

p	q	$p \vee q$
T	T	T
T	F	T
F	T	T
F	F	F

d) Exclusive or (\oplus) :

Let p and q be the propositions, the exclusive or of p and q is true when exactly one of p and q is true and otherwise false.

p	q	$p \oplus q$
T	T	F
T	F	T
F	T	T
F	F	F

e) Conditional Statement. (if... then... / \rightarrow)

Let p and q be the propositions, the conditional statement $p \rightarrow q$ is false when p is true and q is false otherwise true.

p	q	$p \rightarrow q$
T	T	T
T	F	F
F	T	T
F	F	T

f) Biconditional Statement (if and only if / \leftrightarrow)

Let p and q be the propositions, the biconditional statement $p \leftrightarrow q$ is true when p and q have same truth values. otherwise false

p	q	$p \leftrightarrow q$
T	T	T
T	F	F
F	T	F
F	F	T

• If $p \rightarrow q$ is the conditional statement then then.

- 1) Converse : $q \rightarrow p$
- 2) Inverse : $\neg p \rightarrow \neg q$
- 3) Contrapositive : $\neg q \rightarrow \neg p$

eg: Find negation of following propositions

1) p : At least 10 inches of rain fall today in Mumbai.

q : There is no pollution in New Jersey.

r : It is raining now.

\Rightarrow Negation of following propositions

$\neg p$: Less than 10 inches of rain fall today in Mumbai.

$\neg q$: There is pollution in New Jersey

$\neg r$: It is not raining now.

but = and.

eg: 2) p : it is below freezing
 q : it is snowing

Write in following statements using p, q and logical connectives.

- a) it is below freezing and snowing $p \wedge q$
- b) it is below freezing but not snowing $p \wedge \neg q$
- c) it is not below freezing and not snowing. $\neg p \wedge \neg q$
- d) it is either snowing or below freezing $q \vee p$
- e) if it is below freezing, it is also snowing. $p \rightarrow q$
- f) That it is below freezing is necessary and sufficient for it to be snowing. $p \leftrightarrow q$

⇒ 3) Find conjunction and disjunction of following proposition.

p : Today is Friday
 q : It is raining today.

→ Conjunction: (p and q) $p \wedge q$
Today is Friday and it is raining today.

Disjunction: (p or q) $p \vee q$
Today is Friday or it is raining today.

Conditional: (if... then...) $p \rightarrow q$
if Today is Friday then it is raining today

⊗ Biconditional: (if and only if) $p \leftrightarrow q$
Today is Friday if and only if it is raining today

- 4) p : You can take a flight
 q : You buy a ticket

Conjunction: $(p \wedge q)$

You can take a flight and you can buy a ticket

Disjunction: $(p \vee q)$

You can take a flight or you buy a ticket

Conditional: $(p \rightarrow q)$

If you can take a flight then you buy a ticket

Bidirectional: $(p \leftrightarrow q)$

You can take a flight if and only if you ~~can~~ buy a ticket.

~~alt~~ alt: if you can take a flight it is necessary to buy a ticket.

5)