NATIONAL UNIVERSITY OF SINGAPORE

CS1101S — PROGRAMMING METHODOLOGY

CURATED VERSION OF 14/11/2020 (CORRECTED ON 22/11/2020)

(Semester 1 AY2017/2018)

Time Allowed: 2 Hours

INSTRUCTIONS TO STUDENTS

- 1. This assessment paper contains **FIVE** (5) questions and comprises **TWENTY-FIVE** (25) printed pages, including this page and two sheets of scratch paper at the end.
- 2. The full score of this paper is 80 marks.
- 3. This is a **CLOSED BOOK** assessment, but you are allowed to use **ONE** A4 sheet of notes.
- 4. Answer ALL questions within the space provided in this booklet.
- 5. Where programs are required, write them in the **Source Week 11** language.
- 6. Write legibly with a pen or pencil. UNTIDINESS will be penalized.
- 7. Do not tear off any pages from this booklet.
- 8. Write your **Student Number** below **USING A PEN**. Do not write your name.

Student No.:									
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This portion is for examiner's use only

Question	Marks	Question	Marks
Q1 (17 marks)		Q4 (14 marks)	
Q2 (18 marks)		Q5 (14 marks)	
Q3 (17 marks)		TOTAL (80 marks)	

Question 1: Pairs, lists and trees [17 marks]

Recall from the lectures the definition of trees:

A tree of certain data items is a list whose elements are such data items, or trees of such data items.

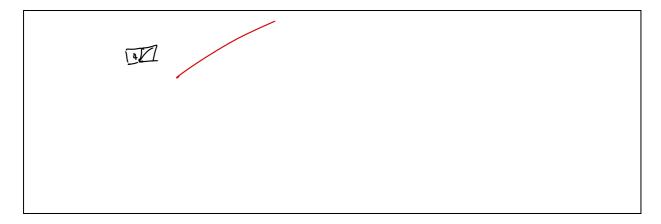
In this question, we restrict ourselves to *trees of numbers*. A tree of numbers thus is a list whose elements are numbers or trees of numbers.

A. Box-and-pointer diagrams of trees of numbers [6 marks]

Draw the box-and-pointer diagrams of results of evaluating the following Source statements.

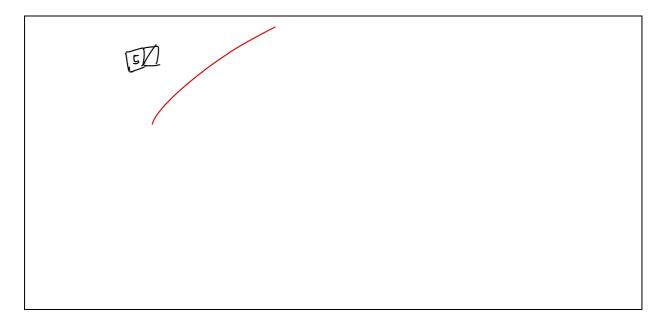
A.1. [1 mark]

pair(4, null);



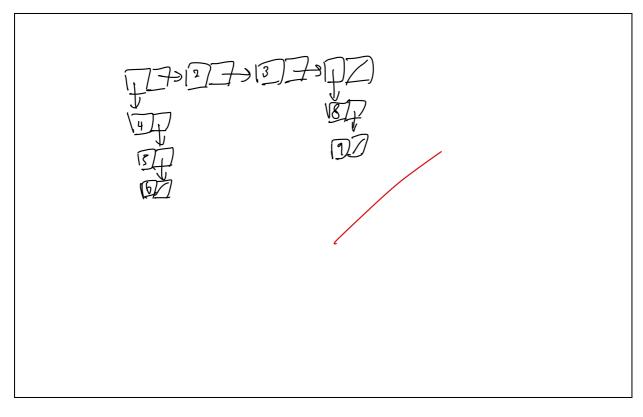
A.2. [1 mark]

list(5);



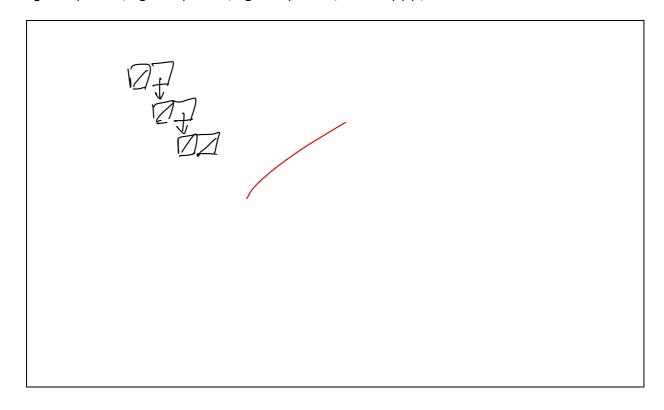
A.3. [2 marks]

list(list(4, 5, 6), 2, 3, list(8, 9));



A.4. [2 marks]

pair(null, pair(null, pair(null, null)));



B. A notion of similarity [4 marks]

Recall the function equal from the lectures. When applied to two trees of numbers, equal returns true, if and only if they have exactly the same structure (same pairs and empty lists) and the same numbers at their leaves.

In this question, we would like to be a bit more liberal, and define two trees to be *similar*, if they have the same structure and if the corresponding number leaves differ by at most 1.

Examples:

Define the function similar such that similar(tn1, tn2) returns true if tn1 and tn2 are similar and false otherwise. You can assume that both tn1 and tn2 are trees of numbers. Make your function as simple and clear as possible. You can assume that the function is number is available, with the obvious meaning.

```
Surtin Finilar ( tal, tal) {

Court bit = howeltal);

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Court bit = howeltal);

Court bit = howeltal);

(f ( is null (houltand)) is inval (houltand)) {

return true;

}

if ( is number (hould bit is number (hould)) {

return troth-order (hil - hould) {

return troth-order (hil - hould (hould));

return shinlar (hilly bit) & planies (houltand);

return shinlar (hilly bit) & planies (houltand);

return film;

}

something (hilly bit) & planies (houltand);

return film;

3.
```

C. Counting differences [4 marks]

For two similar trees, the question arises at how many places they differ. Write a function differences such that differences (tn1, tn2) returns the number of places where tn1 and tn2 have different numbers. You can assume that tn1 and tn2 are *similar* trees of numbers.

Examples:

Make your function as simple and clear as possible. You can assume that the function is_number is available, with the obvious meaning.

```
function difference (tr.1, tn2) {
                if C is millemill is mucha) {
                          num 0;
                 if ( is-number (tn() bb ir-number (fn2) {
                          if c to 1- to 2 !== 0) {
                              vehm 1;
                          3 ch {
                               rehm 0;
                  3
                  return differences ( head arms), head (Ind))
                         + HXPrucy ( fail (thi), tail (th));
  ኝ
```

D. Incrementing trees of numbers [3 marks]

Recall the function map_tree from the lectures.

Use map_tree to define a function increment such that increment (tn) returns a tree that is *similar* to the given tree tn, where each number is incremented by 1. You can assume that tn is a tree of numbers.

Example:

```
increment(list(4, null, list(4,6), 8)); // returns the same as list(5, null, list(5,7), 9);
```

```
Const Increment = (xS) \Rightarrow map-tree(x \Rightarrow is-mull(x)) not : x+1, xs);
```

The following question is not relevant for CS1101S as of 2019/20.

Question 2: Key-value stores [18 marks]

Key-value stores are databases that use lists of strings as keys and strings as values. Today, databases that use key-value stores such as Oracle's NoSQL are popular for Big Data applications.

A. Drawing stores [6 marks]

We shall use literal Source objects in order to implement key-value stores. For example, the following Source object can be seen as a key-value store.

Draw the environment diagram of the environment after evaluating the program above.

70	1	1	\sim	1	α
		- 1	"		

B. Stores and the prototype chain [4 marks]

The string "__proto__" enjoys special treatment in Source (and JavaScript) objects. Consider the following Source object.

What is the result of the following operations:

B.1. [1 mark]

your_key_value_store.a.b.c;

	[1 marl	,1
D.Z.	1 mair	7

your_key_value_store.a.f;

B.3. [1 mark]

your_key_value_store.h.b;

B.4. [1 mark]

your_key_value_store.h.j;

We shall assume henceforth that "proto does not occur in keys of key-value stores.

C. Storing values [4 marks]

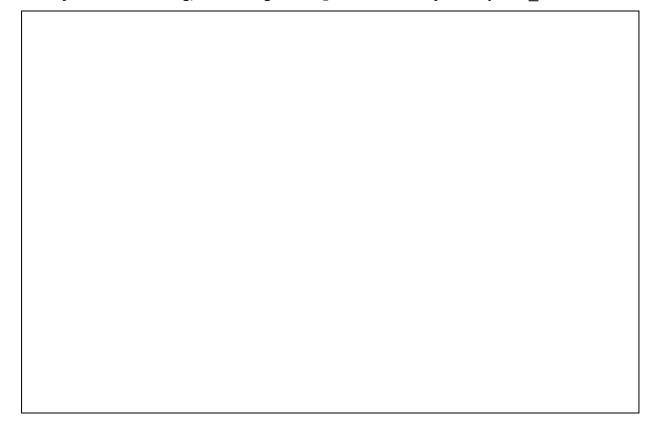
A key-value store is initially empty, and thus is represented by the empty object.

```
function make empty key value store() { return {}; }
```

In order to add entries to the key-value store, we require a function put that takes a *store* as first argument, followed by a *key*, which is a list of strings, followed by the *new value* that we want to enter. The string elements of the key are used to successively access the properties of the respective object, starting with the first element (also called the major key) and the whole store. The process will create objects whenever necessary, on the path to where the value belongs.

After the following session, my_key_value_store_2 will refer to an object with the same structure and values as the object my key value store in Part A.

Define the function put. The call put(store, key, new_value) should always succeed in writing the string new_value to any store, such that it can later be retrieved with the list of strings given in key. If the store already has a value (which might even be an object and not a string) under the given key, that value is replaced by new value.



D. Retrieving values [4 marks]

In order to access a key-value store, we need a function get that is applied to a store and a key. The function get(store, key) should always succeed for a given store my_store and a given list of strings key. If store contains the value val under key, the function get should return val. If there is no string value under key, the function get should return the value undefined. You can assume there are functions is_string and is_object to check if a given value is a string or an object, respectively.

Examples:

Question 3: Counting Sort [17 marks]

The sorting functions discussed in the lectures have in common that they use comparisons to determine the order of the elements in the resulting sorted array. The worst-case runtime for any such comparison-based sorting algorithms has order of growth $\Omega(n \log n)$, where n is the size of the array to be sorted, if no additional information is known about the elements in the array or their order.

One way to do better than $\Omega(n \log n)$ is to use operations other than comparisons. For example, if we know that all elements of a given array are *integers* ranging from 0 to a relatively small maximal value, we could use the integers as *indices* into an array, and use array assignment and access as operations:

```
my array[unsorted array[i]] = ...;
```

In this question, we are given an unsorted array of numbers unsorted, and a number max, with the additional information that all elements are integers between 0 and max.

Possible values for unsorted and max could be:

```
var unsorted = [5, 1, 10, 2, 1, 5, 7, 3];
var max = 12;
```

Our strategy for sorting such arrays is to build an array that represents a <u>histogram</u> for the values of the original array. The histogram indicates for each possible value 0 to max, how many times the value occurs in unsorted. In the example above, the histogram would look as follows:

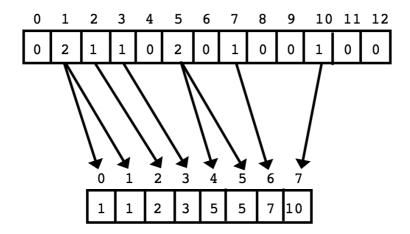
as follows:
$$0 \ 1 \ 2 \ 3 \ 4$$

var histogram = $[0, 2, 1, 1, 0, 2, 0, 1, 0, 0, 1, 0, 0]$;

From such a histogram, we shall then generate the sorted array by placing as many copies of the histogram indices into the target array as indicated by the histogram:

```
var sorted = [1, 1, 2, 3, 5, 5, 7, 10];
```

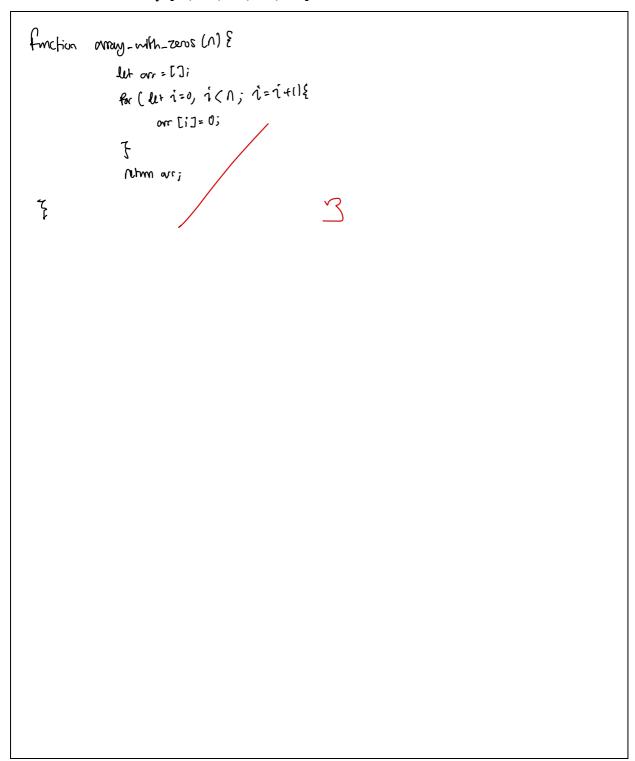
The diagram below illustrates how the sorted array can be obtained from the histogram.



A. Making arrays of zeros [3 marks]

It will be convenient to start with a histogram whose elements are all 0. Write a function array_with_zeros such that a call array_with_zeros(n) returns an array of length n whose values at indices 0 to n - 1 are all 0.

For example,



B. Making a histogram [4 marks]

Write a function make_histogram that takes an array of non-negative integers and a number max as arguments. You can assume that all integers in the array are less than or equal to max. The call make_histogram(arr, max) should return an array of length max + 1 that indicates for each number 0 to max the number of times the element occurs in arr. For example, the resulting histogram for the array unsorted on Page 11 and max = 12 is the array:

```
[0, 2, 1, 1, 0, 2, 0, 1, 0, 0, 1, 0, 0]
```

Define your function as simply and clearly as possible, and make use of the function array_with_zeros in Part A if you think it helps.

```
Proction make _ histogram ( our, max) {
             let ans = orroy-with-zeros (marx+1);
              for ( let i=0; i < array-length(orr); i=i+1)}
                           let no expliss
                           let originaluatue = ans Enj;
                            and Enj z original value +1;
               3
                return ons;
3
```

C. Entering copies [3 marks]

To fill the result array, we may need a function enter_copies such that enter_copies(arr, n, v, start) enters into arr exactly n copies of a given value v, starting at index start. For example, consider the array

```
var some_array = [1, 1, 1, 1, 1, 1, 1, 1];
The call
```

enter_copies(some_array, 4, 8, 2);

should enter 4 copies of the value 8 into some_array, starting at position 2. Thus, after the call, some array should have the form [1, 1, 8, 8, 8, 8, 1, 1, 1].

D. Generating sorted array [5 marks]

We now generate a sorted array from a given histogram. For each index *i* of the histogram, we enter the given number of copies of *i* into the sorted array, starting from 0. For example, generate_sorted([0, 2, 1, 1, 0, 2, 0, 1, 0, 0, 1, 0, 0]); should return the array [1, 1, 2, 3, 5, 5, 7, 10].

E. Complexity of counting sort [2 mark]

We can now define the overall sorting function

```
function counting_sort(unsorted, max) {
    return generate_sorted(make_histogram(unsorted, max));
}
```

The basic operation for this algorithm is array access and assignment, which we will call *array operations*. We define the *size of a sorting problem* as the maximum of the length of the given array unsorted and max, which is the given limit for the largest value of the array. Characterise the number of array operations for running counting_sort(unsorted, max), using Θ -notation.

The number of array operations for solving a sorting problem of size n using counting sort has order of growth:

9(1)

The following question is not relevant for CS1101S as of 2019/20.

Question 4: Digital Orrery [14 marks]

An orrery is a mechanical clockwork model of the solar system, or parts of it. The image on the right shows an orrery at the Museum of the History of Science in Oxford. Jerry Sussman—one of the original authors of the CS1101S textbook—created a digital orrery, and used it in 1988 to predict the behaviour of the solar system for 845 million years, to study if it exhibits chaotic behaviour. In this question, we will lay the foundation for a simple digital orrery using Source.



A. [4 marks]

First, we shall define a coordinate system relative to which we position the bodies in the solar system. We limit ourselves to a classical, 3-dimensional, Euclidean space and choose a

heliocentric ecliptic rectangular coordinate system, where the centre of the sun has coordinates $(x: \theta, y: \theta, z: \theta)$, and the Earth always has $(z: \theta)$. As units, we will use million kilometres. A possible location for the center of the Earth could be characterized by the Source object:

$$({x: 145.9, y: 76.4, z: 0.0});$$

Define a function Body that allows us to create such objects, using

$$var = new Body(145.9, 76.4, 0.0);$$

Add methods get_x, get_y, get_z that enable access to the coordinates as in earth.get x(); // returns 145.9

B. [6 marks]

Now we could define a few bodies in our digital orrery as follows:

```
var earth = new Body(145.9, 76.4, 0.0 );
var moon = new Body(145.3, 76.1, 0.001);
var sun = new Body( 0.0, 0.0, 0.0 );
var system = list(earth, moon, sun);
```

Draw the environment diagram for this program, including the function Body, its methods, and the frames that result from calling Body.

C. [4 marks]

For our orrery to work, we need to keep track of the speed of the bodies, and not just their position. For this we assume we can use 'speed' objects. **Define a function MovingBody** that allows you to create new bodies using

Your function MovingBody should inherit from the function Body and make use of Body in its definition.

Also define a method get_speed such that we can retrieve the current speed of moving_earth by

var current_earth_speed = moving_earth.get_speed();

Question 5: The Source metacircular evaluator [14 marks]

A. Repeated parameters [5 marks]

JavaScript insists that function parameters are unique. For example, a function

```
const power = (x, x) \Rightarrow x === 0 ? 1 : x * power(x, x - 1);
```

lists x twice as parameter of power. Unlike JavaScript, the metacircular evaluator accepts this program although this is clearly a programming error and the meaning of the program is not clear.

Modify the implementation of lambda expressions in the metacircular evaluator such that any lambda expression where the parameters are not unique displays an error and returns undefined. For example, the evaluation of the function definition above will lead to the display of the string

"parameters in function definition not unique" and bind the name power to the value undefined.

Hint: Recall that lambda expressions are implemented in the metacircular evaluator as follows:

```
fination eachere_limbin-expression( comparent, end &
        Const proms - lambon-promoter symbols (composets;
         K( Allyor ( barans))}
              return Mace-Fresher Church,
                                     (ambéen-boe) (compount), en).
         3 elu E
                hoplay (" parameter in tracken not vigue");
          3
```

The following question is not relevant for CS1101S as of 2019/20.

B. Property assignment to primitive values [3 marks]

JavaScript allows property assignment to primitive values such as boolean values, numbers and strings. Any such attempts are just ignored by the JavaScript evaluator. For example,

```
true["aaa"] = 1; // has no effect
"bbb" . ccc = 2; // has no effect
123["ddd"] = 3; // has no effect
```

All these property assignments succeed in JavaScript, but have no effect. Most of the time, such operations will be a programming error, and the author intended something else. JavaScript's strict mode therefore generates an exception in these situations.

Modify property assignment such that error messages are displayed, in the examples above:

```
"expecting array/object/function value before [, found value true"
"expecting array/object/function value before [, found value 'bbb'"
"expecting array/object/function value before [, found value 123"
```

Hint: Recall the current implementation of evaluation property assignment for MetaSource as follows:

```
function evaluate_property_assignment(stmt,env) {
    var obj = evaluate(object(stmt), env);
    var prop = evaluate(property(stmt), env);
    var val = evaluate(value(stmt), env);
    obj[prop] = val;
    return val;
}
```

You can assume that the builtin functions is_object, is_array and is_function are available and return **true** if and only if their argument is a Source object, Source array or Source function, respectively.

C. The Essence of evaluation? [6 marks]

Let us assume we want to support a function evaluate in the interpreted language that takes a string as argument, parses it, evaluates the parsed program, and returns the result. This question explores what environment can or should be used for the evaluation.

Recall that primitive functions such as pair, head and tail are defined in the metacircular evaluator as follows:

```
// the global environment has bindings for all
// primitive functions, including the operators
const primitive functions = list(list("pair", pair),
                                  list("head", head),
list("tail", tail),
                                  . . .
                                  );
const primitive function symbols =
        map(head, primitive functions);
const primitive function objects =
        map(fun => list("primitive", head(tail(fun))),
            primitive functions);
function setup environment() {
    return extend environment(
               append(primitive function symbols,
                       primitive constant symbols),
               append(primitive function objects,
                       primitive constant values),
               the empty environment);
}
const the global environment = setup environment();
function parse_and_evaluate(input) {
    const program = parse(input);
    const implicit top level block = make block(program);
    return evaluate(implicit_top_level_block,
                    the global environment);
}
```

Our approach to provide an evaluate function in MetaSource shall be to add a line in the definition of primitive_functions as follows:

Using this modification of the evaluator, what are the results of the following Source programs?

C.1. [2 marks]

```
let x = 1;
parse_and_evaluate(
    "evaluate('let x = 2; x + x;');");
```

```
4
```

C.2. [2 marks]

```
let x = 1;
parse_and_evaluate(
  `let x = 2;
    evaluate('function f(x) { return x + x; } f(3);');`);
```

C.3. [2 marks]

```
enor. Fire: mound nunx: "x";
```

(Scratch paper. Do not tear off.)

(Scratch paper. Do not tear off.)