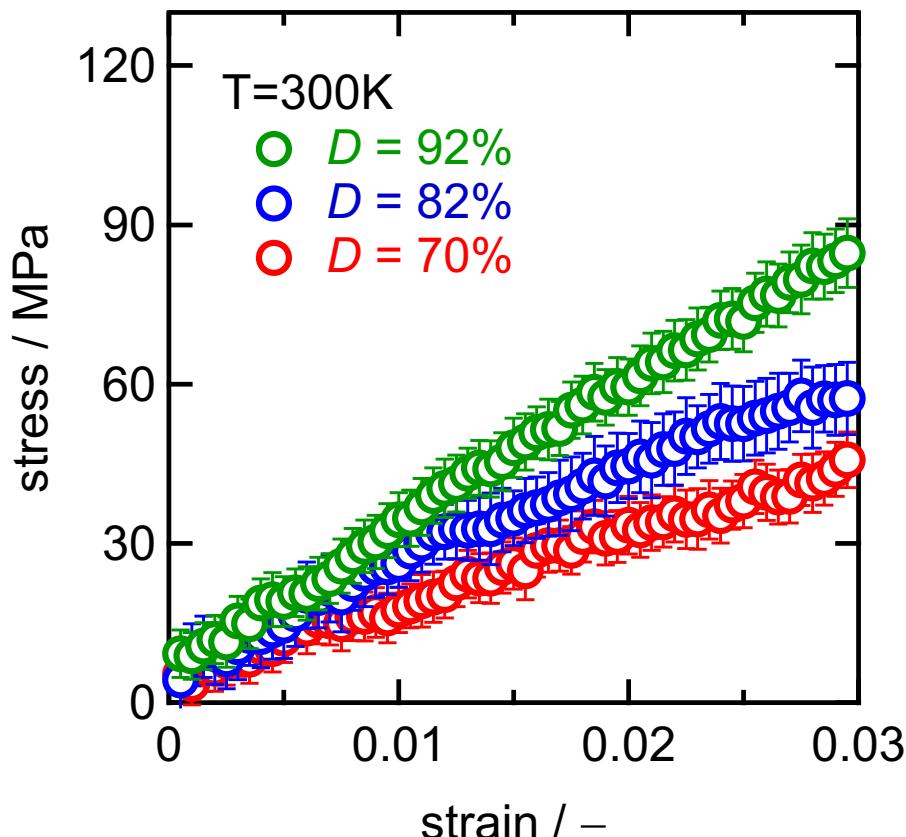


Full Atomistic Molecular Dynamics

- Uniaxial Elongation: Stress–Strain Curves

courtesy of

 SUMITOMO BAKELITE CO., LTD.



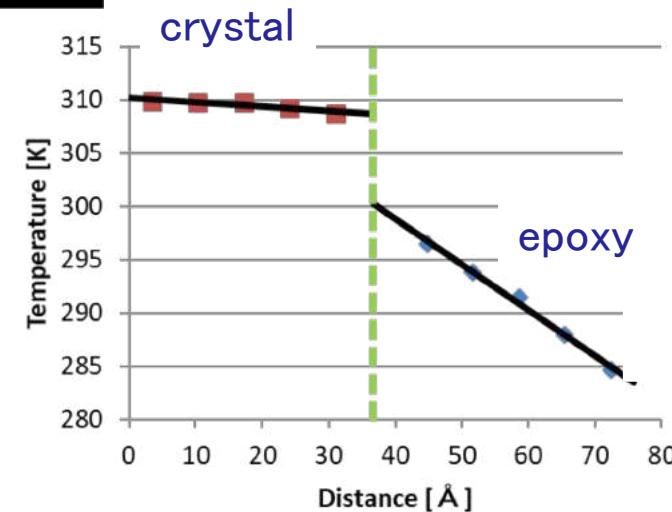
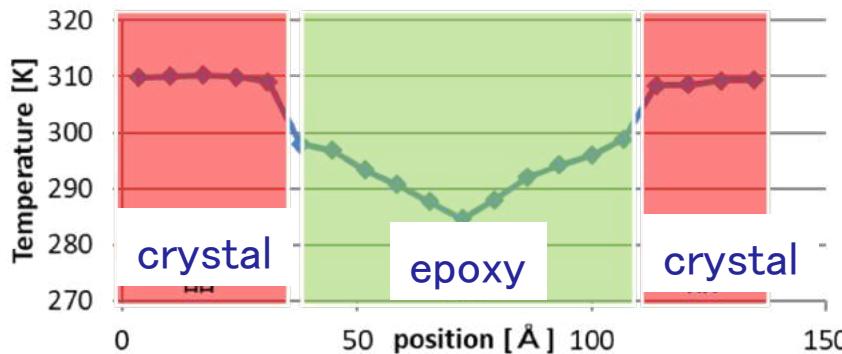
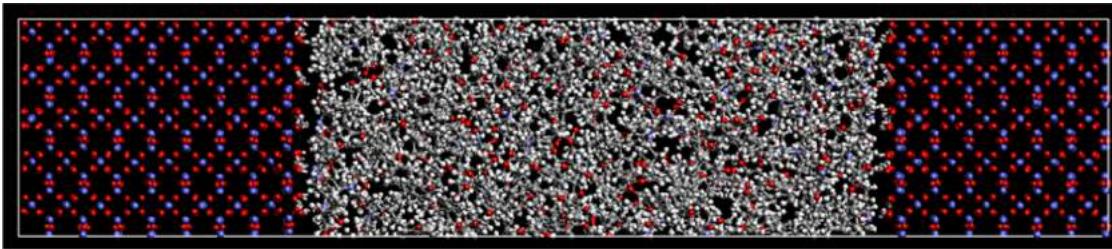
Soft Matter, 8, 5283 (2012)

Thermal conduction



Full Atomistic Molecular Dynamics

- High and low temperature regions are set (RNEMD).
- Not only one component, but also the interface between inorganic crystal and the epoxy resin.
- Effects of the interfacial modification.





Solubility

Full Atomistic Molecular Dynamics

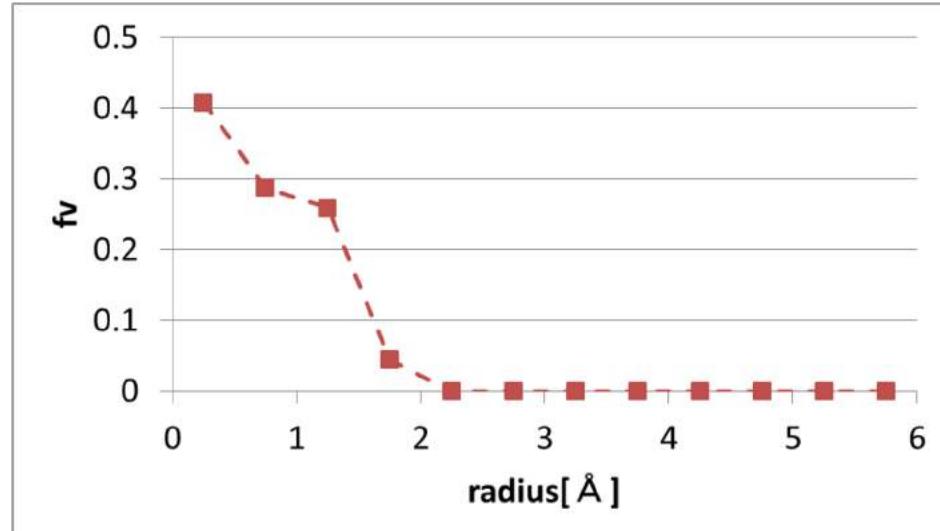
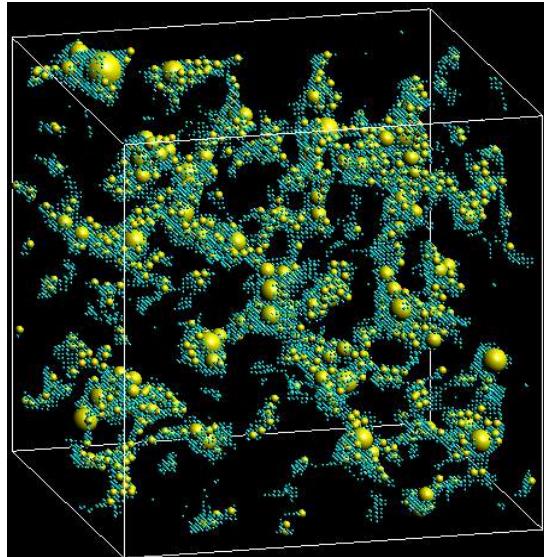
Diffusion D, Solubility S, Permeability P

$$P = D \times S$$

S is calculated by using EVMS (Excluded Volume Map Sampling)

(Ex) CO₂ in *cis* Polyisoprene (聚异戊二烯, 橡胶)

$$S = 4.23E-06 \text{ [cm}^3\text{(STP)/(cm}^3 \text{ Pa)]}$$



Distribution of free volume in bulk polymer system

Diffusion of small molecules in polymers



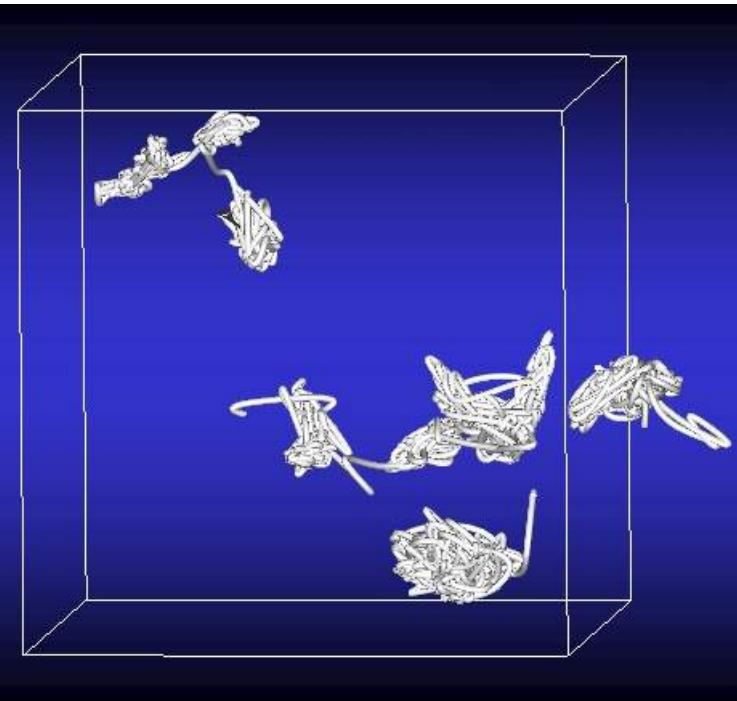
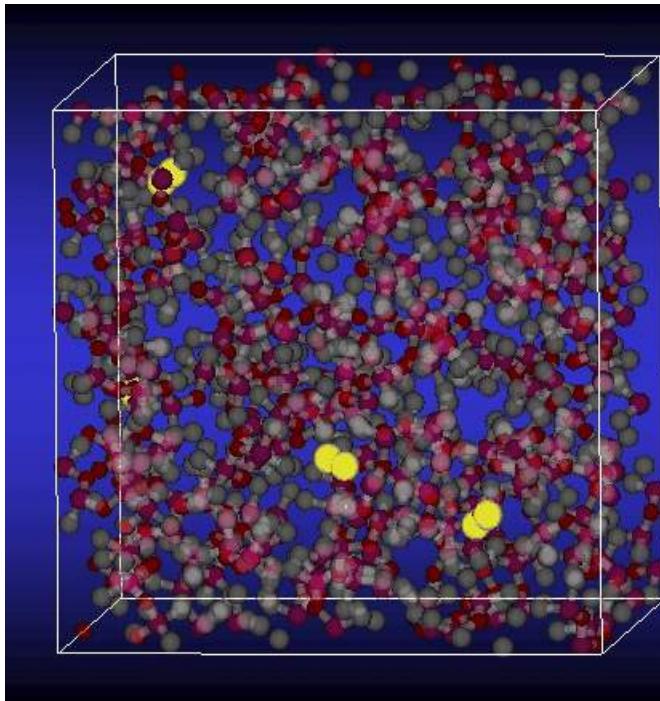
Diffusion of small molecules in PDMS

Full Atomistic Molecular Dynamics

Diffusion coefficients

聚二甲基硅氧烷

Molecule	Calc. (300[K])	Exp. (308[K])
CO ₂	2.65E-05	2.63E-05
O ₂	5.61E-05	3.96E-05

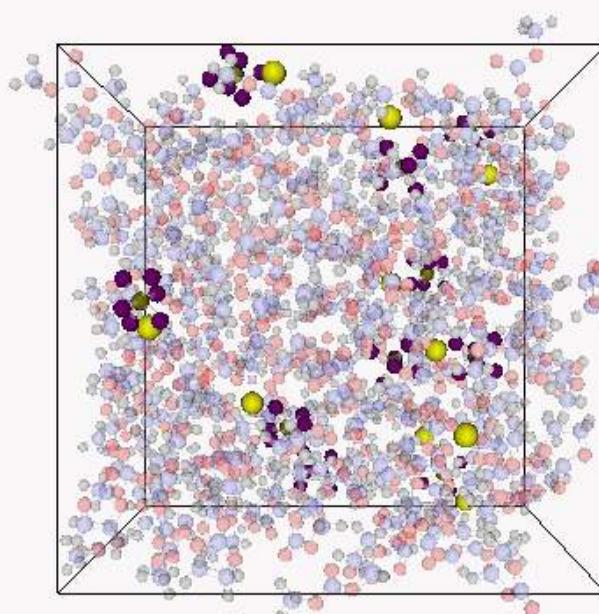


Electrolyte (Li⁺ ion)

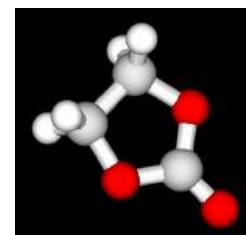


Full Atomistic Molecular Dynamics

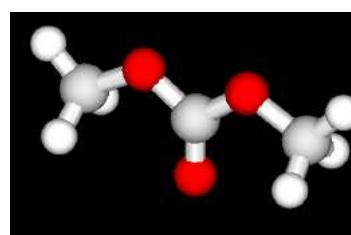
- Diffusion of Li⁺ ion in the electrolyte solution
- Effect of molecular structures
- Evaluation of ionic conductivity from diffusion coefficient



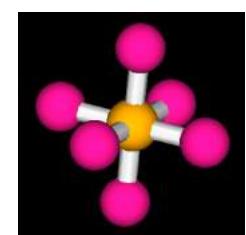
Li⁺ ion (yellow particle) in electrolyte



EC



DMC



PF6

乙基纤维素
碳酸二甲酯
聚酰胺（尼龙材料）

Gas adsorption on zeolite

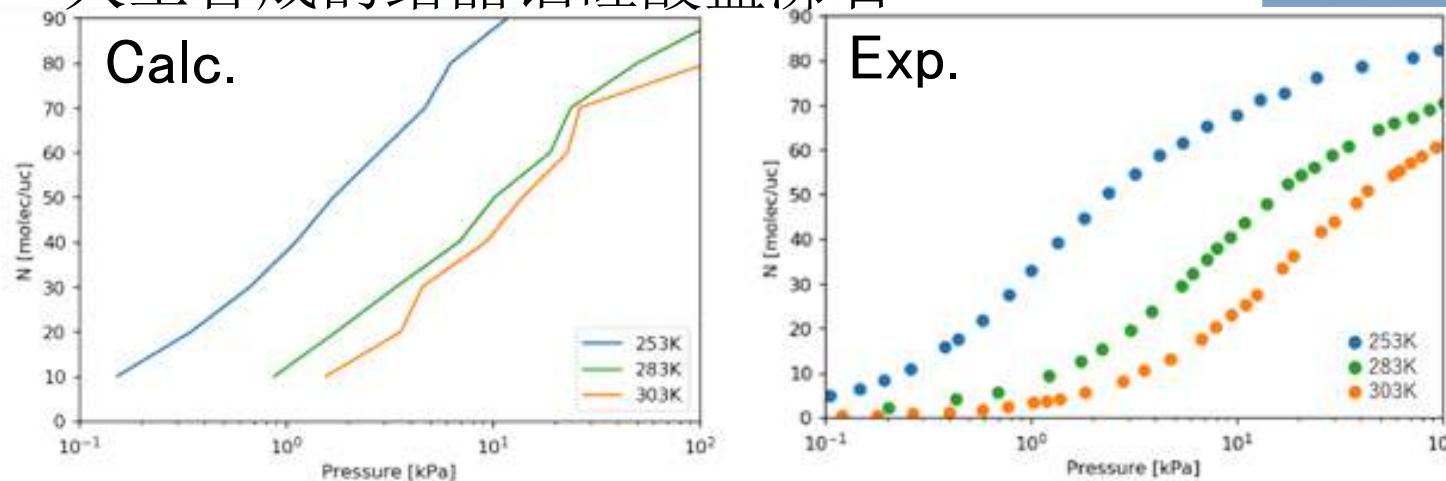
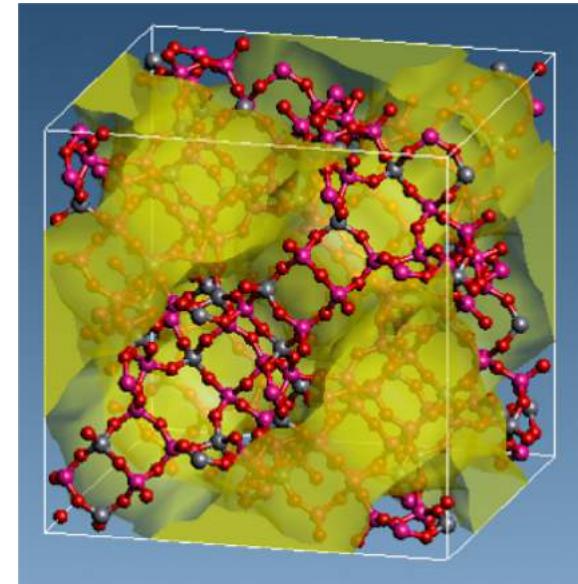


Full Atomistic Molecular Dynamics

- NaY zeolite
(CO₂ is adsorbed in yellow region)
- Evaluation of adsorption isotherms
of gas molecules by free energy
calculations



人工合成的结晶铝硅酸盐沸石



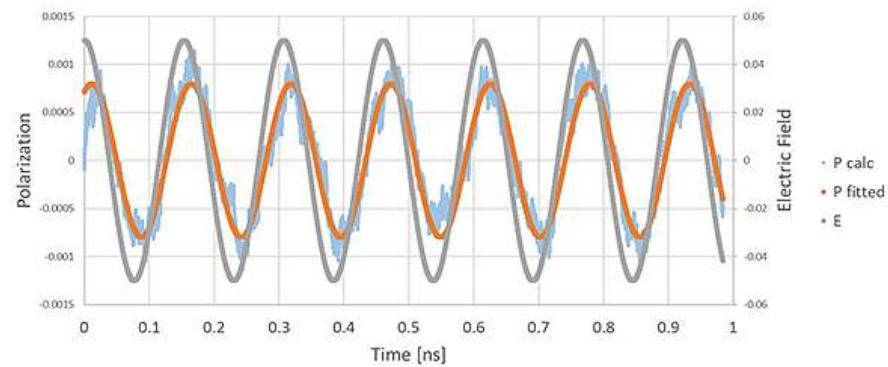
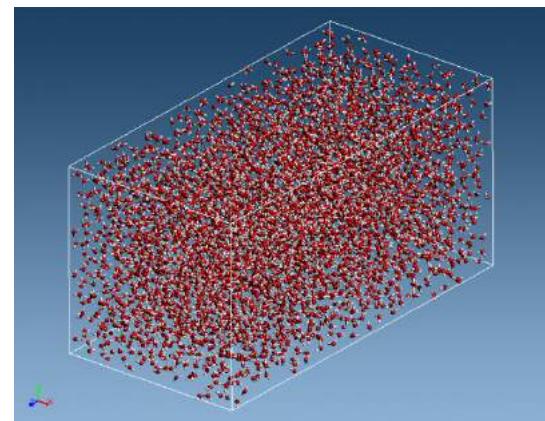
Adsorption isotherms of gas molecules

Dielectric dispersion in the GHz frequency range

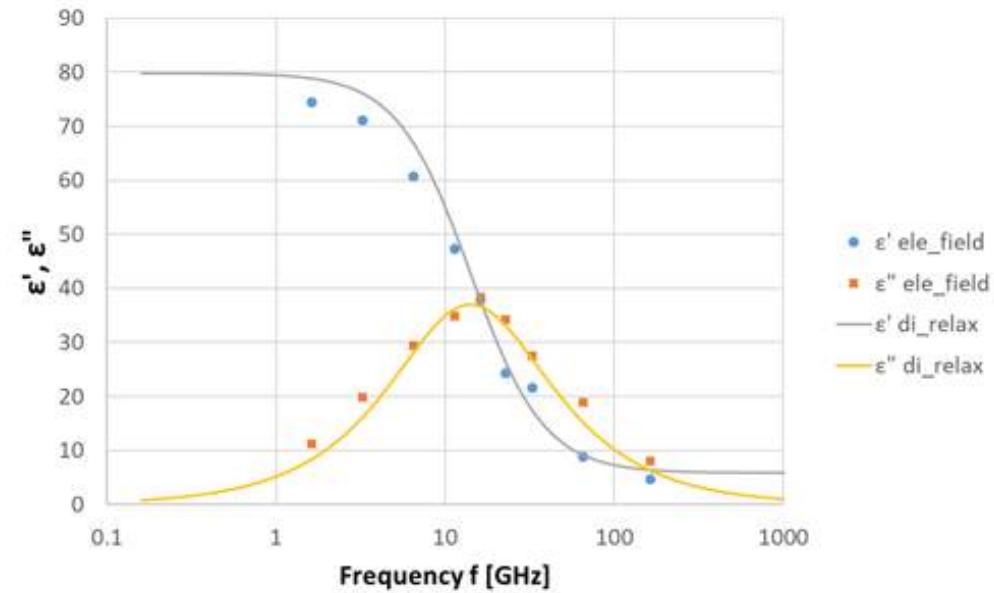


Full Atomistic Molecular Dynamics

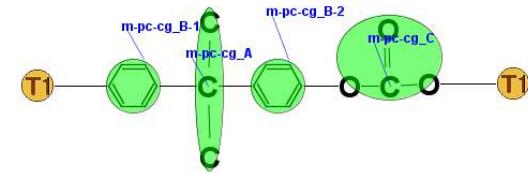
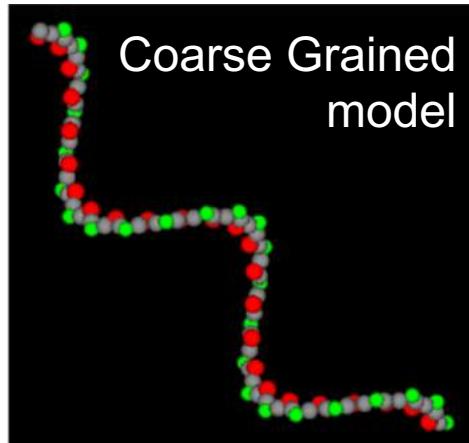
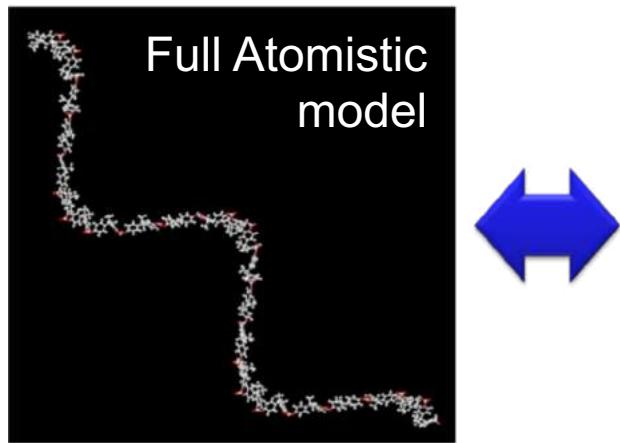
- Evaluate the response of the polarization at each time by applying a periodic electric field
- Evaluation of the complex permittivity



response of the polarization

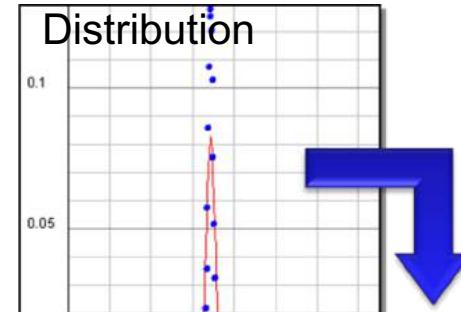


Coarse Grained potential



Bond potential

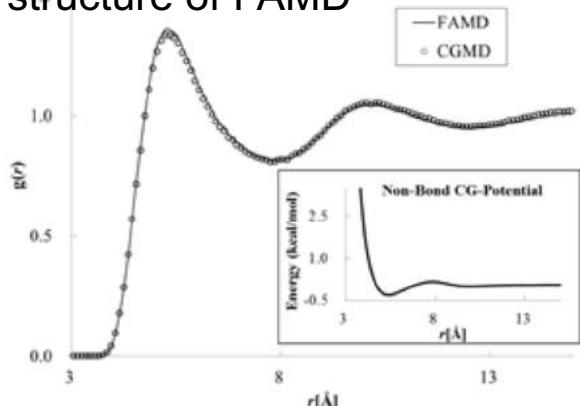
Distribution obtained by FAMD
for isolated system



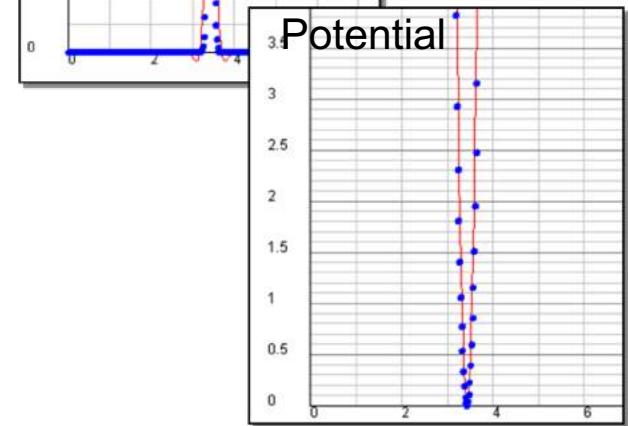
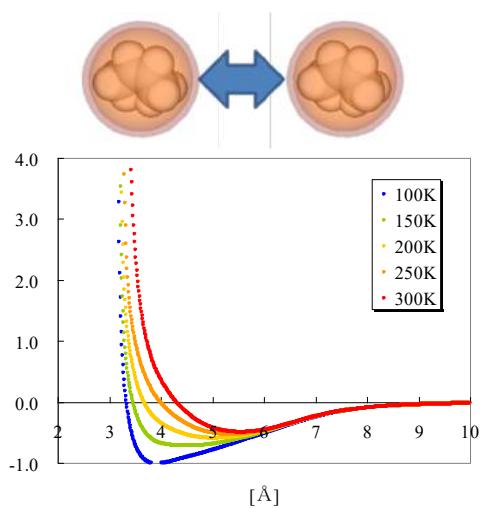
Non-Bond potential

1. Iterative Boltzmann Inversion

Reproduction of amorphous
structure of FAMD



2. Direct estimation

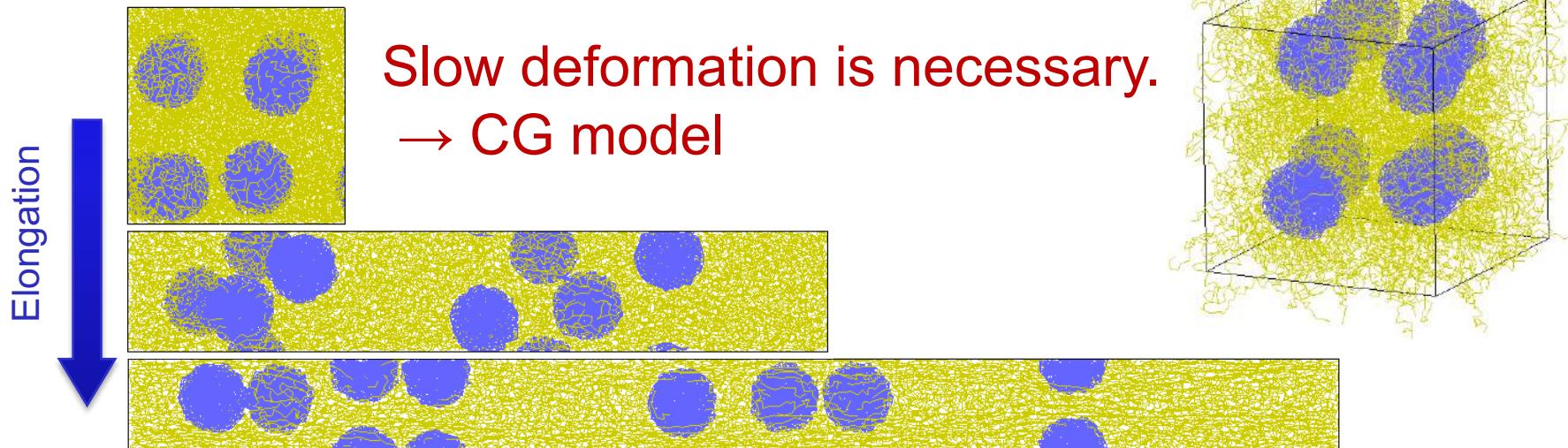


Typical case study of CG model



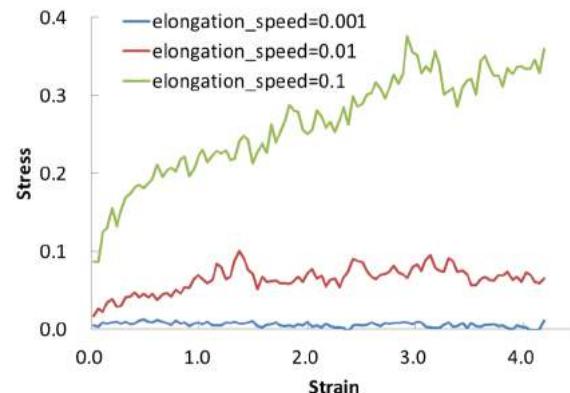
- Cross linked rubber
- Influence of cross link, interaction between filler and polymer

Coarse grained Molecular Dynamics (CGMD)

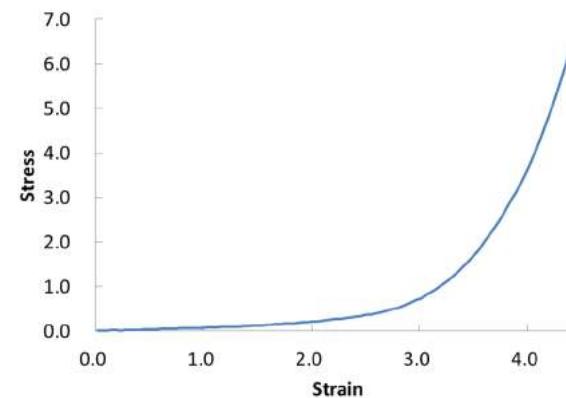


Stress-Strain curve

Non-cross link
Influence of deformation speed



With cross-link (elongation speed is 0.001)



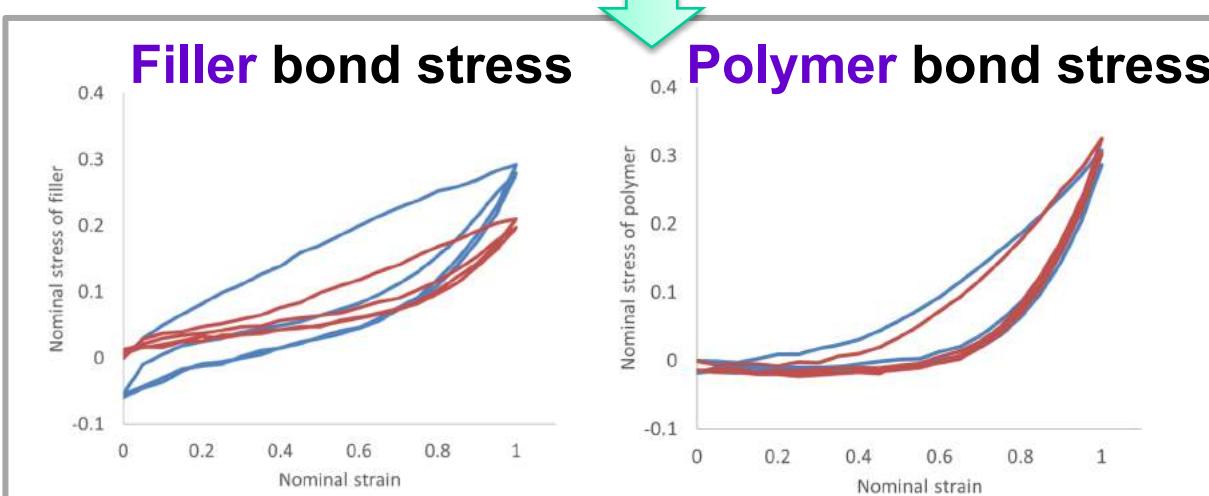
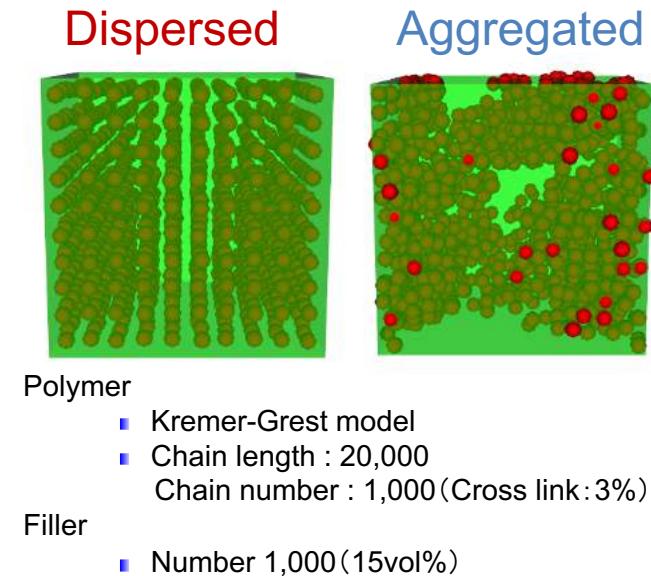
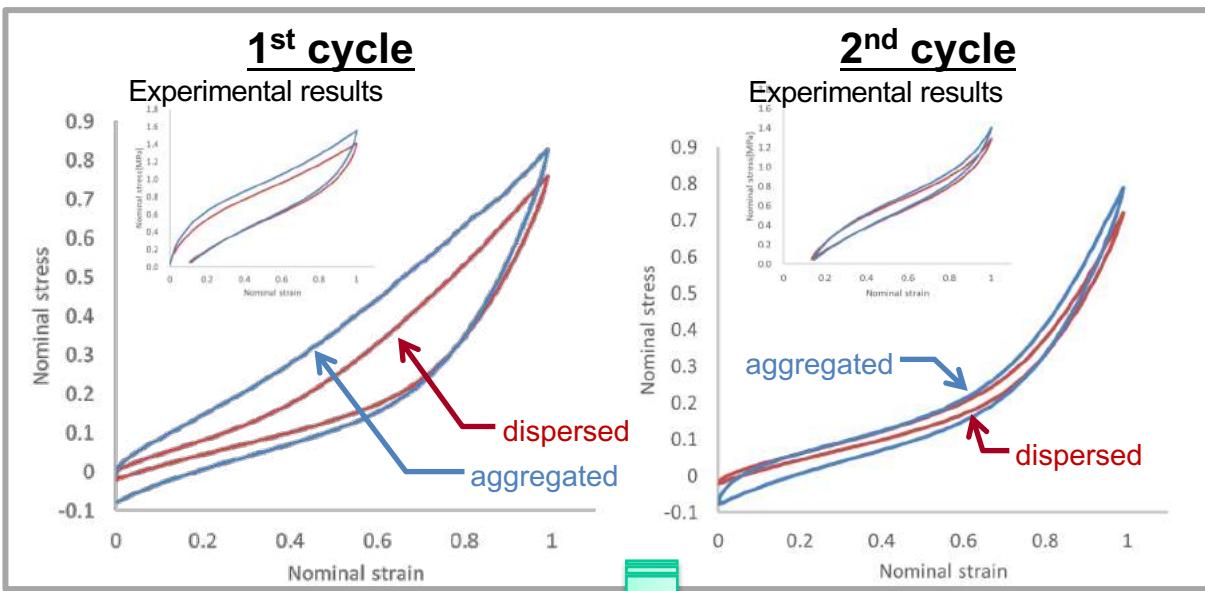
Filled Rubber under Cyclic Tensile Deformation



Courtesy of



The origin of the difference in dynamic response by Morphology



MULLION EFFECT

Filled Rubber under Cyclic Tensile Deformation

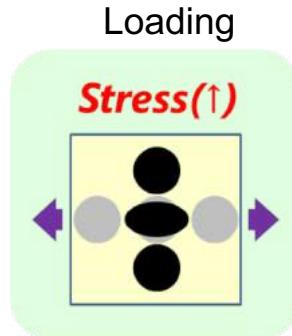


Courtesy of

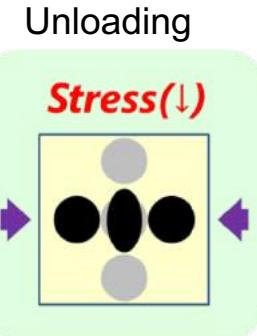
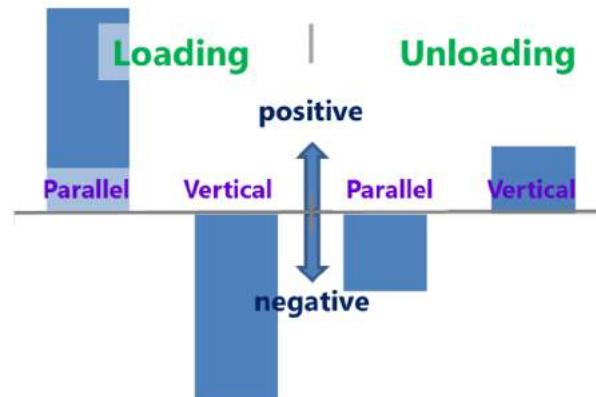


Mechanism of hysteresis

Mechanism (Filler)

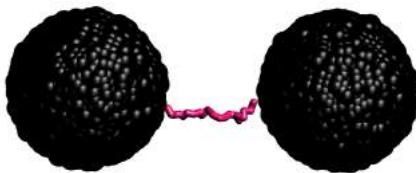


Stress components of filler in aggregated model
(difference from dispersed model)



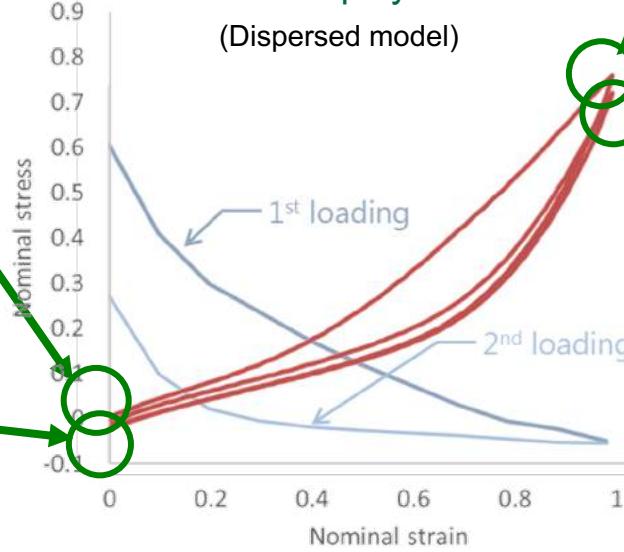
Mechanism (Polymer)

1.



Stress-Strain curve and
Fraction of short polymer network

(Dispersed model)



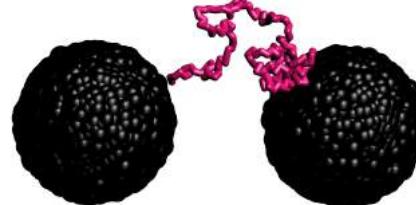
2. *Polymer stretching*



3. *Polymer unfolding*



4. *Polymer folding*



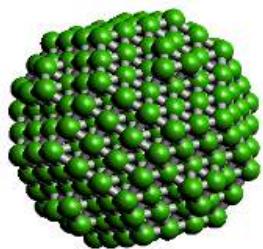
Slurry coating process



TOYOTA

■ Simulation model (Cognac/VSOP)

- Bead-spring model



Particle

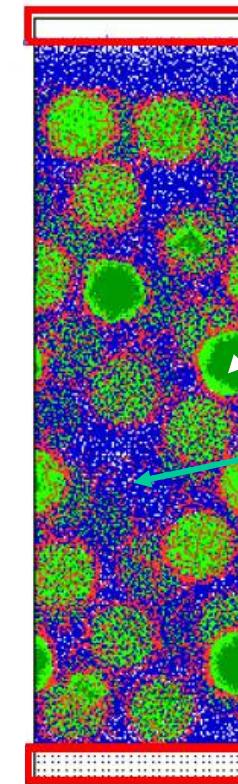


Polymer



Solvent

- Evaporation of the solvent



Delete area :
solvent molecule

Green: Particle

Red: Polymer

Blue: Solvent

Study of material property

- Interactions between molecules
- Polymer rigidity

Objectives

- ✓ Develop the method to simulate diffusion in materials by CGMD
- ➡ ✓ Clarify the mechanism of slurry coating process
- ✓ Understand the correlation between battery performance and material properties

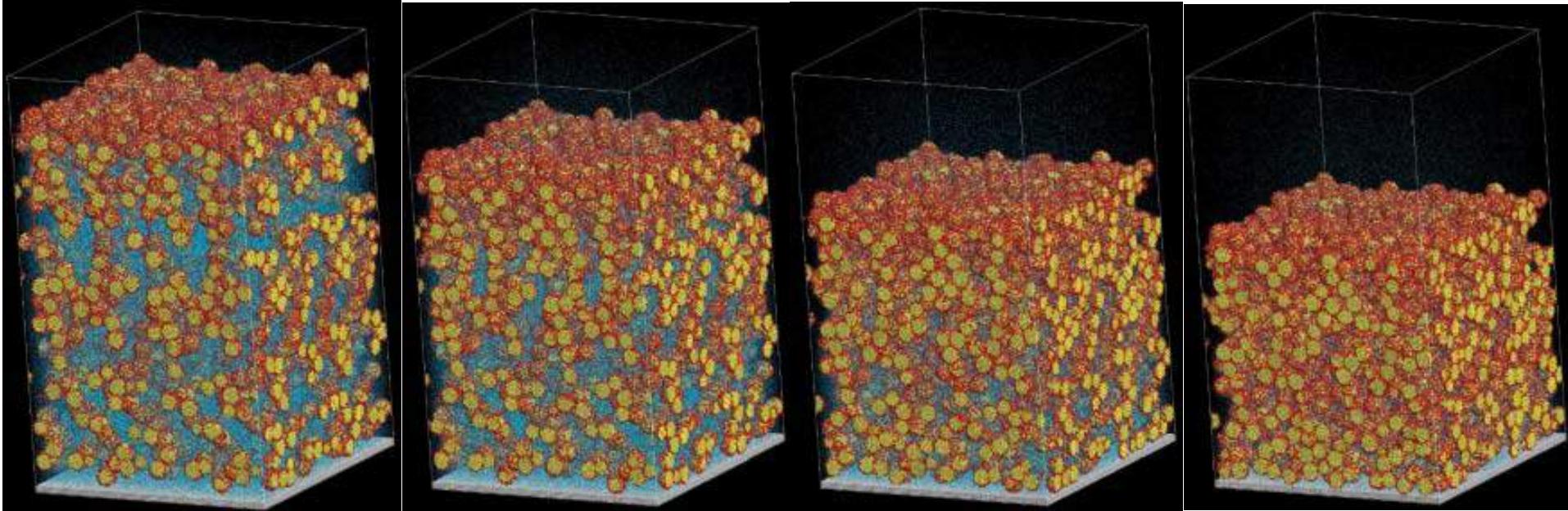
Slurry coating process



TOYOTA

■ 【Result】Molecular Dynamics (Large-scale model)(VSOP)

- Evaporating process (4 millions coarse-grained particles)



Initial → Final

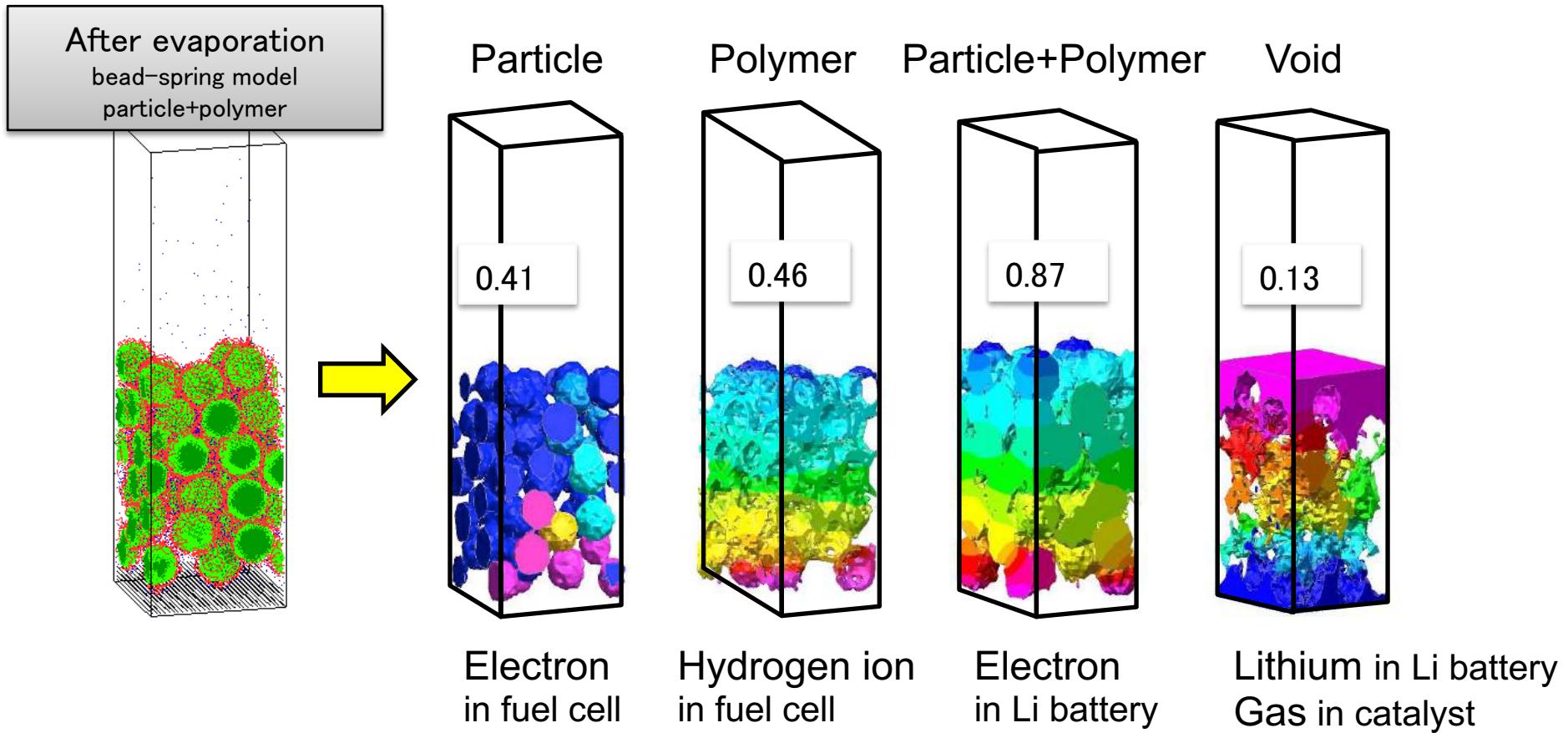
Confirmed that the slurry coating process can be simulated from molecular level

Slurry coating process



TOYOTA

Diffusion coefficient/Conductivity (LS-DYNA/Muffin)



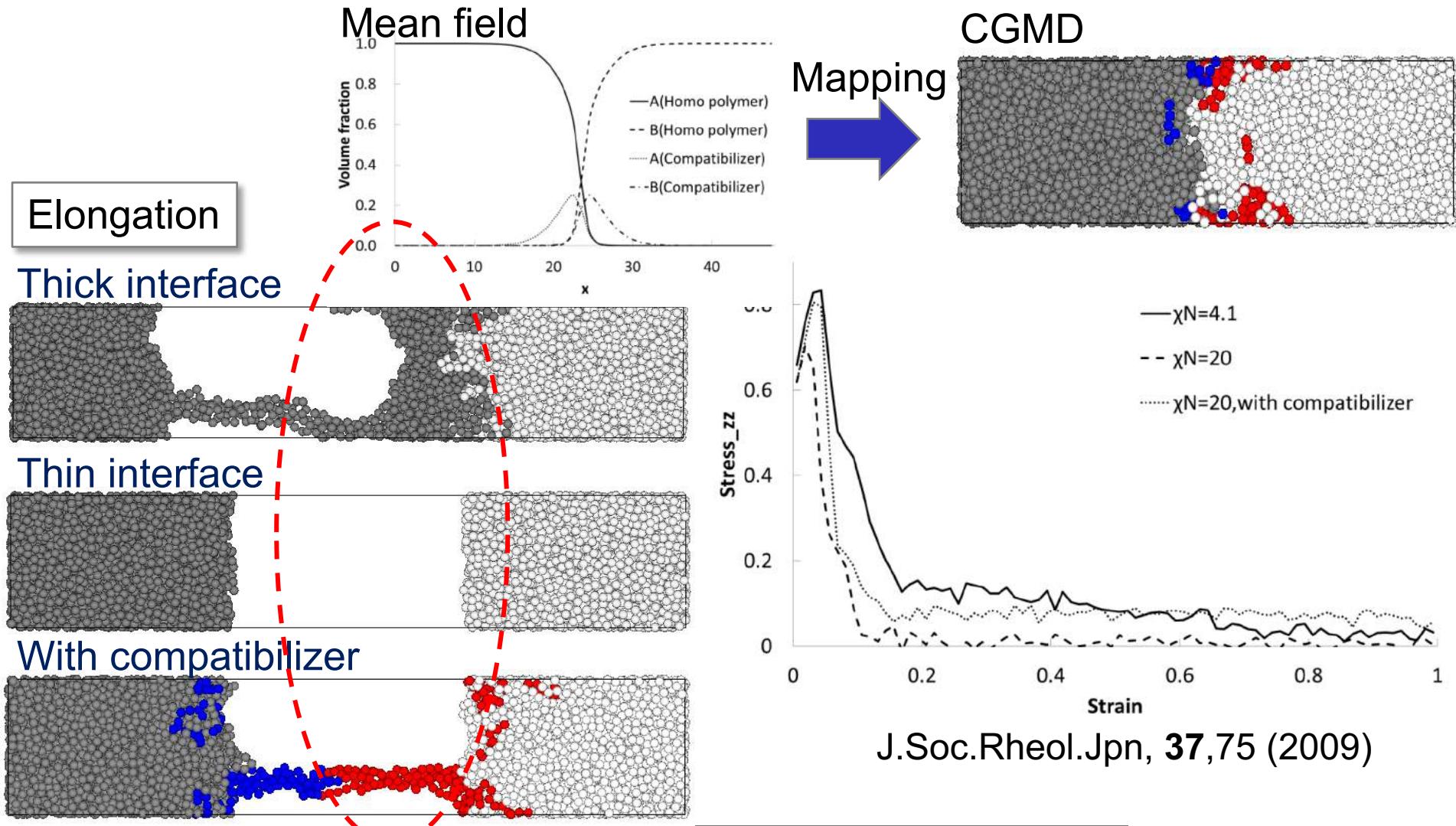
- ✓ Studies of material property with microstructure after evaporation using molecular dynamics (micro) and FEA (macro)

Strength of interface (polymer blend)



Mean Field \rightarrow Coarse grained Molecular Dynamics (CGMD)

For polymer blend, strength and structure of interface is important.

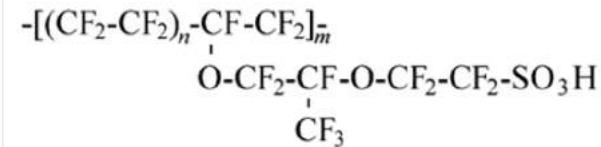
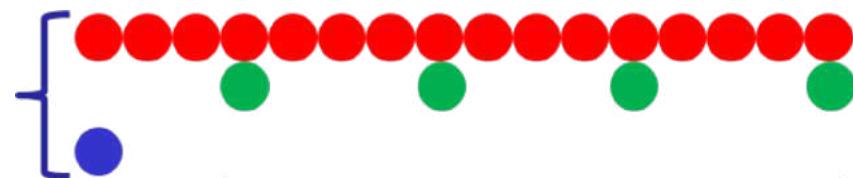
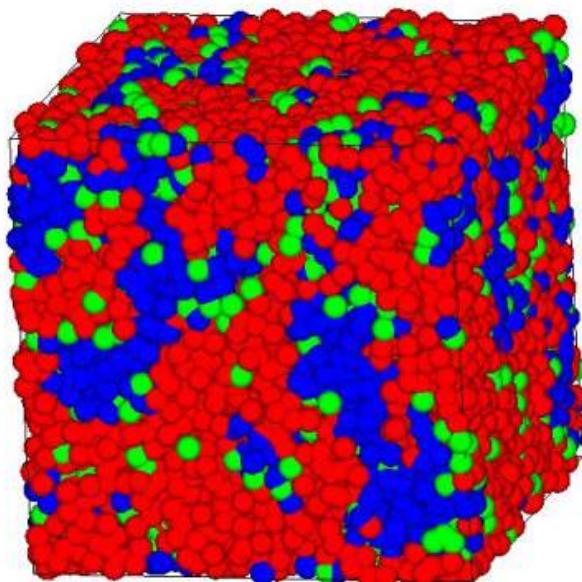


Polymer electrolyte for Fuel Cell



- Phase separation of polymer electrolyte and water
- Proton moves in the channel of water
- Estimation of the interaction parameter is possible on J-OCTA.
- Phase separation near Pt is calculated as well.

DPD



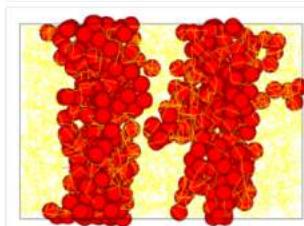
Thermoplastic elastomer



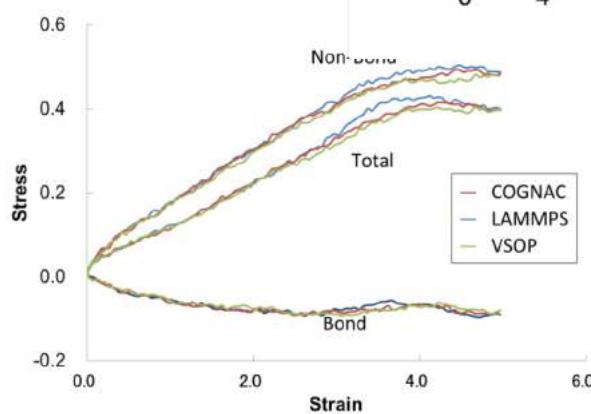
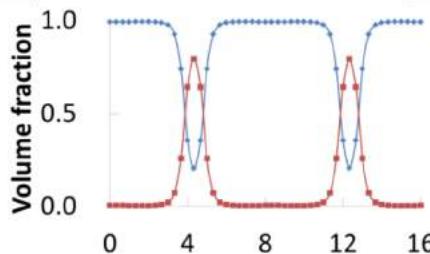
Mean Field -> Coarse grained Molecular Dynamics (CGMD)

- Phase separated structure of ABA triblock copolymer is calculated by using SCFT (SUSHI). Initial structure of Coarse Grained MD is created by using volume fraction distribution obtained by SCFT (Density Biased Monte Carlo method).
- Red; A=Styrene(glass state), Yellow; Isoprene (rubber state)
- Elongation simulation is conducted.

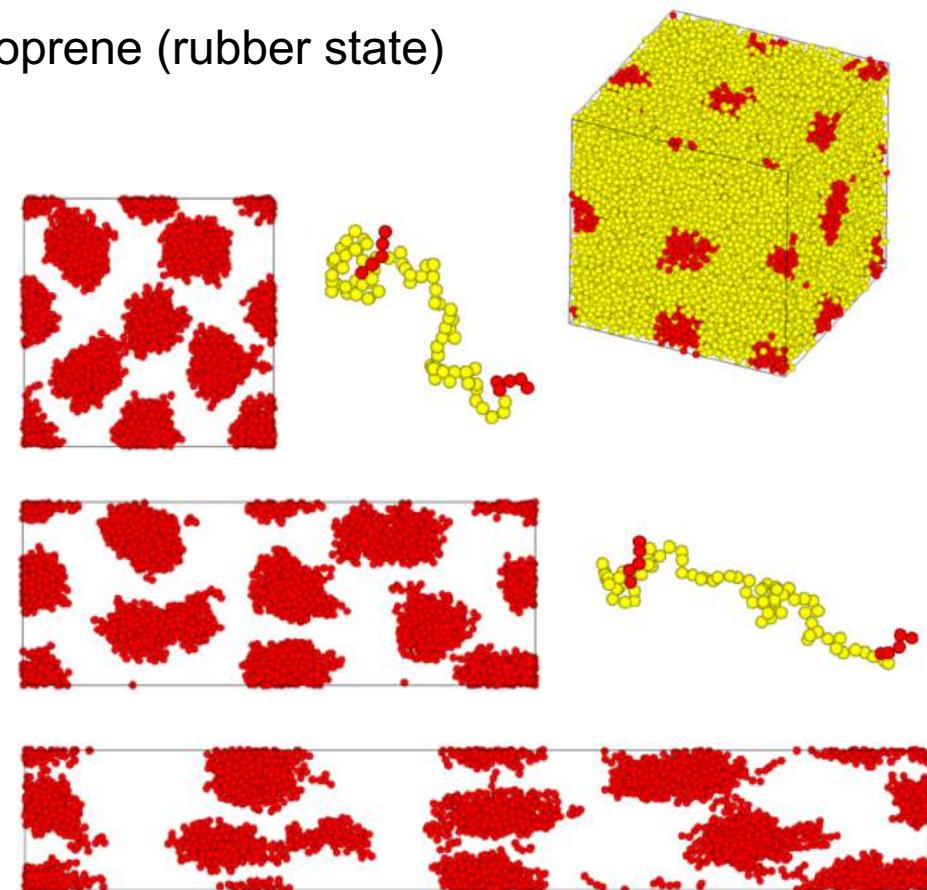
Density Biased Monte Carlo (DBMC) [OCTA-COGNAC]



Self Consistent Field Theory (SCFT) [OCTA-SUSHI]



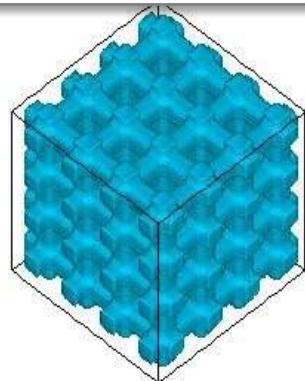
T.Aoyagi and T.Honda, J.Chem.Phys.,117, 8153 (2002)



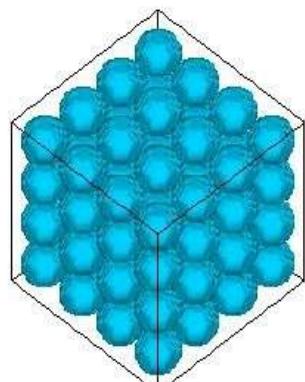
Polymer blend PP/Elastomer



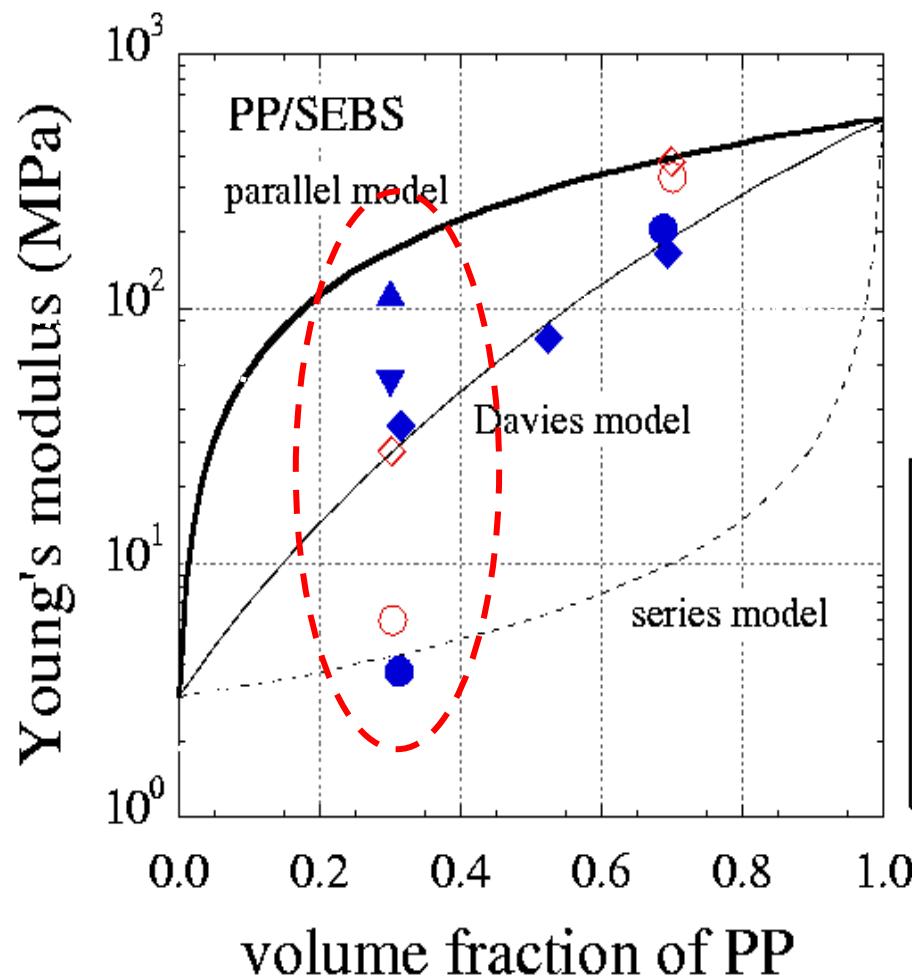
Prediction of average bulk modulus (MUFFIN)



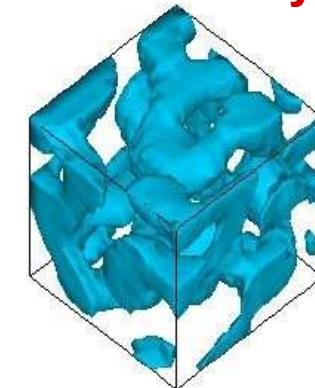
Bicontinuous



Dispersed



Mean field →
Elastic analysis (FEM)



Mean field

- Dispersed(exp.)
- ◇ Bicontinuous(exp.)
- Dispersed(simul.)
- ◆ Bicontinuous(simul.)
- ▲ WI(simul.)
- ▼ NI(simul.)

O_{CT}^A

- Elastic analysis based on phase-separated structure.
- Same volume fraction, but different average elastic modulus.

Polymer blend PP/SEBS



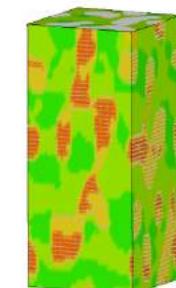
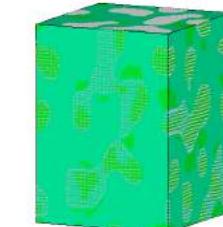
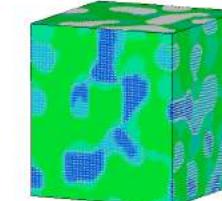
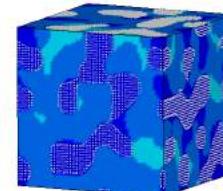
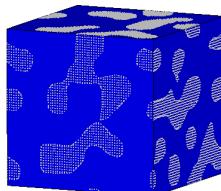
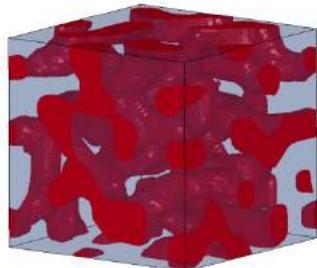
LS-DYNA

Mean field →
Elastic analysis (FEM)

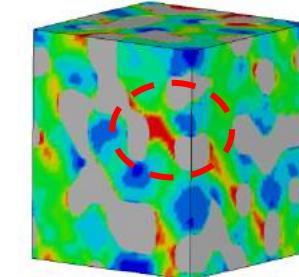
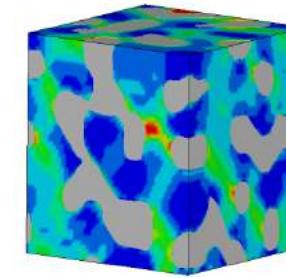
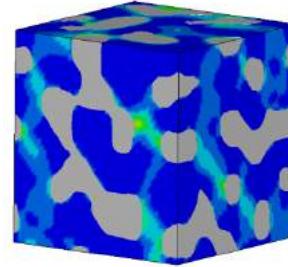
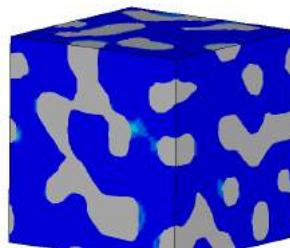
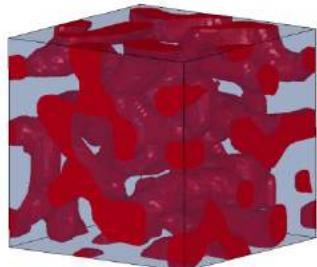
Non-linear structure analysis using LS-DYNA

Direct calculation from J-OCTA is possible.

Stress



Plastic strain

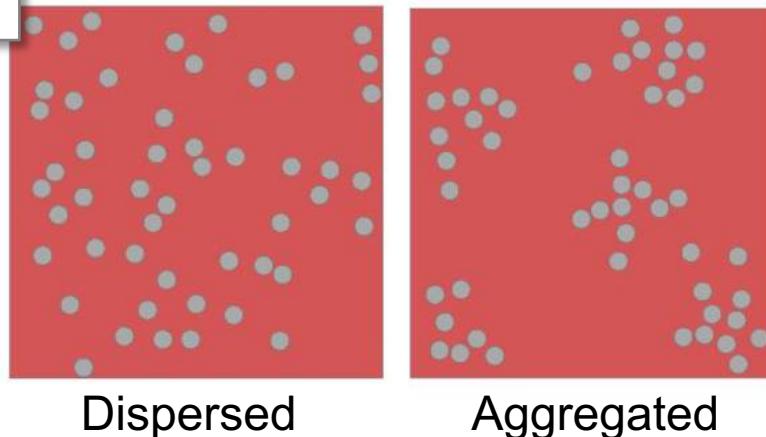


Fracture of CFRTP



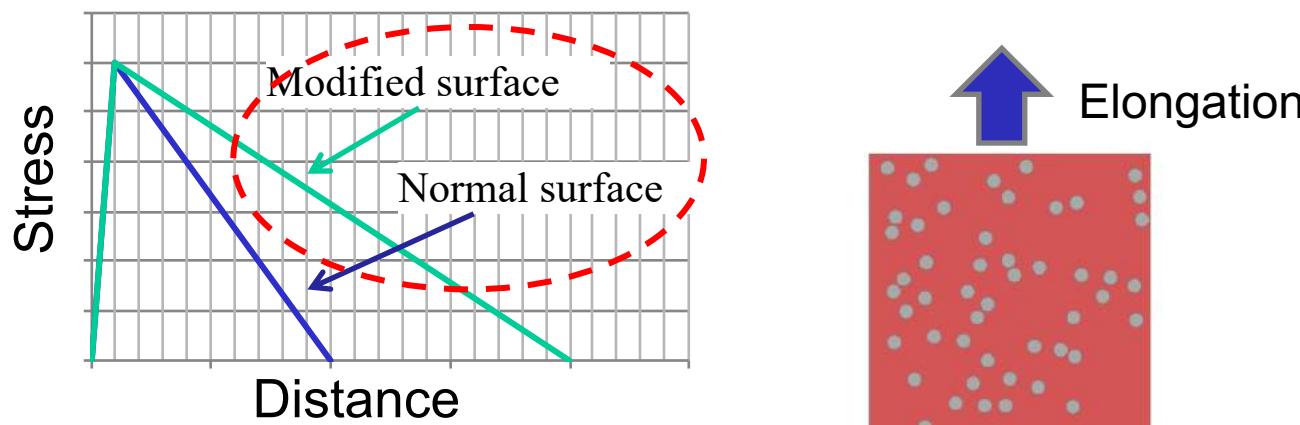
Meso-Structure (UD material)

Sectional view



Matrix : PA
Fiber : CF
10 vol%

Cohesive element considering results of CGMD

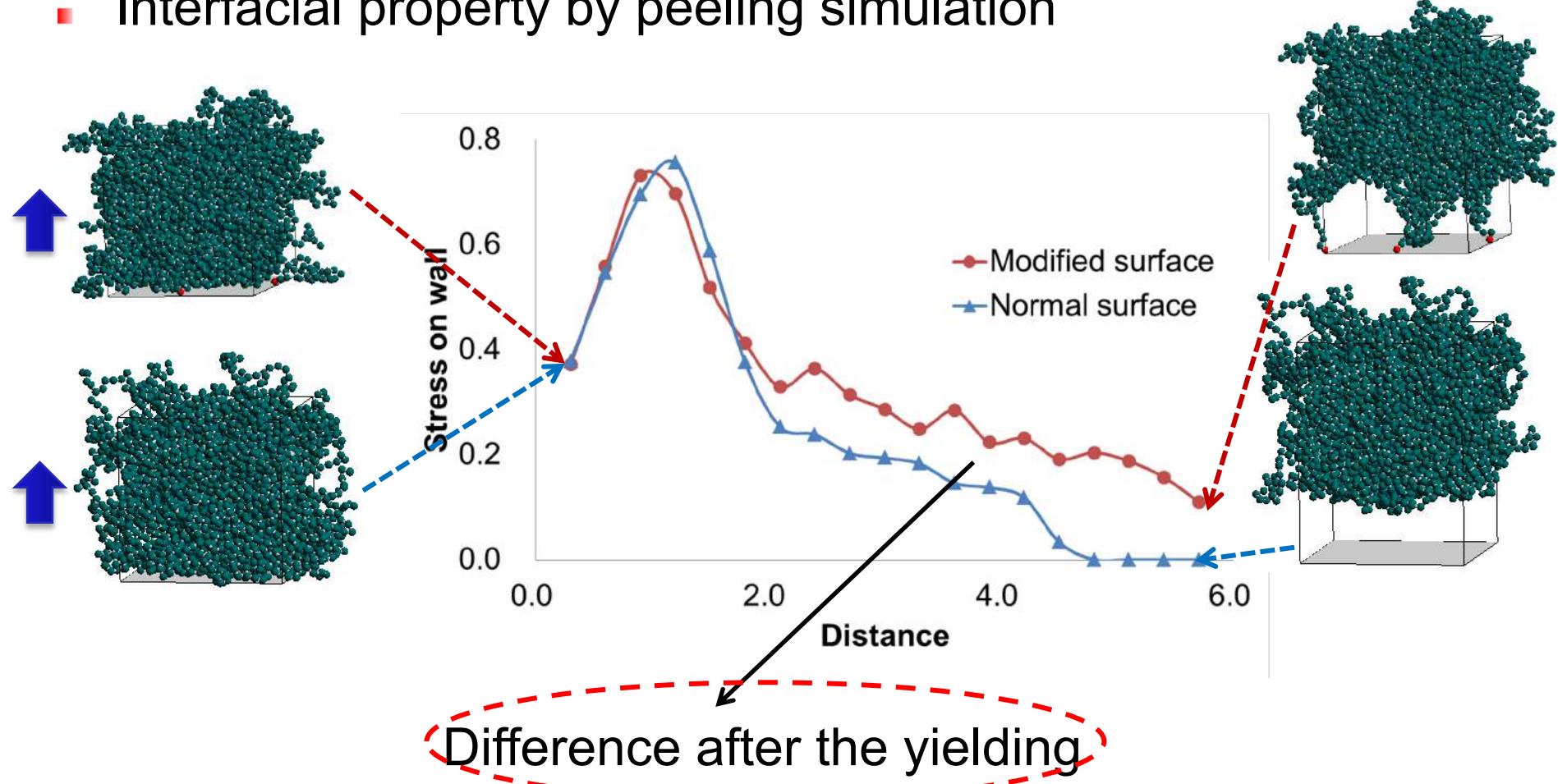


Fracture of CFRTP



Coarse grained Molecular Dynamics (CGMD)

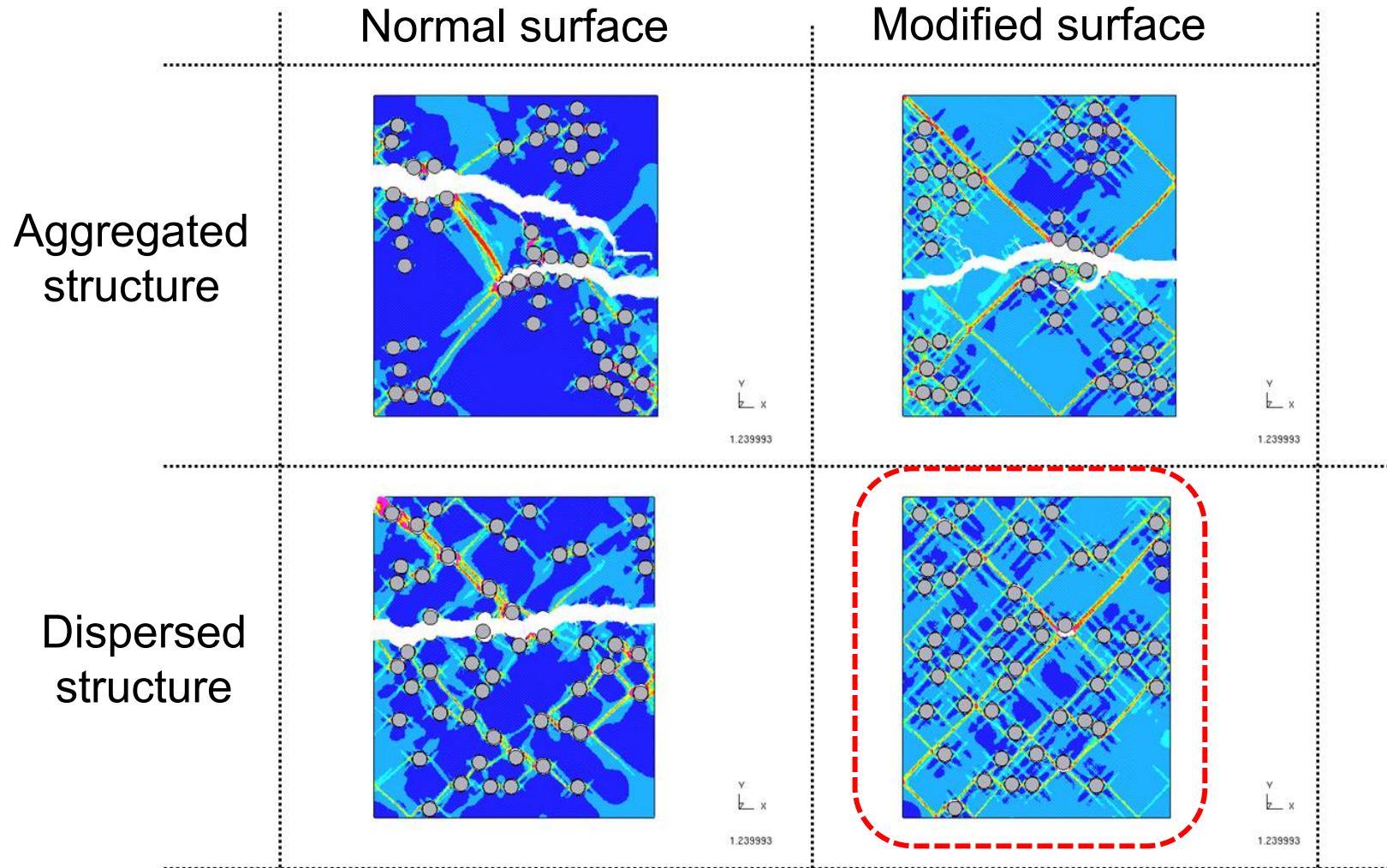
- Interfacial property by peeling simulation



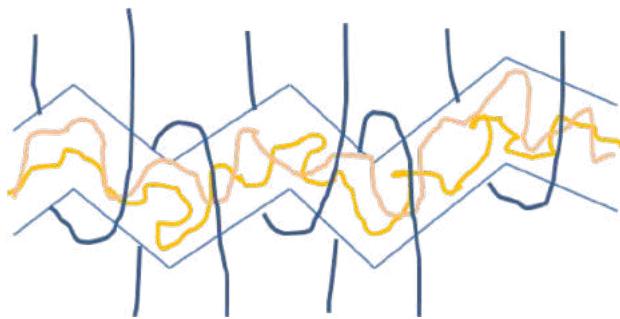


Non-linear structure analysis using LS-DYNA

digimat
LS-DYNA



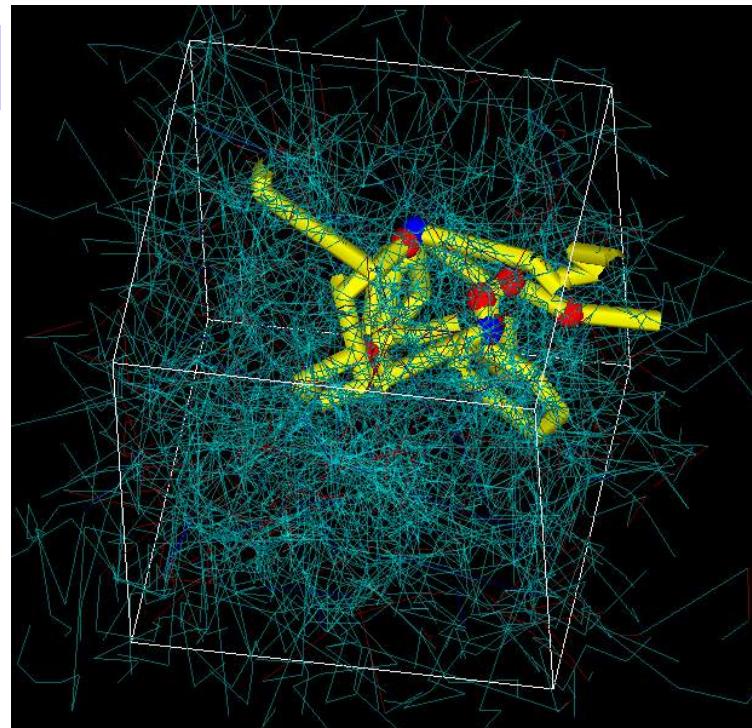
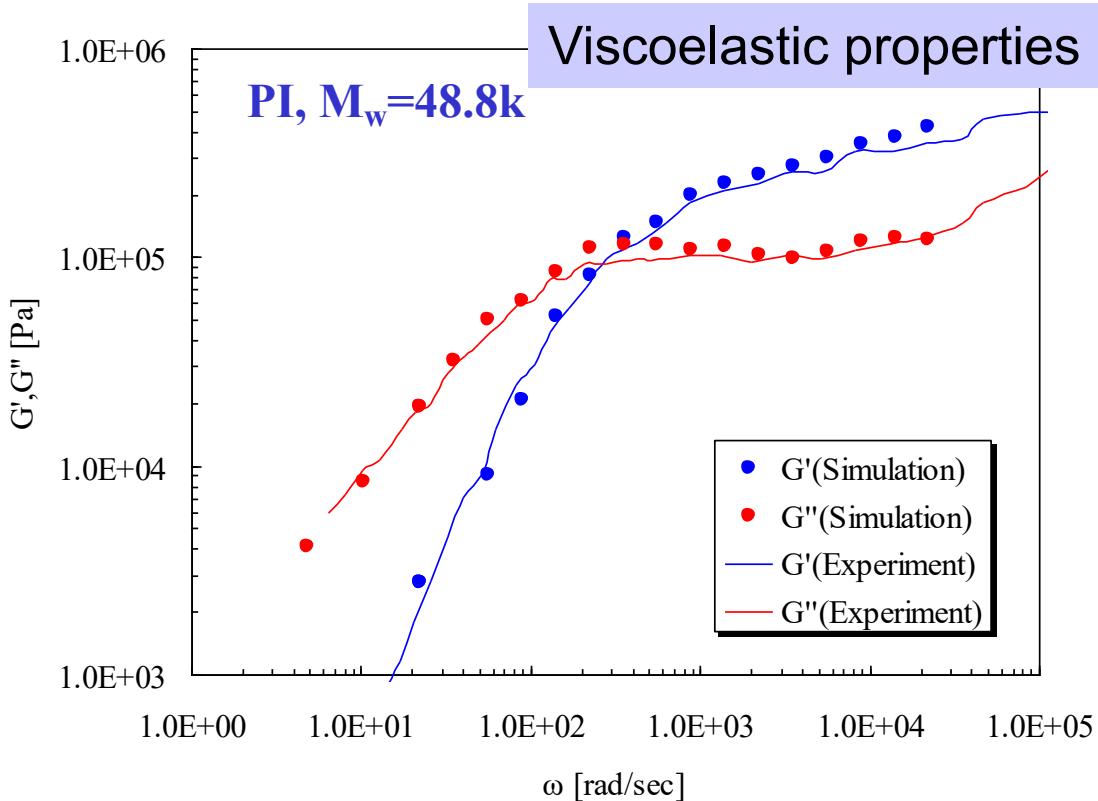
Dynamics of entangled polymer melt



Slip-link model
Primitive chain network model

- Coarse grained unit is based on entanglement
- Entangled polymer chain's long time relaxation
- Shear viscosity, elongation viscosity, etc.

Based on tube model.(Doi-Edwards)



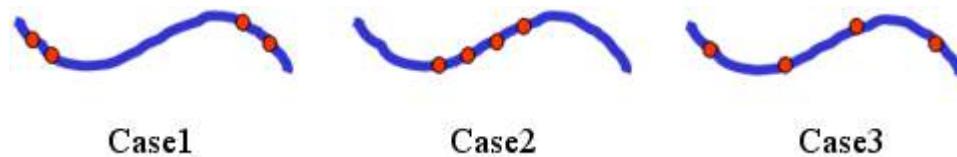
Rolling resistance of tire



courtesy of SUMITOMO RUBBER INDUSTRIES, LTD.

**Slip-link model
(Primitive chain network model)**

Dynamic viscoelastic properties of cross-linked poly-isoprene was calculated by using Primitive Chain Network model (NAPLES of OCTA). Effects of distribution of cross-linked positions (Fig.1) was evaluated. Molar mass of each molecule is about 300k.



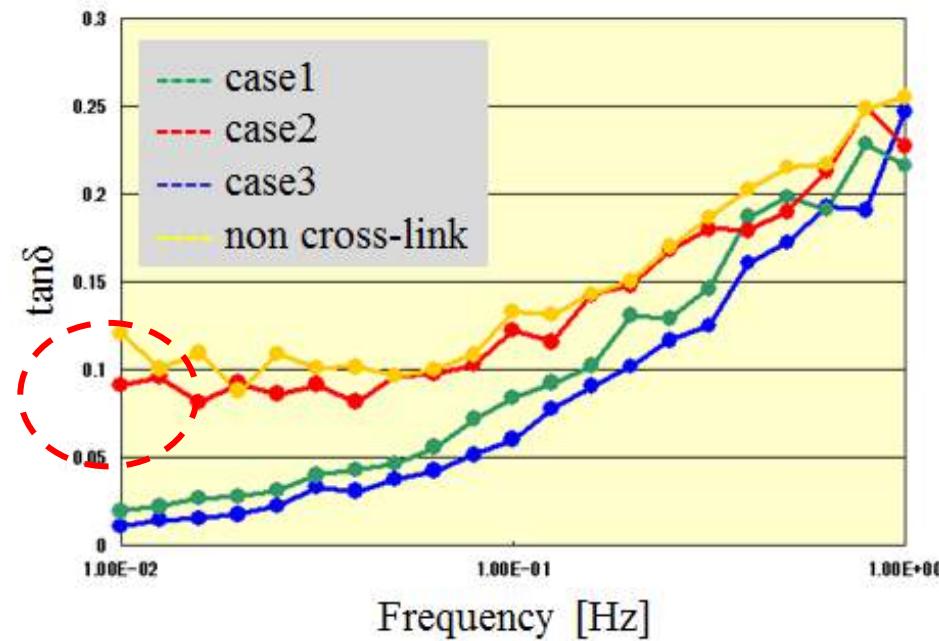
Case1

Case2

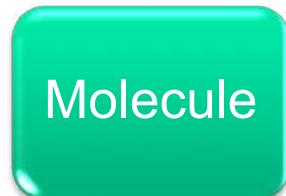
Case3

Rolling resistance of tire is related with $\tan\delta$ ($= G''/G'$). In case1 and 3, $\tan\delta$ shows low value at low frequency (Fig.2).

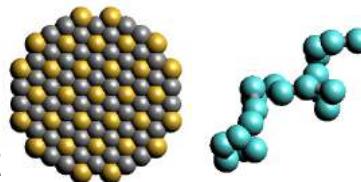
This means that chain end should be cross-linked to get low rolling resistance property.



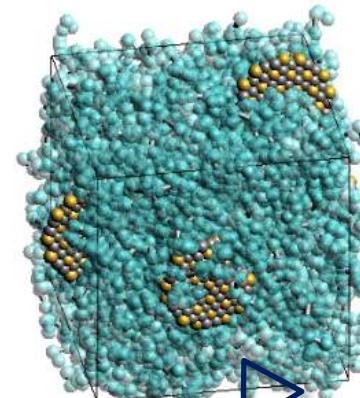
Nano Composite for CFRTP



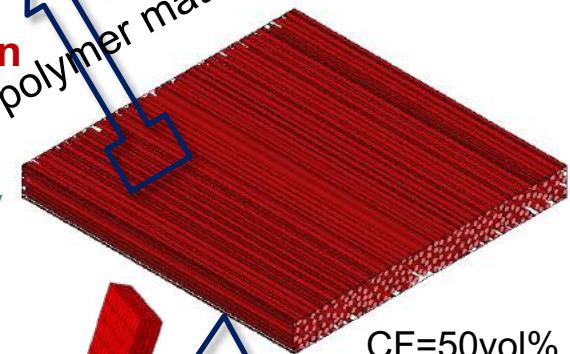
SP values of each component



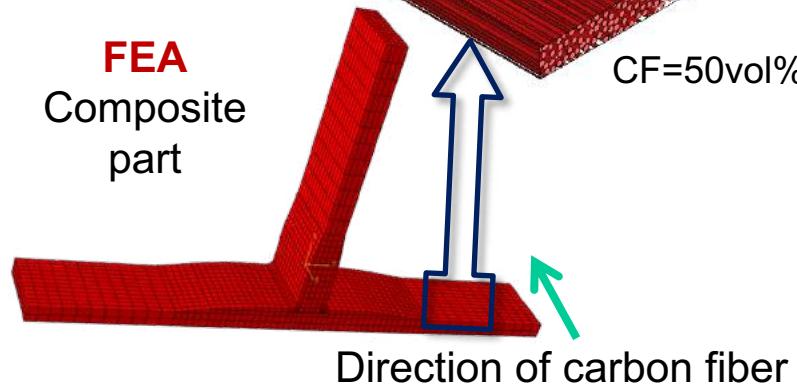
DPD and FEA
Graphene sheets in Polymer (PEEK)
Averaged property of polymer matrix



Equivalent inclusion theory
CFRTP
Averaged property



FEA
Composite part

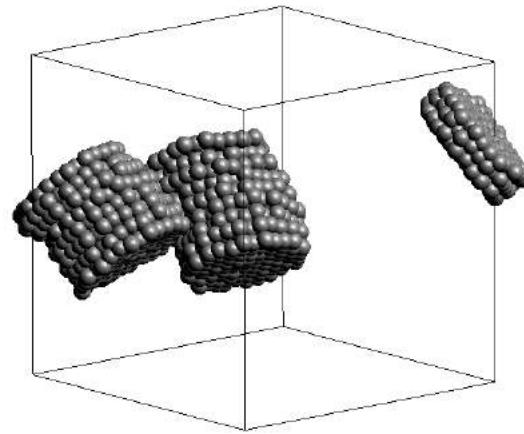


 digimat

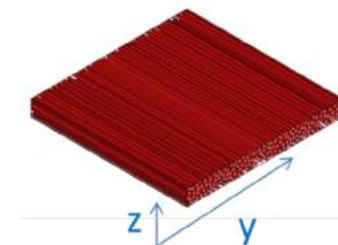
Nano Composite for CFRTP



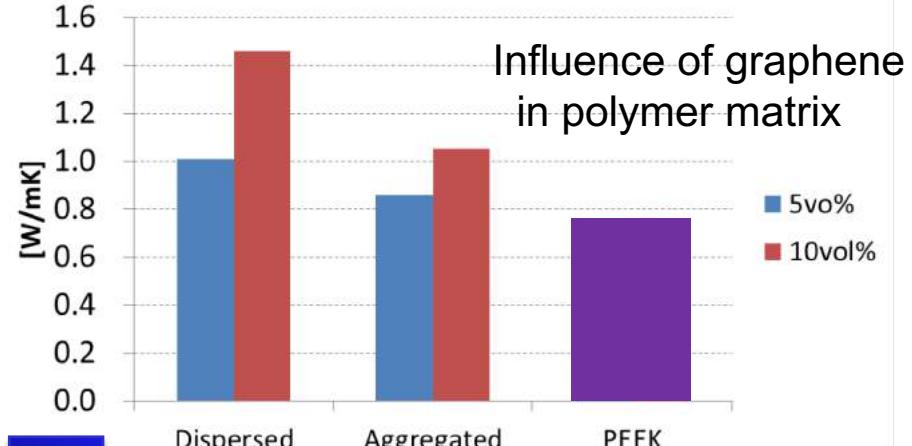
Mean value of thermal conductivity
in transverse direction of CFRTP



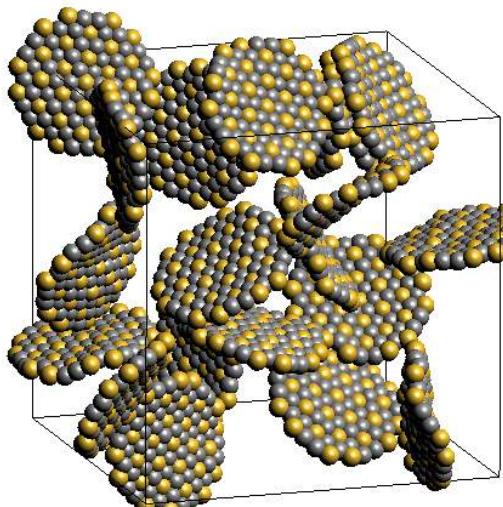
Aggregated



polymer matrix

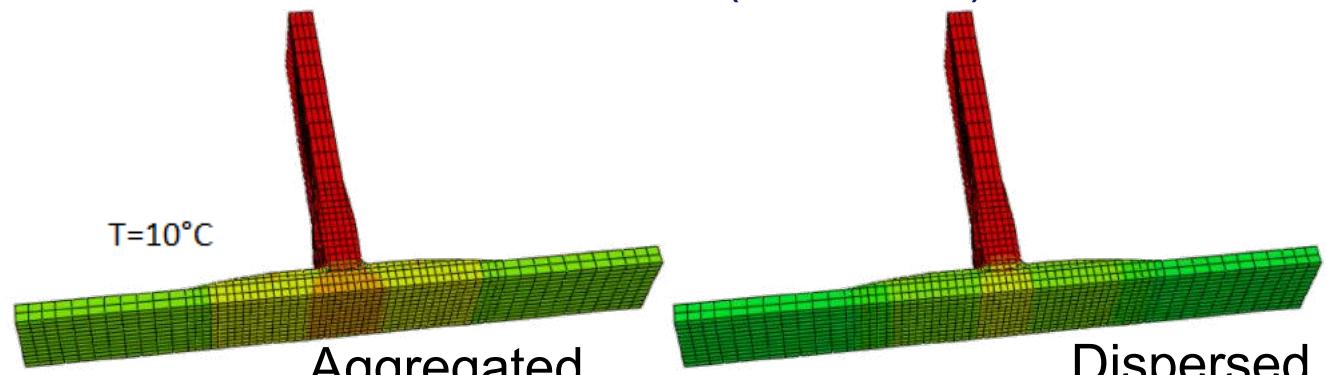


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Dispersed

FEA for macro Part (Heat Flux)



Aggregated

Dispersed

*Green is high, red is zero.



Multiscale studies in Rubber

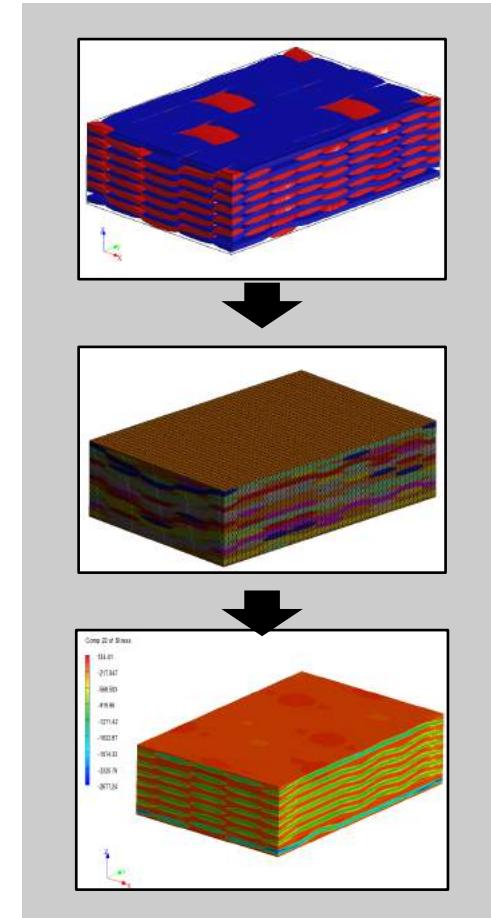
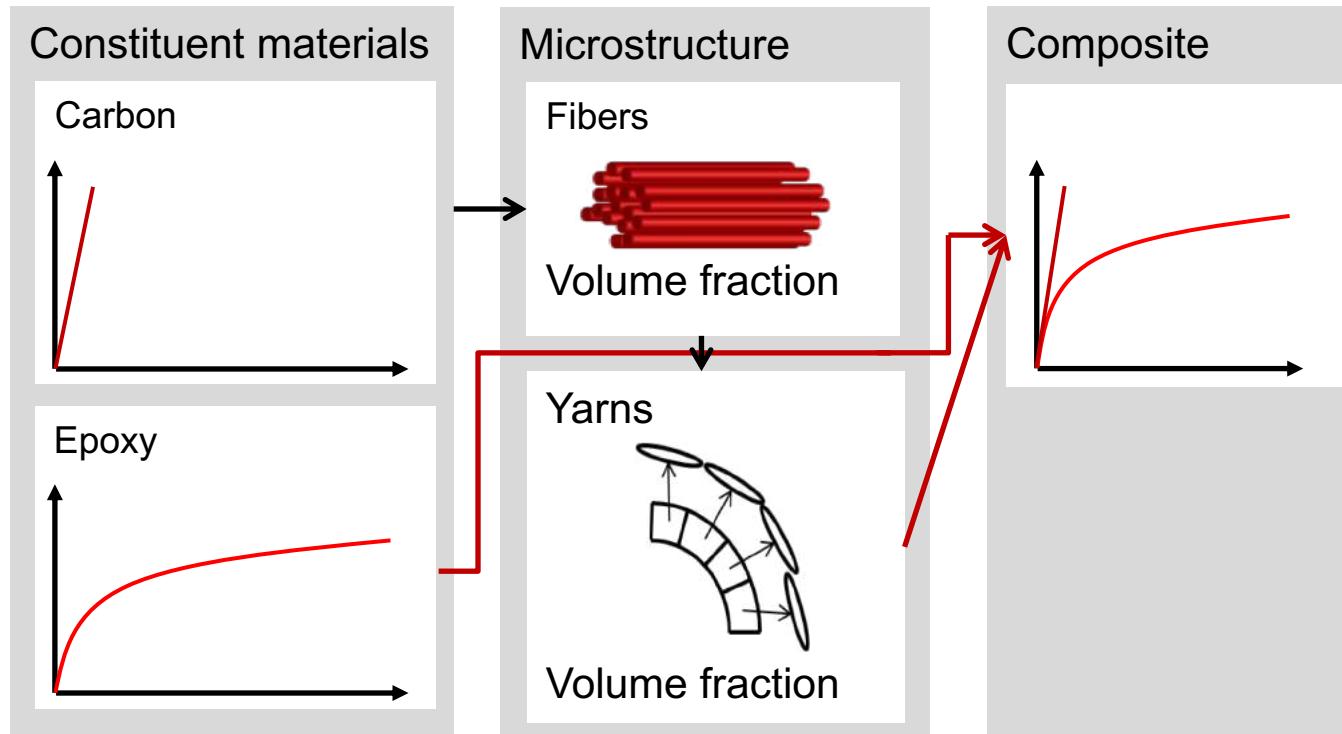


- Dedicated rubber material model
 - Hyperelastic
 - Thermo-hyperelastic
 - Visco-hyperelastic
- Large set of inclusion shapes (spherical, cylindrical , platelets, ...)
 - Including custom CAD
- In-house mesher
 - Conformal tetrahedral mesh
 - Non-conformal hexahedral mesh
 - Conforming extruded hexahedral dominated mesh
- In-house FE solver
 - Direct and iterative solver
 - With dedicated elements for rubber composites
- In-house post-processing

Multi-scale Simulation with Homogeneous Theory



- Two scales simulation for Woven
 - Mean-field homogenization for yarn
 - Full-field homogenization for woven



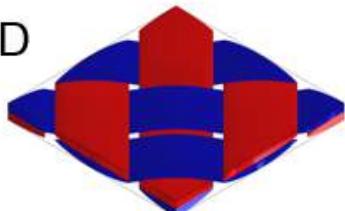


Digimat offers 3D Woven capabilities

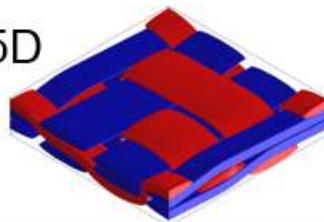
3D Woven from Template to User defined

Fabric type

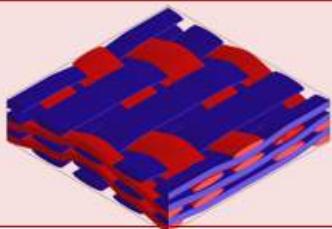
Woven 2D



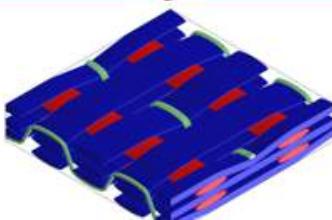
Woven 2.5D



Woven 3D interlock



Woven 3D orthogonal



Weave definition

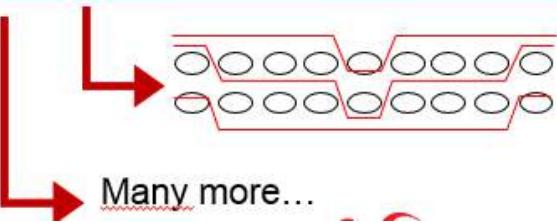
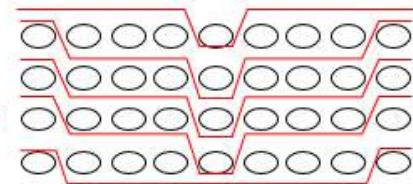
User defined

User defined

Template

Template

Additional templates become accessible for woven 3D interlock

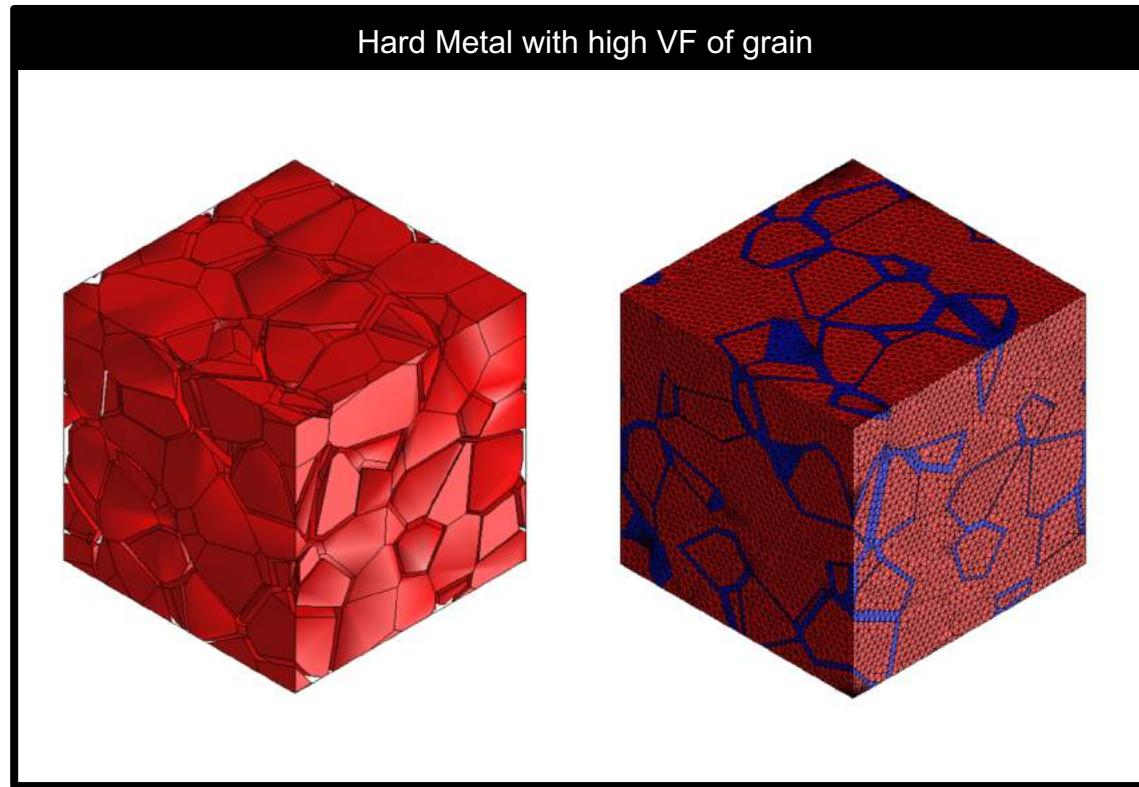




Complex RVE generation with FEM

- For various type of microstructures

- SFRP
- LFRP
- Hard metals
- Woven

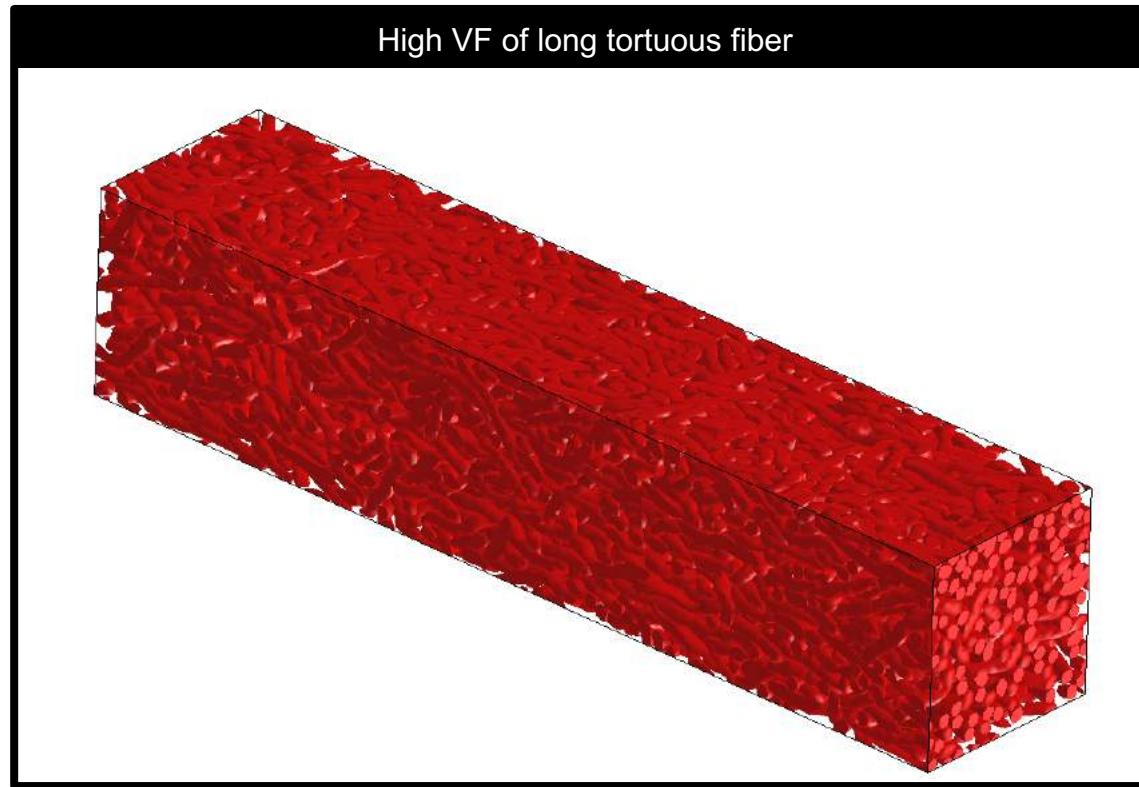




Complex RVE generation with FEM

- For various type of microstructures

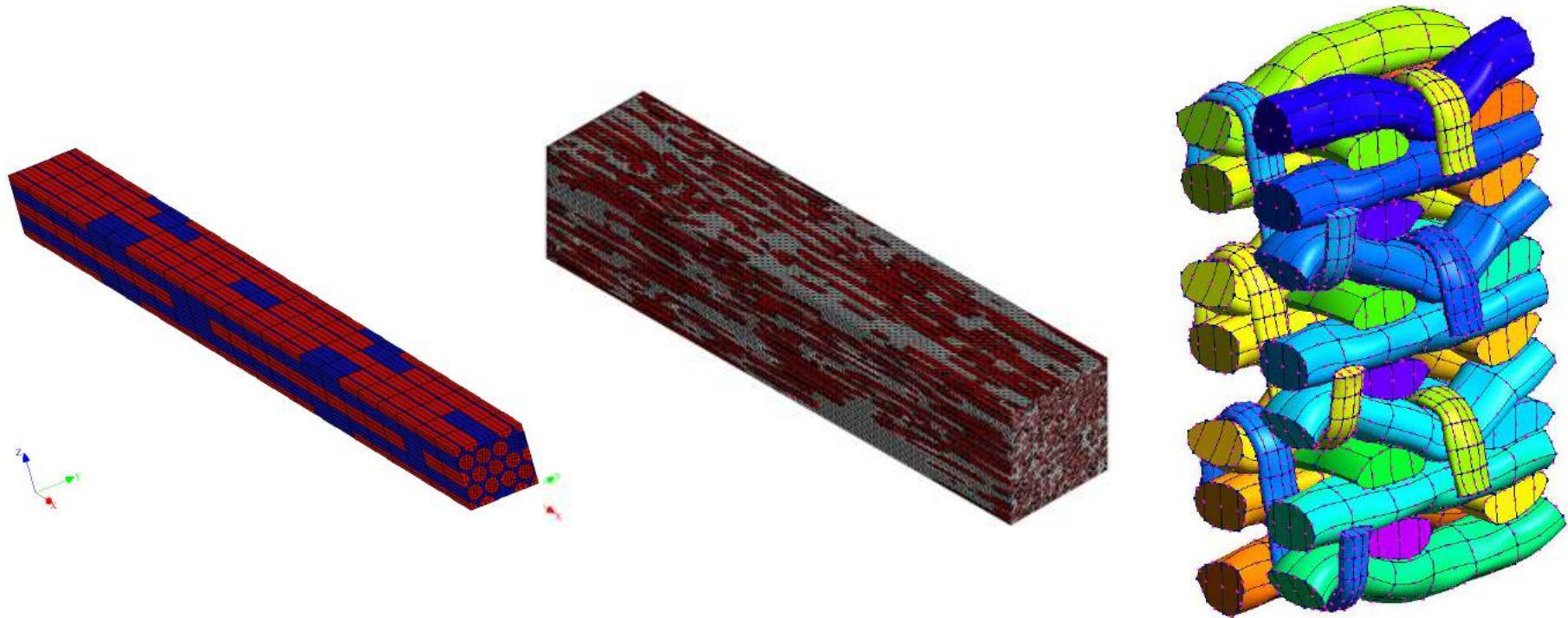
- SFRP
- LFRP
- Hard metals
- Woven



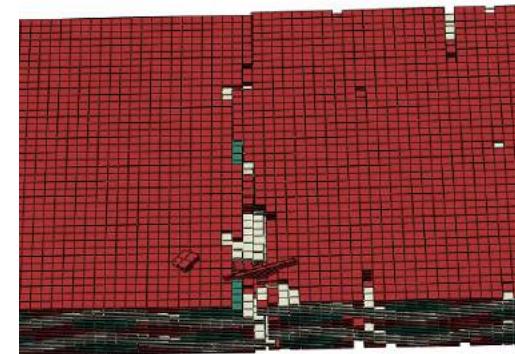
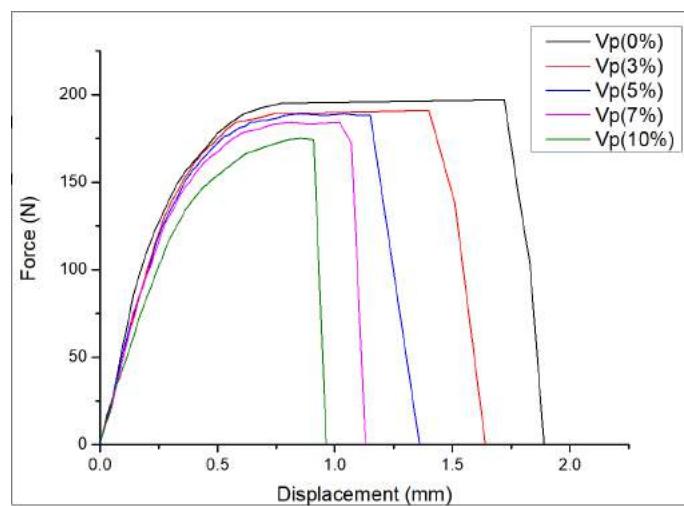
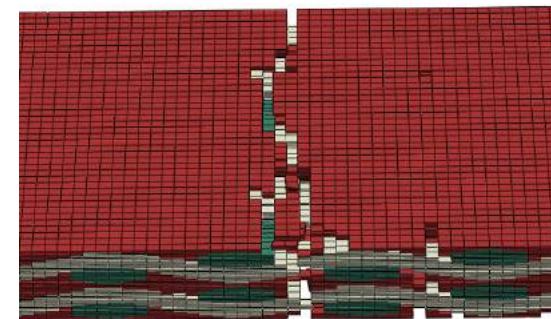
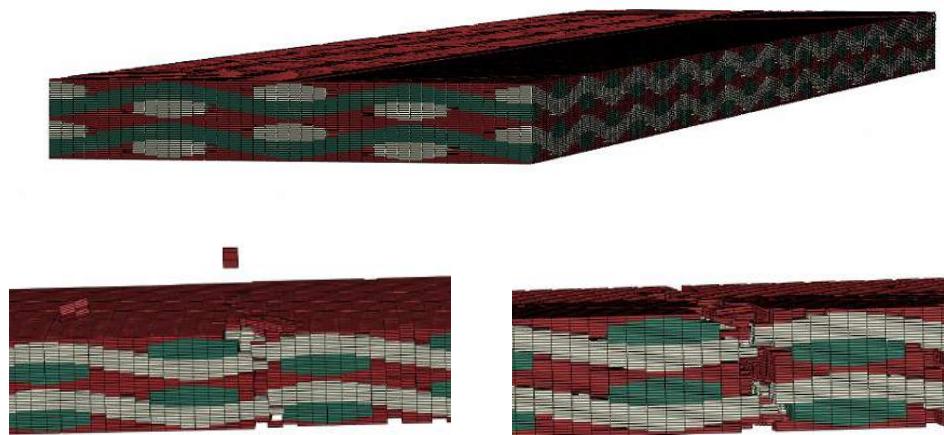


The expertise in advanced meshing

- Conforming extruded hexahedral dominated mesh
- Mesh cutting algorithm

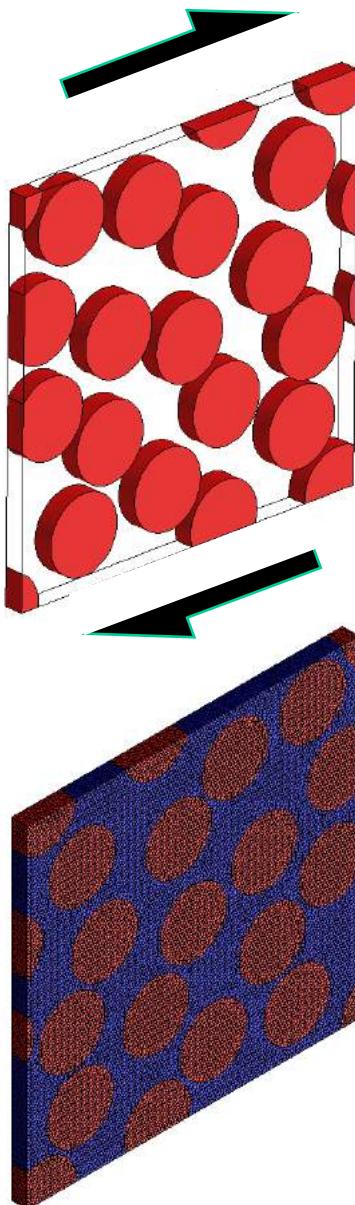


Failure modeling capabilities

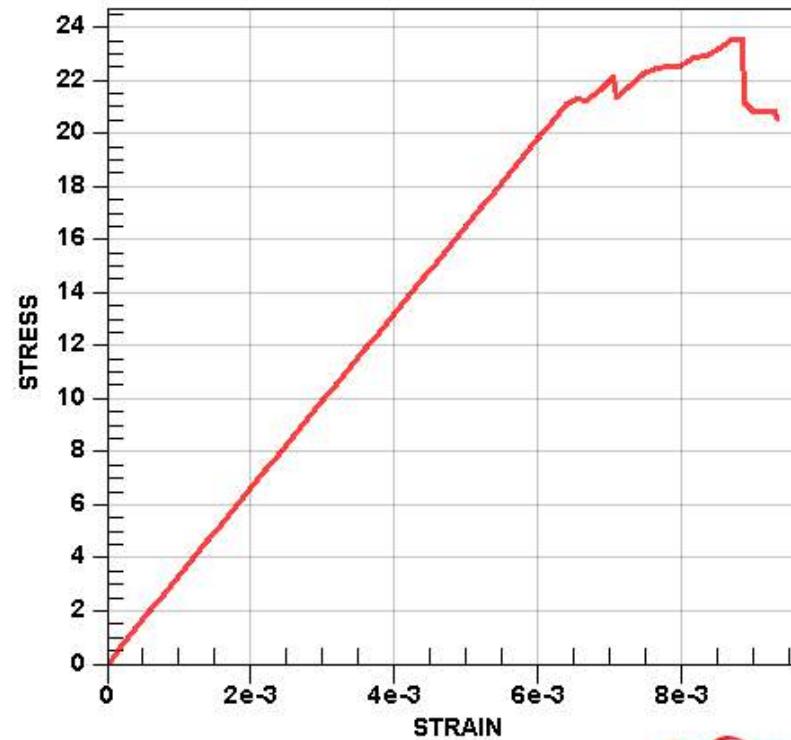


Damage due to different void contents

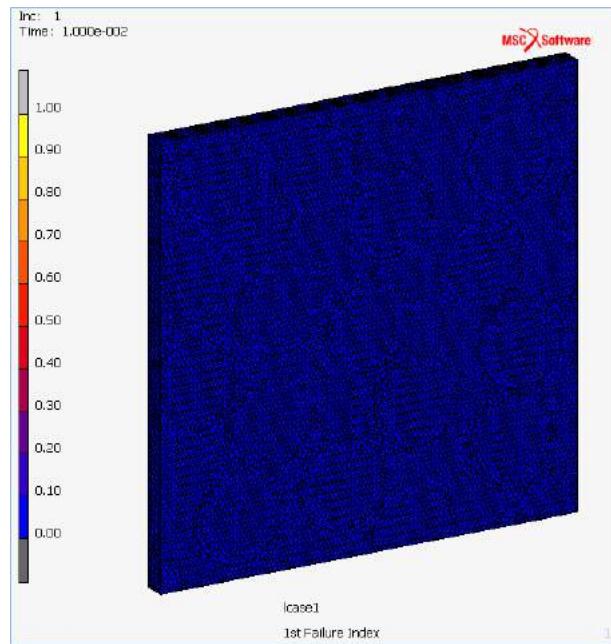
Failure modeling capabilities



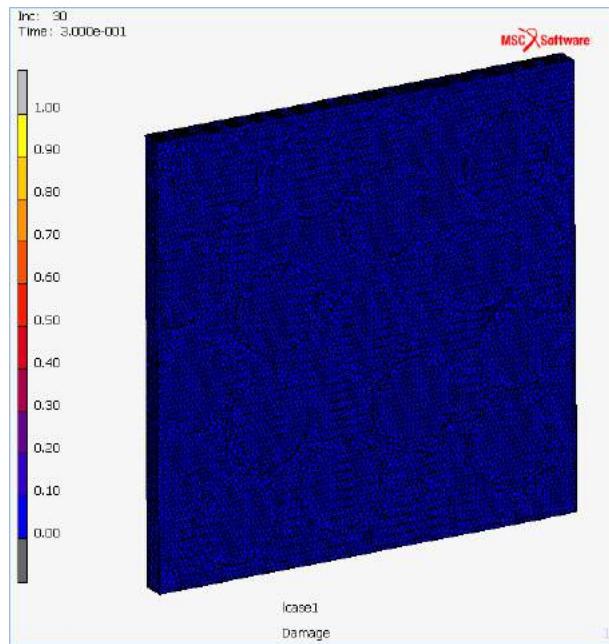
- 3D slice of unidirectional carbon-epoxy composite
- Transverse shear loading
- Elastic with damage resin behavior
- Fiber-matrix debonding using cohesive surfaces



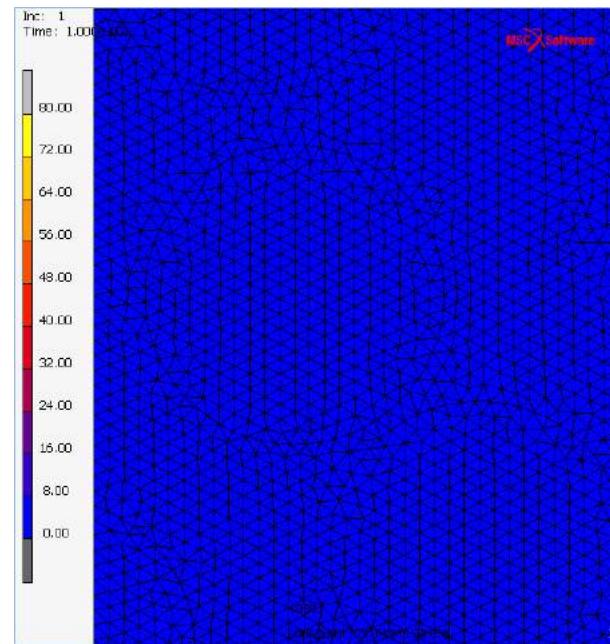
Failure modeling capabilities



Failure criterion



Damage leading to stiffness reduction

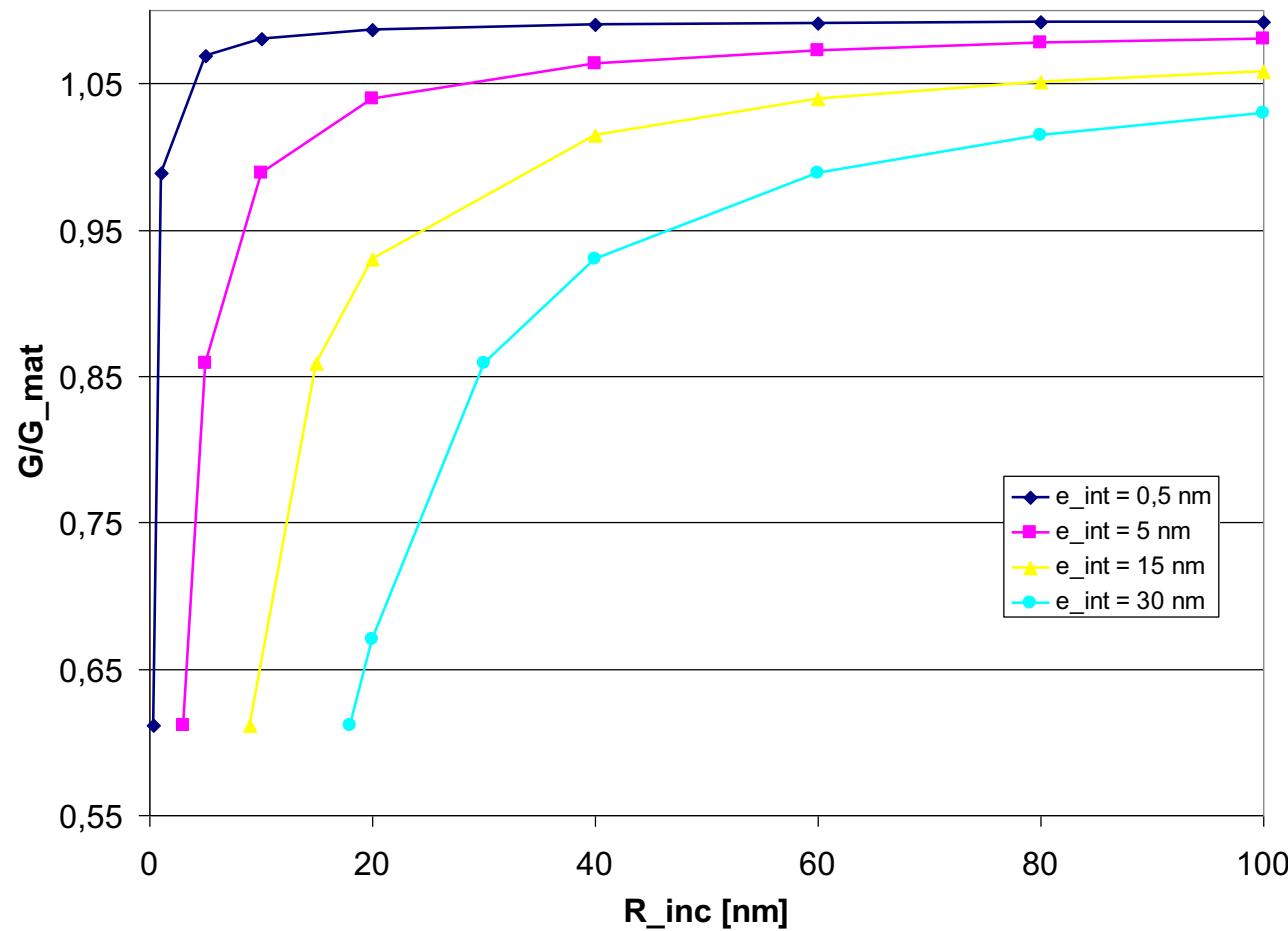


*Zoom over fiber-matrix debonding
(deformation scale factor of 5)*



To model matrix-filler interface

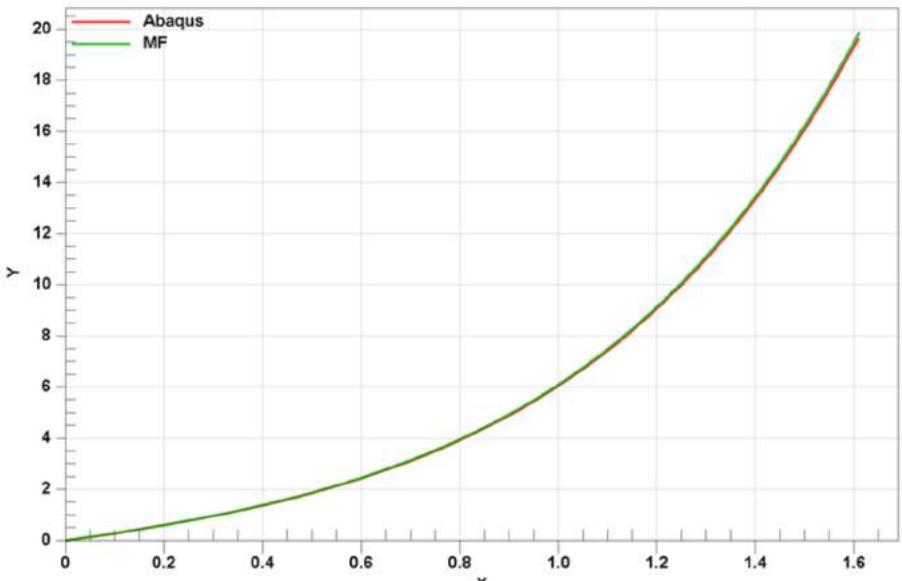
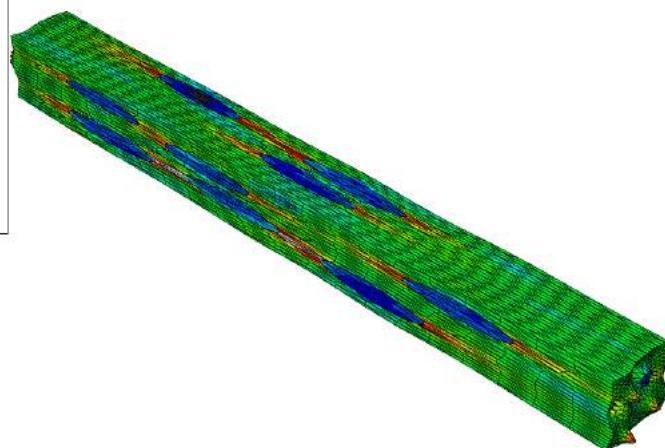
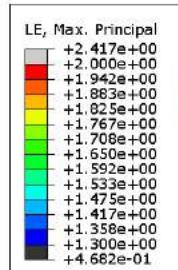
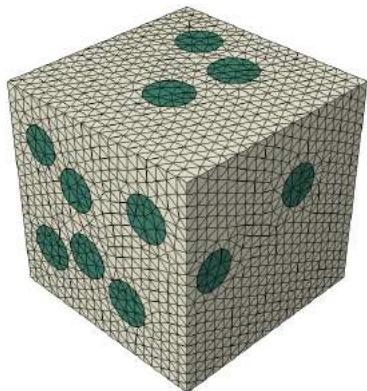
- Coating is a way to model the influence of the filler on the rubber properties at the rubber-filler interface





160% deformation in large strain

- For rubber blend



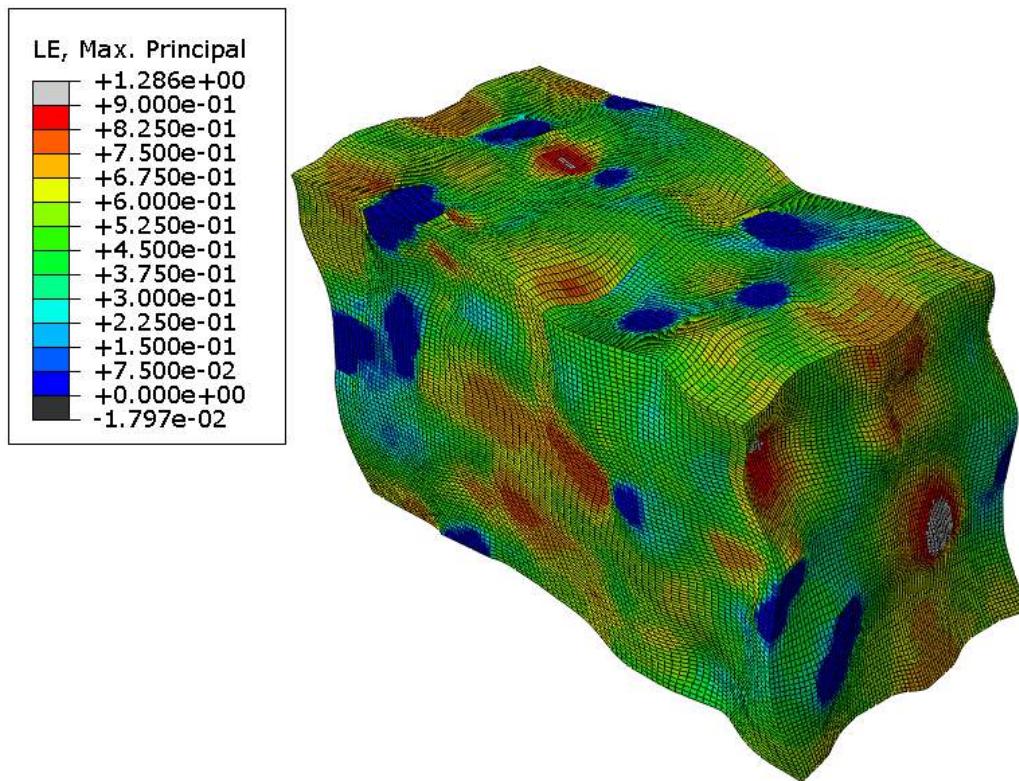
© digimat

100% deformation in the matrix in large strain



- For silica with silane

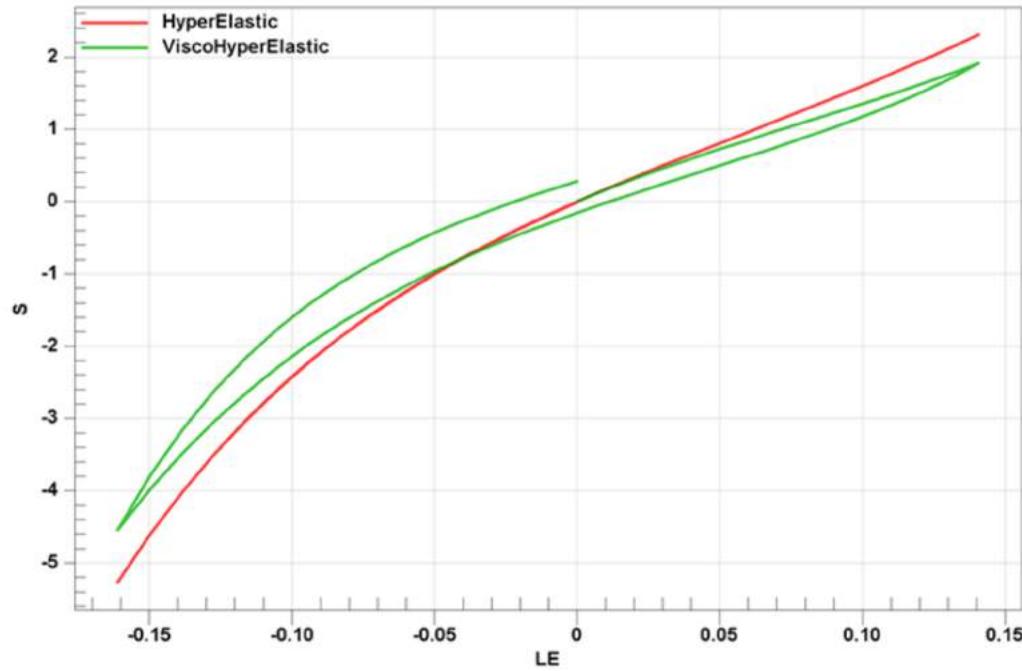
- Reduced integrated elements allow to reach the highest strain but requires large number of elements to reduce hourgassing
- Fully integrated elements allow accurate predictions for a low number of elements but final strain is lower





Extend its material library to advanced hyper-elastic model

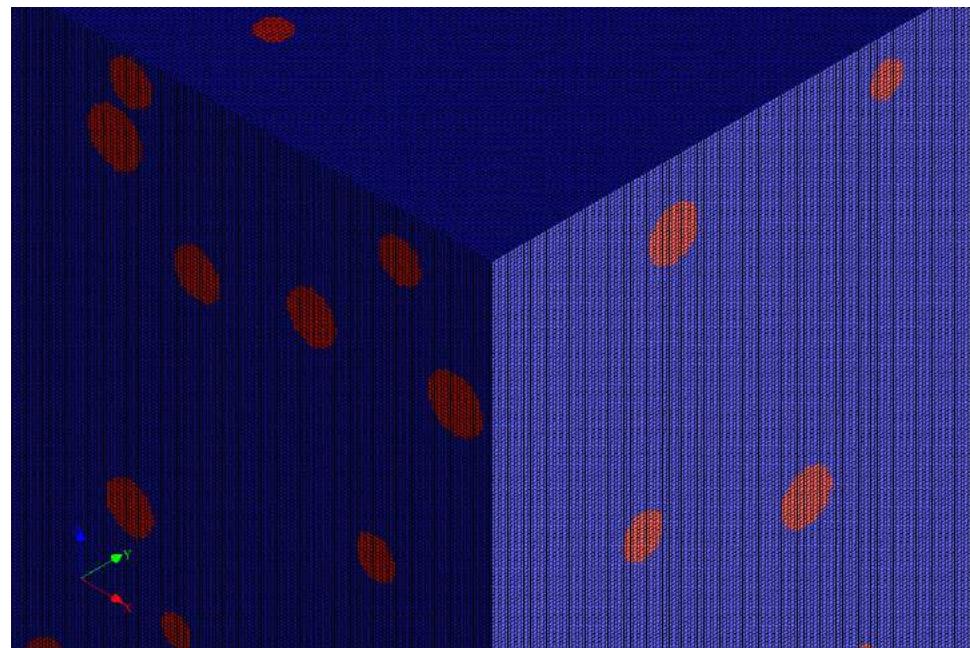
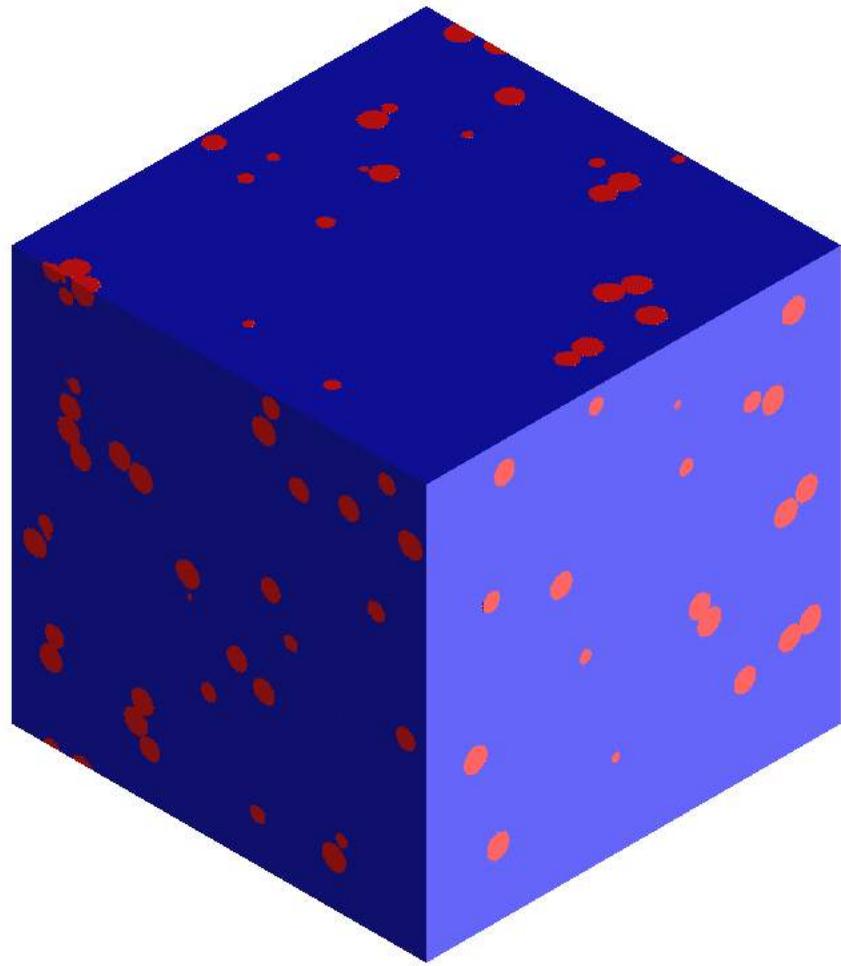
- Visco-hyperelastic model has been tested
 - In FE-Solver
 - In Abaqus
- Other models could be added
 - Thermo-visco-hyperelastic



Digimat can generate very large RVE

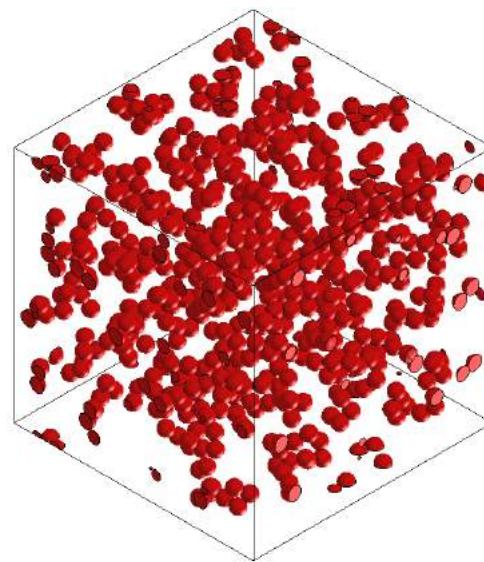


- Illustration with 640 inclusions and 30M voxels





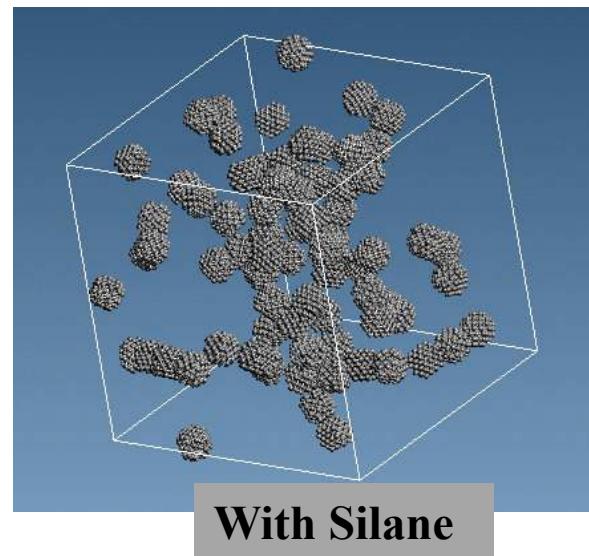
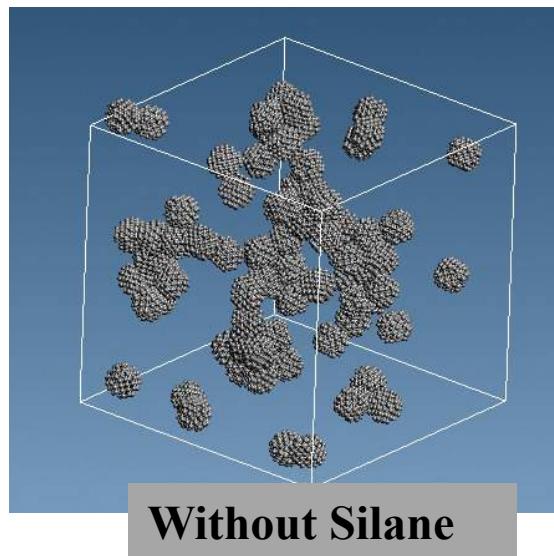
■ Connection to Molecular Dynamics



Molecular Dynamics predict dispersion of nano-fillers based on Dissipative Particle Dynamics (DPD)



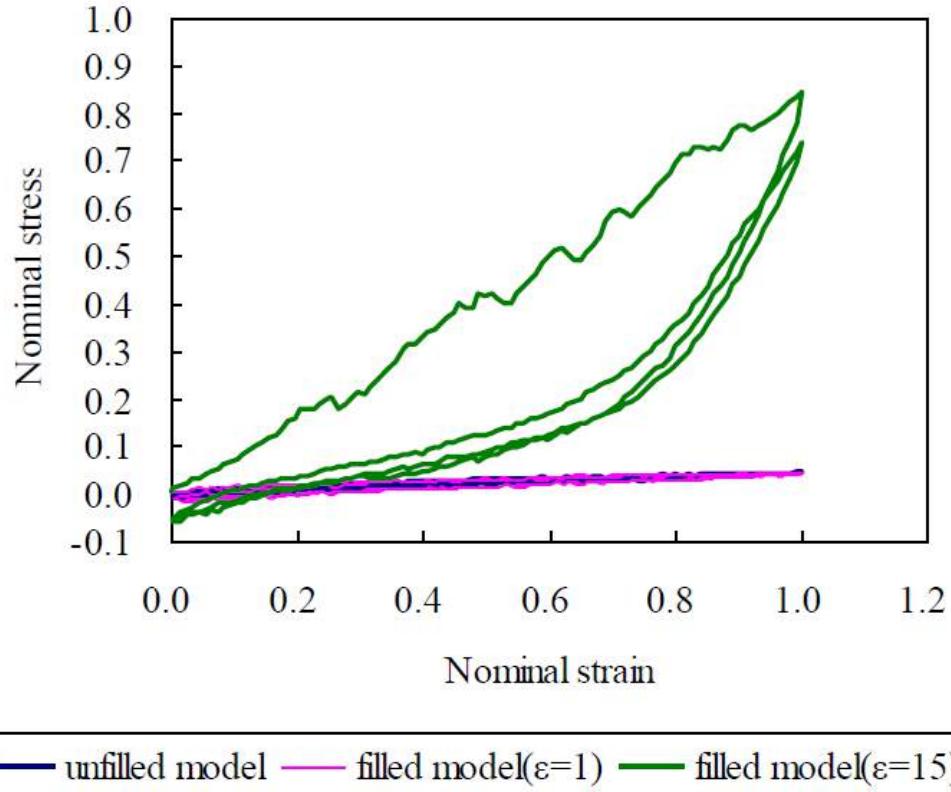
- Dispersion of silica particles in rubber
Solubility parameters of silane modified silica particle from reference
M.Khayet&al, Polymer 46 (2005) 9881-9891



Molecular Dynamics predict the influence of fillers on the rubber composite based on CGMD



- Yokohama Rubber (JSME 2015)
 - Influence of bridging polymer chains between fillers
 - Elongation and compression, hysteresis curve.
 - Small system (under 0.1M beads), using J-OCTA.



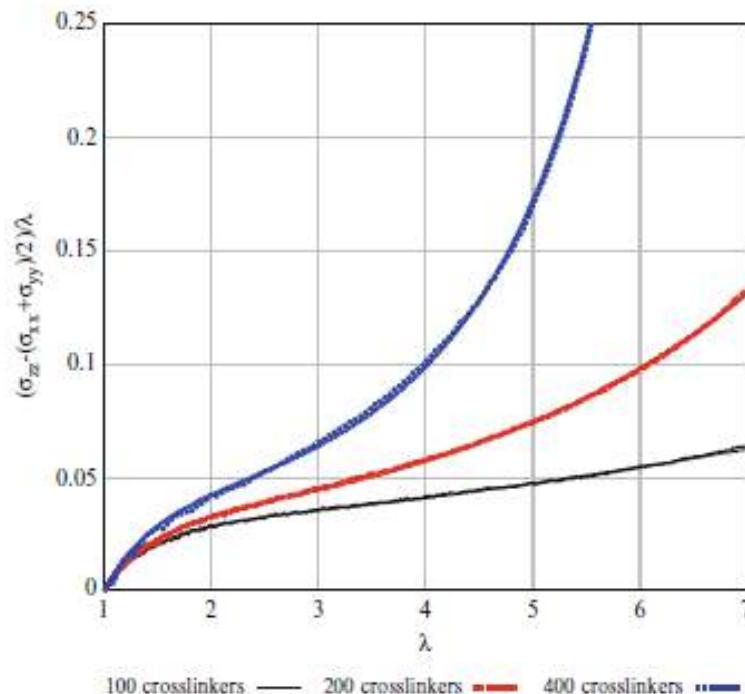
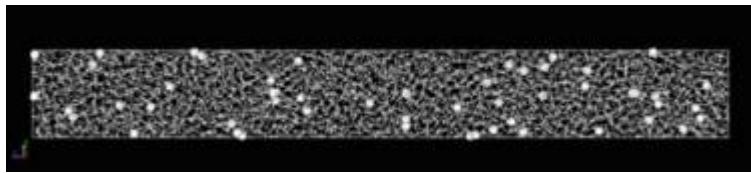
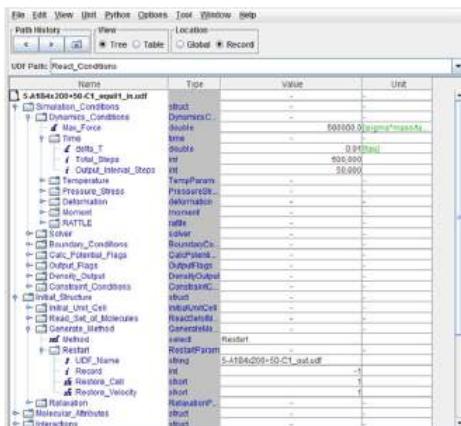
Molecular Dynamics predict the influence of fillers on the rubber composite based on CGMD



- **Cross-Linked Rubber**

Hiroshi Shima, BRIDGESTONE Corporation, Tokyo, Japan
 Chapter 15, Computer Simulation of Polymeric Materials
 Applications of the OCTA System, Springer, 2016

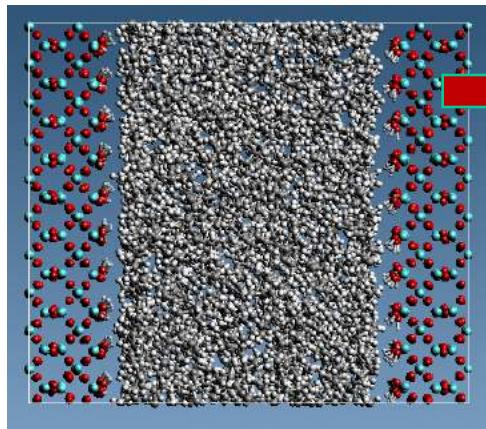
- **Formation of cross-linked structures and elongational physical properties using OCTA**



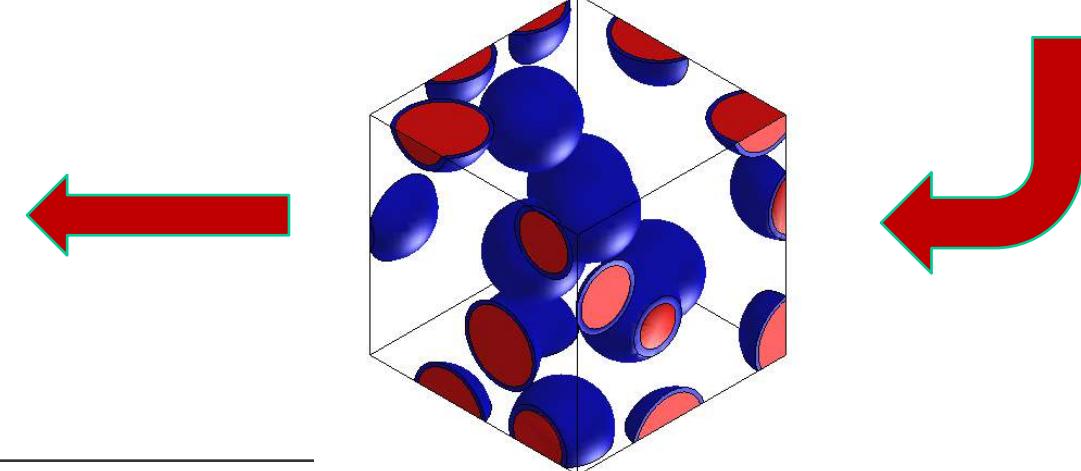
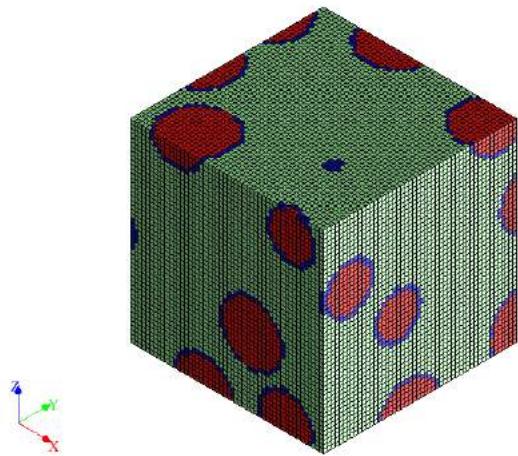
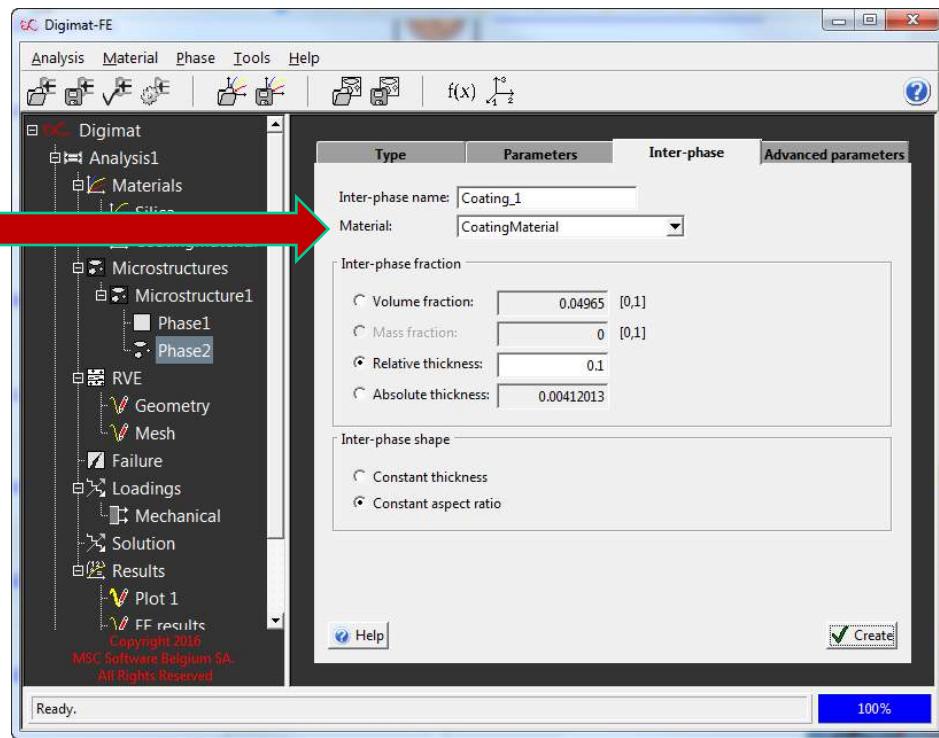
Digimat-FE/J-OCTA Inclusion-Matrix Coupling



J-OCTA



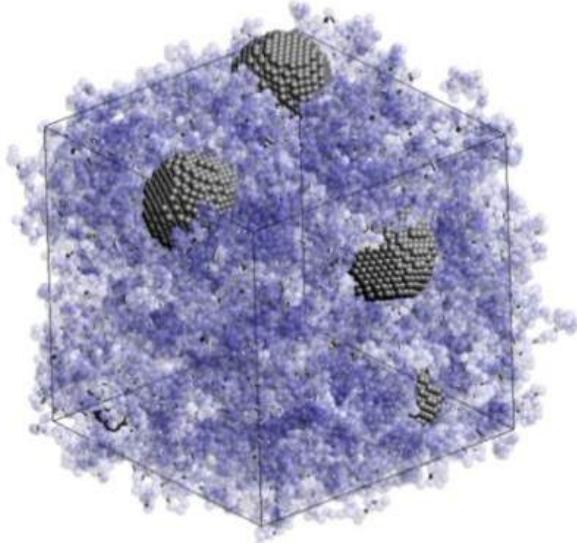
Silica-Rubber interaction



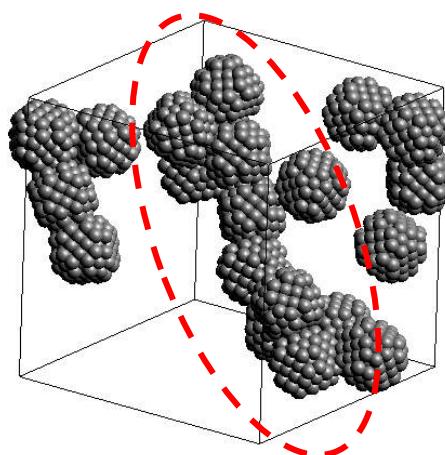
Estimation of the dispersion of nano-filters



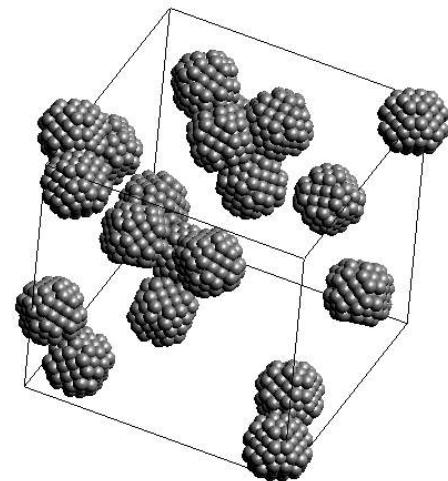
Dispersion of silica particles in polyisoprene (Natural Rubber).
Interaction parameters are decided by using SP values from reference.



aggregation



Without Silane coupling

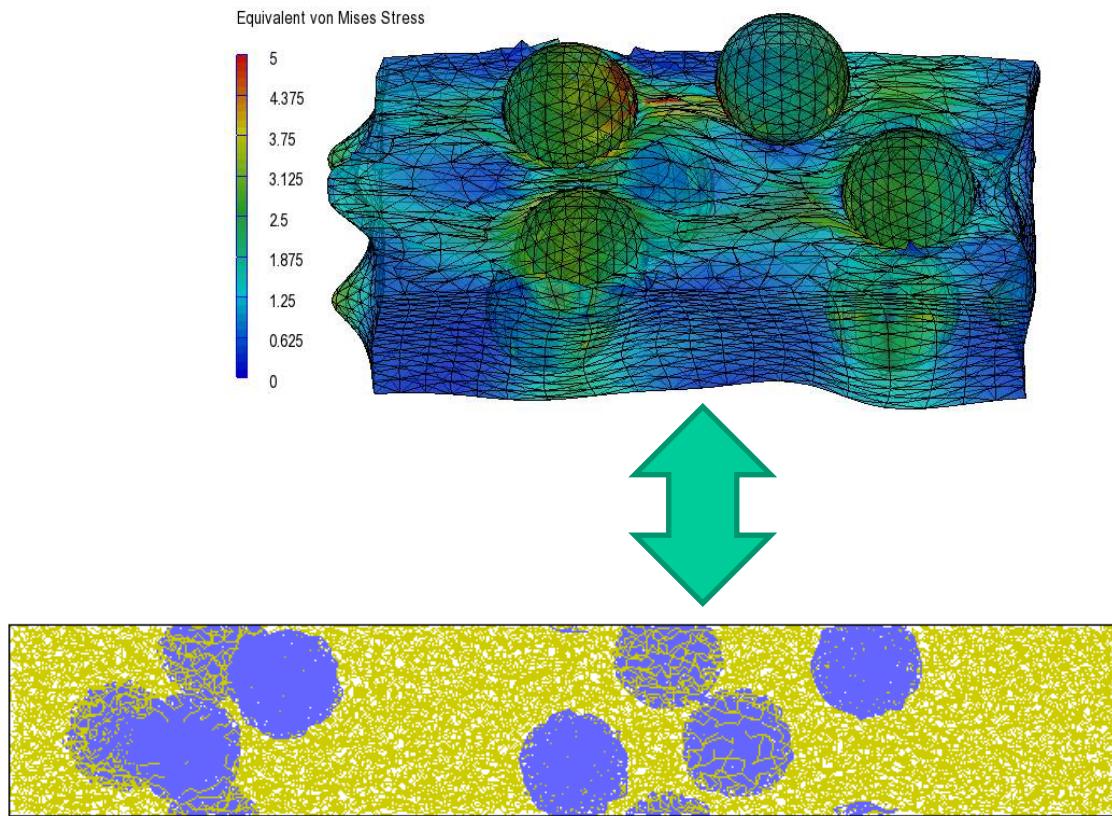


With Silane coupling

Mechanical property using meso-scale simulation



- Just an idea.
- By using the results of CGMD for small system, is it possible to decide parameters of each region(part)'s constitutive eq.?
- Same scale simulation are conducted and compared each others.
- Decided parameters are used for large scale FEA. This region is difficult for CGMD as described before.
- JSOL has interest in this technology.

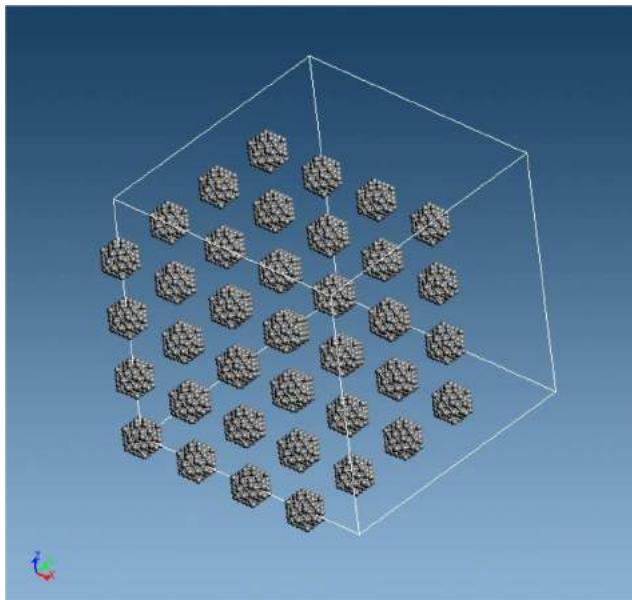


Stress distribution in CGMD can be compared with FEA.



Digimat proposes an interface to Molecular Dynamics

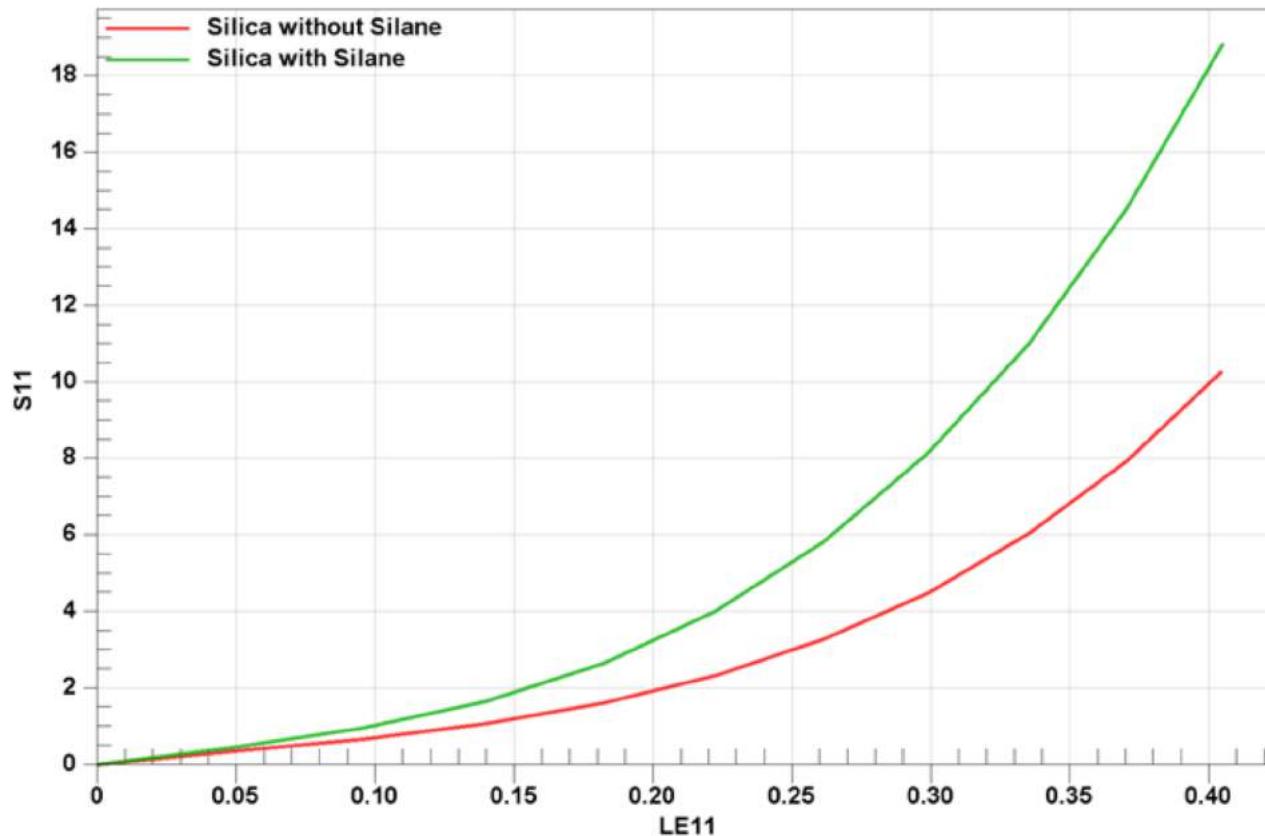
- RVE generation based on inclusion position obtained through DPD



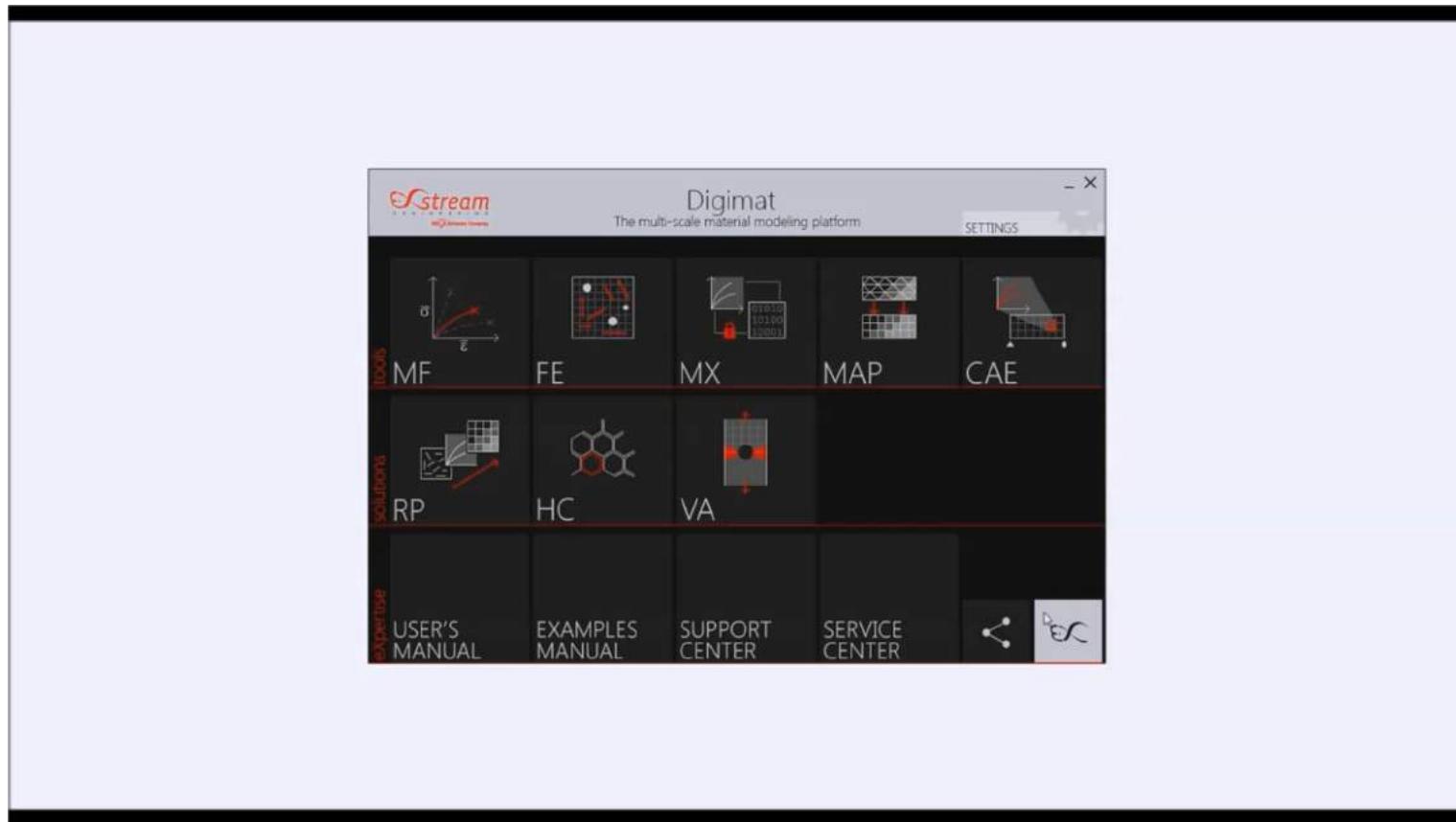
Molecular dynamics coupled with Digimat predict the influence of the nano-fillers dispersion on the composite properties



- The influence of the Silane on the fiber dispersion has a direct influence on the stress-strain curve
 - Hence probably also on the rolling resistance



Digmat has the expertise to identify an hyper-elastic model based on CGMD predictions



Molecular dynamics

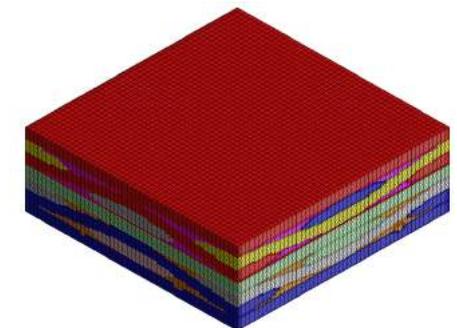
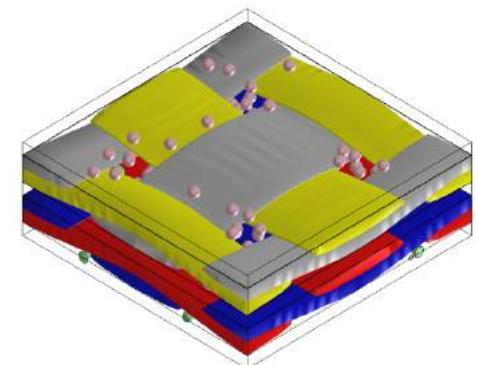
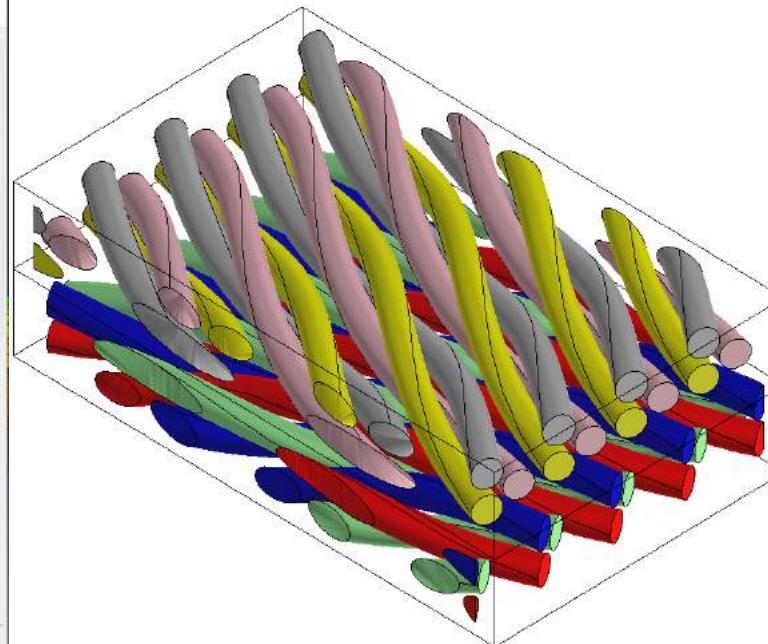
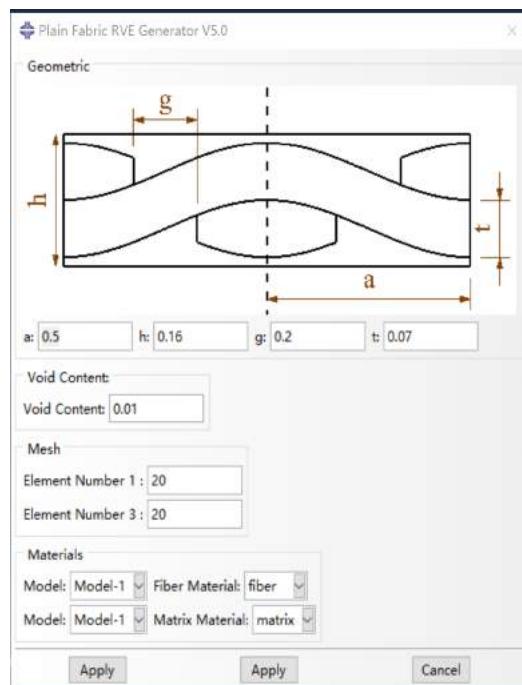
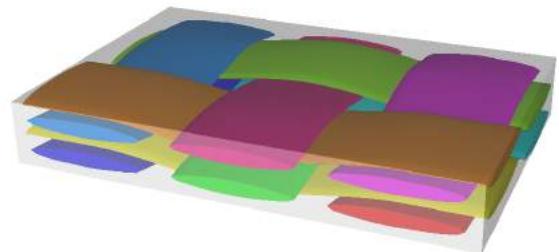


Macro
hyper-elastic
model

To define a parametrizable cord and meso-structure



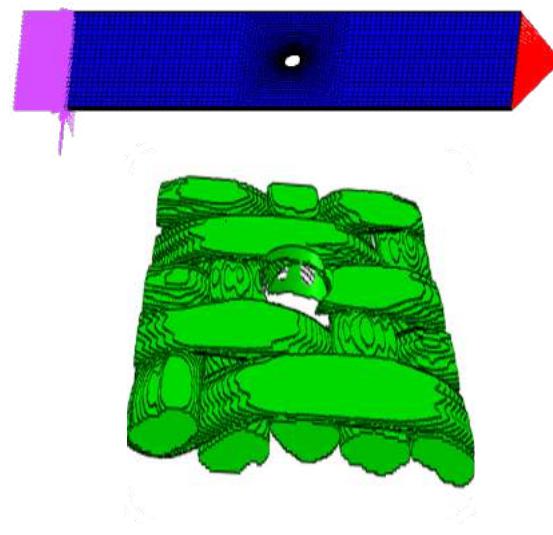
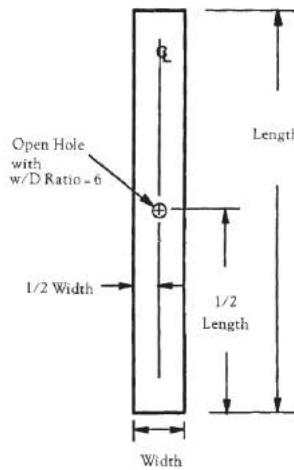
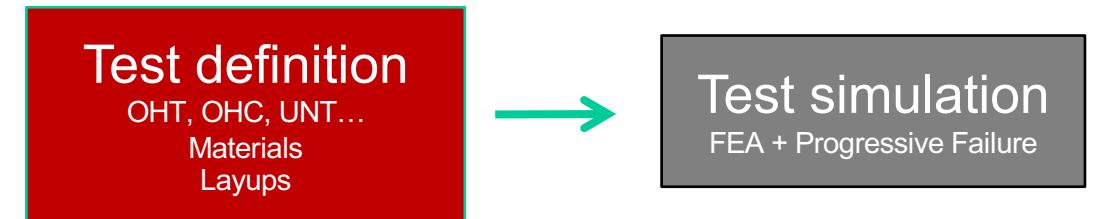
- Define amount of twist per cord length
- Define cord
 - structure
 - material properties
- Computation of homogenized cord properties





To link virtual testing with full-field homogenization

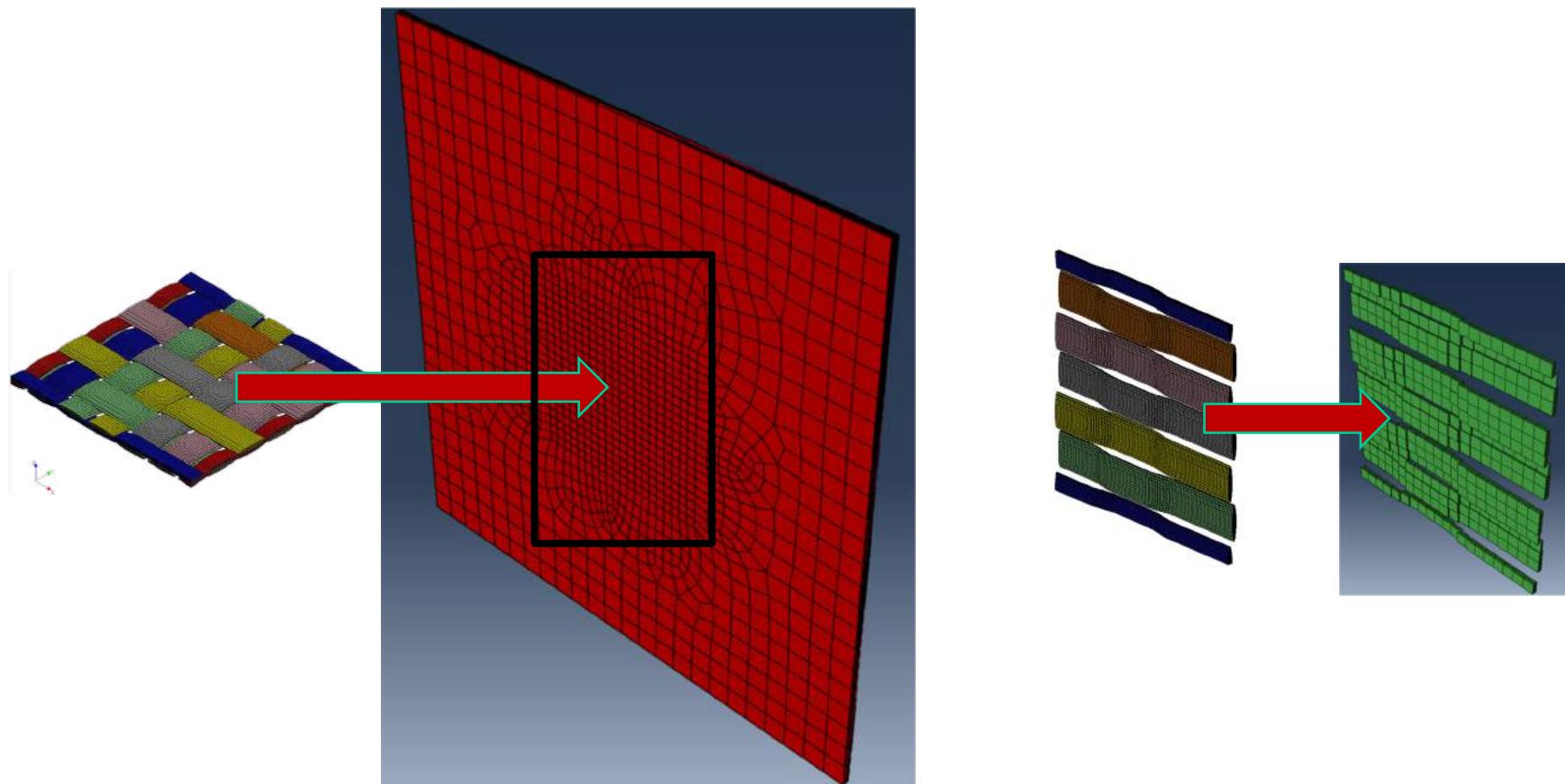
- Design your coupon
- Digimat fill it with fine cord discretization



Developping workflow to mix macro and micro modeling



- Mapping of RVE definition onto structural applications
 - Composite behaviour out of the zone of interest
 - Per-phase behaviour in the zone of interest

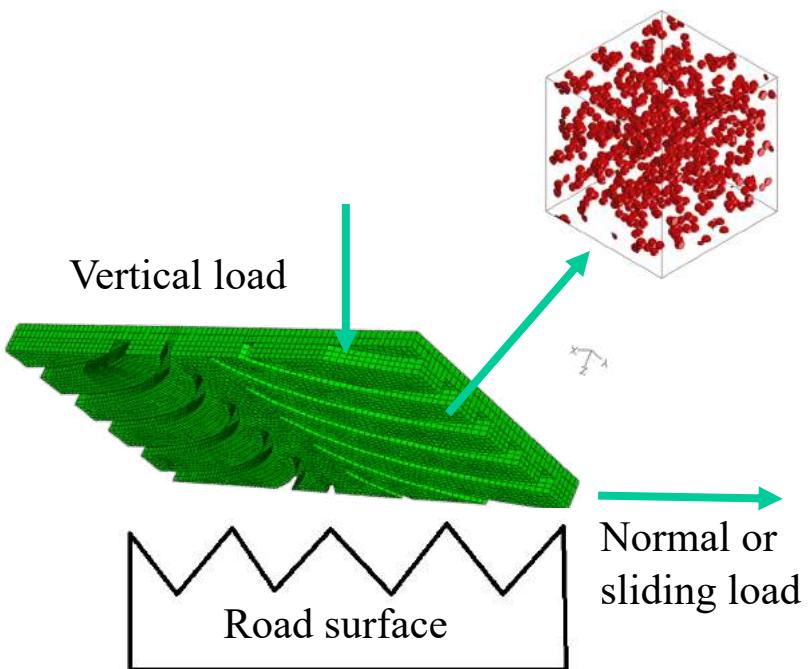
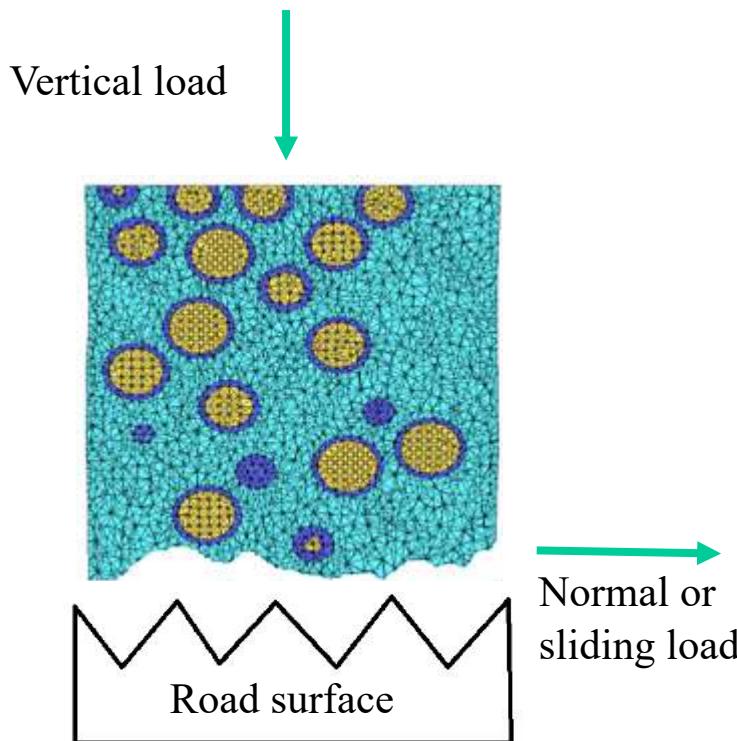




To predict the friction coefficient of a tyre

- Performing simulation at various scale

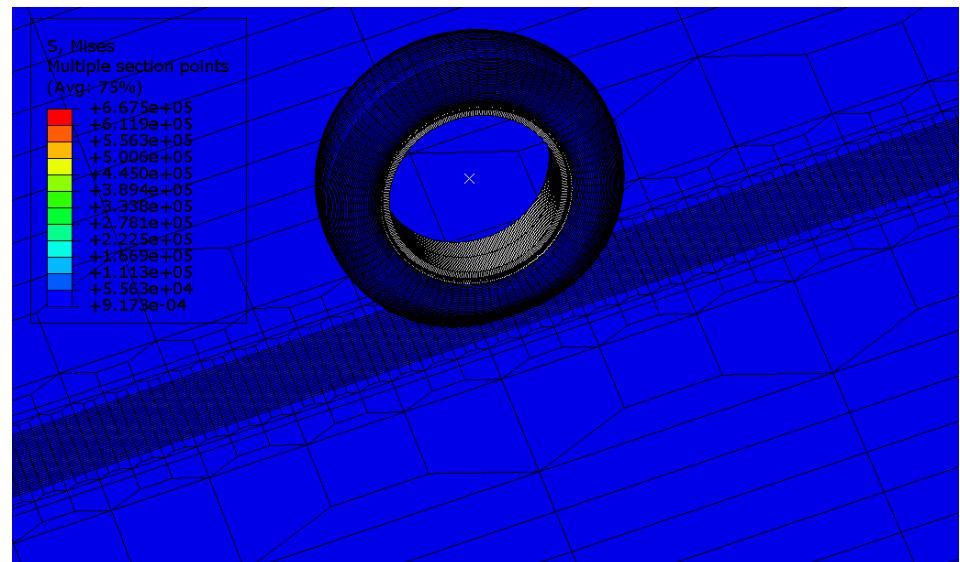
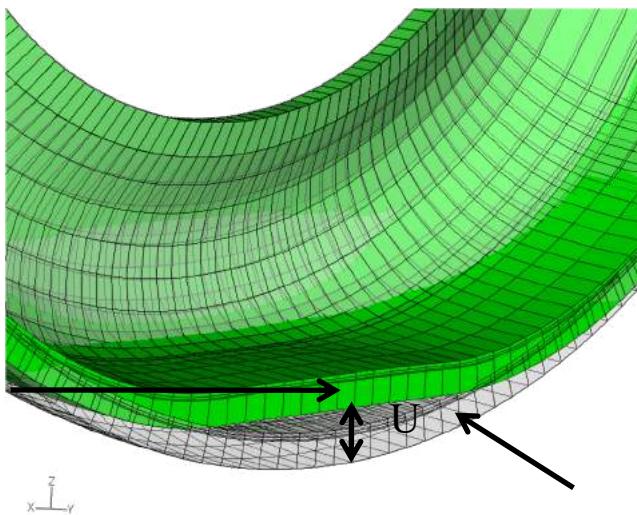
- Rubber vs road
- Thread vs road
- Tire vs road

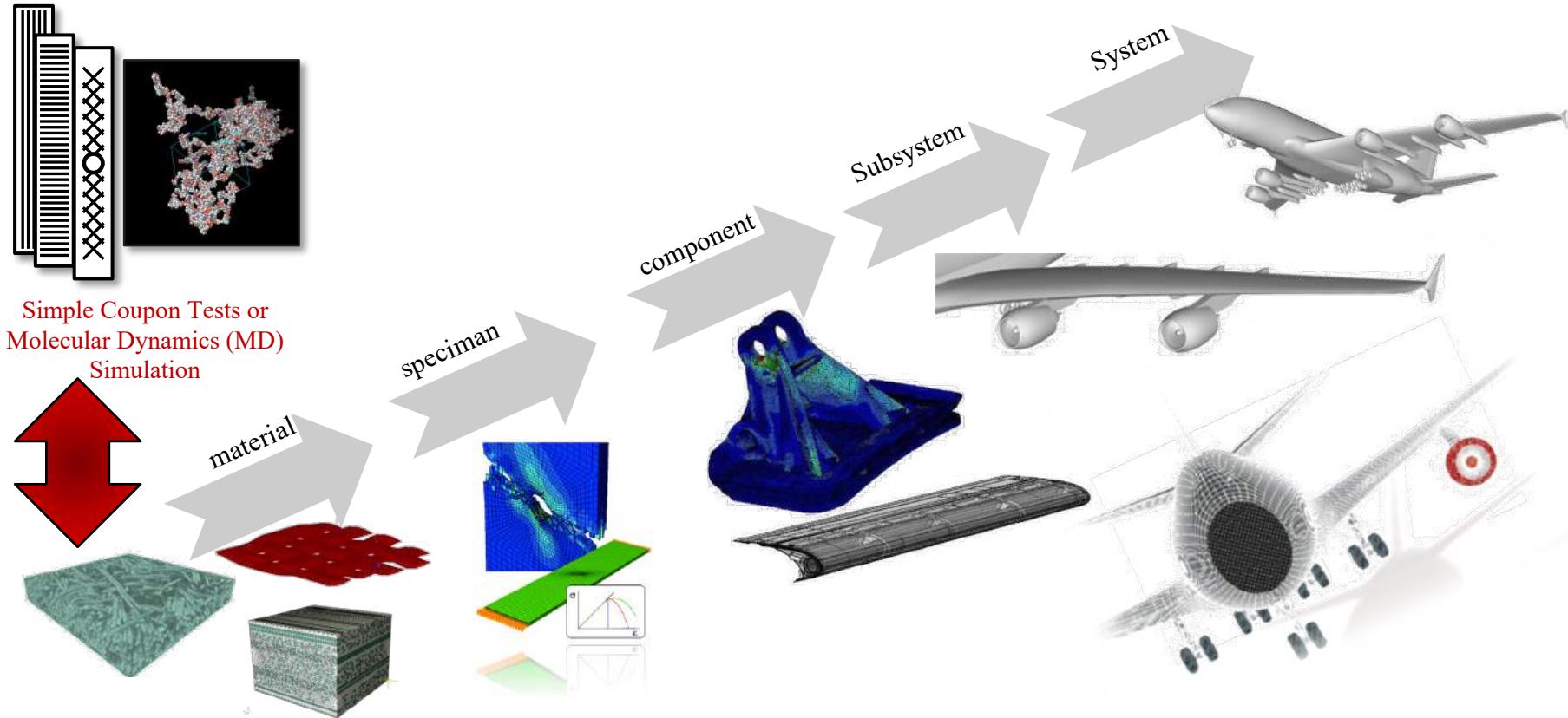


To predict the tire foot print and dynamic simulation



- Predict the tire foot print with various material model based on Digimat
 - Filled rubber
 - Rubber with cords





Thanks for your attention

